

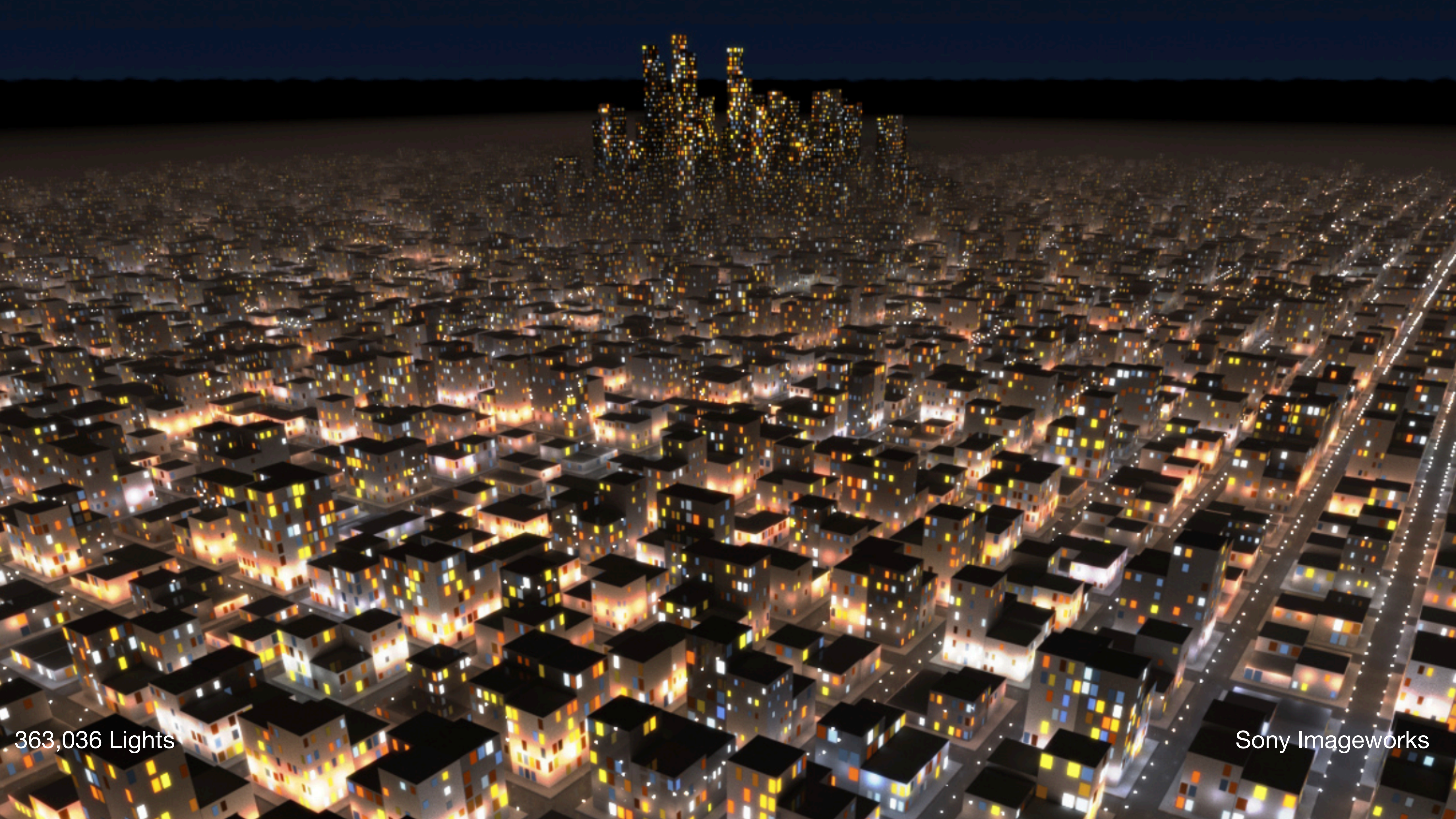
Many Light Methods

Gurprit Singh

Philipp Slusalek

Karol Myszkowski

Captured: Andrey Vasiliskov
Owner: Gurprit Singh



363,036 Lights

Sony Imageworks



Creator and Credit: Paul Thouvenin Copyright: olweb



Captured: Andrey Vasiliskov
Owner: Gurprit Singh



<https://www.oberlin.edu/dye-lecture-hall>

Overview

Instant Radiosity

Virtual Point Lights

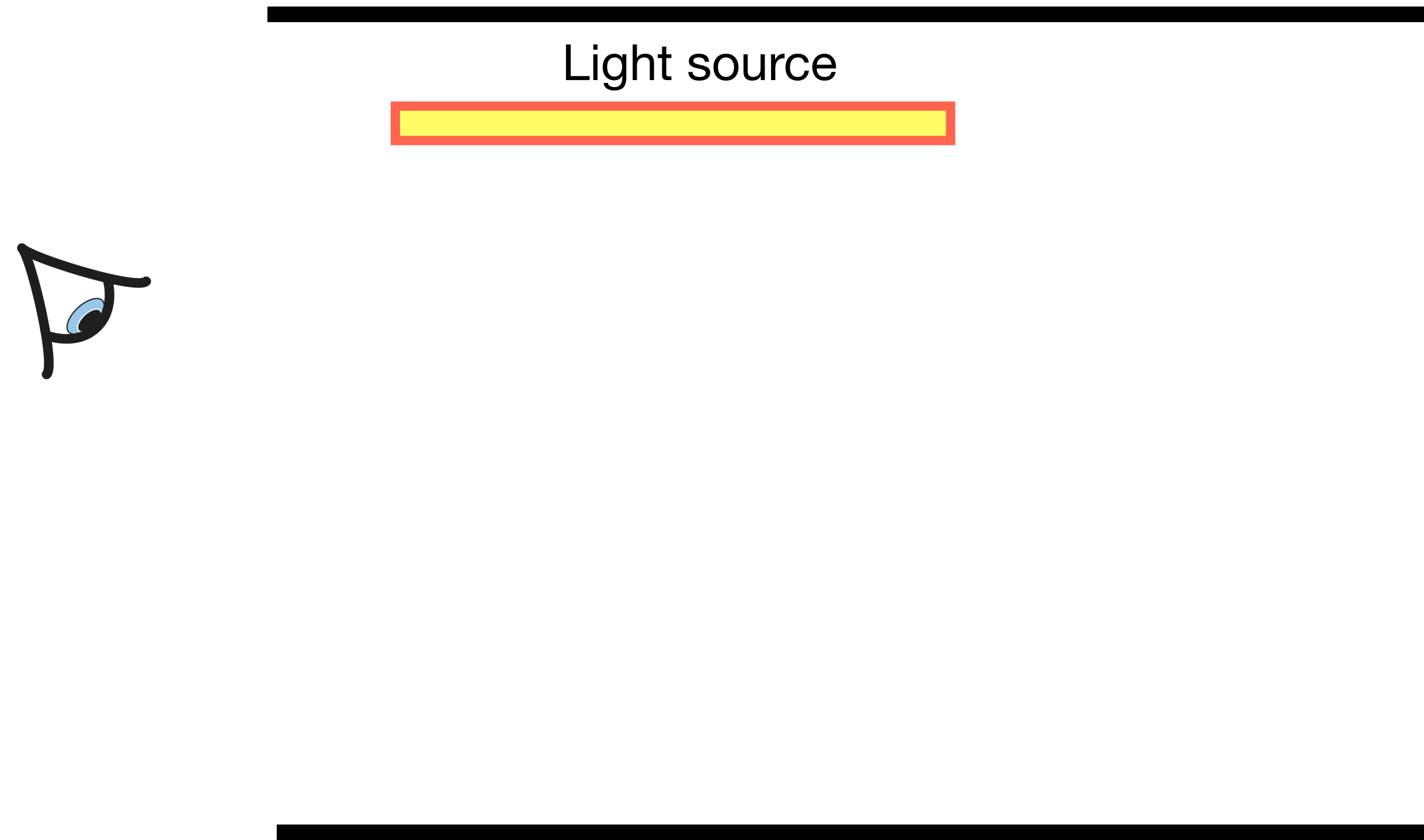
Virtual Ray Lights

LightCuts

Stochastic LightCuts

Lighting Grid Hierarchy

Bidirectional Path Tracing

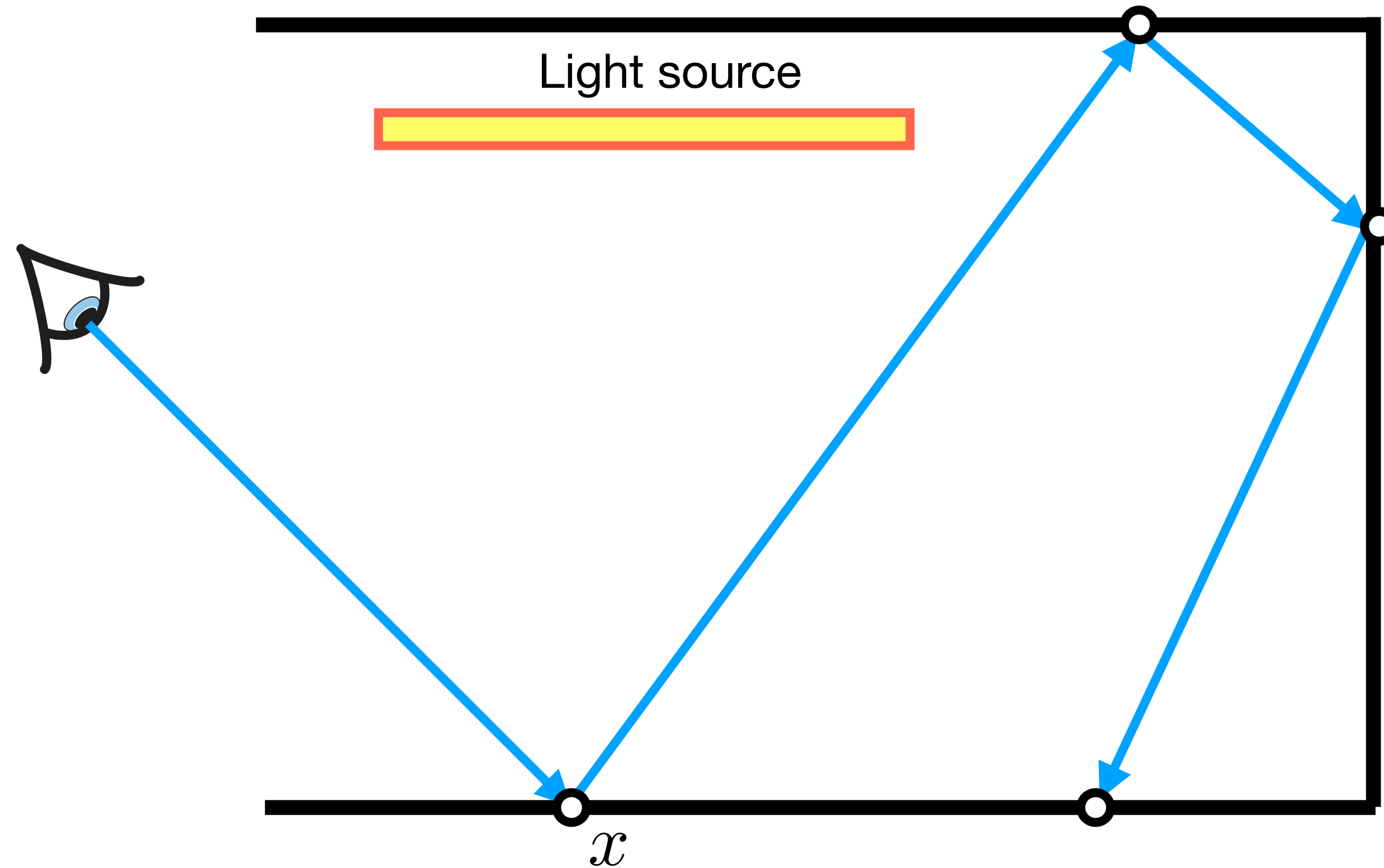


$$L(x, \omega) = L_e(x, \omega) + \int_{\mathcal{H}^2} f(x, \omega', \omega) L(r(x, \omega'), -\omega') \cos \theta' d\omega'$$

$$\approx L_e(x, \omega) + \frac{f(x, \omega', \omega) L(r(x, \omega'), -\omega') \cos \theta'}{p(\omega')}$$

7

Bidirectional Path Tracing

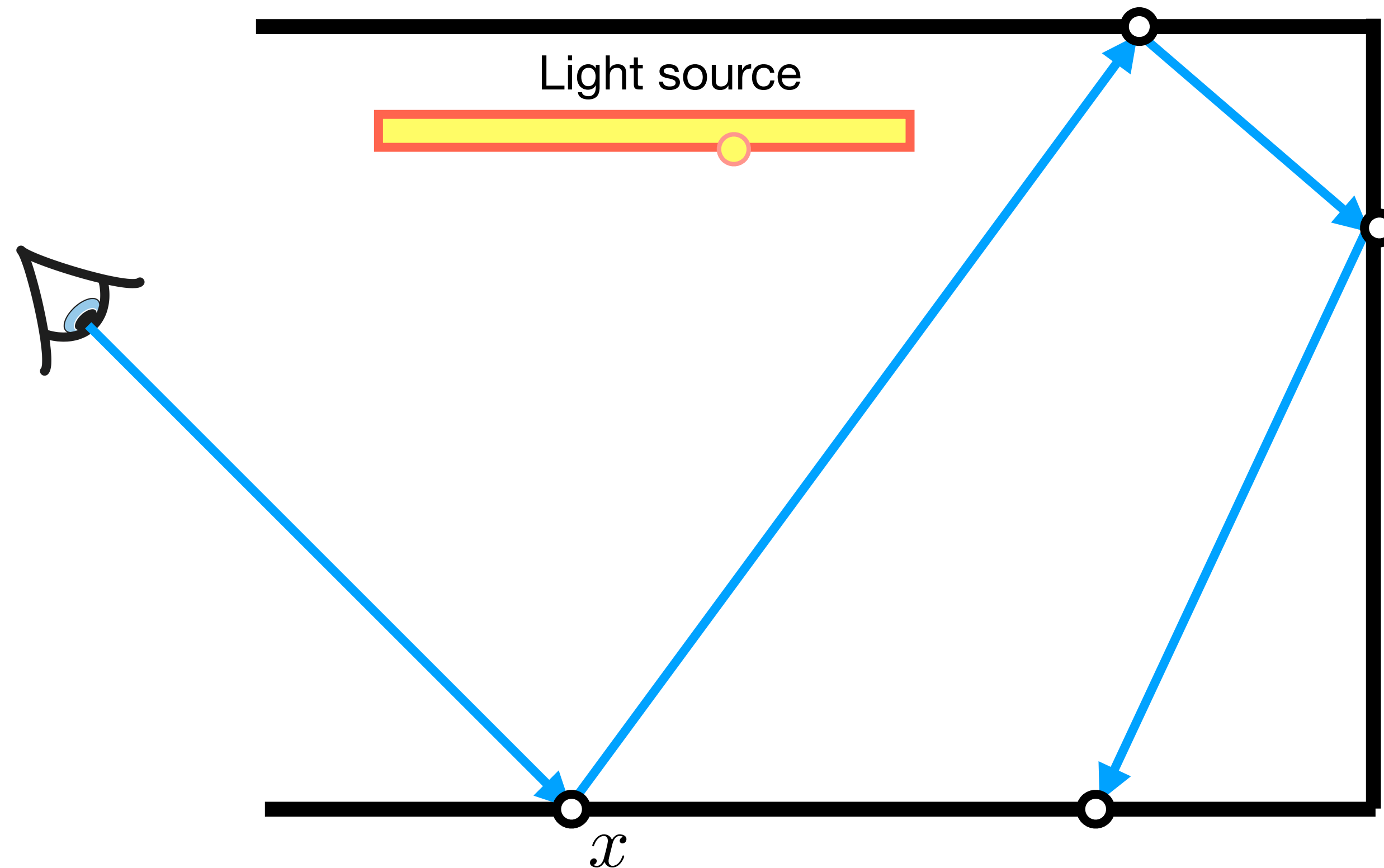


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Bidirectional Path Tracing

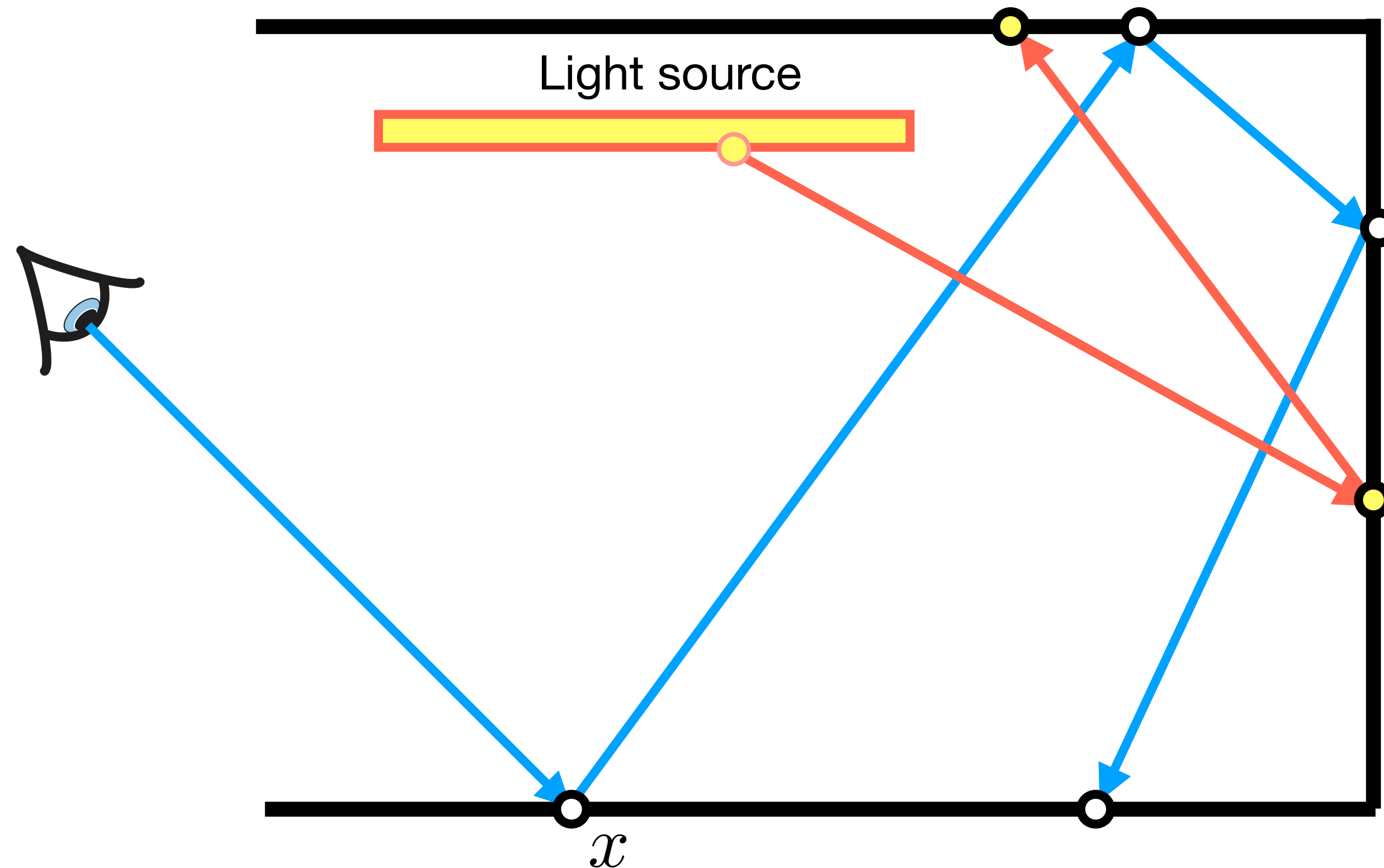


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Bidirectional Path Tracing

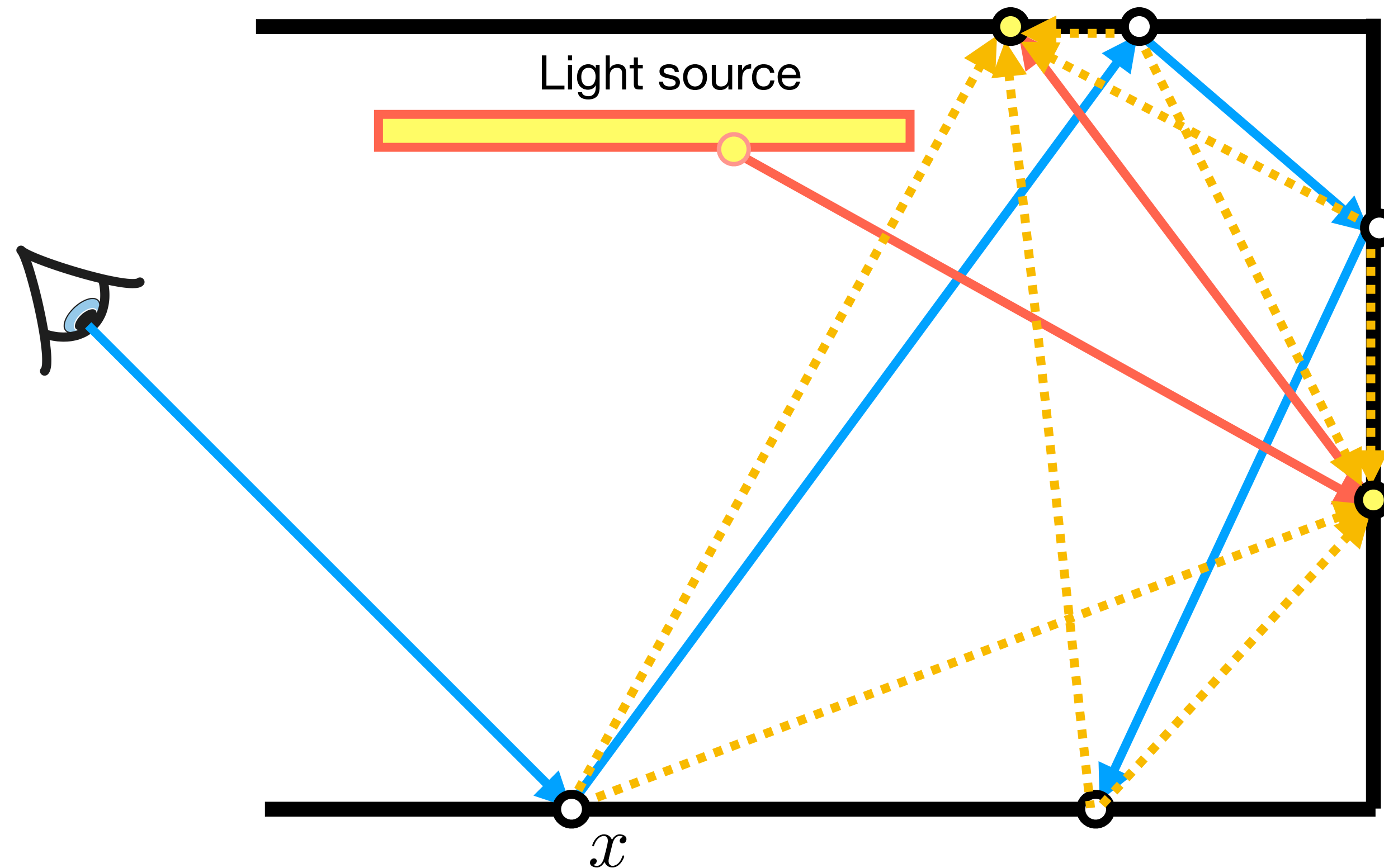


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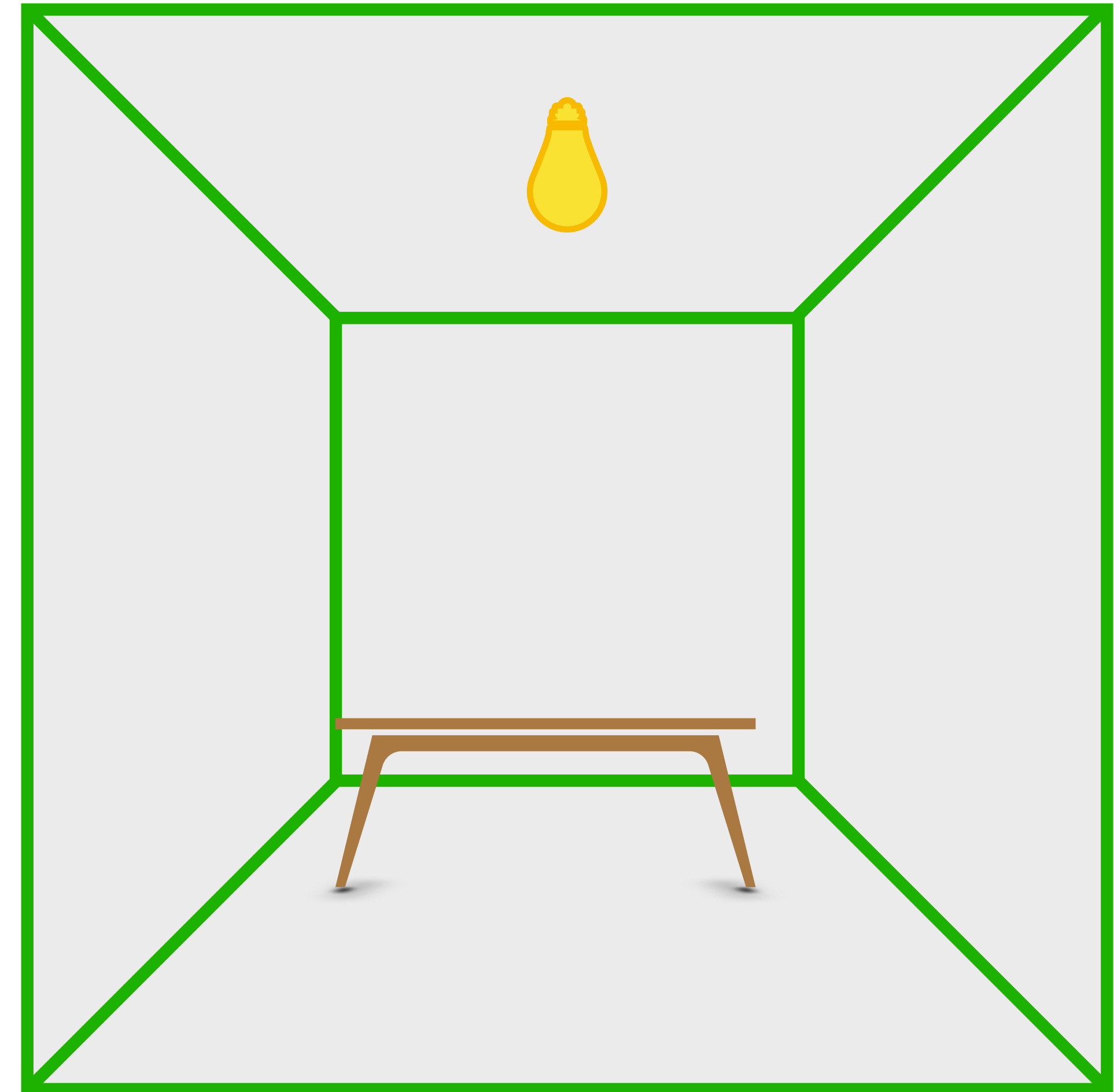
Instant Radiosity

Virtual Point Light: Generation

Step 1:

- Trace paths from light source(s)
- Treat path vertices as Virtual Point Lights (VPLs)

