A Data Layout Transformation for Vectorizing Compilers

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ABSTRACT
Modern processors are often equipped with vector instruction sets. Such instructions operate on multiple elements of data at once, and greatly improve performance for specific applications. A programmer has two options to take advantage of these instructions: writing manually vectorized code, or using an auto-vectorizing compiler. In the latter case, he only has to place annotations to instruct the auto-vectorizing compiler to vectorize a particular piece of code. Thanks to auto-vectorization, the source program remains portable, and the programmer can focus on the task at hand instead of the low-level details of intrinsics programming. However, the performance of the vectorized program strongly depends on the precision of the analyses performed by the vectorizing compiler. In this paper, we improve the precision of these analyses by selectively splitting stack-allocated variables of a structure or aggregate type. Without this optimization, automatic vectorization slows the execution down compared to the scalar, non-vectorized code. When this optimization is enabled, we show that the vectorized code can be as fast as hand-optimized, manually vectorized implementations.

CCS CONCEPTS
• Computing methodologies → Vector/streaming algorithms;
• Software and its engineering → Compilers; Software performance;

KEYWORDS
Vectorization, Compiler, Optimization

ACM Reference Format:

1 INTRODUCTION
Vectorization is the process of transforming a program that operates on single elements of data into a program that operates on arrays of data. This transformation requires to convert the control flow of the input program to data flow, by inserting masking instructions and guards. As a result, the program can be executed on a machine that provides vector instructions, and execute faster. In order to perform this transformation, developers can either use compiler intrinsics and directly write vector code, or use a semi-automatic vectorizing compiler and write annotations in the parts of the program that should be vectorized. The advantages of the second approach are clear: The programmer can write cleaner, more portable code with less effort.

```
struct Pair {
    a: int,
    b: int;
};

for $i$ in vectorize($*$ ... $*$) {
    let mut pair_a = 0;
    let pair_b = 0;
    while pair_a < 10 {
        pair.a++
    }
}
```

(a) Code before transformation

```
for $i$ in vectorize($*$ ... $*$) {
    let mut pair_a = Pair { a: 0, b: 0 };;
    while pair_a < 10 {
        pair.a++
    }
}
```

(b) Equivalent code after transformation

Figure 1: Result of the vectorization analysis before and after our transformation. Uniform and varying expressions are colored in green and orange respectively.

Using state-of-the-art guided vectorization, the programmer only places a minimal amount of annotations, and the compiler analyzes the program to determine the shape of every variable or statement. For the sake of simplicity, such shapes can either be: varying, in which case the variable or statement will be vectorized; or uniform, in which case it will remain scalar. However, these analyses do not detect when only part of a structure or aggregate type is varying.
and the rest is uniform, and therefore will mark all their members as varying (see Figure 1a).

To solve this issue, we introduce a transformation that is executed in fixed point with the vectorization analysis. This transformation operates on the input scalar program and breaks aggregates or structures that are assigned a varying shape into smaller parts. The result (see Figure 1b) is a program in which the varying members of the aggregates are separated from the uniform ones. This transformation may impact the way control flow is vectorized. For instance, if the shape of a loop condition was changed from varying to uniform, masking is no longer necessary, because all lanes enter and exit the loop together. This, in turn, results in a spectacular performance improvement, as shown in Section 4.

2 RELATED WORK

We first review standard vectorization techniques, and then present region vectorization. Finally, we describe support for vectorization in programming languages.

2.1 Traditional Approaches

2.1.1 Superword Level Parallelism (SLP). Vectorization on straight-line code exploits SLP: The compiler tries to merge several scalar operations into a vector operation. This can be done on a per-basic-block level [13] or in the presence of control flow [23]. SLP algorithms will usually give up if the exact number of needed instructions cannot be fed into the SIMD lanes. Padded SLP tries to overcome this limitation by injecting redundant instructions [22]. Throttled SLP uses a cost model in order to estimate whether SLP vectorization is actually worthwhile at all [21].

2.1.2 Loop Vectorization. Allen et al. [1, 2] present a technique to translate loop nests to array statements. An alternative is outer loop vectorization using a so-called unroll-and-jam technique [3, 16, 20]: A chosen outer loop is unrolled several times while the resulting loop bodies are re-fused (“jammed”). There is a good chance that the instructions stemming from the same instruction in the original version can be grouped into SIMD instructions.

Other work on loop vectorization also considers data alignment, reductions [19], and interleaved data accesses [18]. Furthermore, the polyhedral model [7]—a powerful mathematical loop analysis framework using Presburger sets—has also been instrumented for loop vectorization [17, 25].