Pass 1

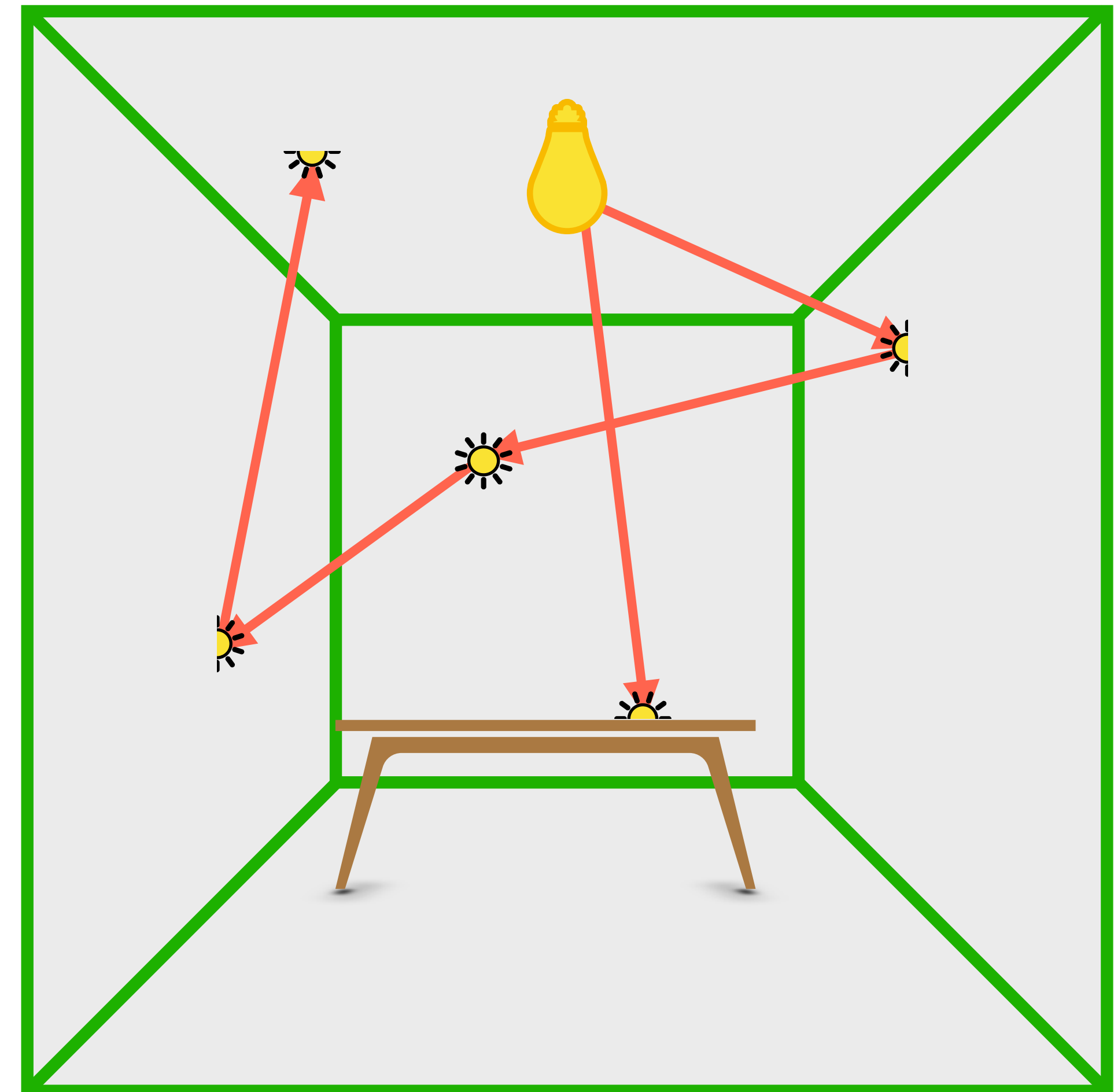


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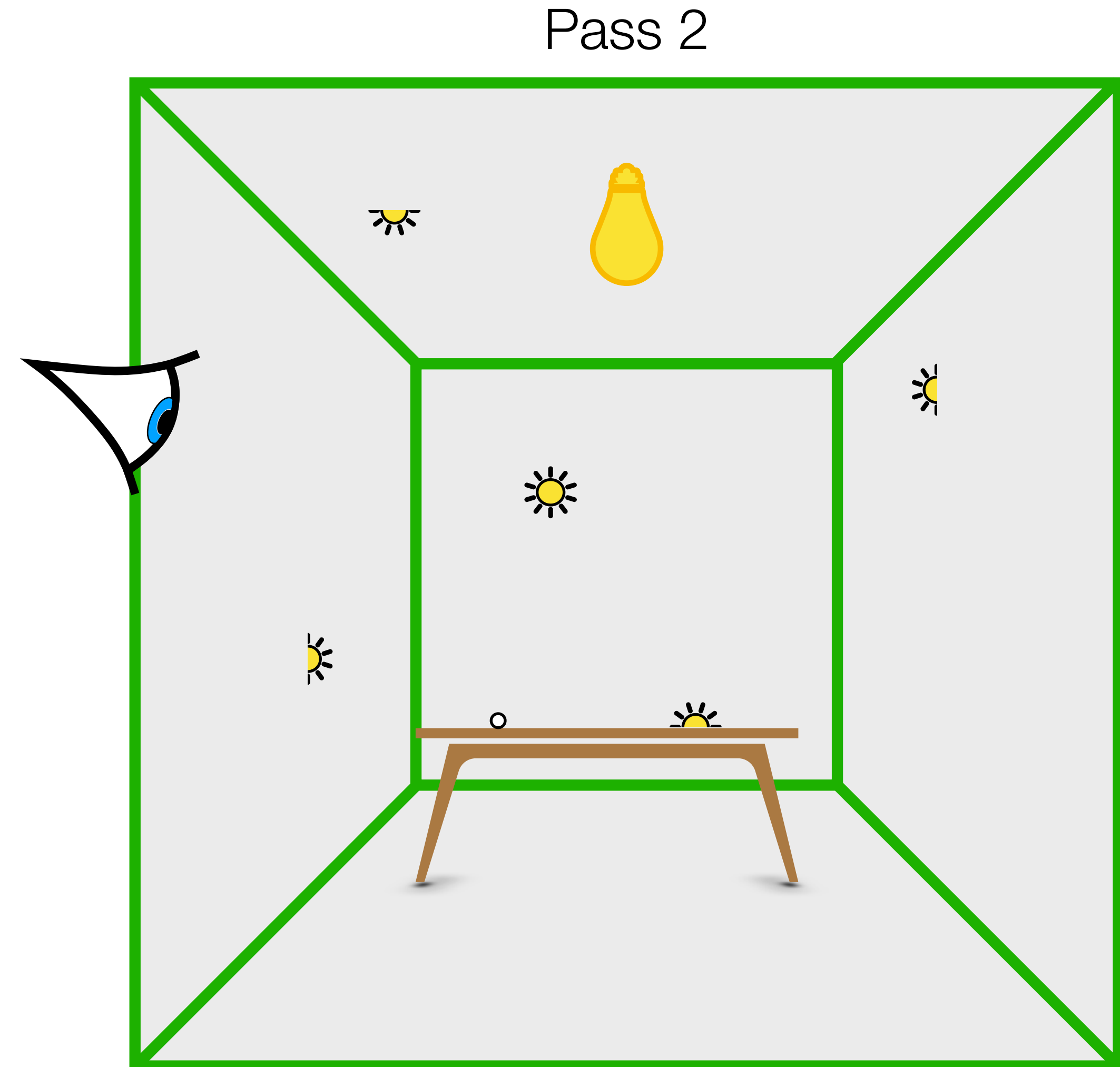
Virtual Point Light: Lighting

Step 1:

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Step 2:

- Render scene with VPLs



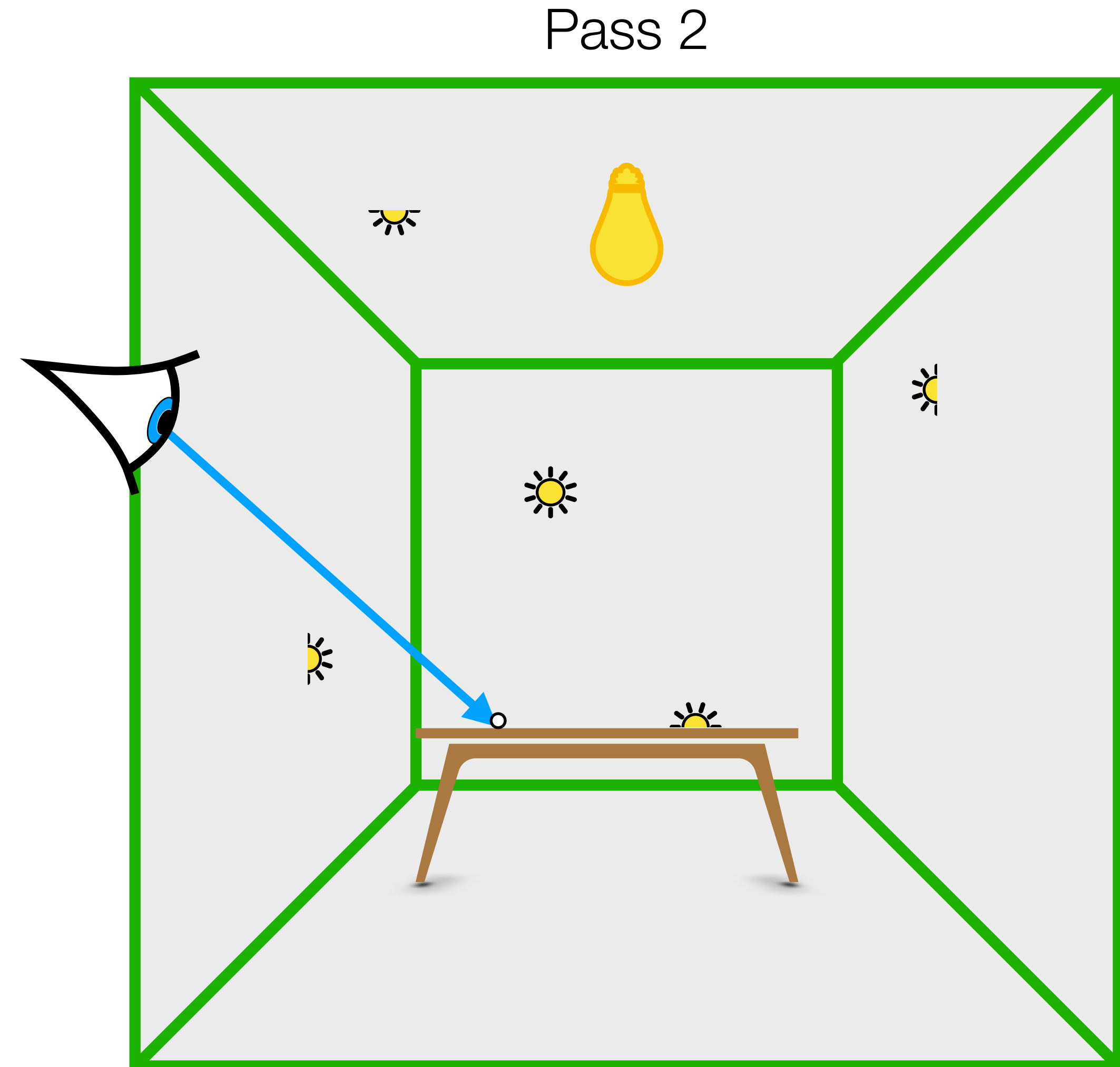
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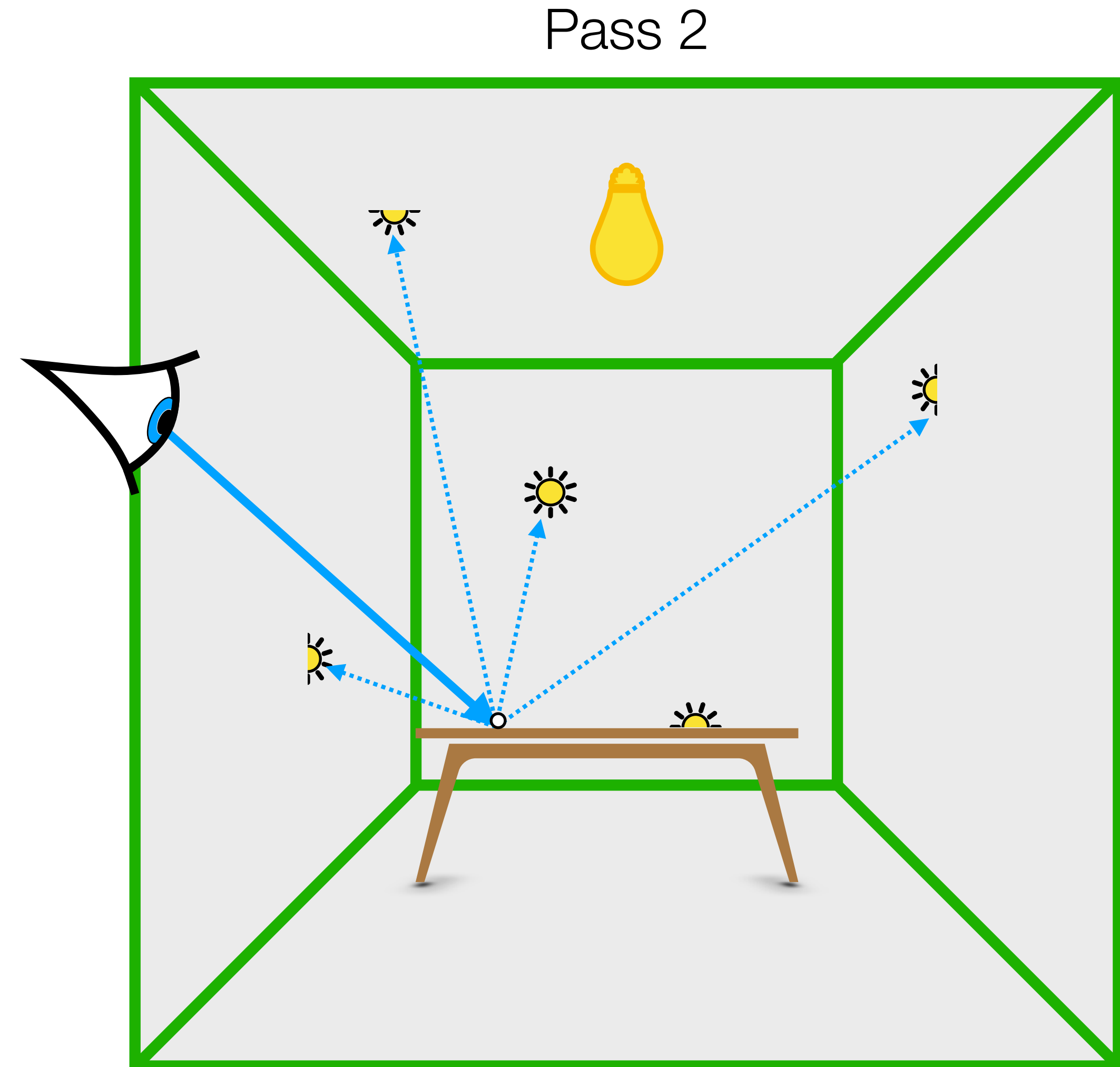
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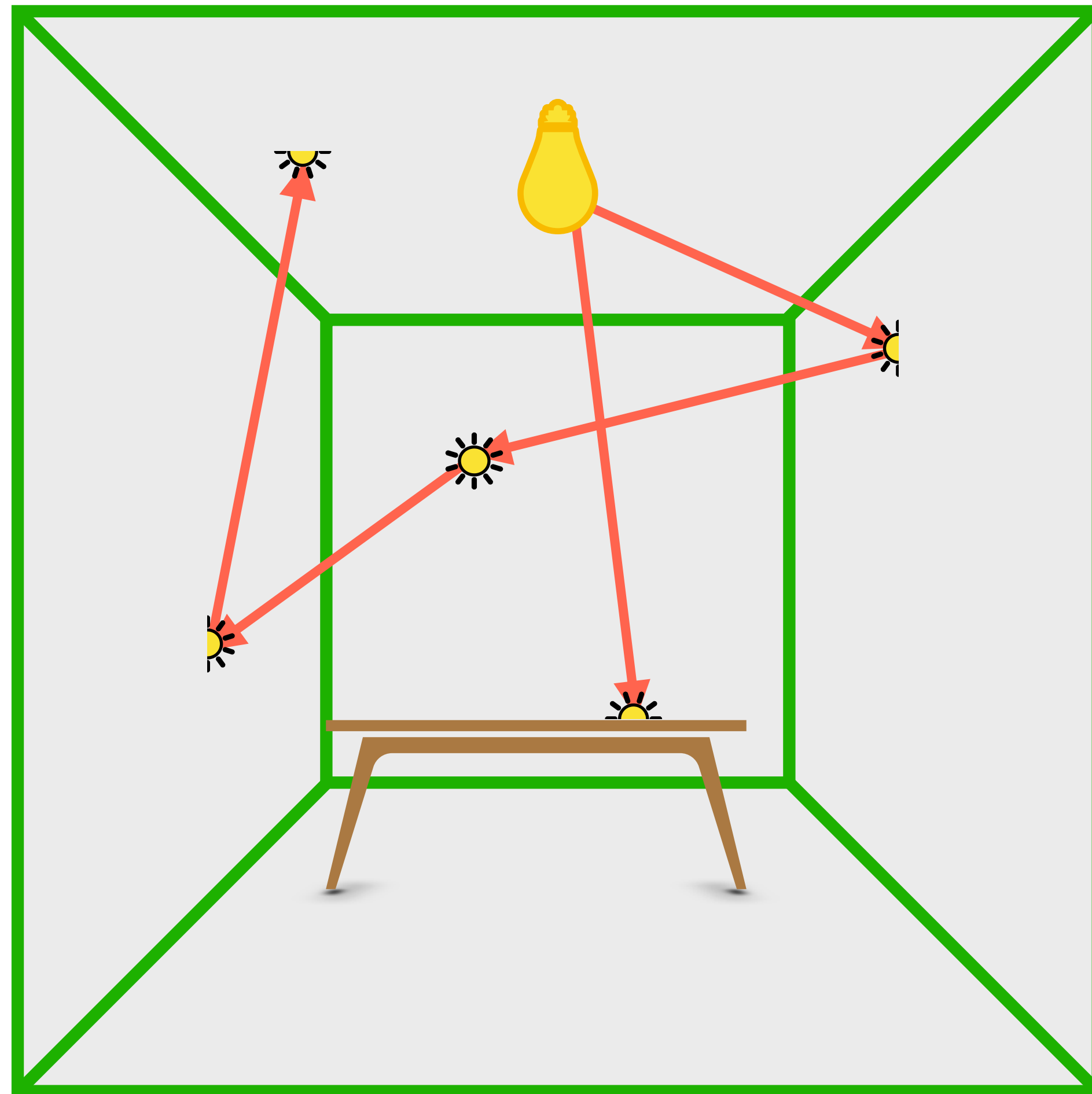
Step 2:

- Render scene with VPLs

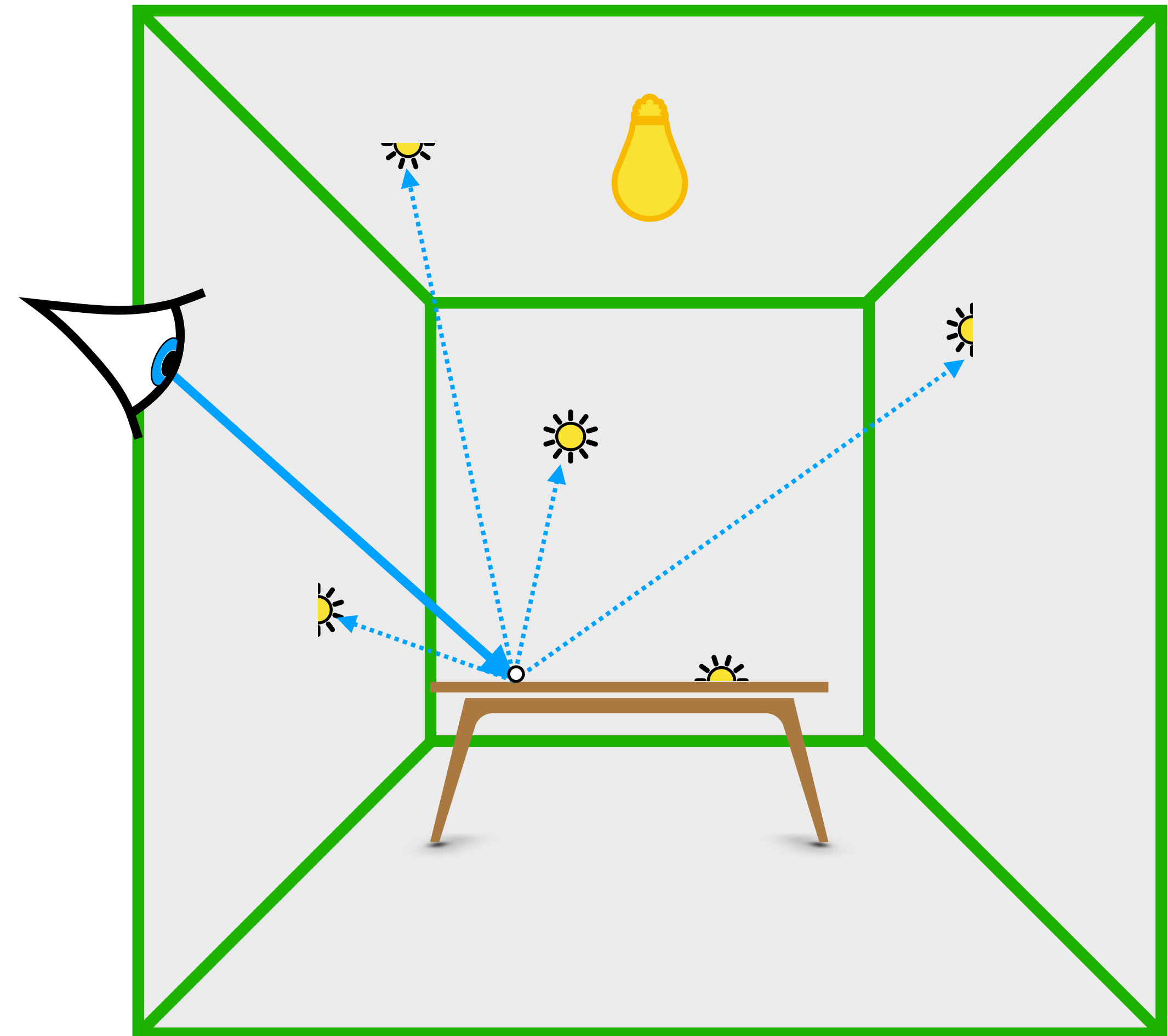


Virtual Point Light: Two-Pass

Pass 1: Generating VPLs

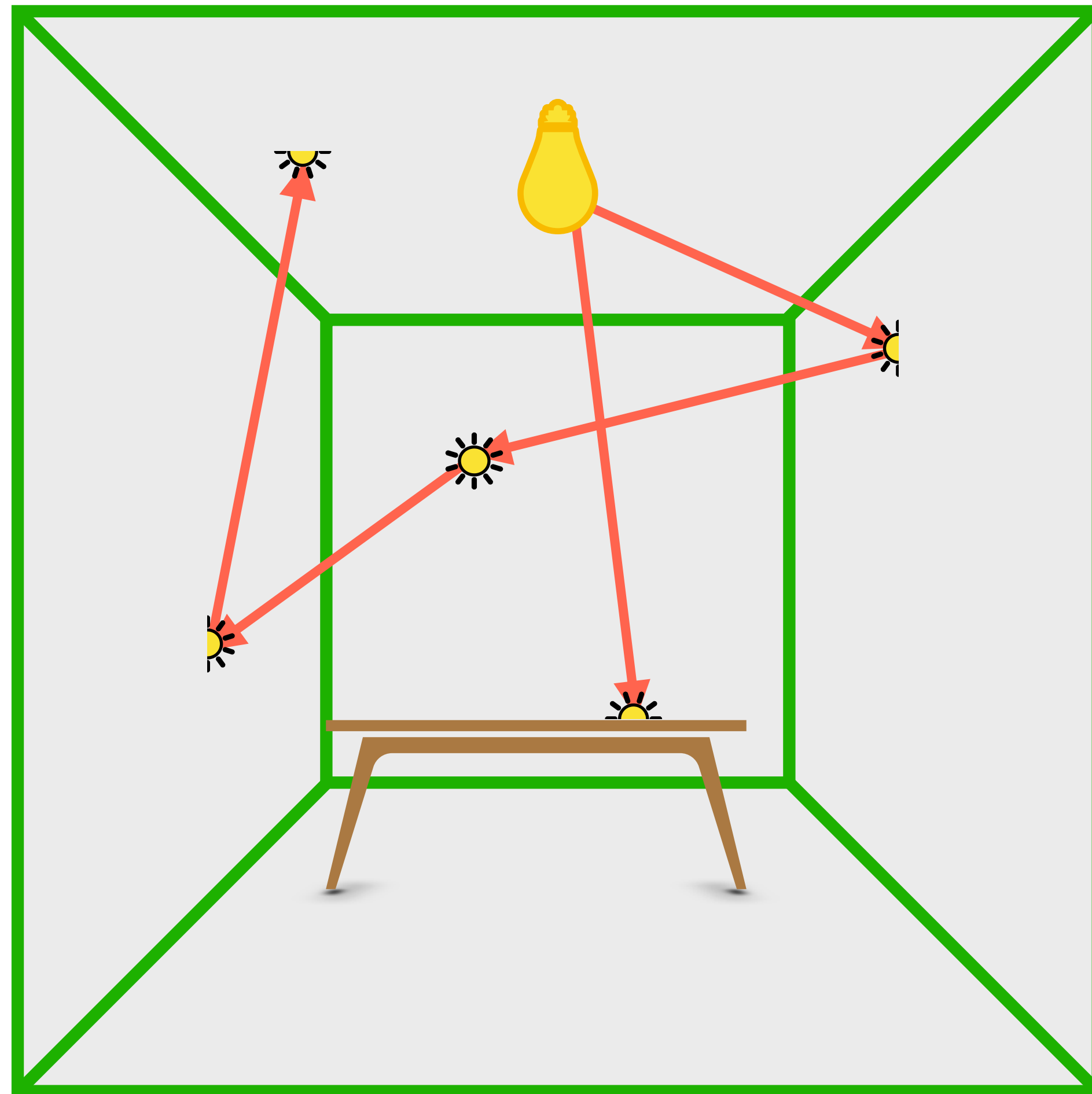


Pass 2: Lighting with VPLs

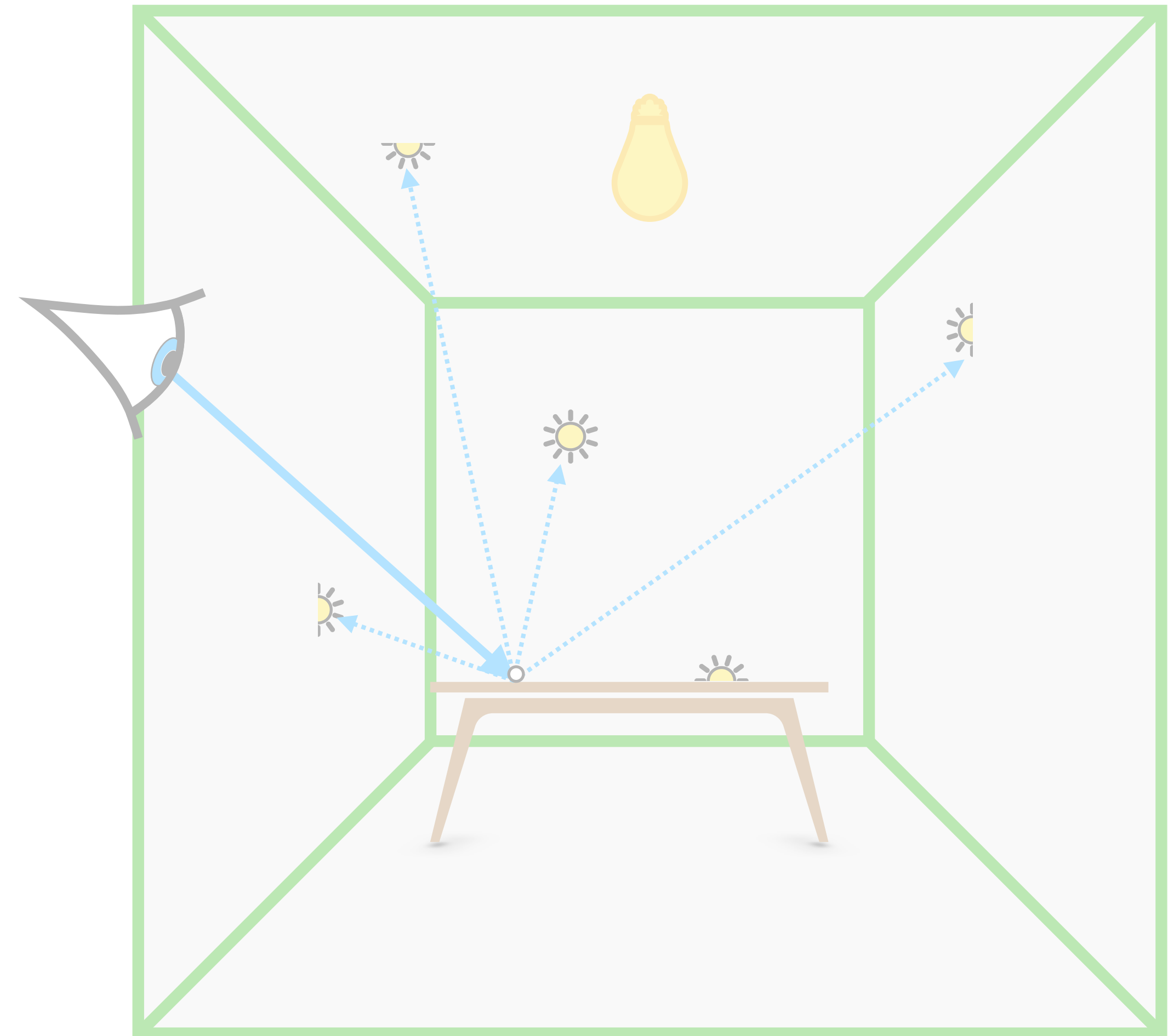


Virtual Point Light: Two-Pass

Pass 1: Generating VPLs



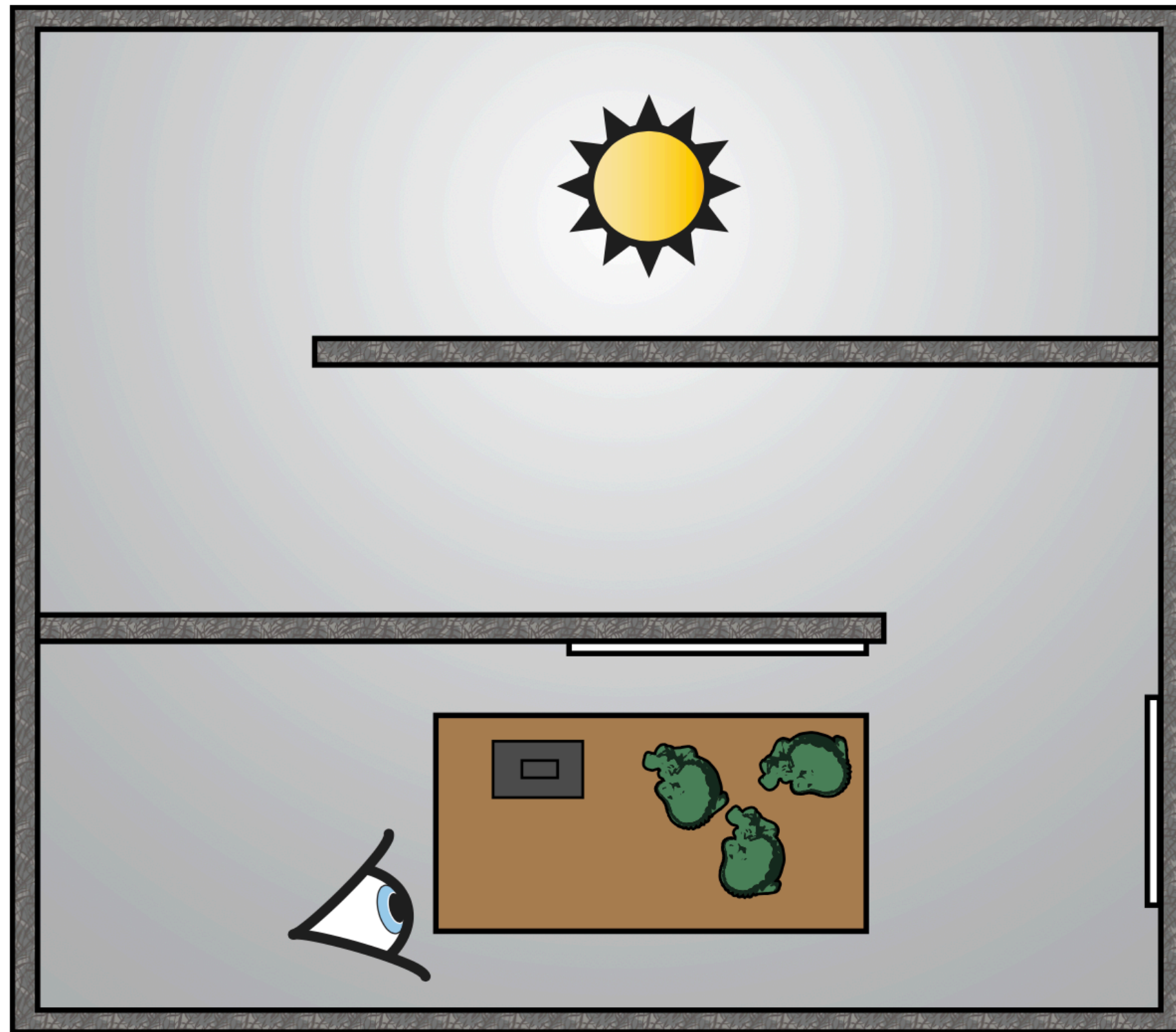
Pass 2: Lighting with VPLs



Generating Virtual Point Lights (VPLs)

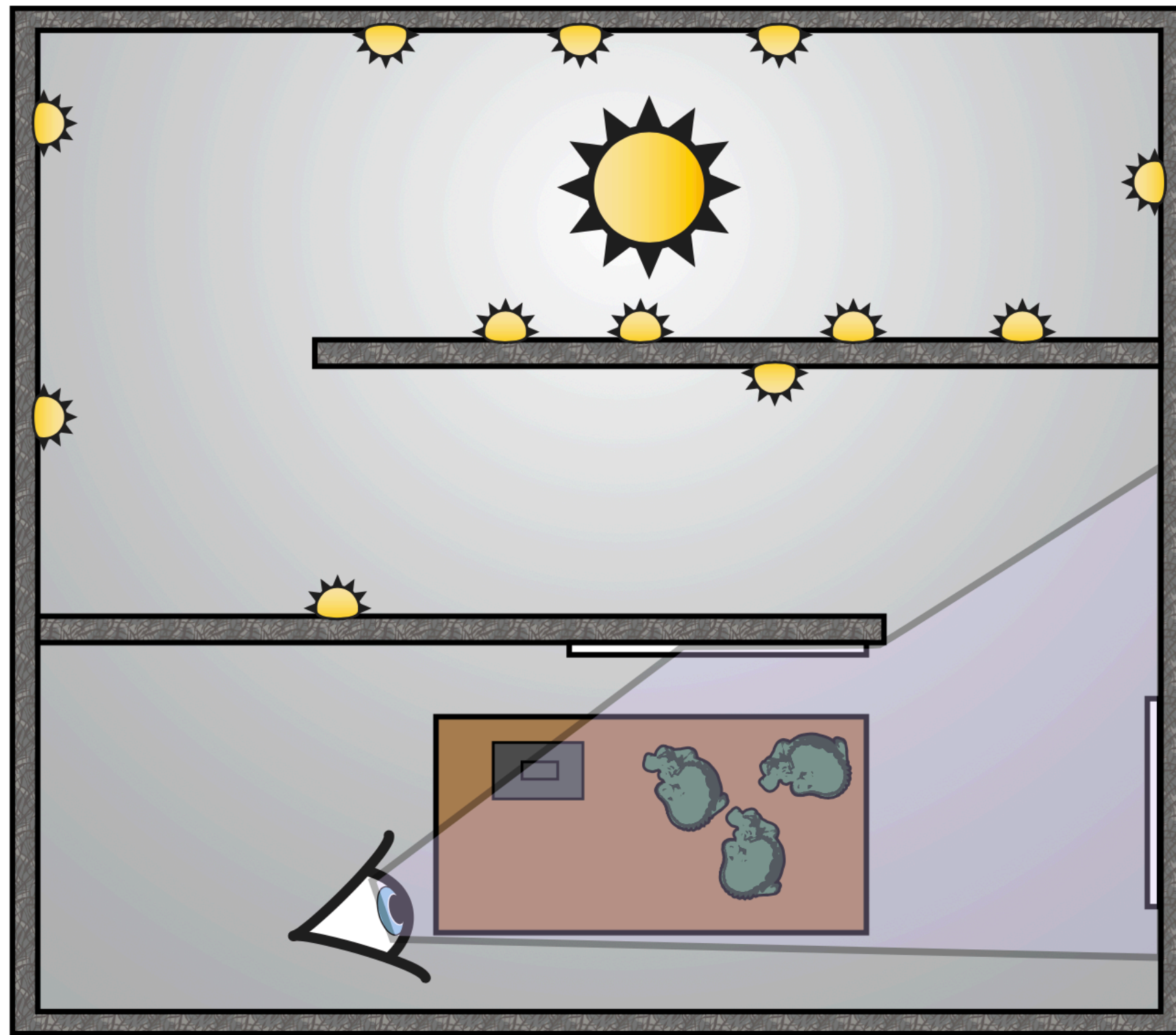
Naive Generation of VPLs

Problem 1 (in complex scenes): - many VPLs do not contribute



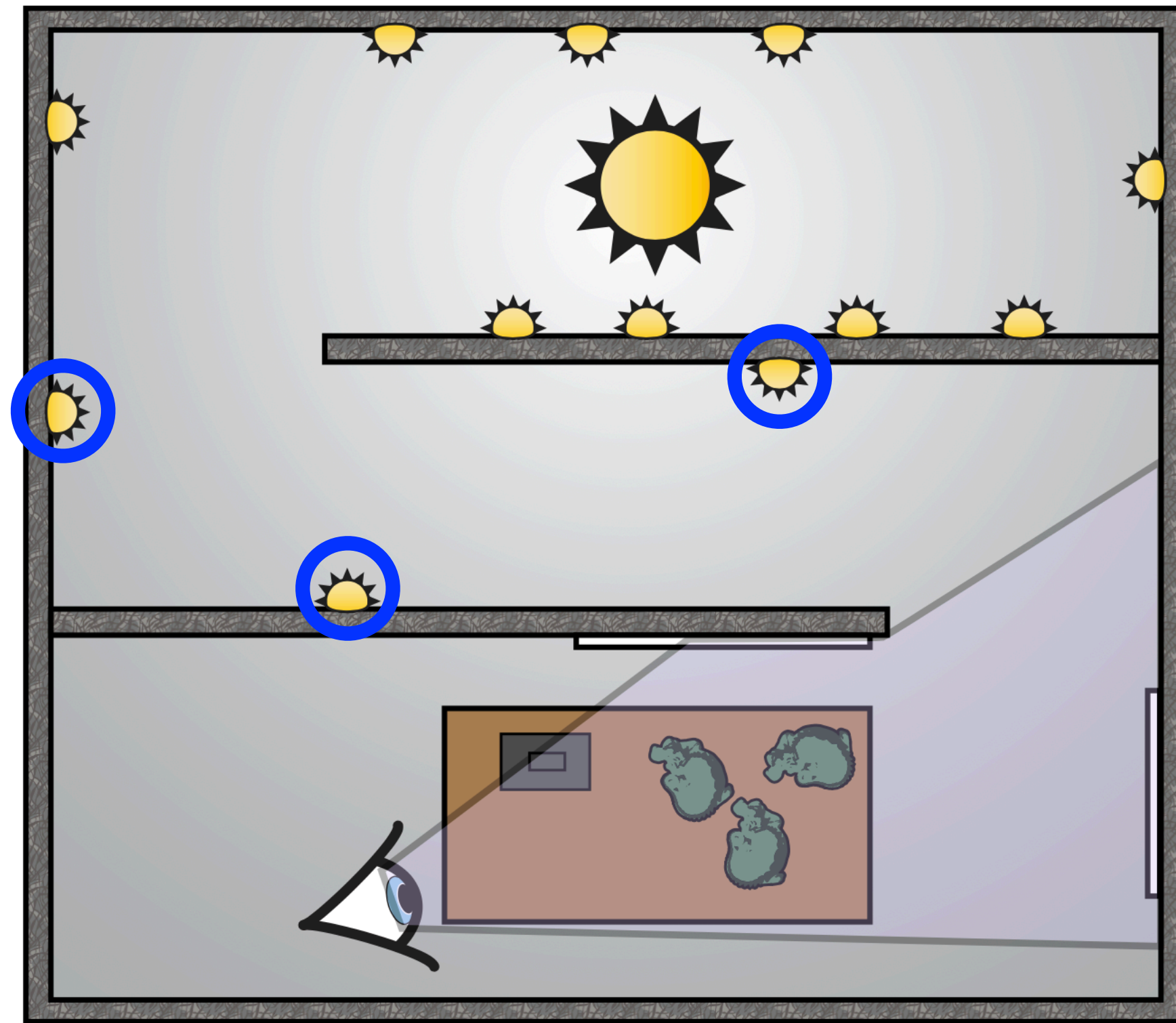
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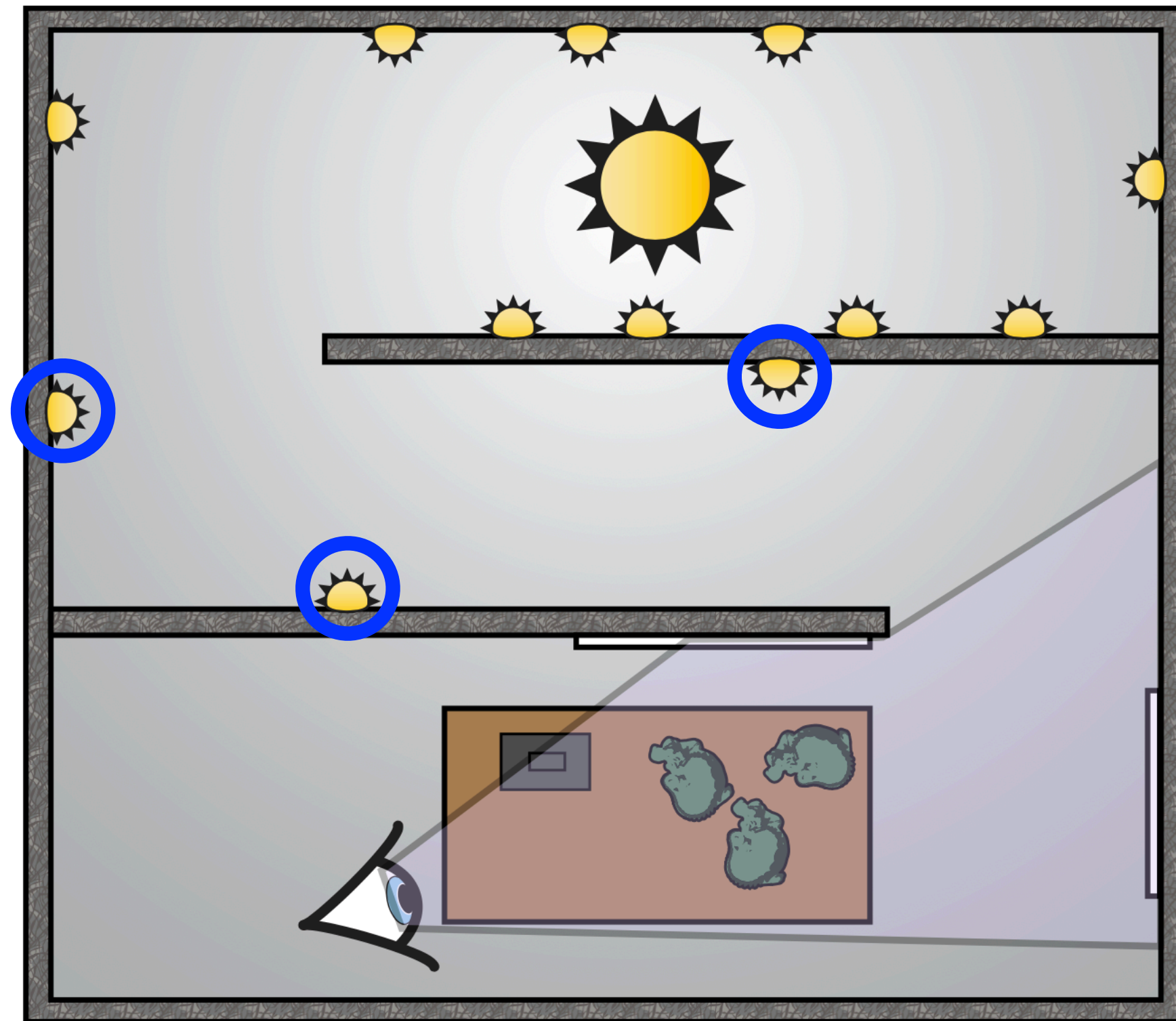
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Naive Generation of VPLs

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Instant Radiosity



Reference

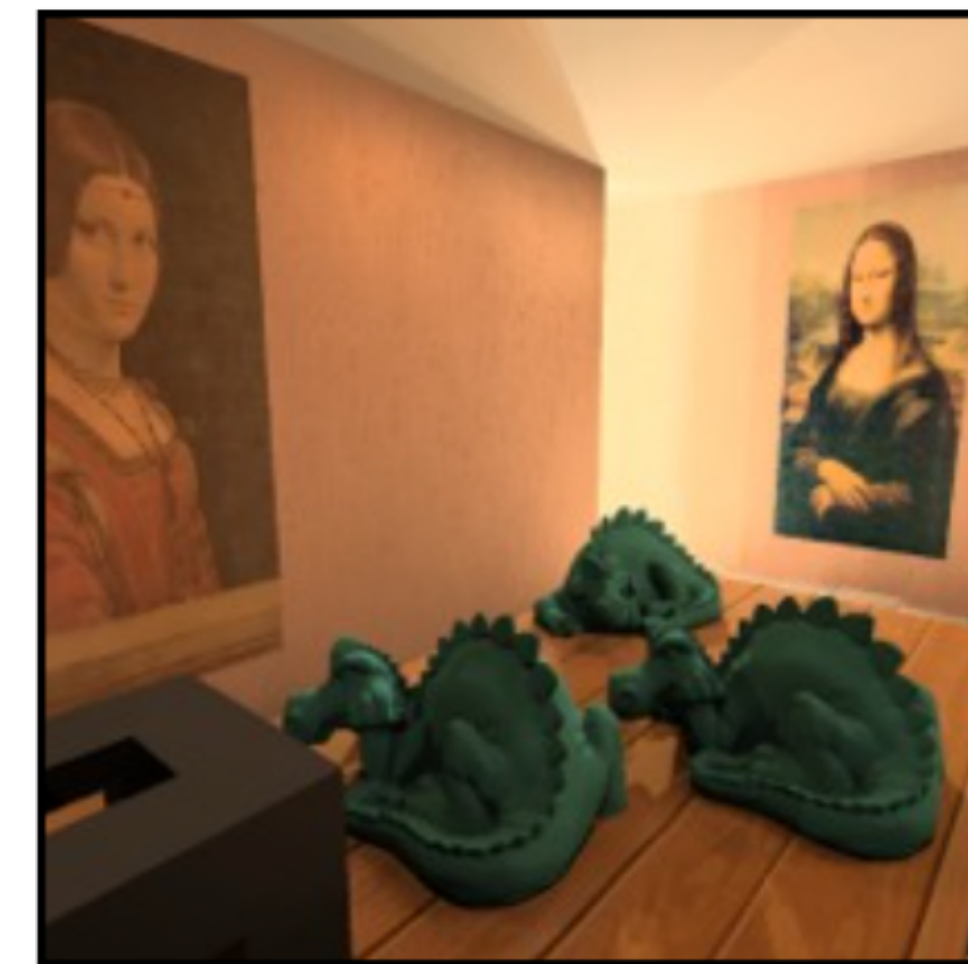


Image courtesy Segovia et al.

Naive Generation of VPLs

Problem 2 (in glossy scenes): - Glossy inter-reflections suffer from splotches

Naive Generation of VPLs

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Instant Radiosity



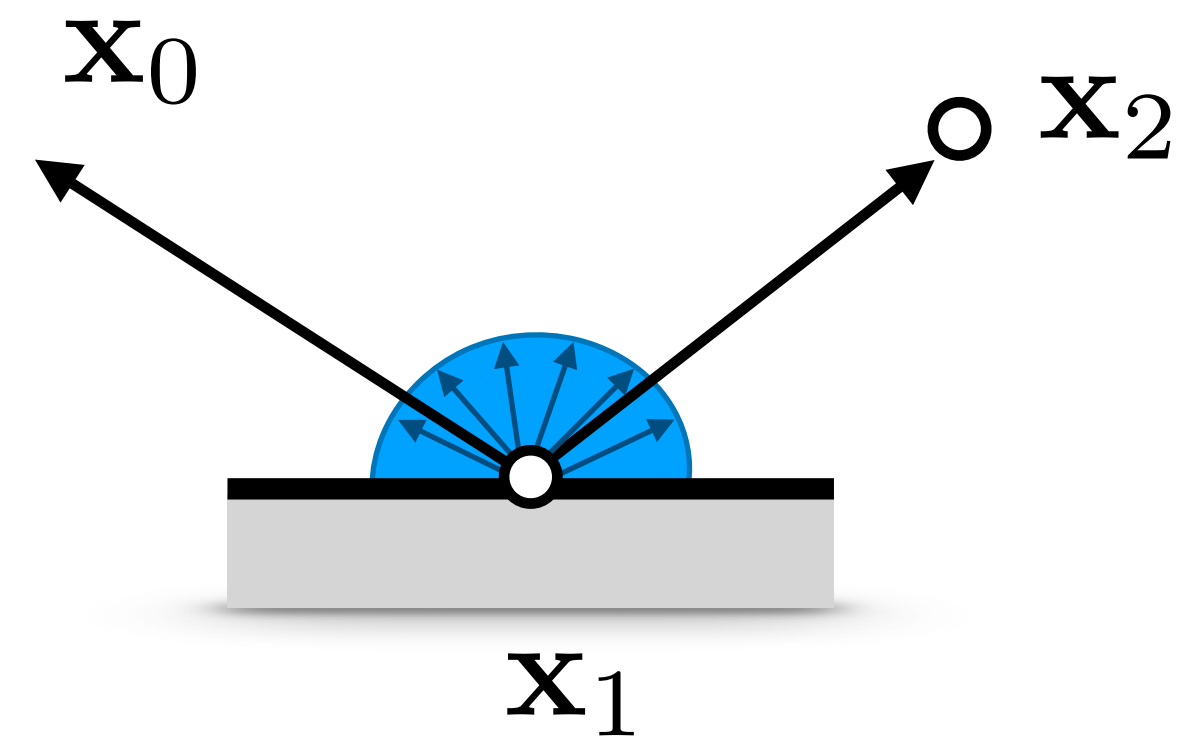
Naive Generation of VPLs

Problem 2 (in glossy scenes): - Glossy inter-reflections suffer from splotches

Instant Radiosity



Instant radiosity assumes all surfaces are diffuse



Naive Generation of VPLs

Problem 2 (in glossy scenes): - Glossy inter-reflections suffer from splotches

Instant Radiosity



Naive Generation of VPLs

Problem 2 (in glossy scenes): - Glossy inter-reflections suffer from splotches

Instant Radiosity



Clamped



Naive Generation of VPLs

Problem 2 (in glossy scenes): - Glossy inter-reflections suffer from splotches

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Clamped



Reference



Naive Generation of VPLs

- Problem 2 (in glossy scenes):
- Glossy inter-reflections suffer from splotches
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Instant Radiosity



Clamped



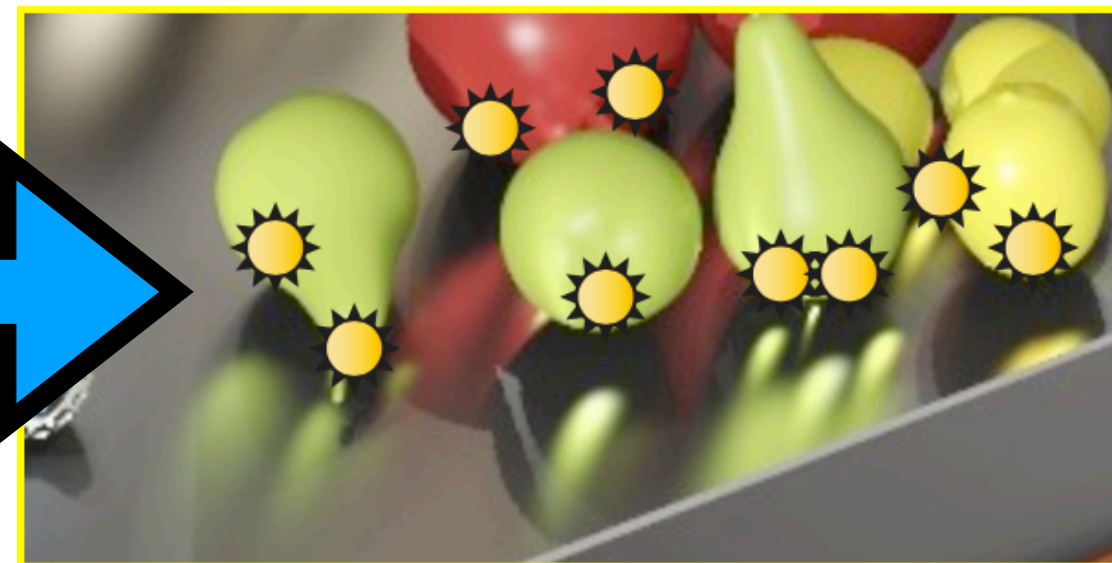
Reference



Naive Generation of VPLs

- Problem 2 (in glossy scenes):
- Glossy inter-reflections suffer from splotches
 - Insufficient number of VPLs in some regions

Instant Radiosity



Reference



Improved Generation of VPLs

Goal:

- place VPLs only where needed

Approaches:

Rejection of unimportant VPLs [Gerogiev and Slusallek 2010]