2.2 The Region Vectorizer

The region vectorizer (RV) is a state-of-the-art vectorization framework based on LLVM. RV is derived from the whole-function vectorizer (WFV) [10–12]. RV vectorizes regions, which are single-entry, multi-exit subgraphs of the Control-Flow Graph (CFG). If the region encapsulates a loop nest, RV performs outer-loop vectorization. If the region contains the whole CFG, RV will vectorize the whole function.

RV maps each SIMD lane to one instance of a region in a CFG. The region instances execute in SPMD-like fashion, meaning that RV assumes that there are no data races between SIMD lanes.

2.2.1 Analysis and Transformations. RV operates in three main phases. First, it performs a divergence analysis [5, 12, 14] that assigns each instruction and branch a vector shape. This vector shape determines which instructions and branches in the region will behave uniformly across the instances of the region.

RV uses a sophisticated lattice to keep track of each instruction’s vector shape [8]. However, for the purpose of the paper it is sufficient to just differentiate between the vector shapes uniform and varying (see Section 1). Optimistically, RV assigns each instruction uniform (the bottom element in the lattice), and ascends in the lattice as required in a fixed-point iteration.

Second, because SIMD CPUs can not handle divergent branches in hardware—unlike GPUs, RV linearizes divergent control by if-conversion: RV emulates the original control flow by inserting bit operations and masking instructions. This linearization and the additional masking operations take their toll on the program’s performance. Thus, it is a good idea to keep control flow uniform whenever possible.

Finally, the vector code generator emits vector instructions, thereby concluding the vectorization process.

2.2.2 Vectorization of stack objects. Due to the SPMD semantics, if the code makes use of stack-allocated objects (alloca in LLVM) RV assumes that each SIMD lane sees its own copy of the object. RV vectorizes stack objects in the general case by replicating the structure in an array (array-of-struct) such that each SIMD lane receives its own instance. Vector accesses to these arrays are inefficient since if all SIMD threads access an element of their stack object in lock step, the accessed pointers will have a large stride. However, RV employs several optimizations to generate efficient data layouts for vectorized stack-allocated objects.

First, if all SIMD lanes access the same offsets and write only uniform values, the stack object remains scalar. Second, if all SIMD lanes access the same offsets of the stack object but write varying values, RV changes the layout of the object to struct-of-array instead of array-of-struct [24, 26]. For example, a scalar stack object with the type struct{int, int} will be replicated as struct{[int x N], [int x N]} where N refers to the vectorization factor.

2.3 Support in Programming Languages

Programming languages usually incorporate some mechanism to allows programmers to vectorize code. For instance, C/C++ compilers provide short vector data types that can be easily mapped to hardware vector units. Other languages, like APL [6], Vector Pascal [4], MatLab/Octave, or FORTRAN, and language extensions like ArBB [15] provide operations on arrays.

In order to instruct the compiler to vectorize a particular piece of code, languages can also provide a way to annotate a scalar program. In C/C++, Intel® Cilk™ Plus [9] and OpenMP 4.0 allow to place preprocessor directives in front of loops or functions. For the benchmarks used in the evaluation section of this paper, we integrated RV into the programming language Impala (see 4.1). The vectorization annotation is naturally added to the language through higher-order functions.
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3 ANALYSIS AND TRANSFORMATION

Our analysis and transformation is integrated in RV (see subsection 2.2). Therefore, our transformation operates on the LLVM Intermediate Representation (IR), but the description we give here is valid for any other SSA-based IR.

Our transformation is applied in a fixed-point loop: We first run the vectorization analysis of RV. Then, we look for stack allocated structures or array of structures, and split those that have a varying shape. We repeat those two steps until the transformation has nothing left to split.

With such a design, the transformation is selective: In the case of a varying structure containing other structures, the first iteration of the transformation will only split the parent structure. In the next iteration, the vectorization analysis will be more precise, because the members of the parent structure will be split: They will now have their own shape. Therefore, the transformation will only split the members of the innermost structure if necessary (see Figure 2).

3.1 Notation

In order to present the transformation in a concise and formal manner, we introduce a simplified version of the LLVM IR in Figure 3.