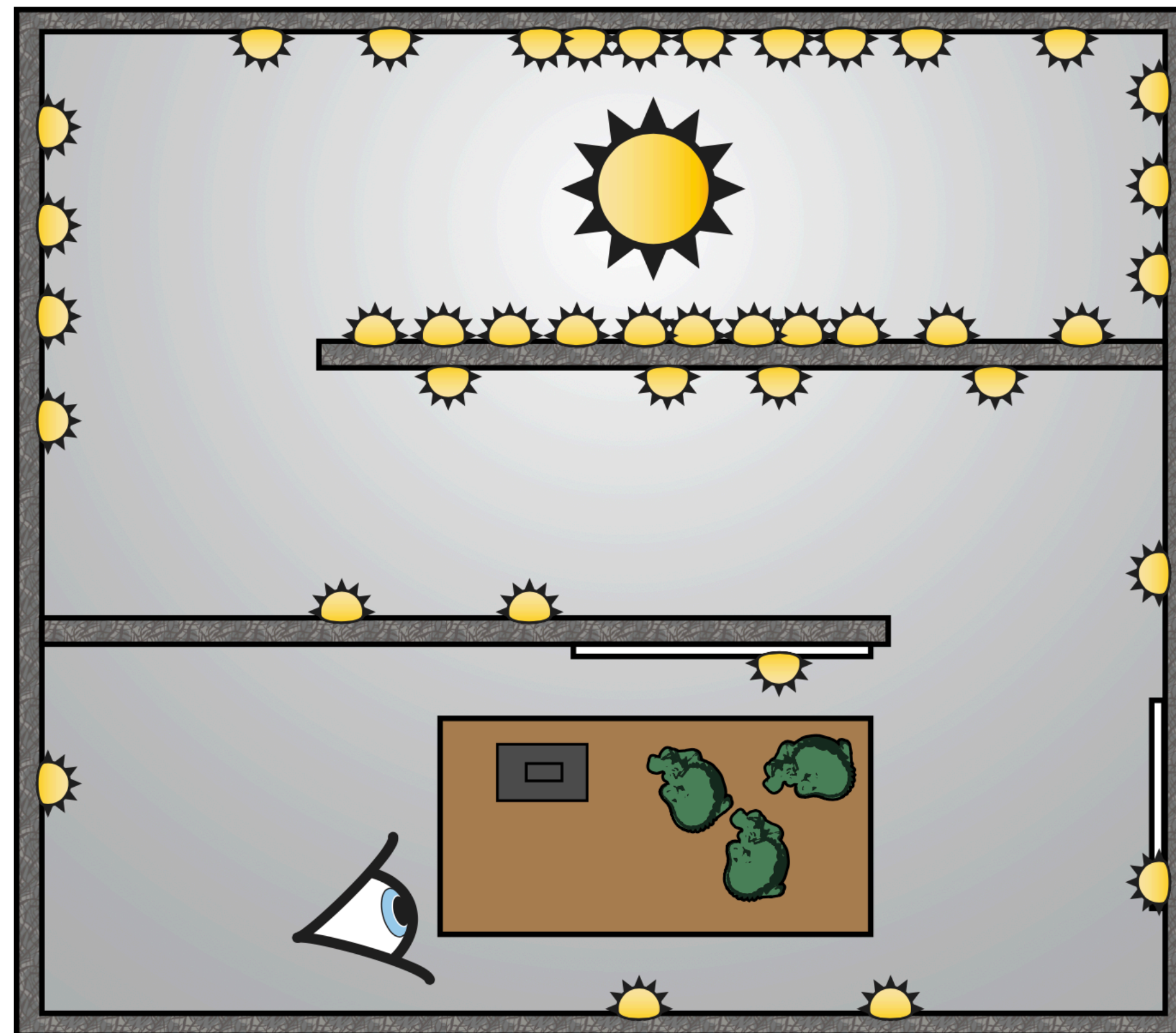
Bidirectional Instant Radiosity [Segovia et al. 2006]

Metropolis sampling for VPL distributions [Segovia et al. 2007]

Improved Generation of VPLs

Rejection of unimportant VPLs [Gerogiev and Slusallek 2010]

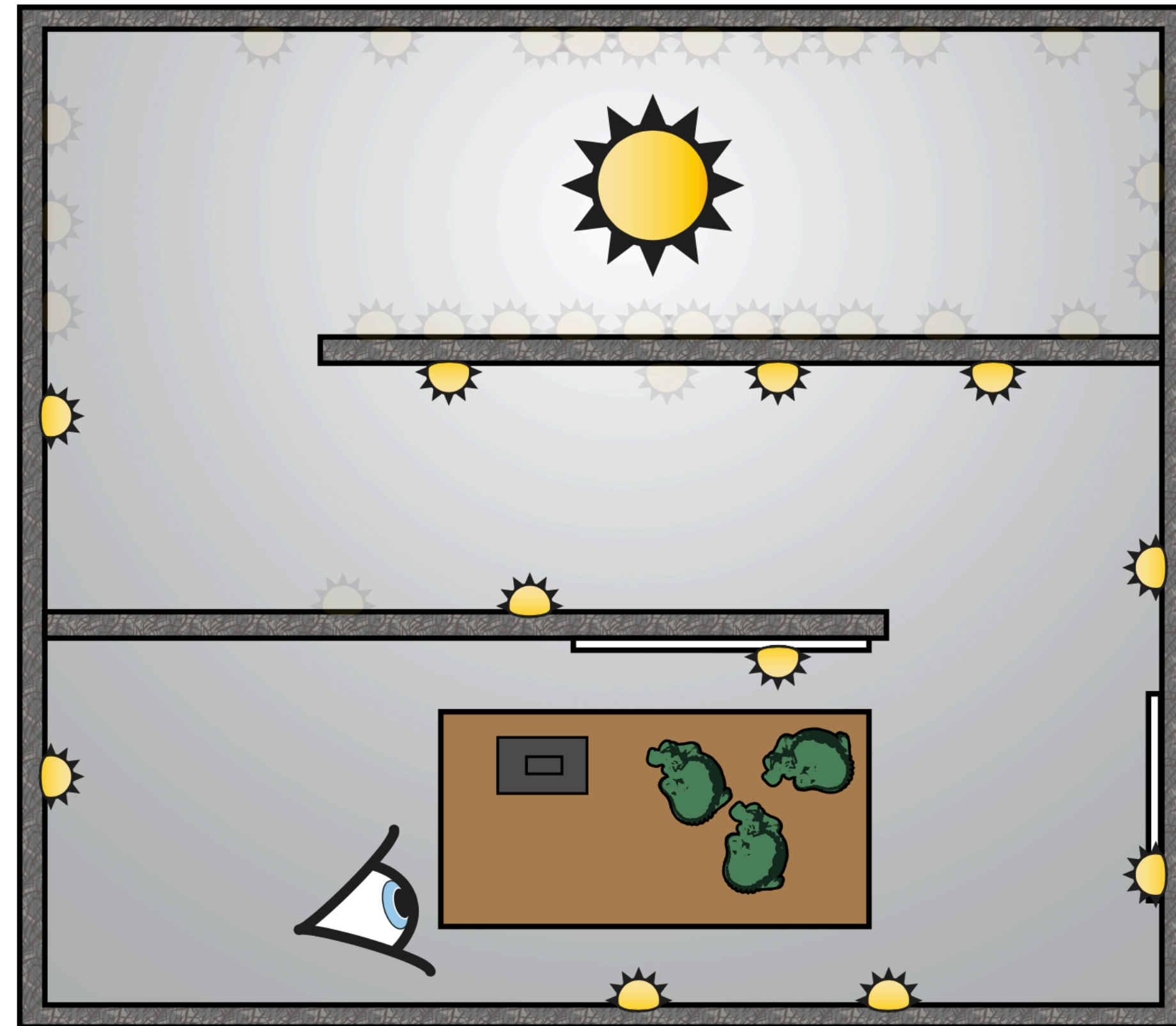
- probabilistically reject VPLs with low expected contribution



Improved Generation of VPLs

Rejection of unimportant VPLs [Gerogiev and Slusallek 2010]

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Improved Generation of VPLs

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Approach:

Improved Generation of VPLs

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Approach:

1) estimate average contribution of a VPL Φ_v

- few pilot VPLs illuminate few surface points seen by the camera

Improved Generation of VPLs

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- 2) generate VPLs

Improved Generation of VPLs

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 - for each VPL
 - estimate its contribution Φ_i to points seen by the camera

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- accept with probability $p_i = \min \left(\frac{\Phi_i}{\Phi_v} + \epsilon, 1 \right)$

Improved Generation of VPLs

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 - If accepted, divide its energy by p_i

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} Russian roulette

Improved Generation of VPLs

Rejection of unimportant VPLs [Gerogiev and Slusallek 2010]

Advantages:

Cheap and simple to implement!

VPLs have roughly equal contribution

Works well most of the time

Improved Generation of VPLs

Rejection of unimportant VPLs [Gerogiev and Slusallek 2010]

Advantages:

- Cheap and simple to implement!

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- Works well most of the time

Disadvantages:

- Increase the cost of VPL distribution

- "one-pixel image" assumption

- Does not help with local inter-reflections

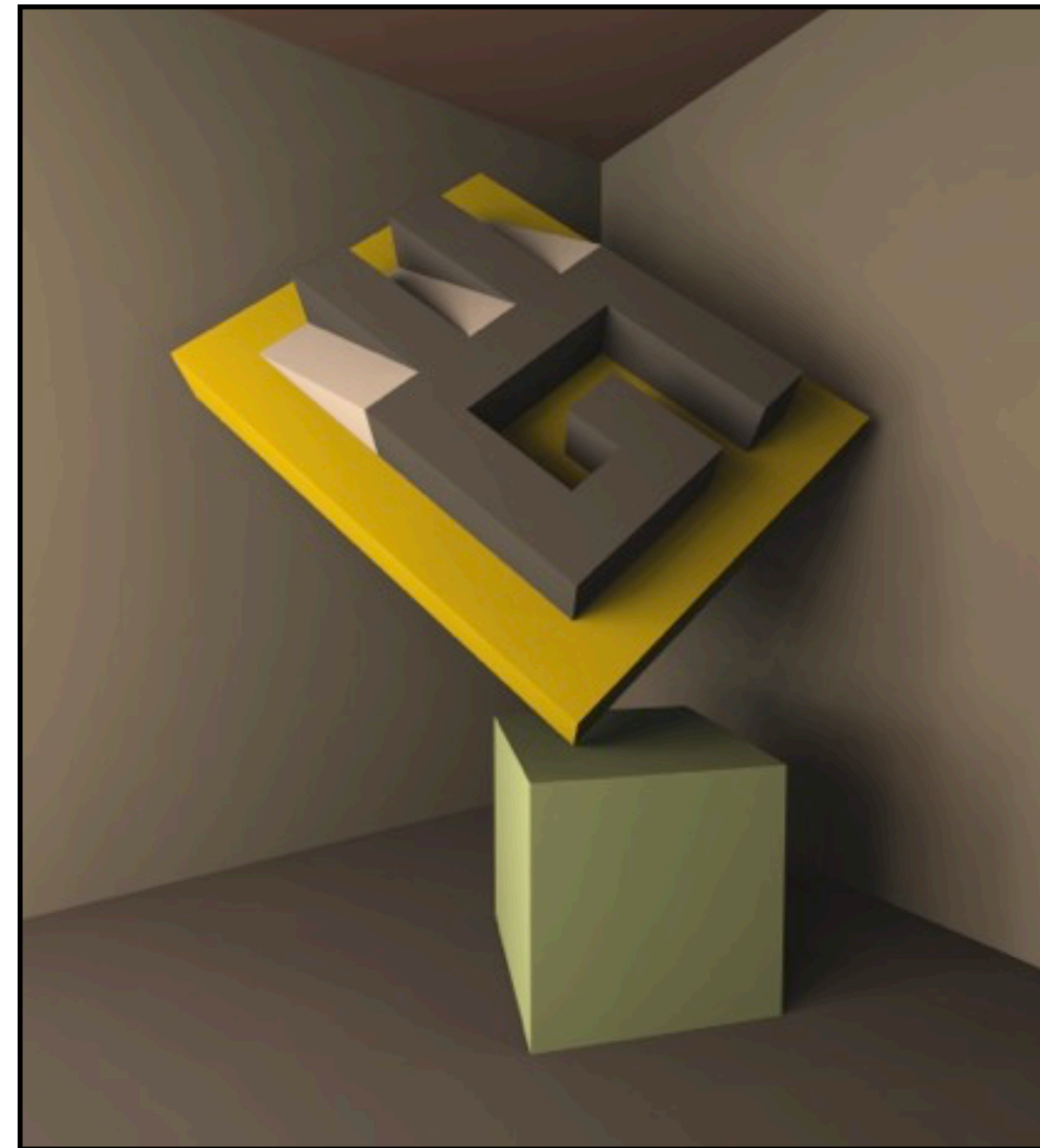
Improved Generation of VPLs

Rejection of unimportant VPLs [Gerogiev and Slusallek 2010]

Without rejection

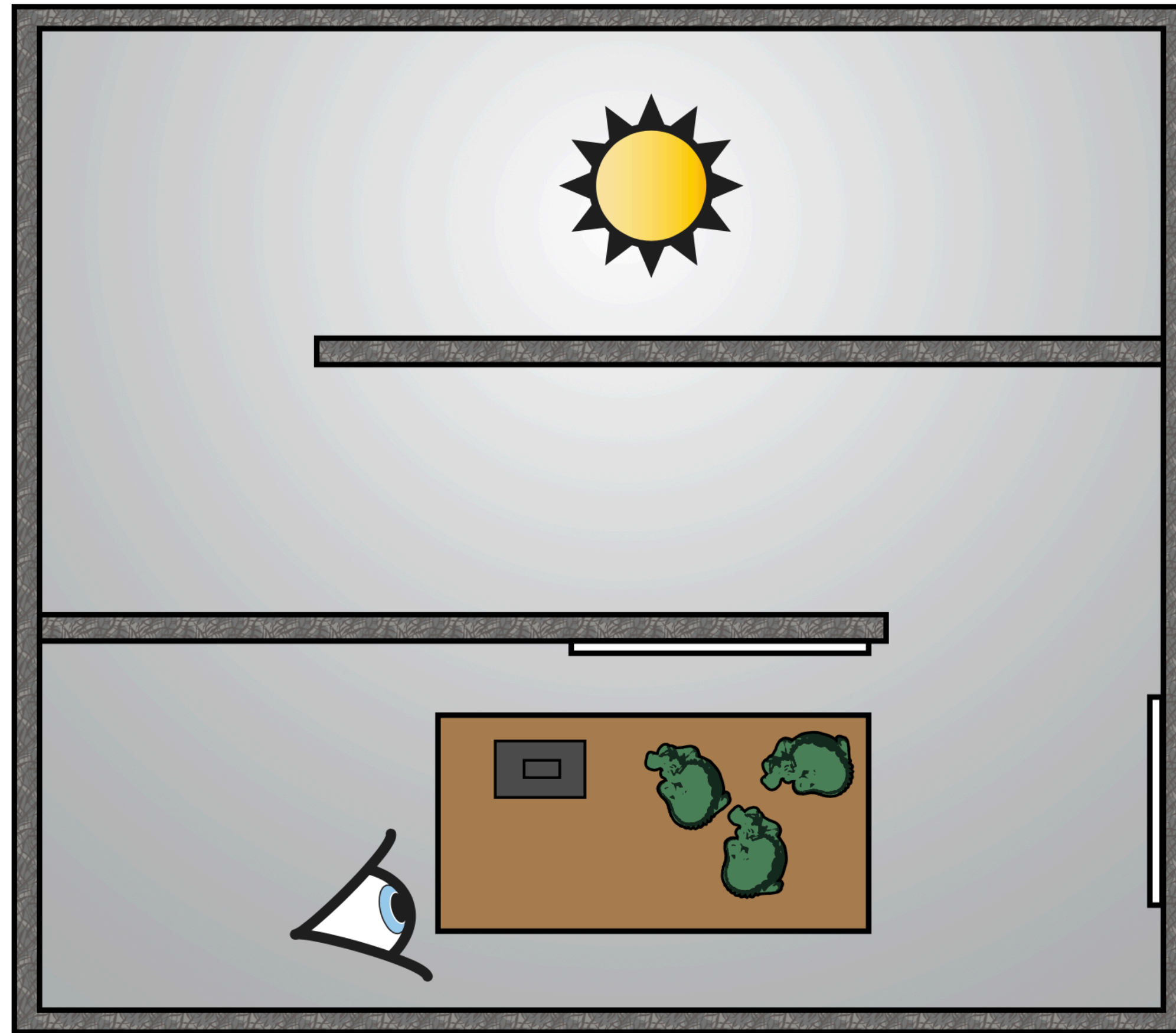


With rejection (7% acceptance)



Improved Generation of VPLs

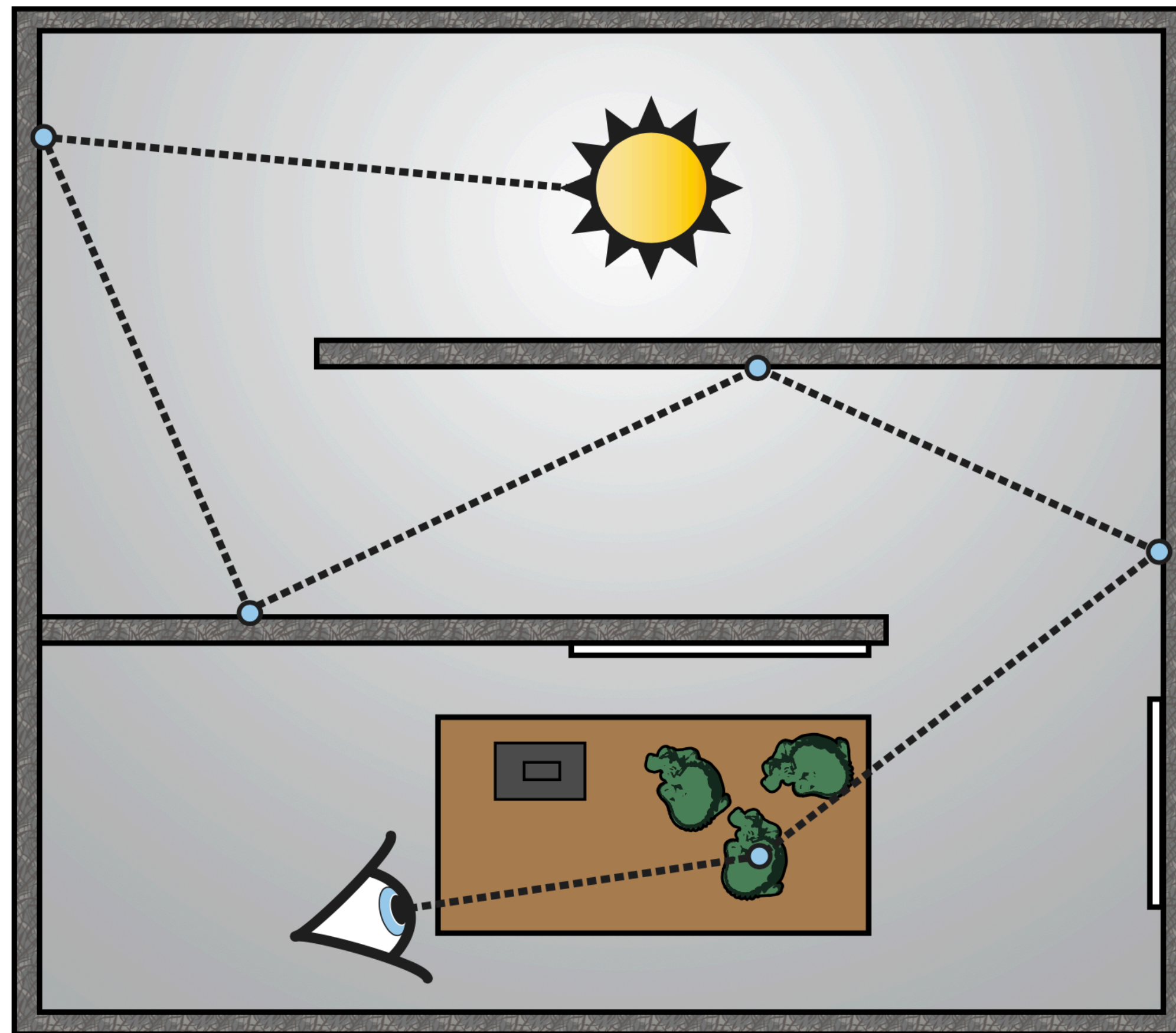
Bidirectional Instant Radiosity [Segovia et al. 2006]



Create a VPL at the second bounce from the camera

Improved Generation of VPLs

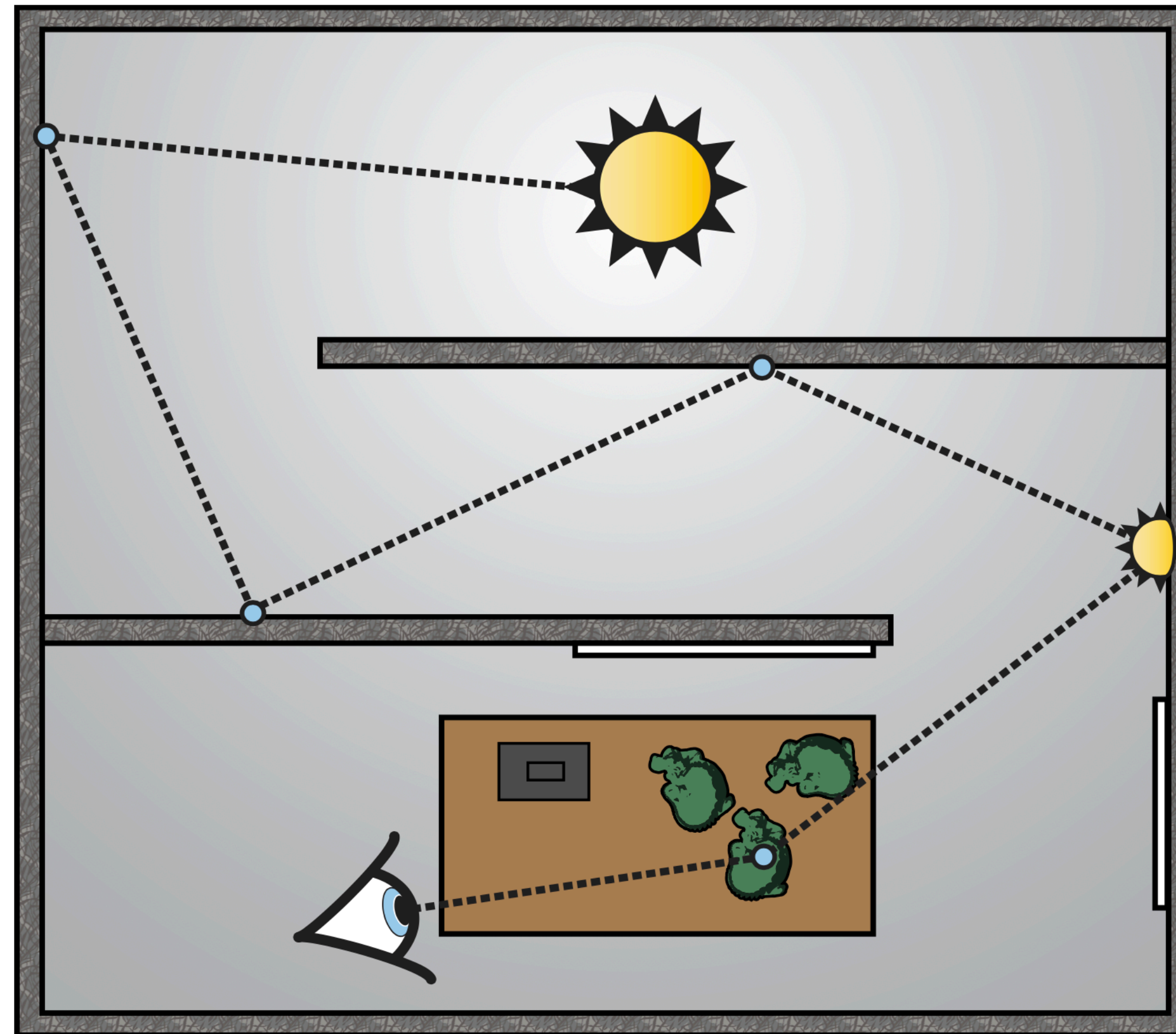
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Improved Generation of VPLs

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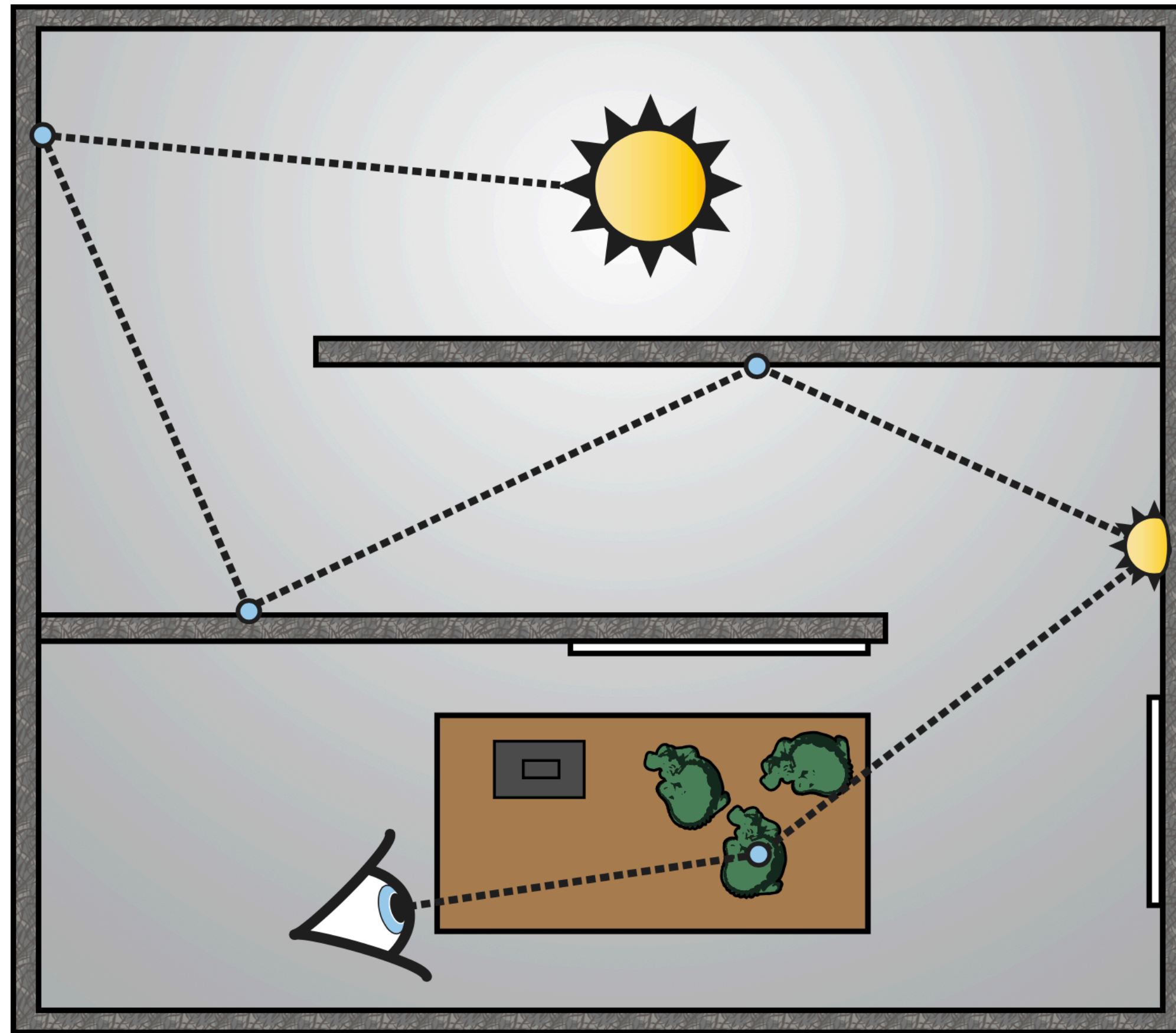
← 2nd vertex from camera

Improved Generation of VPLs

Metropolis Instant Radiosity [Segovia et al. 2007]

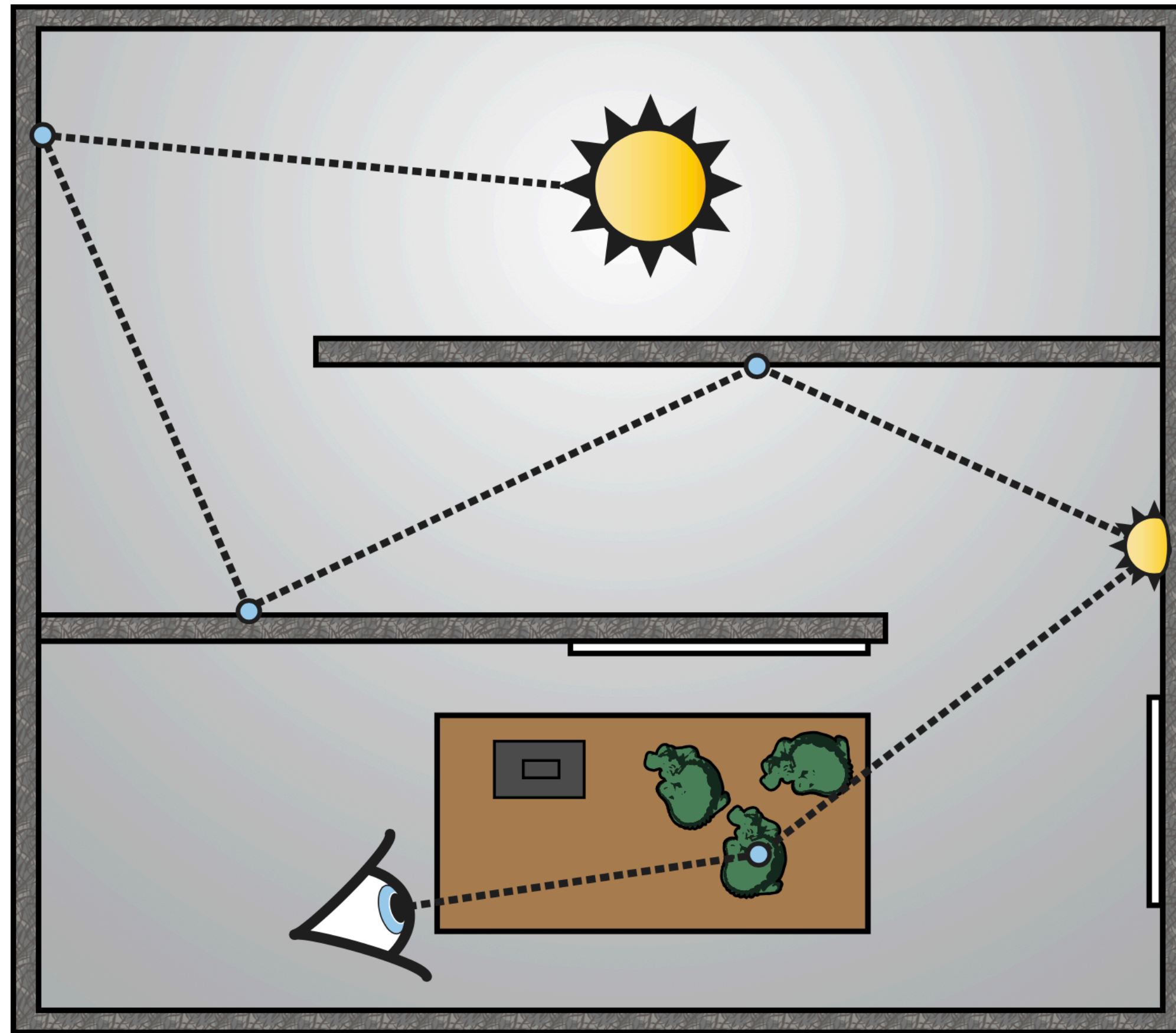
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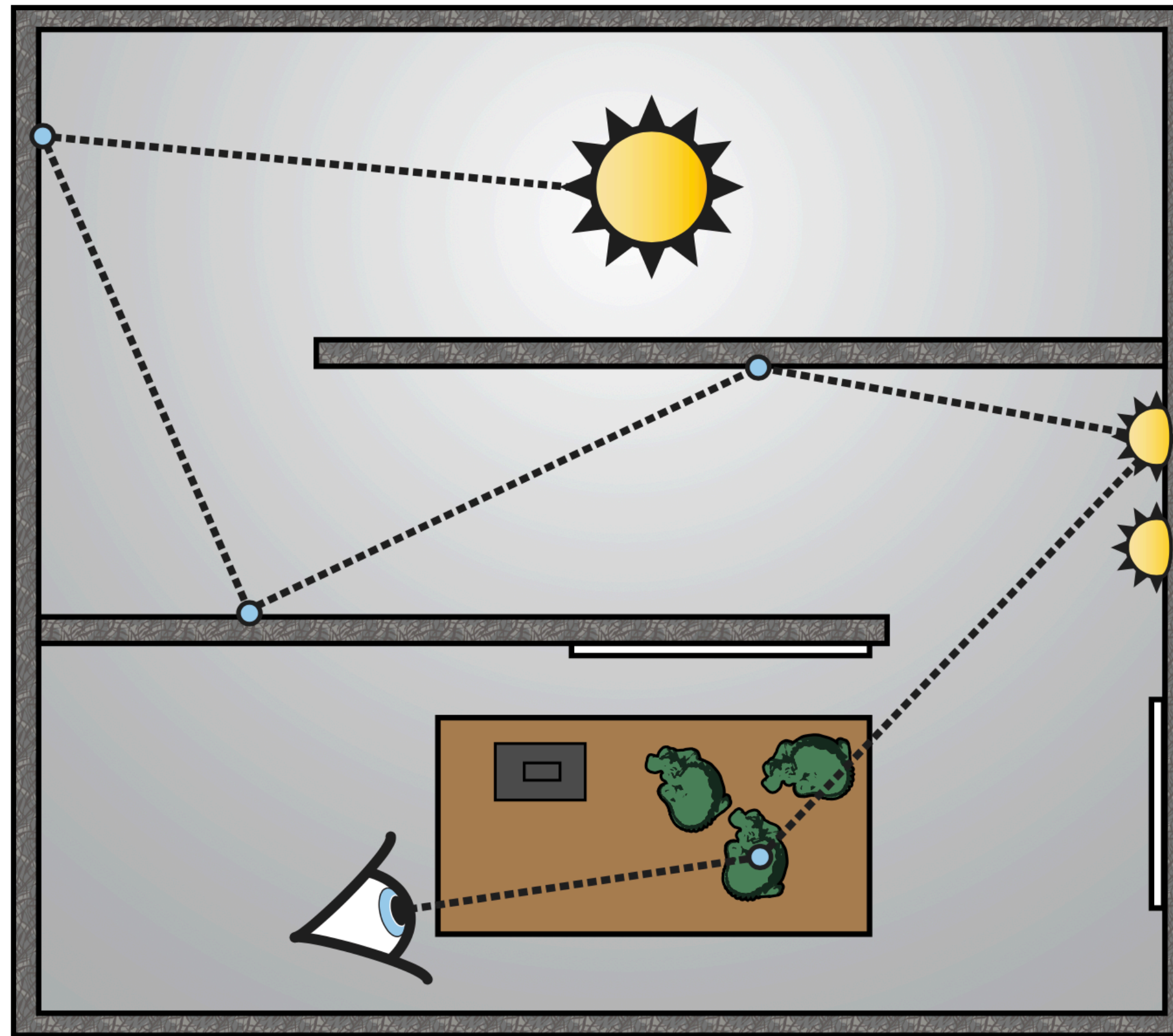
Metropolis Instant Radiosity [Segovia et al. 2007]



Generate VPLs by mutating paths

Improved Generation of VPLs

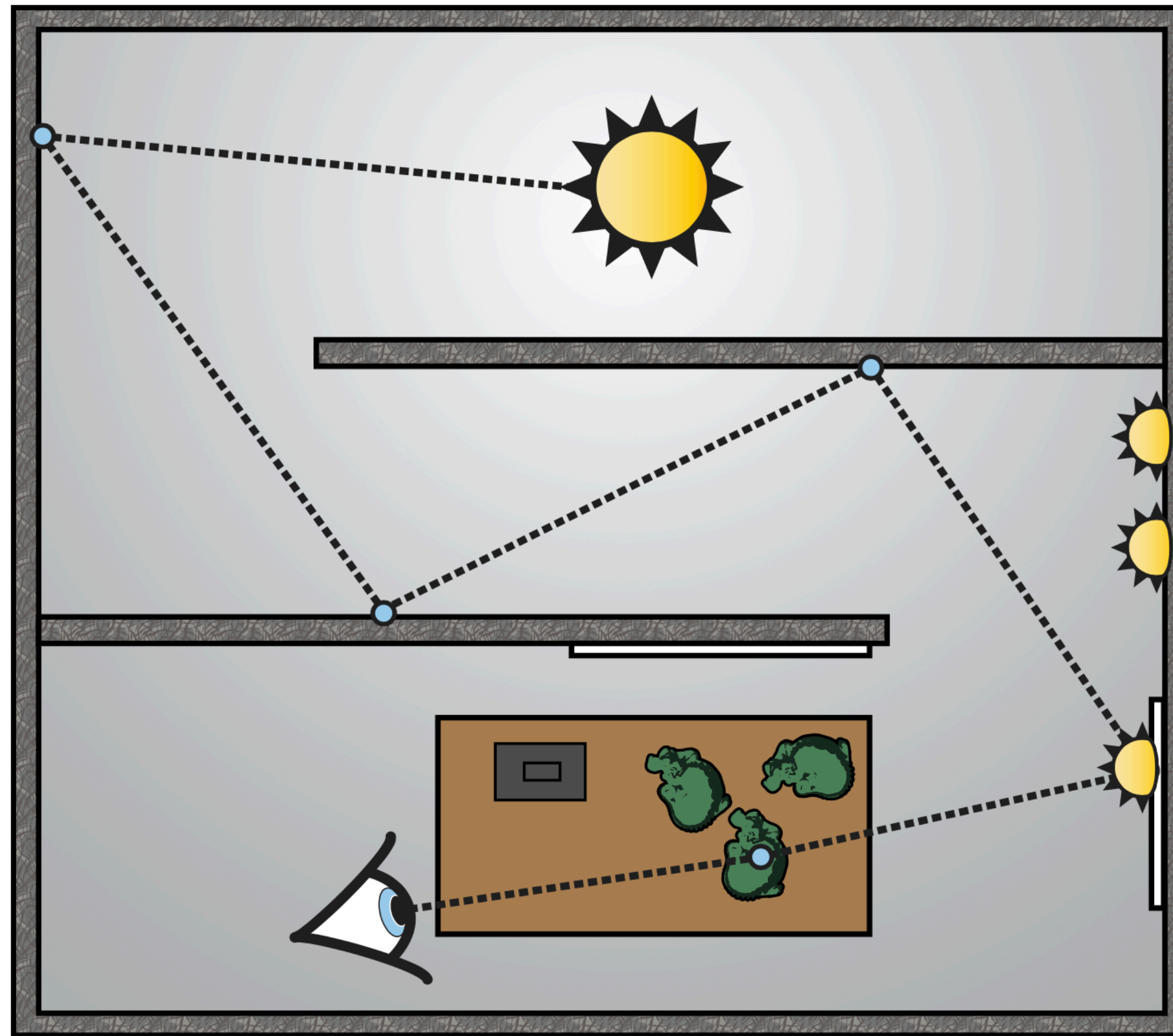
Metropolis Instant Radiosity [Segovia et al. 2007]



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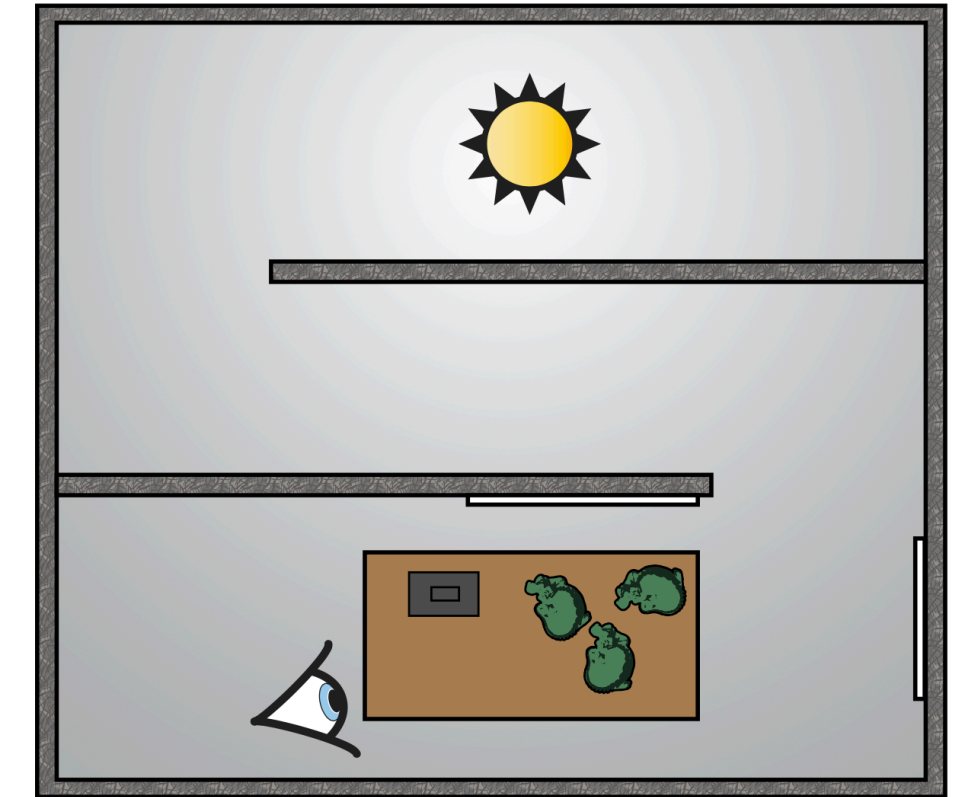
Metropolis Instant Radiosity [Segovia et al. 2007]



Generate VPLs by mutating paths

Comparisons

Metropolis Instant Radiosity [Segovia et al. 2006]



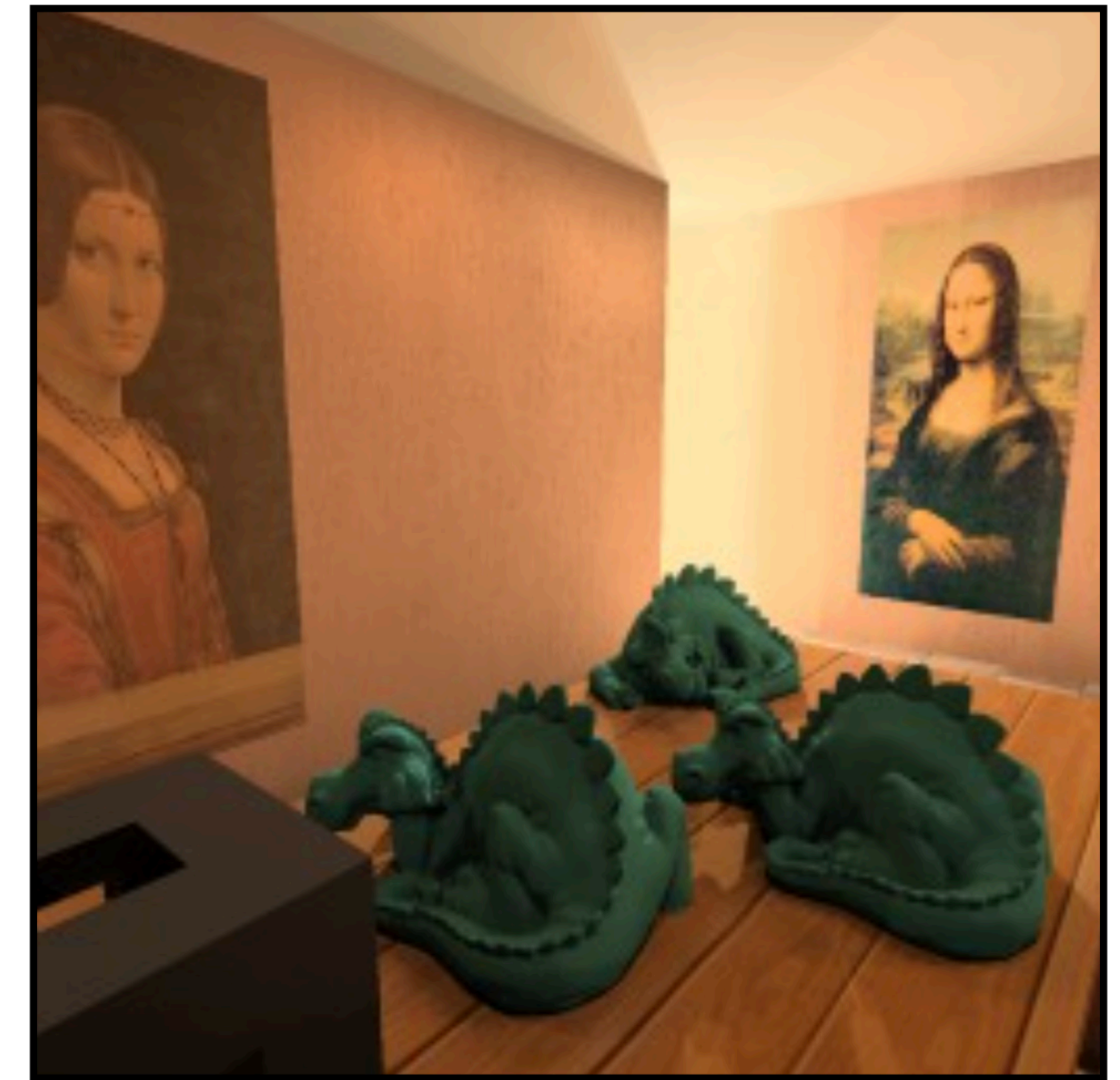
Instant Radiosity



Bidirectional Instant Radiosity



Metropolis Instant Radiosity



Comparisons

Metropolis Instant Radiosity [Segovia et al. 2006]

Advantages:

Handles large and difficult scenes

VPLs have equal contribution

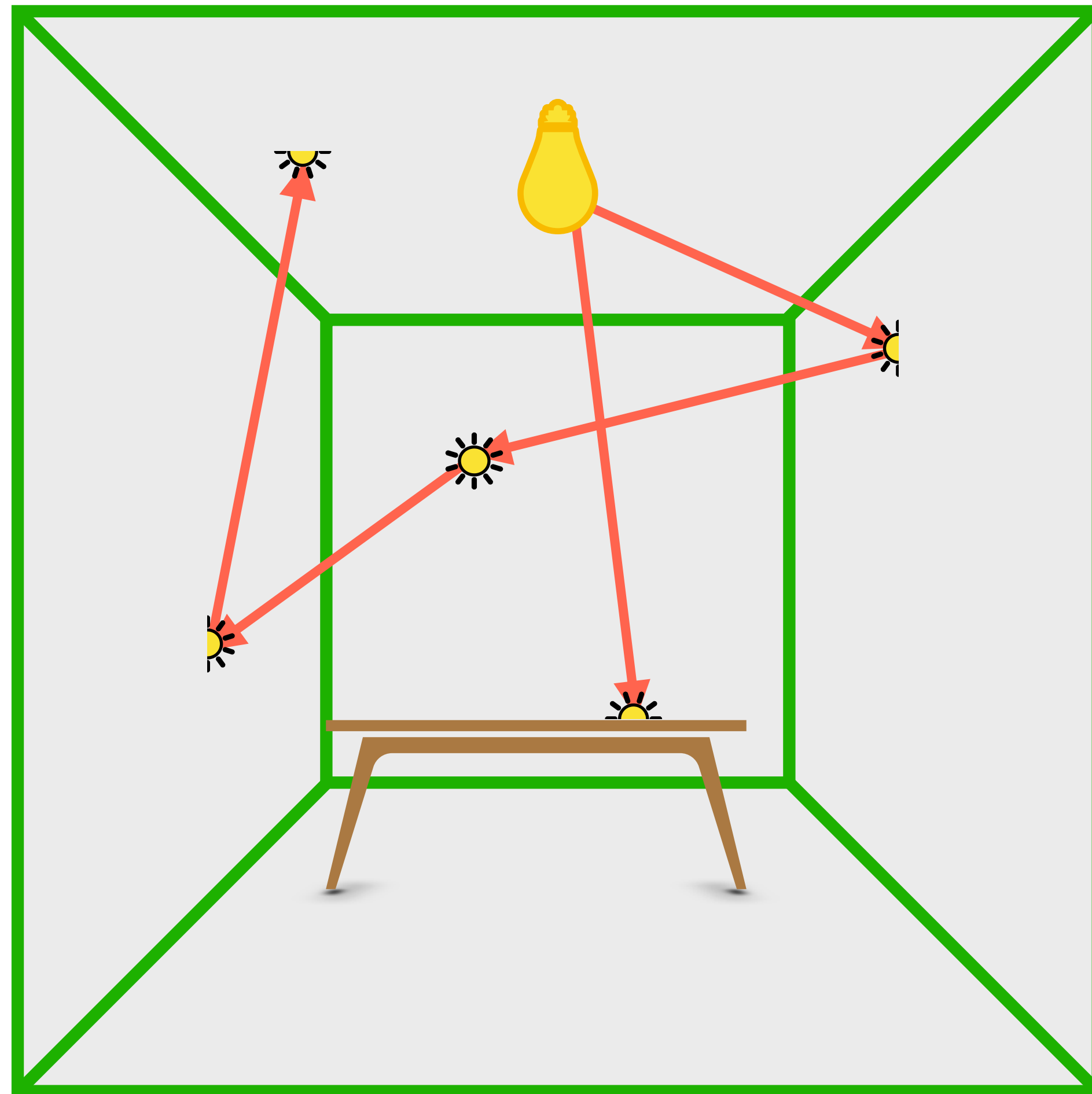
Disadvantages:

Complicated implementation

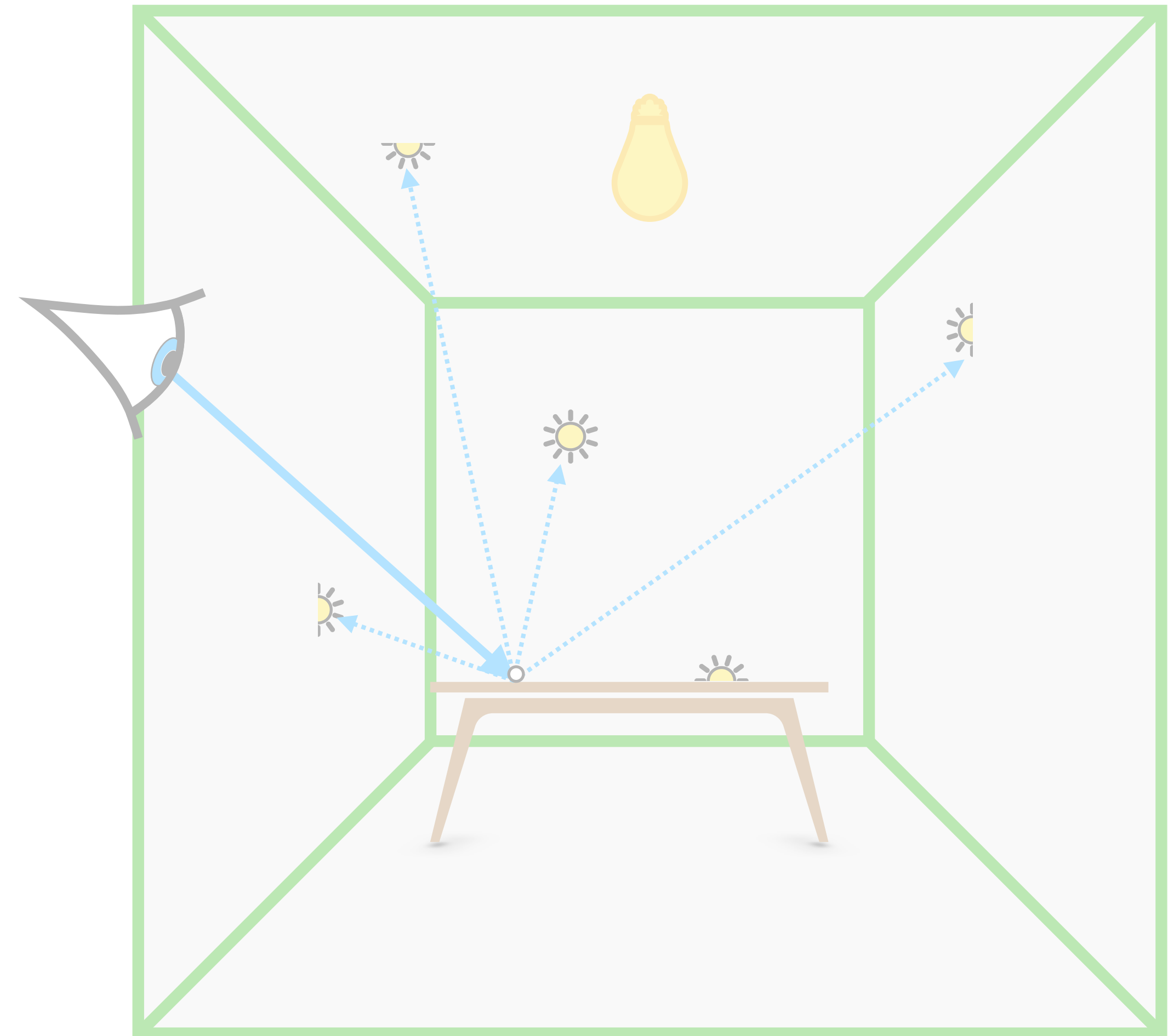
Does not help with local inter-reflections