This IR represents the relevant parts of the LLVM IR for our setting. In particular, it models LLVM instructions such as load, store, alloca, or getelementptr. A load takes only one pointer argument and loads the corresponding piece of memory into a register. A store takes a value to store and a pointer to store the value to. An alloca allocates stack memory to hold a value of the given type and returns a pointer to the new chunk of memory. Note that this instruction is not to be confused with the homonymous GNU C library function; Its purpose is to model stack allocated variables. The getelementptr instruction performs pointer arithmetic on the argument with the given indices. The first index is multiplied by the size of the pointed object and added to the pointer. The meaning of the next index depends on the type of the pointer. If the pointer points to a structure, then it represents the index to a structure member. If the pointer points to an array, then it represents the index into the array. The following indices are interpreted in the same way, creating a path inside the type of the memory location. For instance, if a pointer p has type [struct {int, int}] × 2, then the instruction getelementptr p indices 0, 1, 0 returns a pointer that points to the first member of the structure in the second element of the array pointed by p.

The uses of an instruction I are denoted with U(I): it is a set containing all instructions that use I as an operand.

3.2 Analysis

The goal of the transformation is to split structures or arrays of structures allocated on the stack. Before doing so, we must ensure that the transformation is desirable (the structure is marked as varying) and valid (the address of the stack object is not used in incorrect ways). For these reasons, Algorithm 2 inspects every stack object and returns whether or not the transformation should be applied: For every varying alloca in the program, the algorithm checks if the allocated type is a structure or an array of structures, and if so, analyzes the uses of the alloca to ensure that they can be transformed (by calling the function AnalyzeUses in Algorithm 1). For instance, we must prevent the following instruction sequence from being transformed:

\[
I_1 = \text{alloca struct} \{\text{int, int}\} \\
I_2 = \text{alloca struct} \{\text{int, int}\} \\
I_3 = \text{store} I_2 \text{ to } I_1
\]

In this example, the pointer I_2 is stored to the memory location pointed by I_1, which makes precise tracking of instructions writing to I_2 generally impossible.

We also make sure that the users of an alloca to transform can only be loads, stores, or getelementptrs. In the case of a getelementptr, we check the indices to verify that the transformation is possible. In particular, we reject the following instruction sequence:

\[
I_1 = \text{alloca struct} \{\text{int, int}\} \\
I_2 = \text{getelementptr} I_1 \text{ indices } 5, 0
\]

In this case, I_2 points to memory outside of the region allocated by I_1: The getelementptr offsets the pointer in I_1 by 5 times the size of struct{int, int}.

The users of a getelementptr have to be analyzed as well if the pointer arithmetic does not descend into the alloca. To illustrate this point, consider the program:

\[
I_1 = \text{alloca struct} \{\text{int, int}\} \\
I_2 = \text{getelementptr} I_1 \text{ indices } 0 \\
I_3 = \text{getelementptr} I_2 \text{ indices } 0, 1
\]
In this small sequence of instructions, $I_2$ is in fact pointing to the same memory location as $I_1$. We must then also analyze its single use $I_3$. Since $I_3$ points to the second member of the structure, its uses do not need to be analyzed.

The program in Algorithm 1 formalizes these constraints.

### 3.3 Transformation

Once the analysis determines that the transformation is valid, we split the `alloca`. This process follows the same principle as the analysis: We start by creating one `alloca` per structure member, then replace the uses of the original `alloca`. For example, we may perform the following transformation:

\[
I_1 = \text{alloca struct}(\text{int}, \text{int}) \quad I_2 = \text{alloca int} \\
I_2 = \text{getelementptr } I_1 \text{ indices } 0,1 \Rightarrow I_2 = \text{alloca int} \\
I_3 = \text{alloca struct}\{\text{int}, \text{int}\} \quad I_3 = \text{alloca int} \\
I_3 = \text{getelementptr } I_3 \text{ indices } 0,1 \quad I_3 = \text{alloca int} \\
I_3 = \text{alloca struct}\{\text{int}, \text{int}\} \\
I_4 = \text{alloca int} \\
I_5 = \text{alloca int} \\
I_5 = \text{alloca struct}\{\text{int}, \text{int}\}
\]

If the original program contains a `load` or `store` to the entire `alloca`, we have to replace it by as many `loads` or `stores` as there are structure members, as in the following example:

\[
I_1 = \text{alloca int} \\
I_2 = \text{alloca struct}(\text{int}, \text{int}) \Rightarrow I_2 = \text{alloca int} \\
I_3 = \text{alloca int} \\
I_4 = \text{alloca struct}\{\text{int}, \text{int}\} \\
I_5 = \text{alloca struct}\{\text{int}, \text{int}\}
\]

### 4 RESULTS

#### 4.1 Benchmarks

In order to evaluate our approach, we implemented two benchmarking programs. The first one is a vectorized version of Bresenham’s line drawing algorithm, and the second is a vectorized ray-tracing kernel. These two programs differ in complexity: While Bresen- ham’s algorithm represents only a few lines of code, the ray-tracing program is more representative of real-world applications, as it amounts to approximately 1K lines of code.