Virtual Point Light: Two-Pass

Pass 1: Generating VPLs

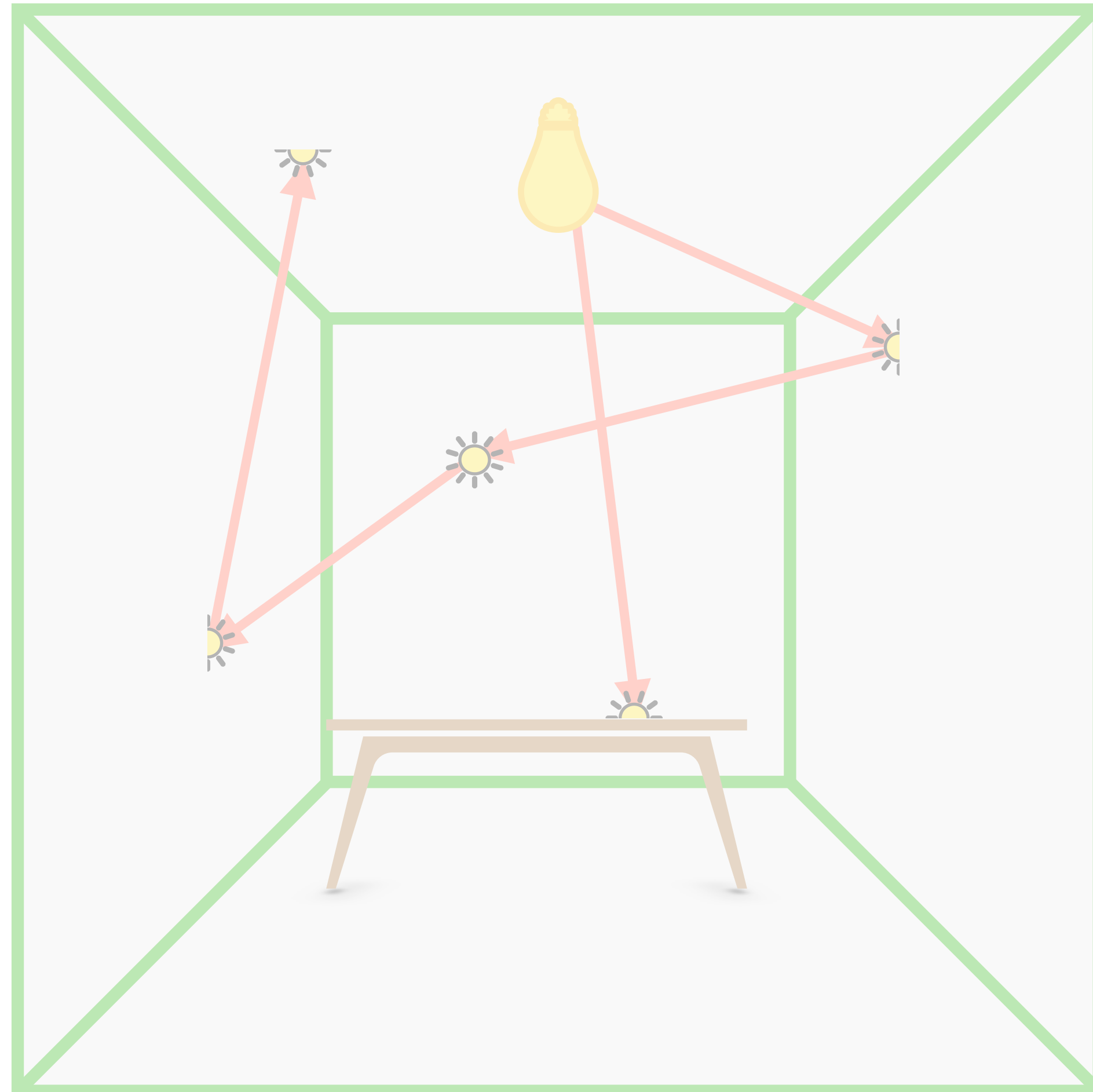


Pass 2: Lighting with VPLs

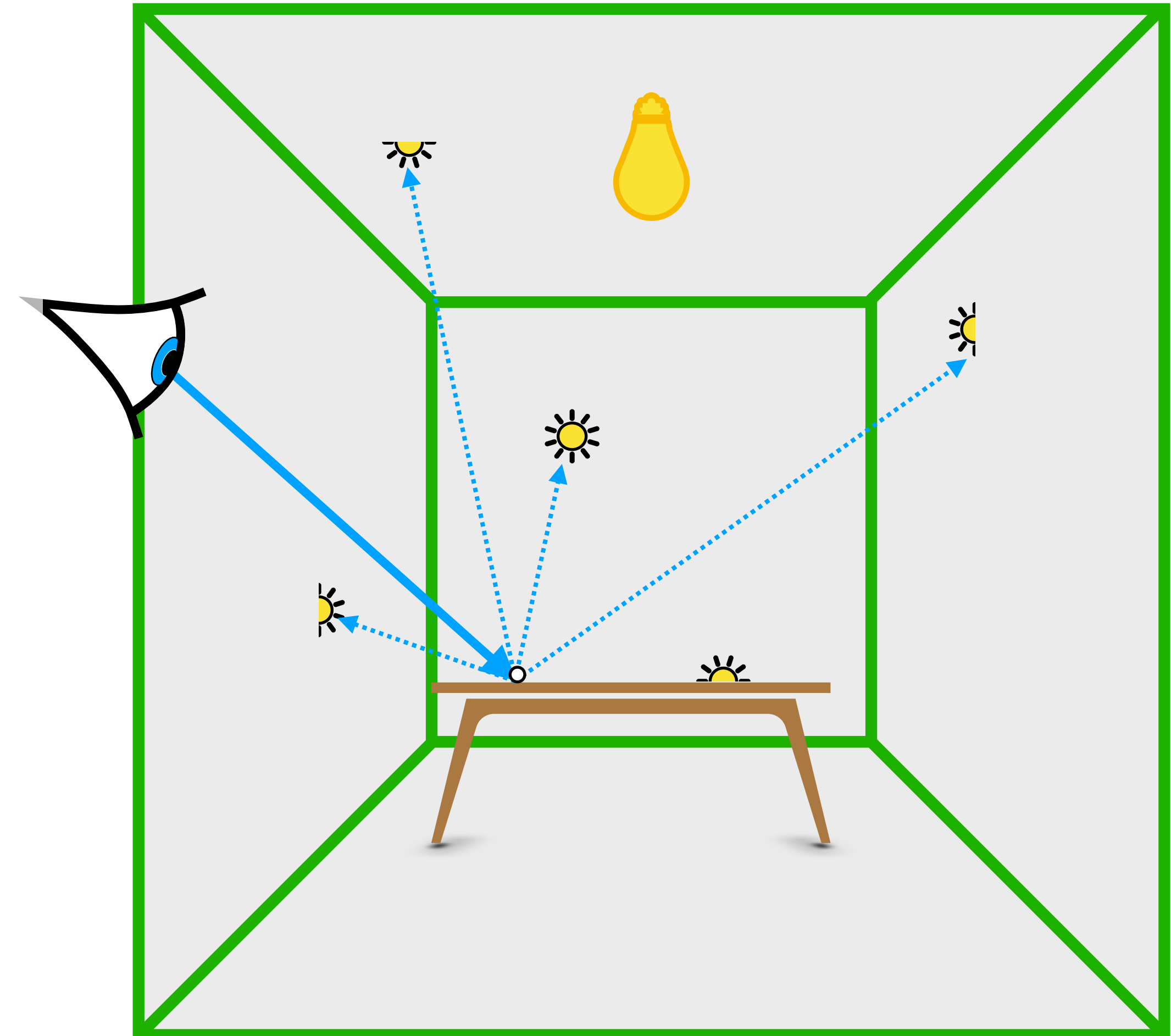


Virtual Point Light: Two-Pass

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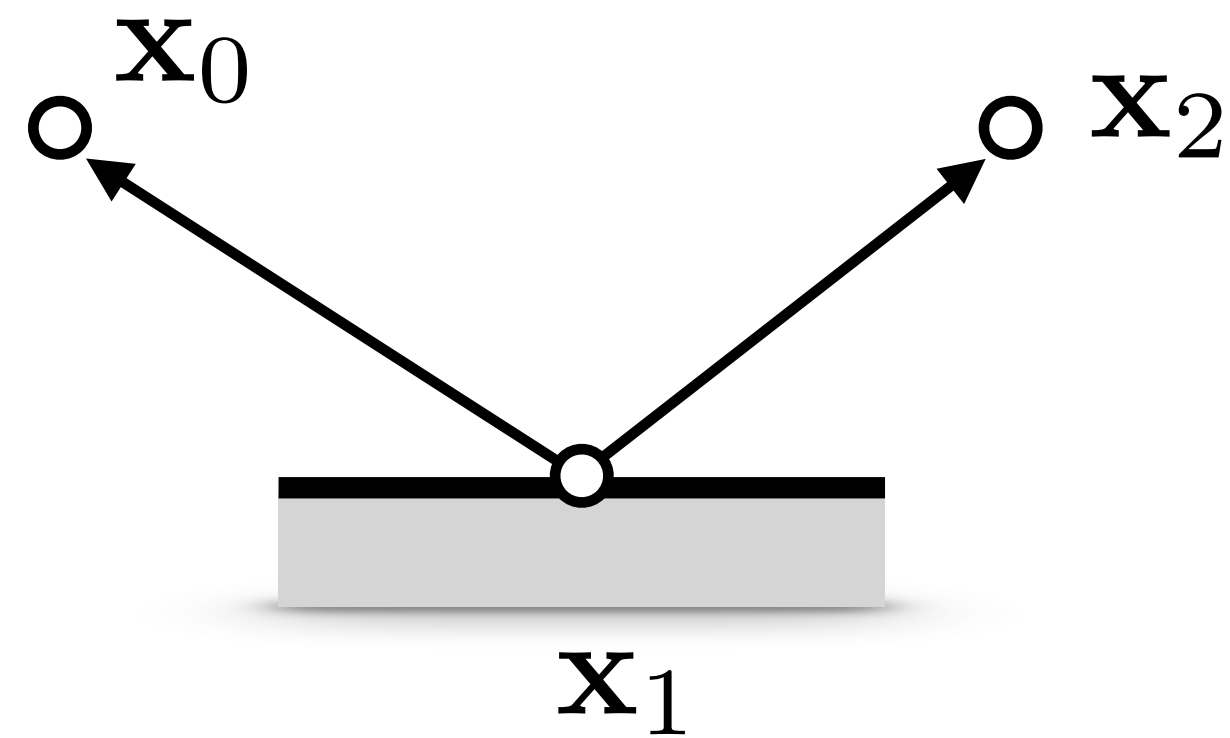


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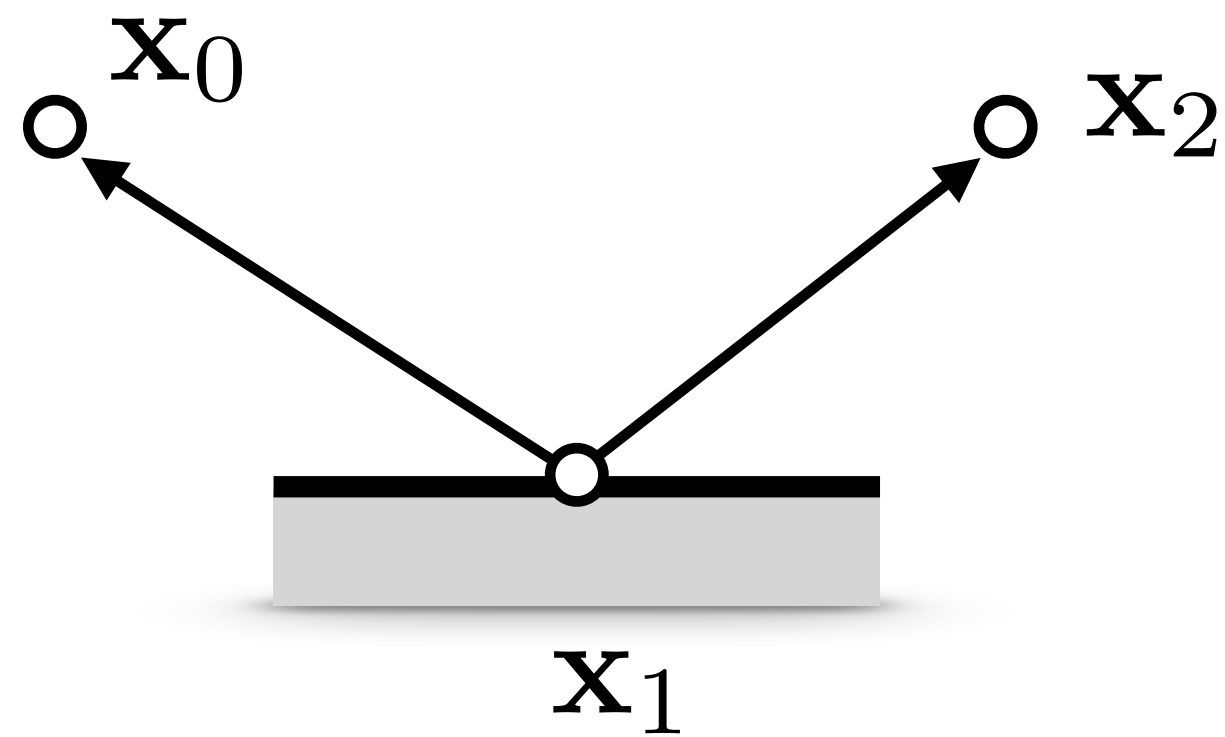
Lighting with Virtual Point Lights (VPLs)

Rendering Equation (area formulation)



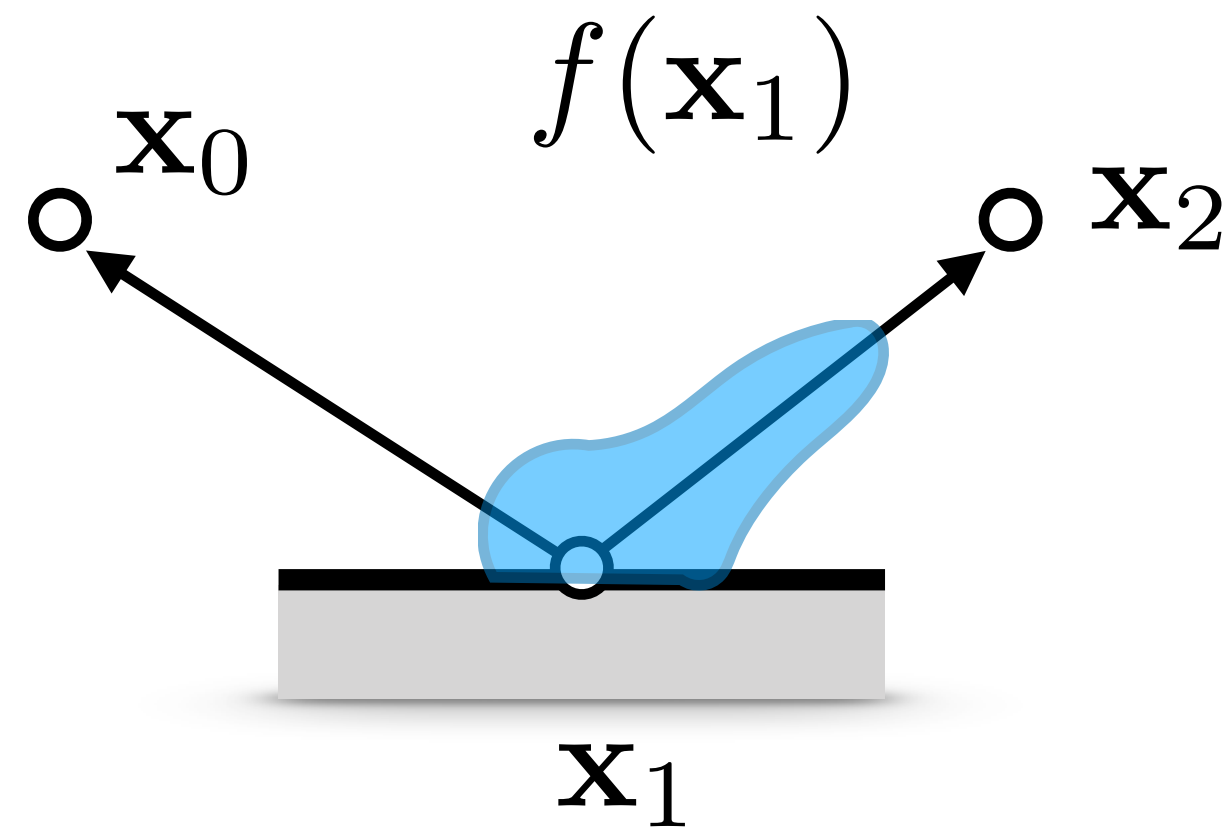
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$$L(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = L_e(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + \int_A f(\mathbf{x}_1) G(\mathbf{x}_1, \mathbf{x}_2) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$