Both of these programs are implemented using Impala, a dialect of Rust. In Impala, vectorization is triggered with the function `vectorize`. Impala then orders RV to vectorize the provided piece of code.

```rust
fn plot_line(line: &Line, plot: fn (i32, i32) -> () -> () {
    let dx = (line.x1 - line.x0) as f32;
    let dy = (line.y1 - line.y0) as f32;
    let de = fabsf(dy / dx);
    let ky = if line.y > line.y0 { 1 } else { 0 };

    let mut e = 0.0f;
    let mut y = line.y0;
    for x in range(line.x0, line.x1) {
        plot(x, y);
        e += de;
        if e > 0.5f {
            y += ky;
            e -= 1.0f;
        }
    }
}
```

In this example, the loop counter `i` is marked by Impala as being varying. Every variable captured from the inside of the vectorize block is assumed to be uniform across SIMD lanes, and marked uniform by Impala. RV then uses this initial information during the vectorization analysis.

#### 4.1.1 Line Drawing

Bresenham’s line drawing algorithm is an algorithm to plot lines on a bitmap image. The core of its implementation is given below:

```rust
for i in vectorize(vec_width, default_alignment, 0, N) {
    /* ... */
}
```

#### 4.1.2 Ray-tracing

Our ray-tracing benchmark uses a Bounding Volume Hierarchy (BVH) to compute the intersection between a ray and a 3D scene. The BVH is a tree containing a bounding box in each inner node, and list of triangles in the leaves. The children of a node are always contained in the bounding box of their parent.

The algorithm takes a ray as input and recursively descends into the tree, culling nodes whose bounding boxes are not intersected by the ray. In Impala, the ray-box intersection function is the following, and only consists in floating point arithmetic followed by min/max pairs:
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Algorithm 1 Analysis for the uses of an instruction.

Inputs:
I: Instruction to analyze
Arr: True iff I is an alloc of array type
Off: True iff the first getelementptr index can be non-zero

Output:
True iff I can be transformed

1: function AnalyzeUses(I, Arr, Off)
2:   for J ∈ U(I) do
3:     switch J
4:       case load J1
5:         break
6:       case store J1 to J2
7:         if J1 = I then
8:           return False  ▷ Pointers cannot escape
9:         end if
10:        break
11:       case getelementptr J1 indices J2, J3, . . . , Jn
12:          for k ∈ [2, n] do ▷ Check indices
13:            if Jk ∉ N & !(Arr ∧ k = 3) then
14:              return False ▷ Non-constant indexing
15:            end if
16:          end for
17:          if Off & k = 2 & Jk ≠ 0 then  ▷ First index must be zero
18:            return False
19:          end if
20:       end for
21:     end switch
22:   end for
23:   if Arr then ▷ Analyze uses of getelementptr
24:     if n < 4 then
25:       R ← AnalyzeUses(J, n = 2, n = 3)
26:     end if
27:   else
28:     if n < 3 then
29:       R ← AnalyzeUses(J, False, False)
30:     end if
31:   end if
32:   if !R then  ▷ Uses break constraints
33:     return False
34:   end if
35:   default
36:     return False ▷ Others instructions
37:   end switch
38: end function

Algorithm 2 Analysis for a single instruction.

Inputs:
I: Instruction to analyze
S: Map from instruction to vector shape

Output:
True iff I can be transformed

1: function AnalyzeInstruction(I, S)
2:   if S(I) ≠ varying then
3:     return False ▷ I must be varying
4:   end if
5:   if I = alloc T then
6:     if T = [T1 × N] then ▷ Analyze arrays of structs
7:       S ← T1
8:     else
9:       S ← T
10:    end if
11:   end if
12:   if S = struct(S1, . . . , Sn) then
13:     return AnalyzeUses(I, Arr, False)
14:   else
15:     return False ▷ Only applies to structs
16:   end if
17: end function

Once the algorithm reaches a leaf of the tree, the triangles contained in it are intersected with the ray, and only the closest intersection is kept. A typical use case for this algorithm is a global illumination renderer, where many of such queries have to be performed to produce a single image.

The algorithm is vectorized by assigning every SIMD lane a different ray:

for i in vectorize(vec_width, default_alignment, 0, N) {
  let ray = load_ray(i);
  let hit = traverse_bvh(bvh, ray);
  store_hit(i, hit);
}

Inside the traverse_bvh function, nodes are pushed on the stack whenever any ray intersects their bounding boxes:

let (mask, tentry, texit) =
intersect_ray_box(math, ray, node.bbox);
if any(mask) {
  if any(stack.top().tmin < tentry) {
    stack.push(child_id, tentry);
  } else {
    stack.push_after(child_id, tentry);
  }
}

Nodes are pushed in an approximate order on the stack, and we store their distance along the ray. This approximate sorting makes finding the closest intersection faster, and the distance can be used to cull nodes.
4.2 Performance

We compare the performance of our benchmarks in three versions: Vectorized with our optimization enabled, vectorized with our optimization disabled, and non-vectorized (scalar).

Overall, Table 1 shows that our transformation greatly improves performance, reaching sometimes up to $17 \times$ the speed of the non-optimized version. Without the transformation, vectorization is virtually useless, as the resulting code is slower than the non-vectorized version.

The reason for this huge gap is that our transformation makes the analyses in RV more precise. In our ray-tracing algorithm, the traversal stack is represented as an array of structures containing the distance to the node and its index into the array of nodes. Before the optimization, the stack is kept as a whole and therefore marked as varying by RV. The generated vector code then assumes that the control flow is not uniform, and generates masks and guards. After the optimization, the stack is split in two: One stack for the distance, and one for the index. RV marks the latter uniform, which in turn makes the traversal loop uniform. Therefore, no masks or guards are needed, and the generated code is similar to the hand written code in the Embree library, a ray tracing library by Intel.

With the simpler line drawing algorithm (Table 2), the difference is only a factor of 2 over the vectorized variant. This shows that our transformation is more beneficial to complex algorithms. Indeed, smaller programs have simpler control flow, and hence fewer opportunities to remove redundant masking logic.

## 5 CONCLUSION

We have described a transformation that operates on an SSA-based IR. This transformation splits stack-allocated objects in order to improve existing vectorization analyses.

We proved that without our transformation, automatic vectorization fails to generate efficient code for a ray-tracing algorithm. For this algorithm, vectorization without our transformation is not a viable option, since the resulting code is slower than the scalar version. When our transformation is applied, the performance of the algorithm is within 10% of a hand-vectorized library by Intel.

Because this transformation is selective, it will not affect the whole program, but only the parts where the transformation is beneficial. Hence, the programmer can now use structures, arrays and aggregates without performance penalties.

## ACKNOWLEDGMENTS

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## REFERENCES


### Table 1: Performance in Mray/s (higher is better) of the ray tracing algorithm with vectorization enabled (with and without our transformation) and disabled (the scalar variant), in different scenes. The speedups in parentheses are reported with respect to the version with vectorization enabled without our transformation.

<table>
<thead>
<tr>
<th>Scene</th>
<th>With opt.</th>
<th>Without opt.</th>
<th>Scalar</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sponza</td>
<td>5.79 (×17)</td>
<td>0.34</td>
<td>0.88</td>
</tr>
<tr>
<td>Crown</td>
<td>15.33 (×14)</td>
<td>1.08</td>
<td>3.27</td>
</tr>
<tr>
<td>San-Miguel</td>
<td>3.13 (×16)</td>
<td>0.19</td>
<td>0.53</td>
</tr>
<tr>
<td>Powerplant</td>
<td>6.69 (×15)</td>
<td>0.45</td>
<td>1.38</td>
</tr>
</tbody>
</table>

### Table 2: Performance in Mline/s (higher is better) of the line drawing algorithm with vectorization enabled (with and without our transformation) and disabled (the scalar variant). The speedups in parentheses are reported with respect to the version with vectorization enabled without our transformation.

<table>
<thead>
<tr>
<th></th>
<th>With opt.</th>
<th>Without opt.</th>
<th>Scalar</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>32.31 (×2)</td>
<td>15.41</td>
<td>14.63</td>
</tr>
</tbody>
</table>
We show the x86 assembly after vectorization by RV with our optimization disabled (4a) and enabled (4b). We also provide the assembly generated by LLVM for the ray-box intersection routine of Embree (4c), a manually vectorized ray-tracing library by Intel. For brevity, we do not reproduce the listing in 4a in its entirety.

\[\text{(a) Assembly without our transformation} \quad \text{(b) Assembly with our transformation} \quad \text{(c) Reference assembly in Embree}\]

Figure 4: Comparison of the assembly generated by LLVM for the ray-box intersection routine of our ray-tracing algorithm.

We show the x86 assembly after vectorization by RV with our optimization disabled (4a) and enabled (4b). We also provide the assembly generated by LLVM for the ray-box intersection routine of Embree (4c), a manually vectorized ray-tracing library by Intel. For brevity, we do not reproduce the listing in 4a in its entirety.