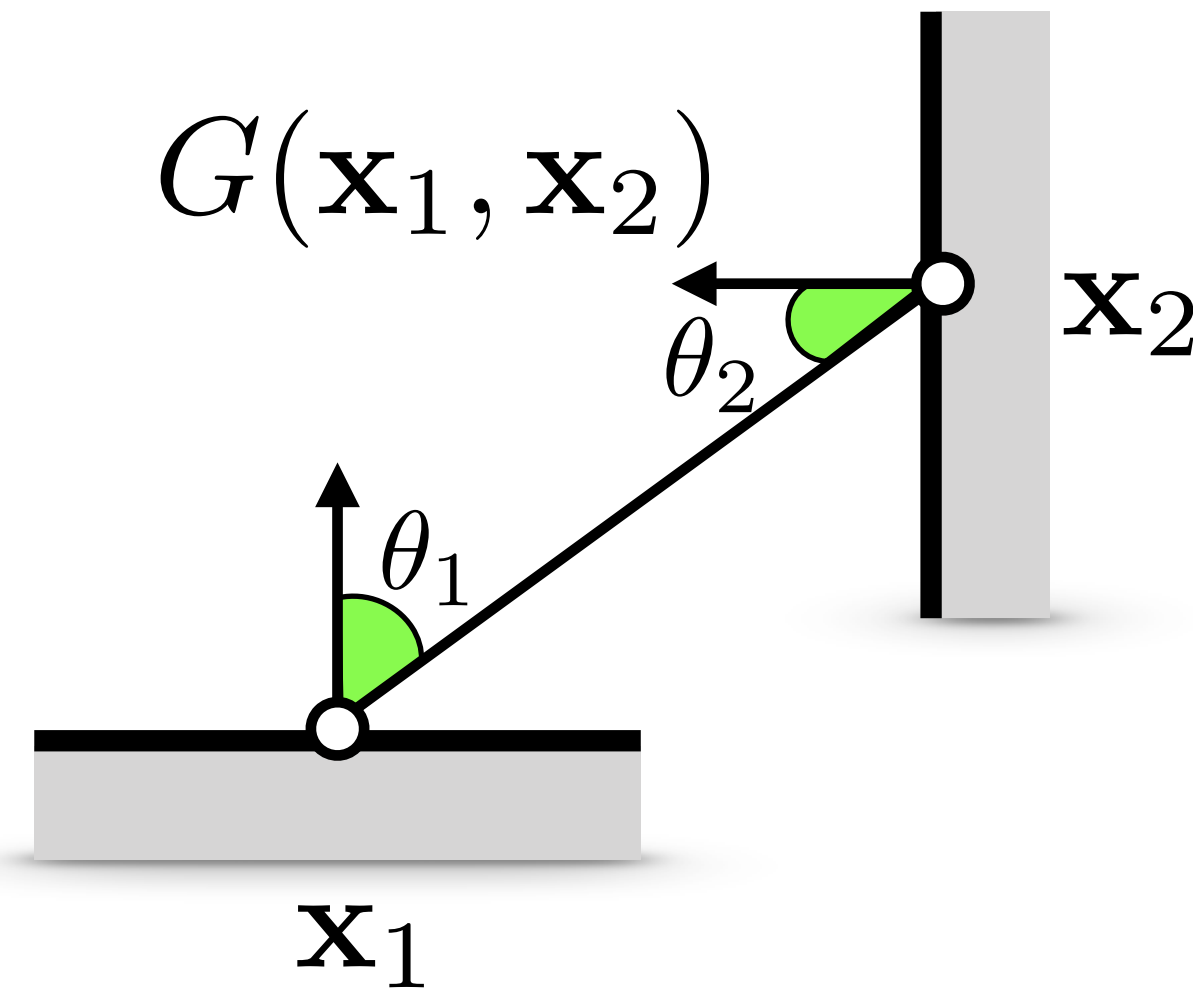
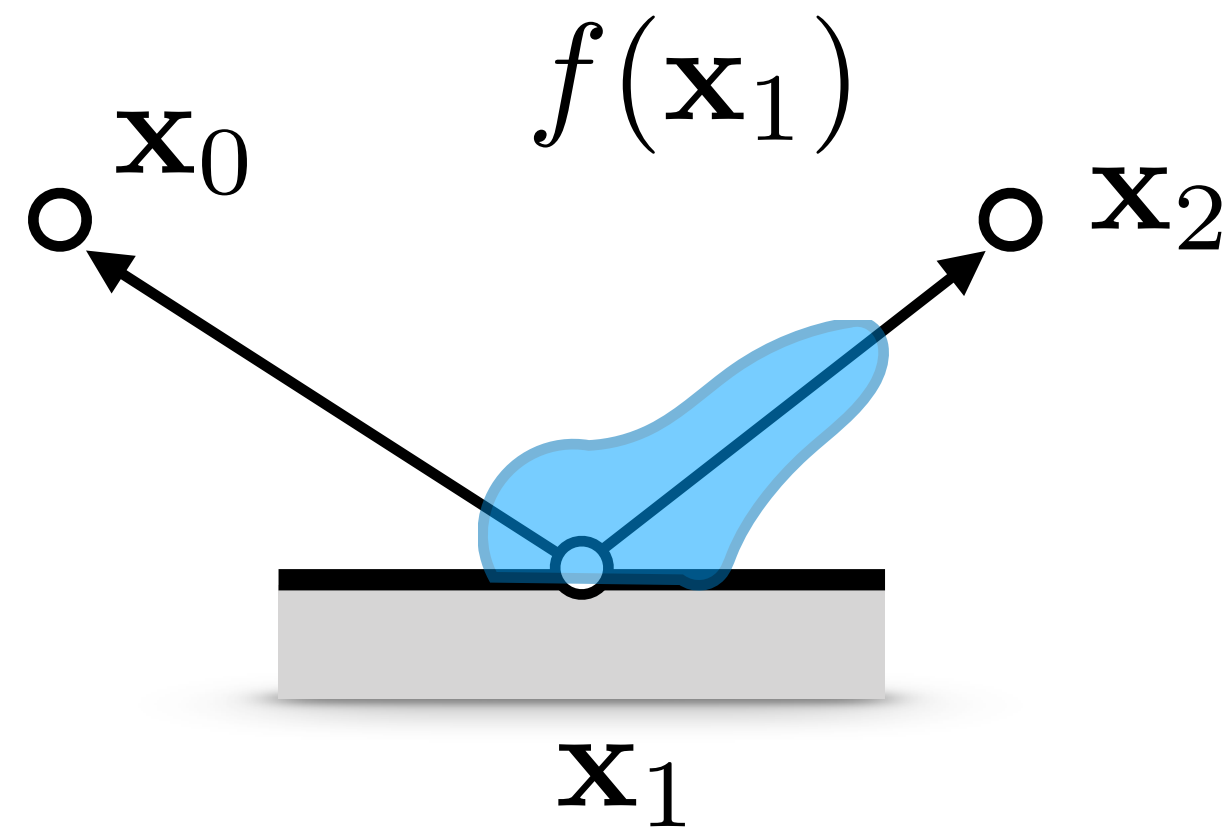
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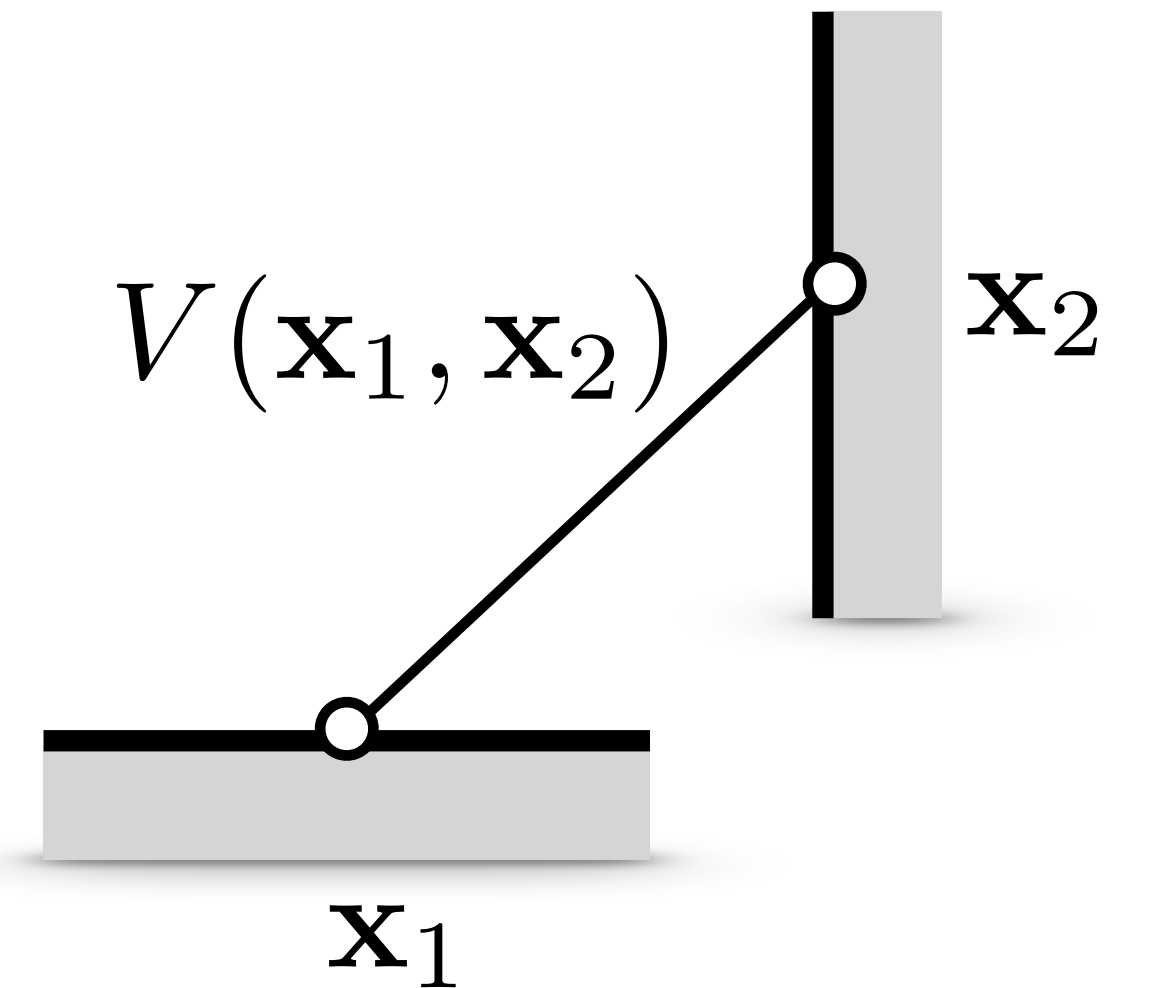
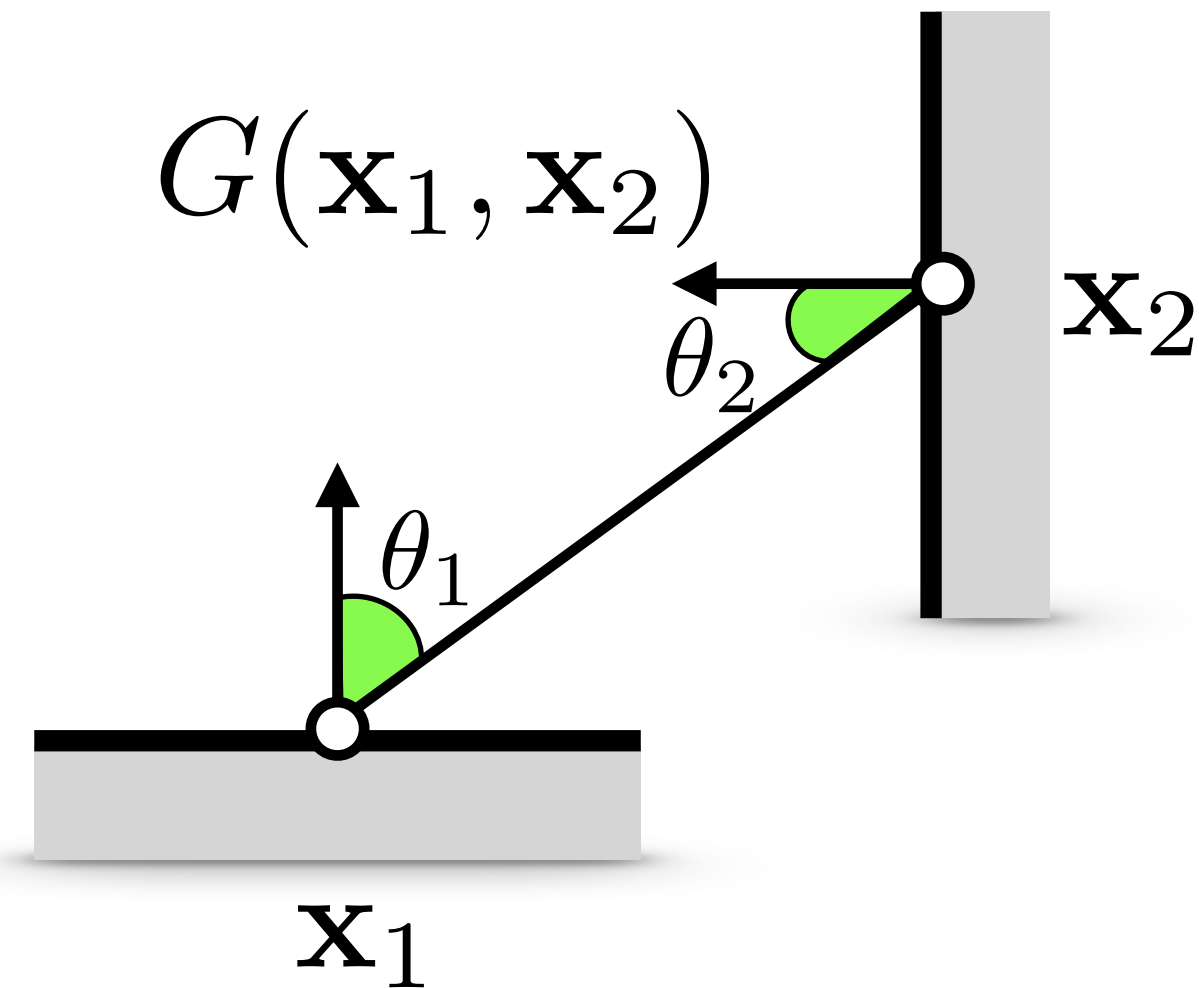
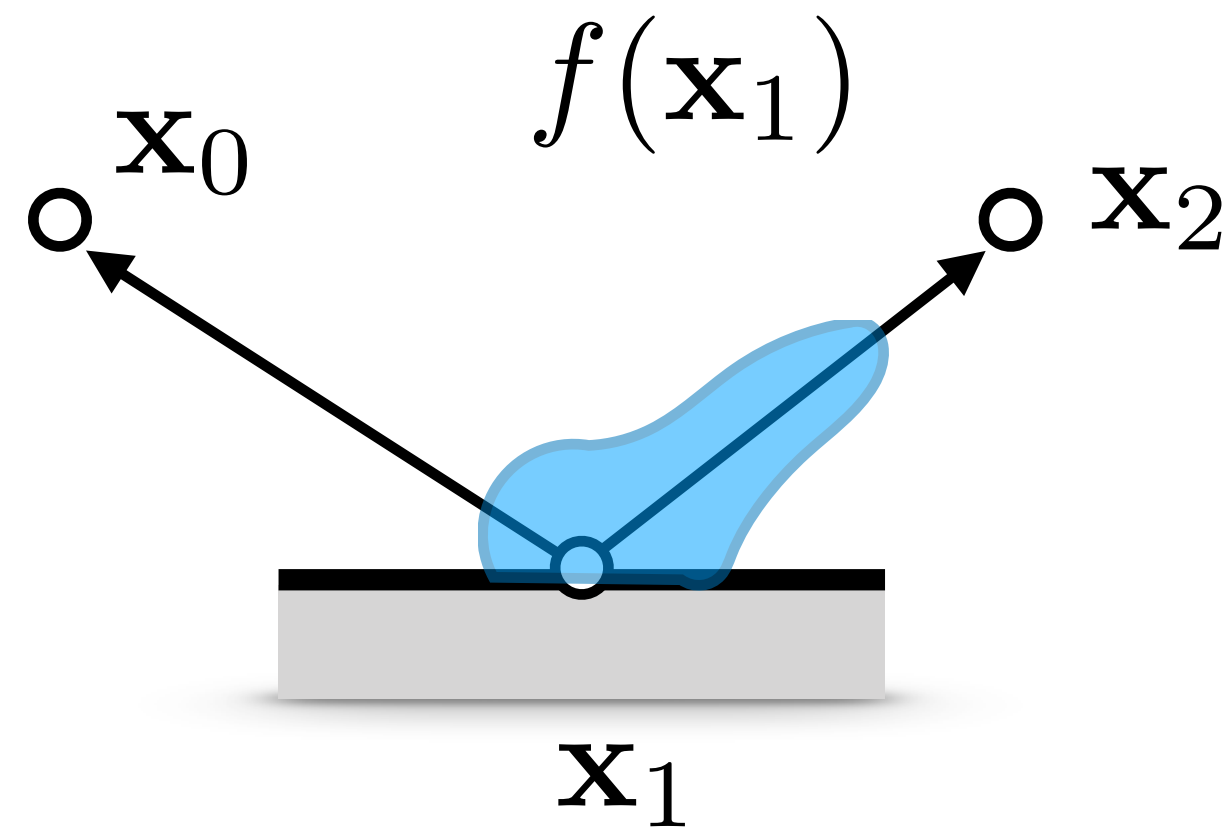
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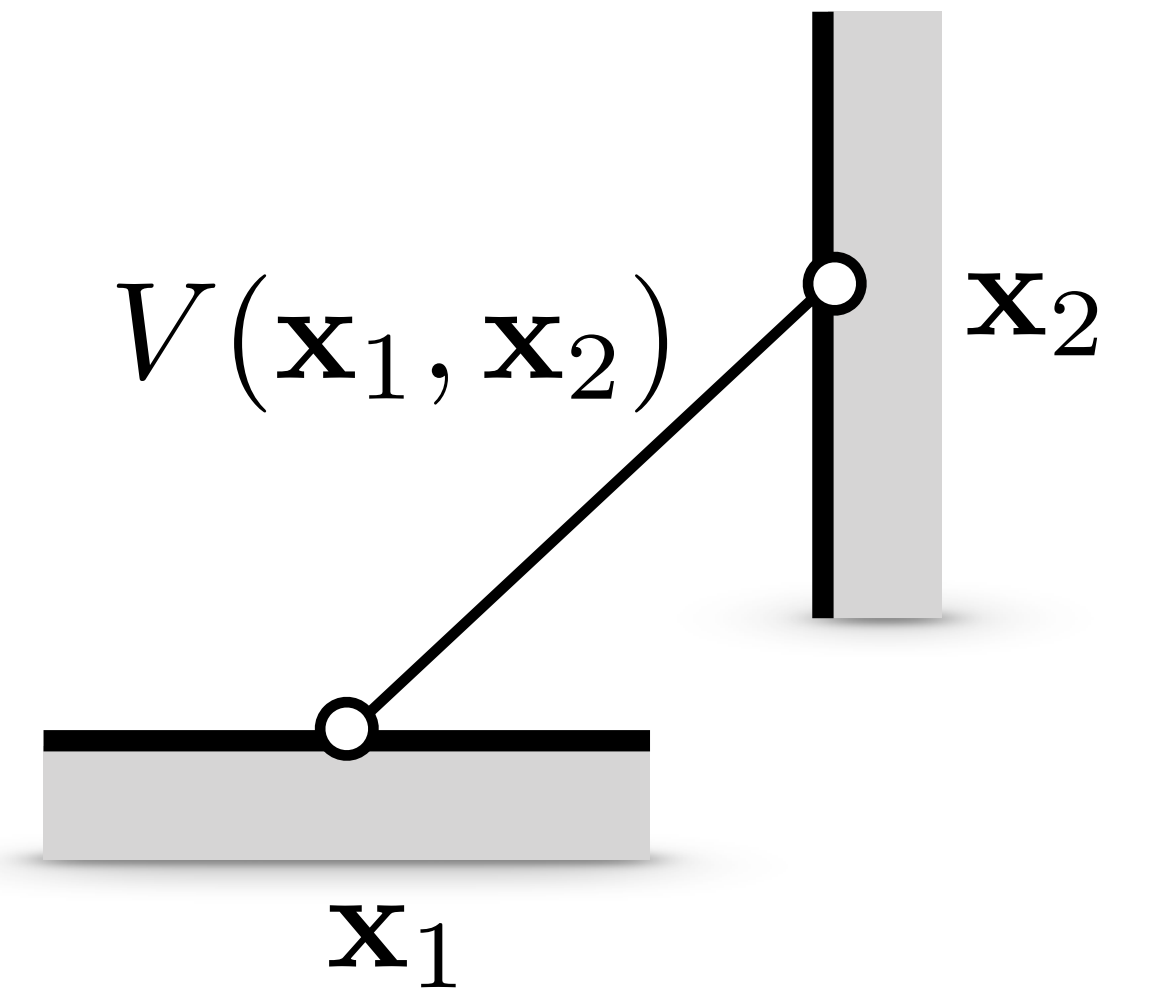
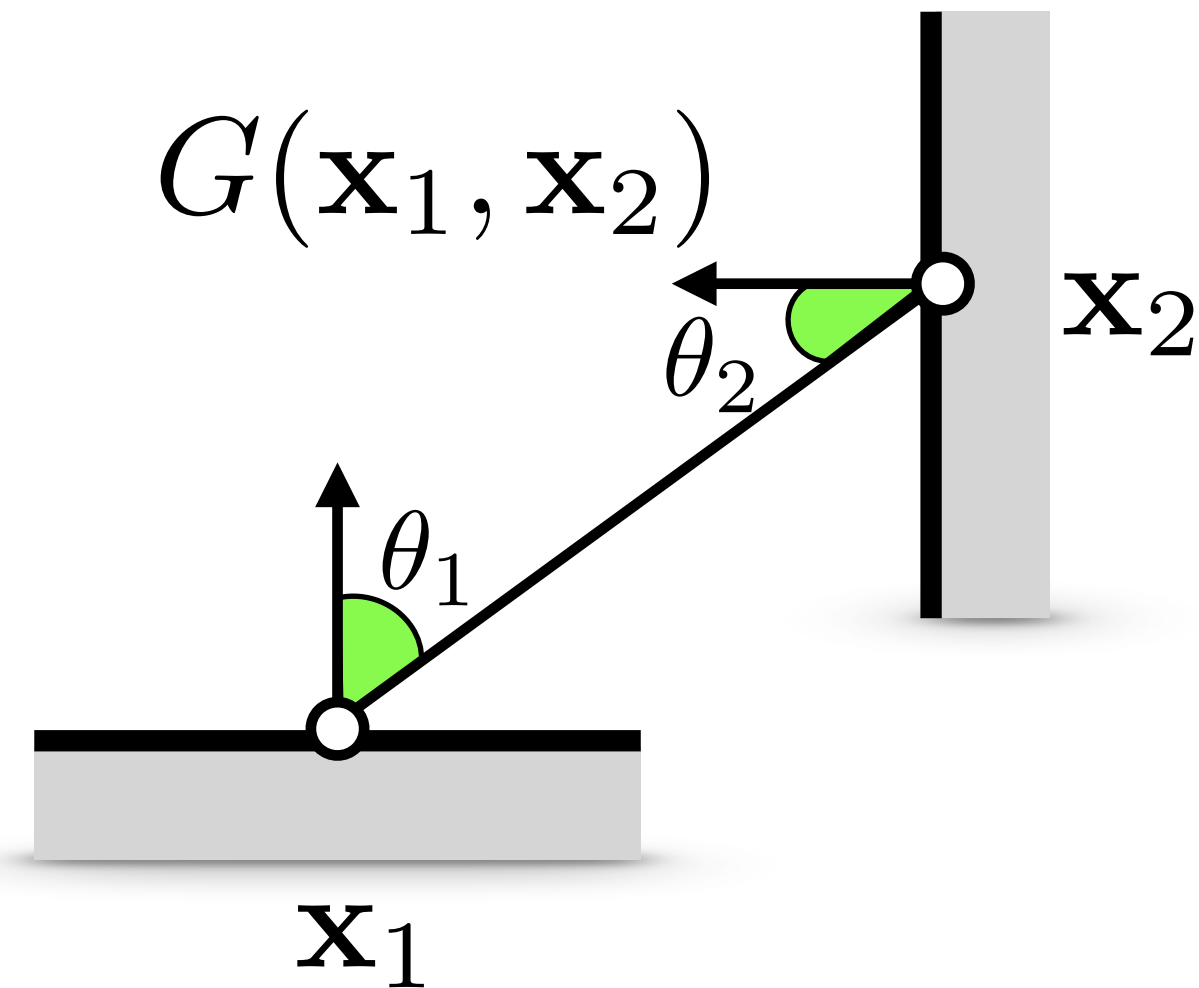
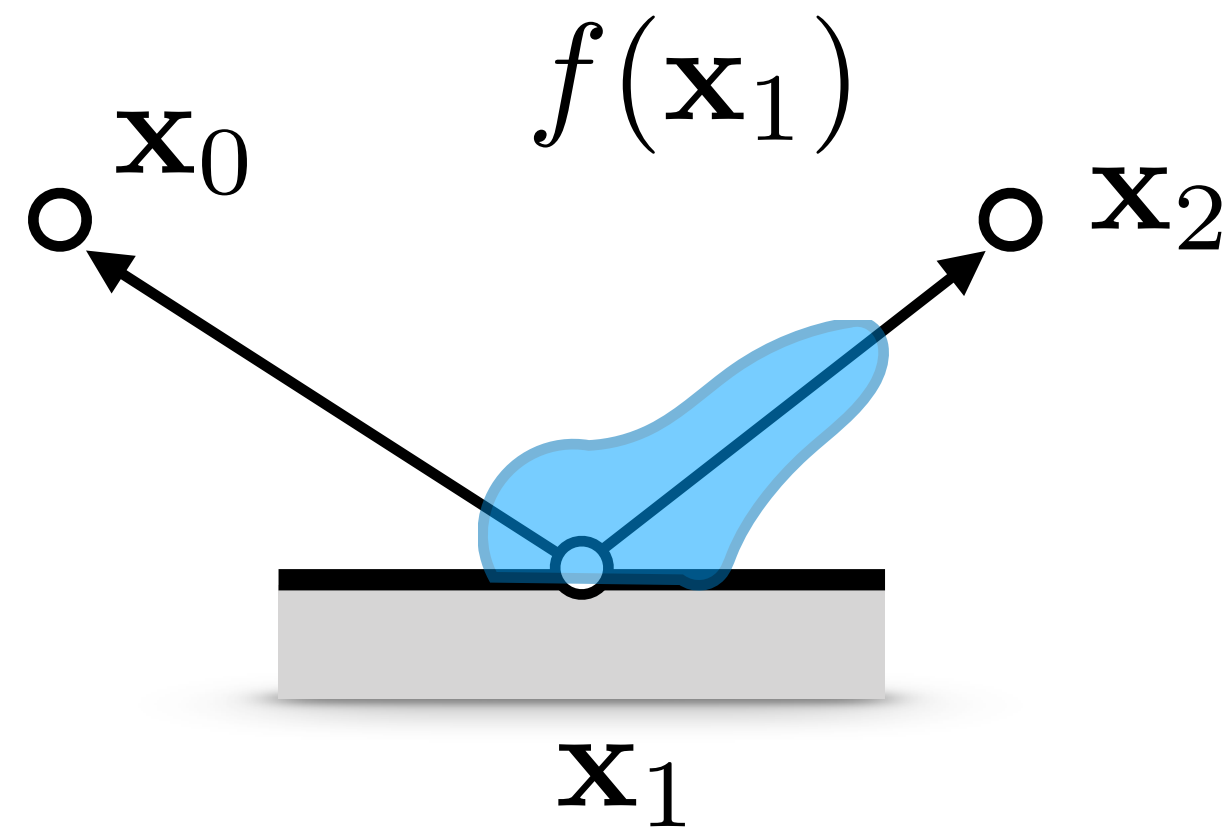
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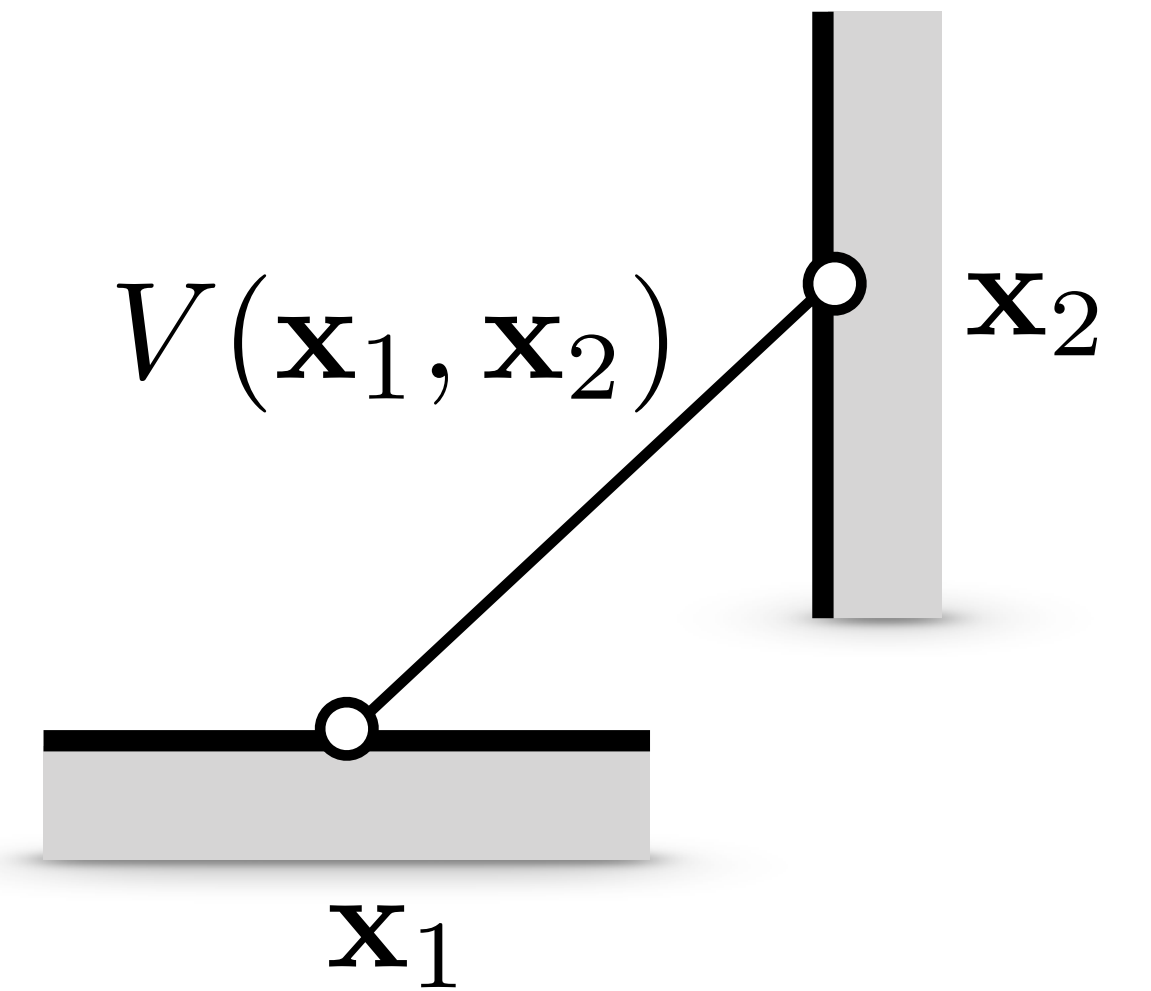
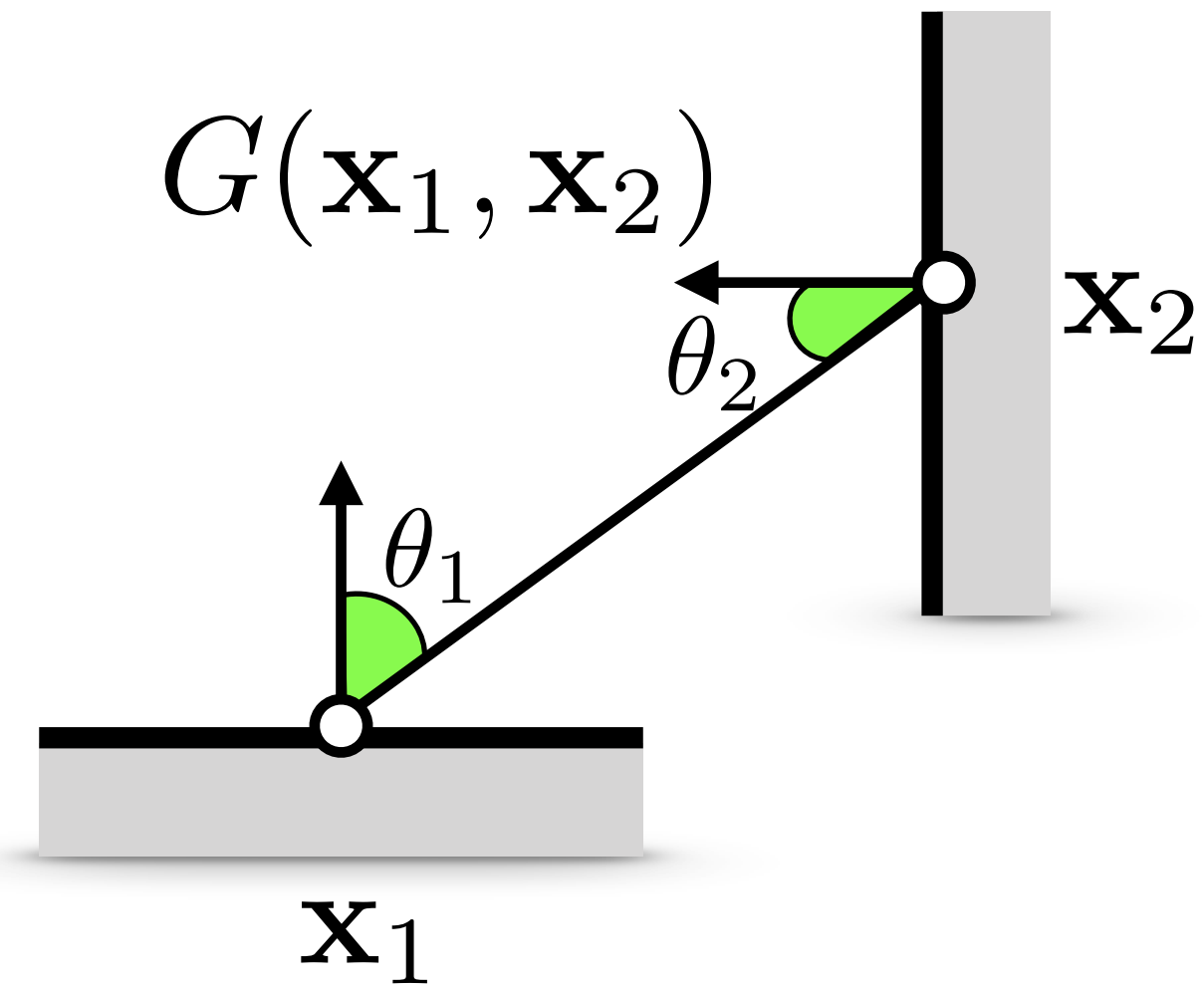
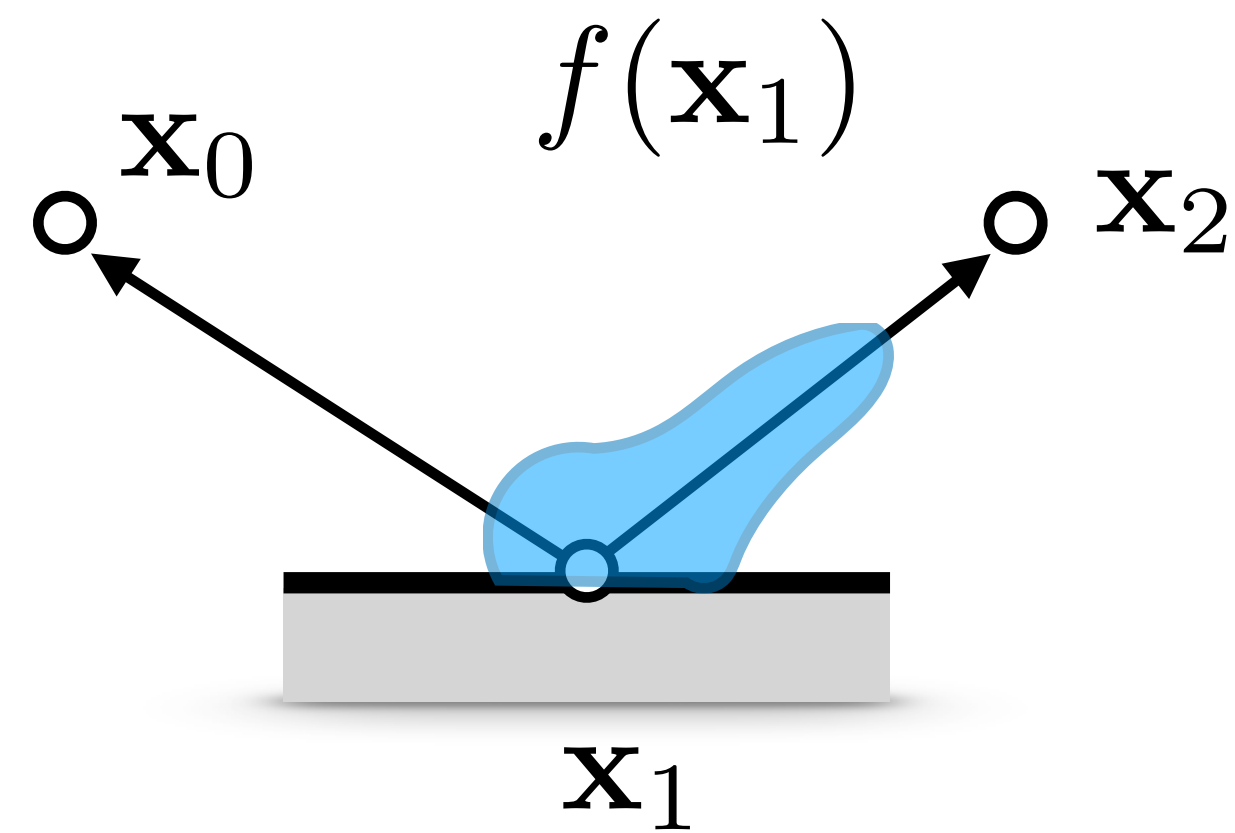
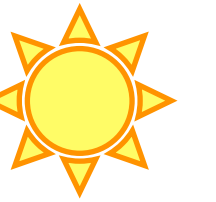
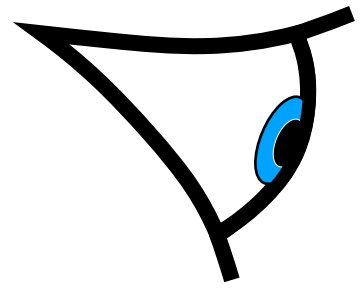


Rendering Equation (area formulation)

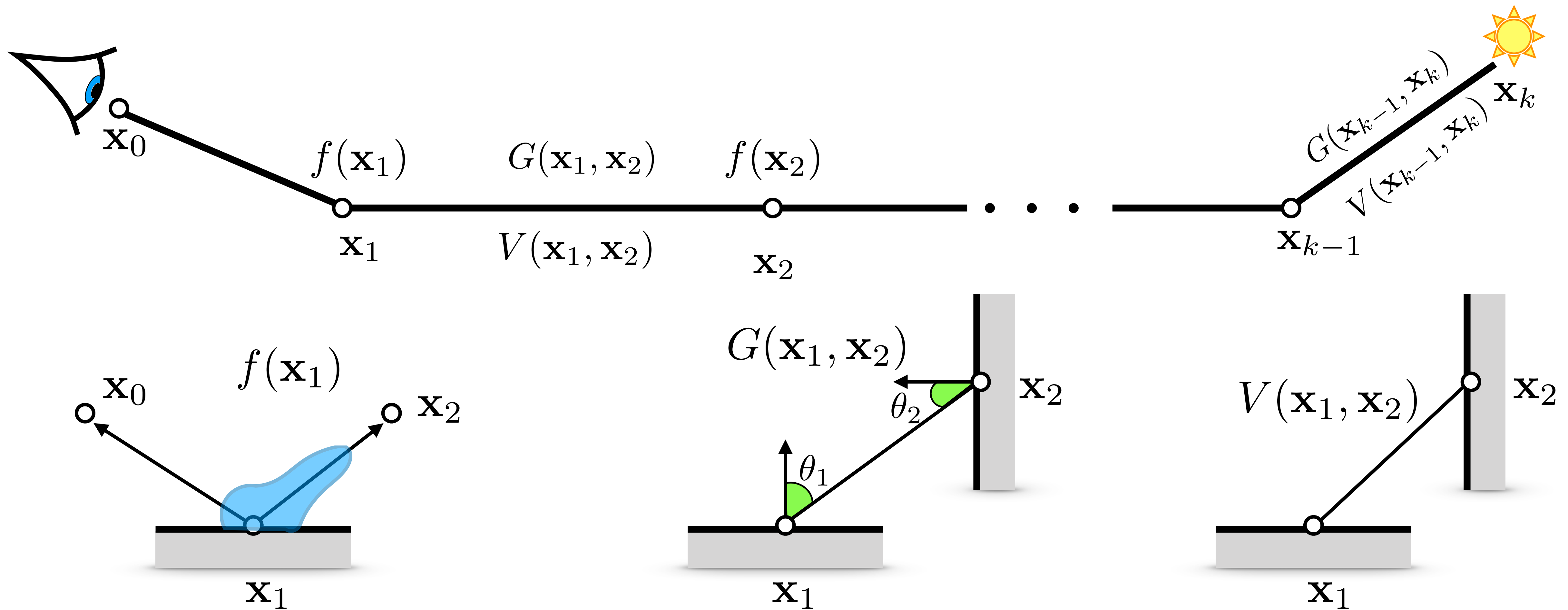
$$L(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = L_e(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + \int_A f(\mathbf{x}_1) G(\mathbf{x}_1, \mathbf{x}_2) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$



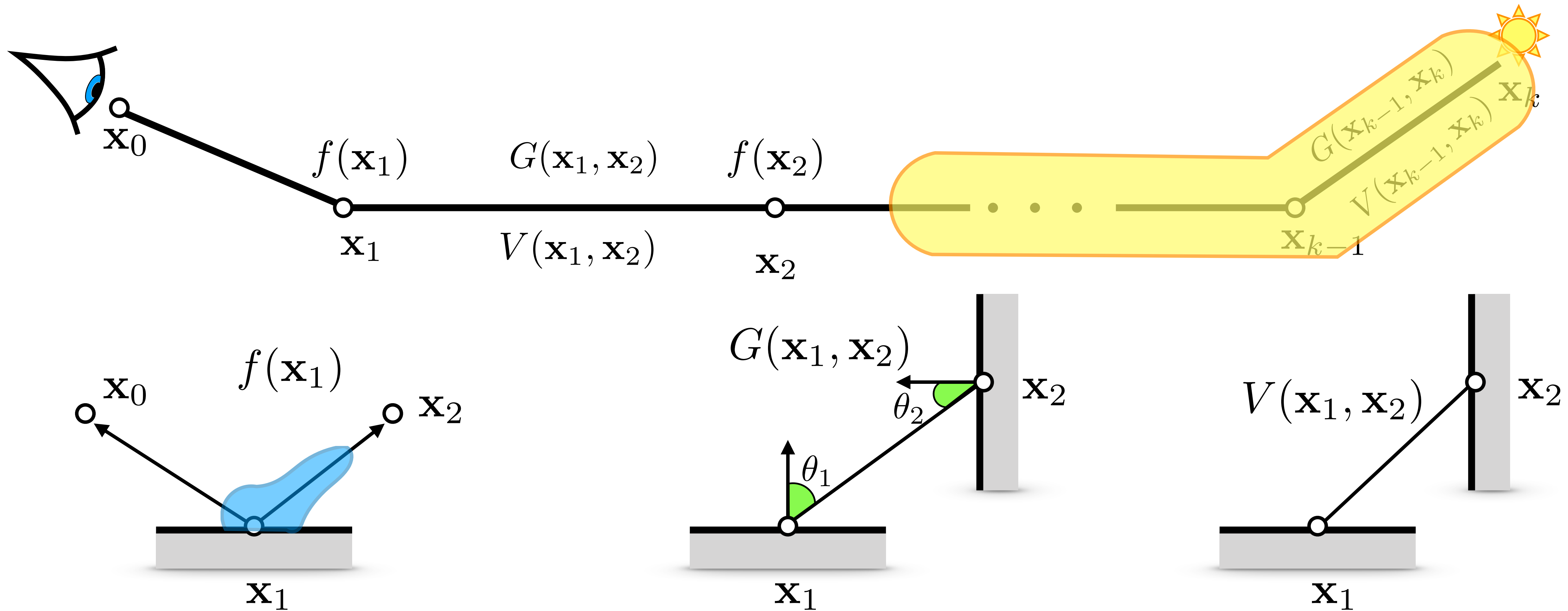
Rendering Equation (area formulation)



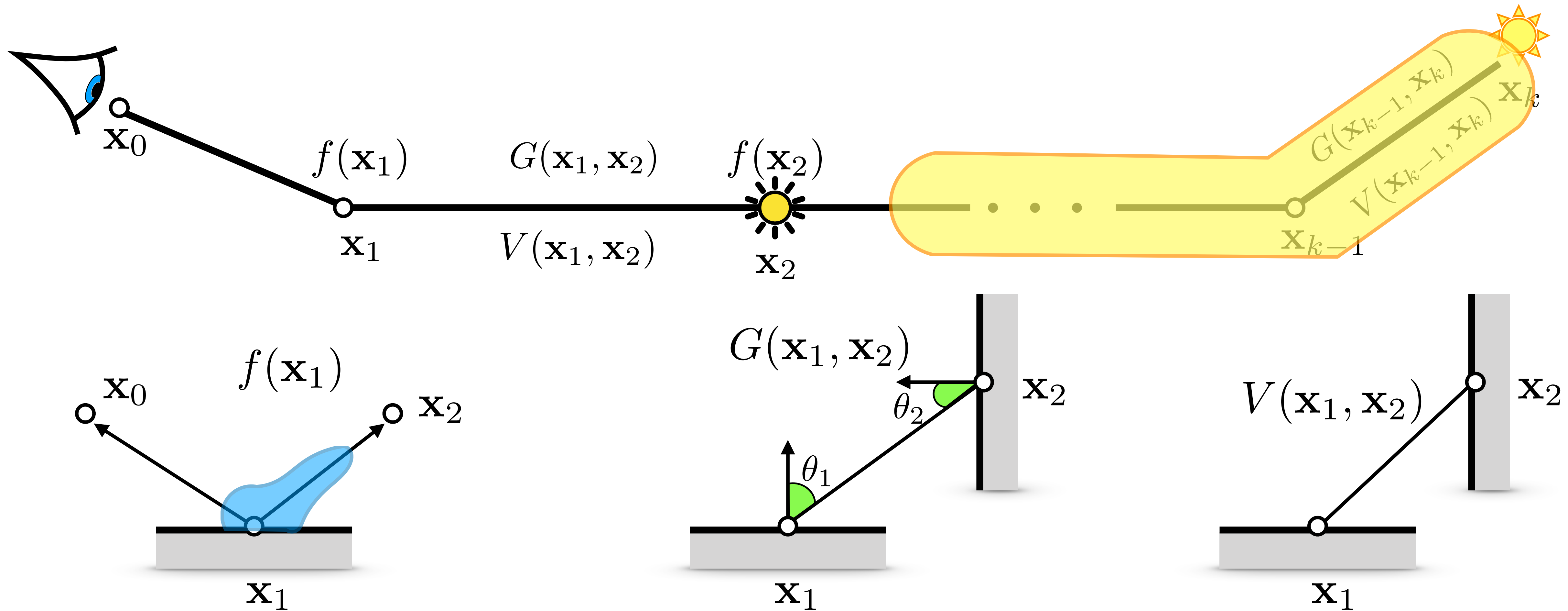
Rendering Equation (area formulation)



Rendering Equation (area formulation)



Rendering Equation (area formulation)



Lighting with VPLs

$$L(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = L_e(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + \int_A f(\mathbf{x}_1) G(\mathbf{x}_1, \mathbf{x}_2) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Lighting with VPLs

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$$L(\mathbf{x}_1 \rightarrow \mathbf{x}_0) \approx L_e(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + \sum_{k=1}^N f(\mathbf{x}_1) G(\mathbf{x}_1, \mathbf{x}_2^i) V(\mathbf{x}_1, \mathbf{x}_2^i) f(\mathbf{x}_2^i) \Phi_i$$

Lighting with VPLs

$$L(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = L_e(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + \int_A f(\mathbf{x}_1) G(\mathbf{x}_1, \mathbf{x}_2) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$
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Lighting with VPLs

$$L(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = L_e(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + \int_A f(\mathbf{x}_1) G(\mathbf{x}_1, \mathbf{x}_2) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

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Lighting with VPLs

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Lighting with VPLs

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Approximation using VPLs

\mathbf{x}_2^i : position of the i -th VPL

Φ^i : flux of the i -th VPL

recursion is hidden
in the generation of VPLs

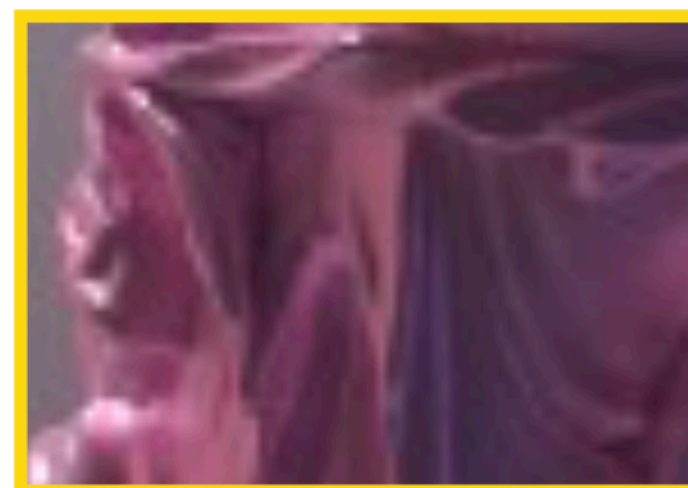
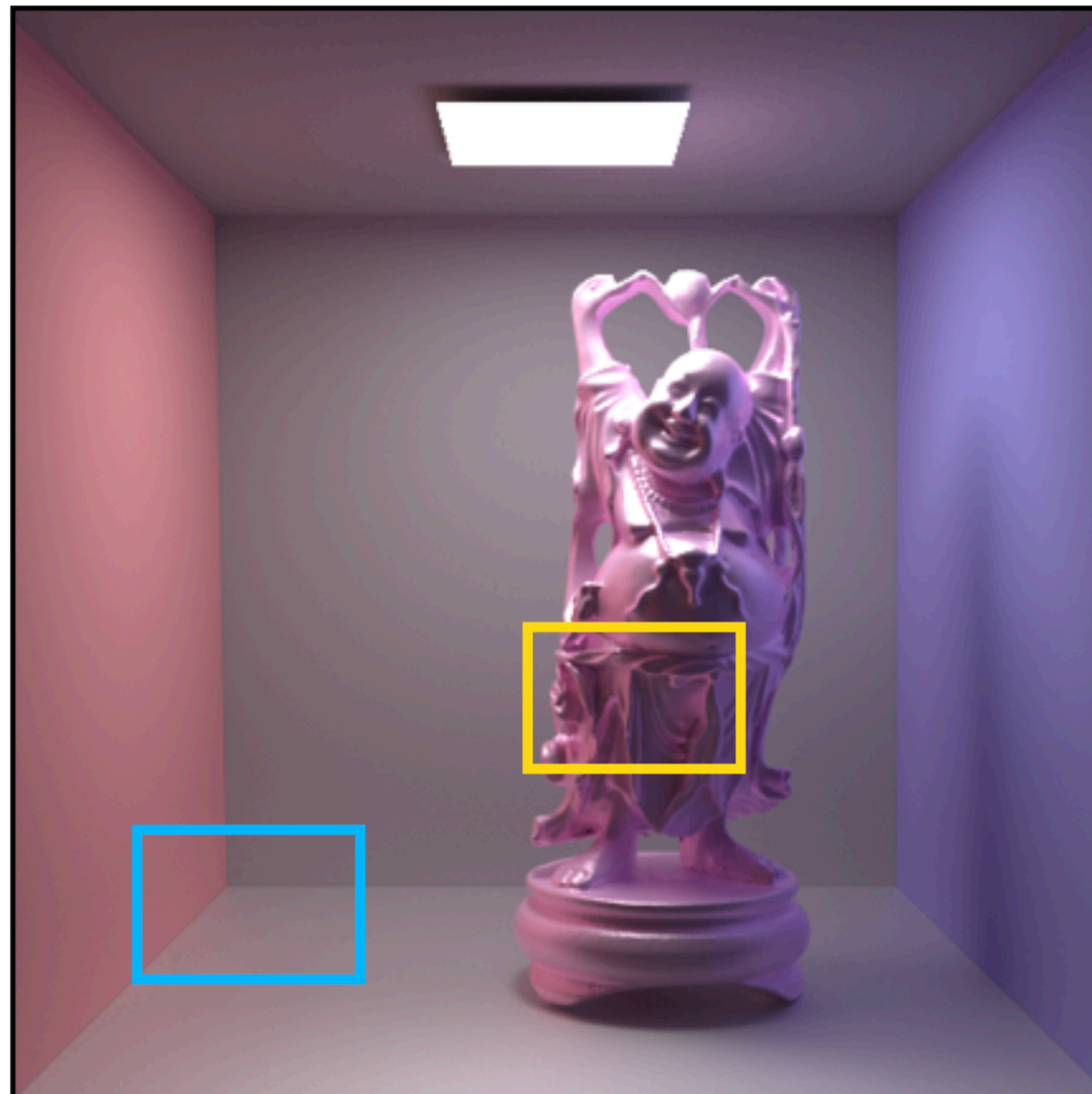
Lighting with VPLs

Reference

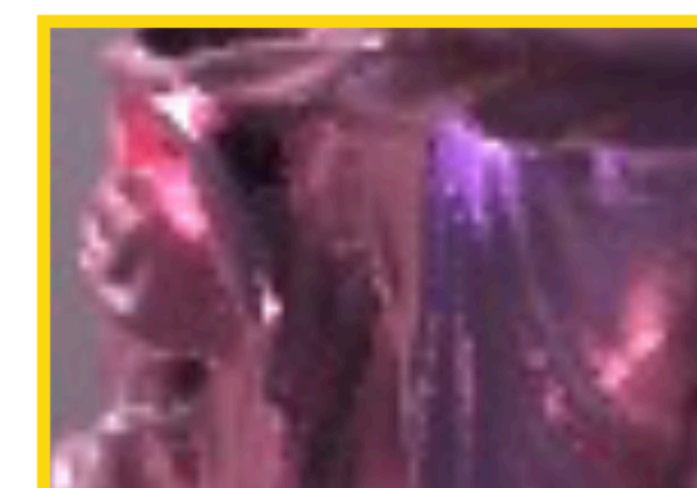
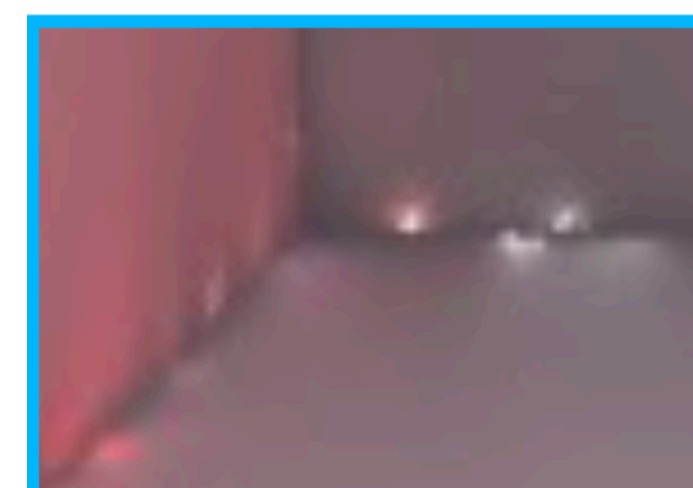


Lighting with VPLs

Reference



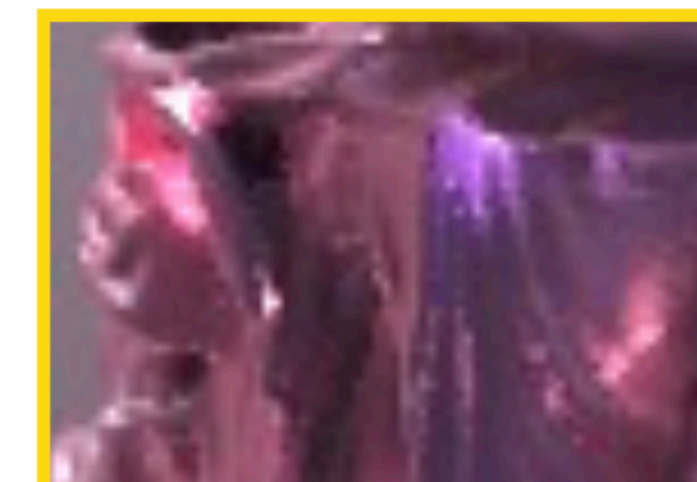
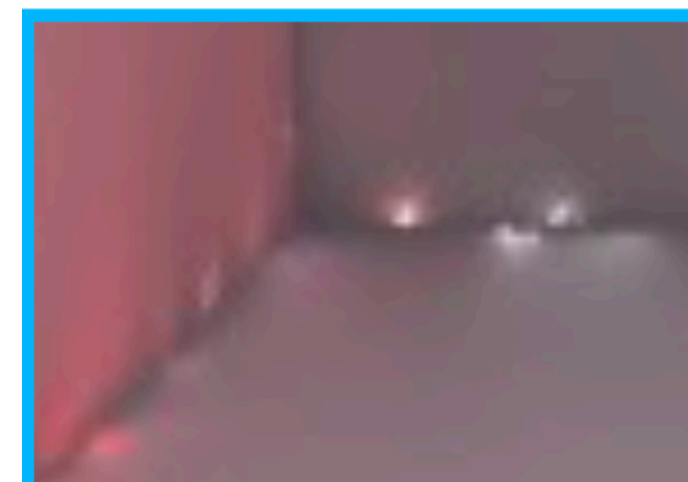
Approximation with VPLs



Lighting with VPLs

Why there are Splotches?

Approximation with VPLs

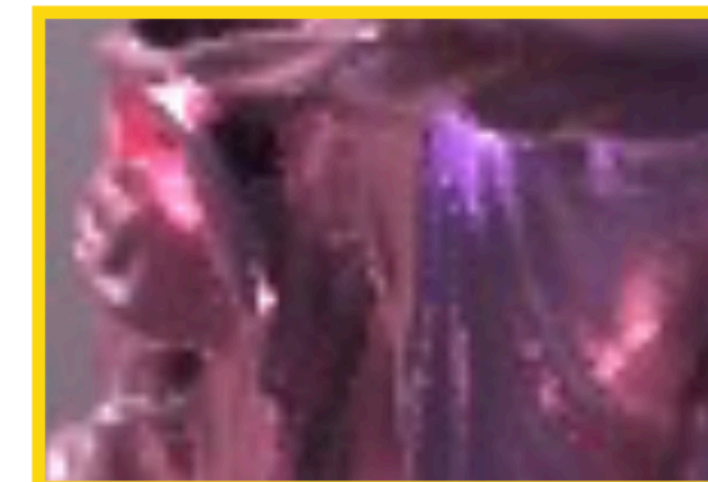
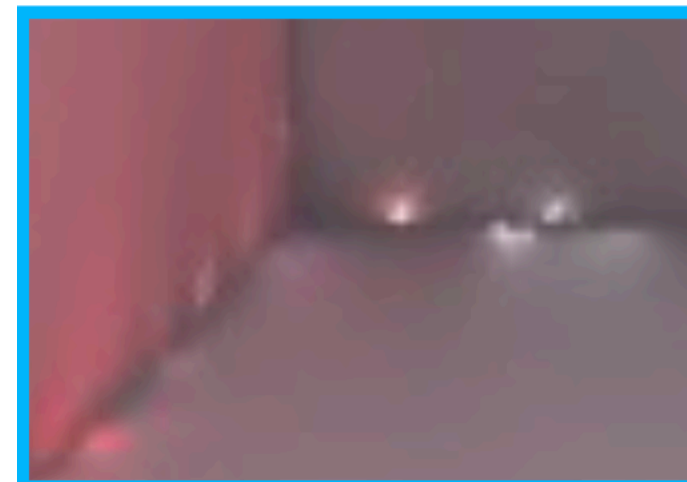


Lighting with VPLs

Why there are Splotches?

1. Have a look at the geometric term:

Approximation with VPLs

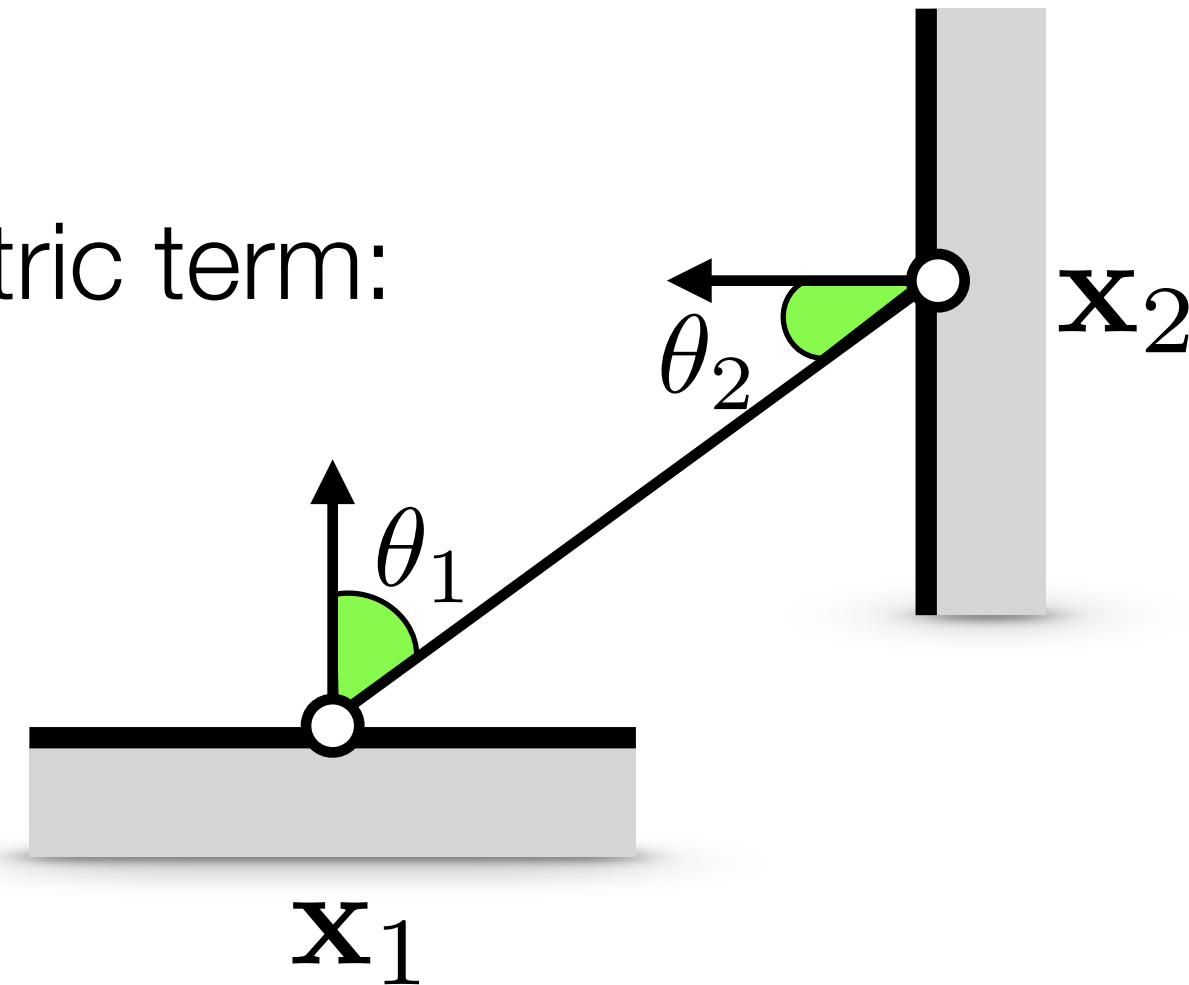


Lighting with VPLs

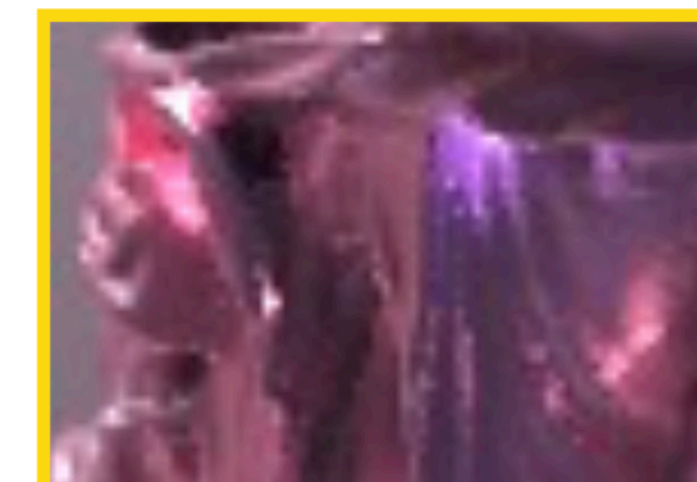
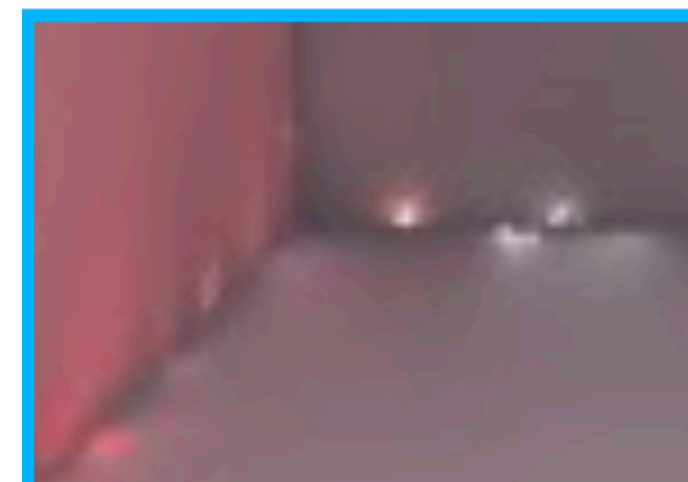
Why there are Splotches?

1. Have a look at the geometric term:

$$G(\mathbf{x}_1, \mathbf{x}_2) = \frac{\cos \theta_1 \cos \theta_2}{\|\mathbf{x}_1 - \mathbf{x}_2\|^2}$$



Approximation with VPLs

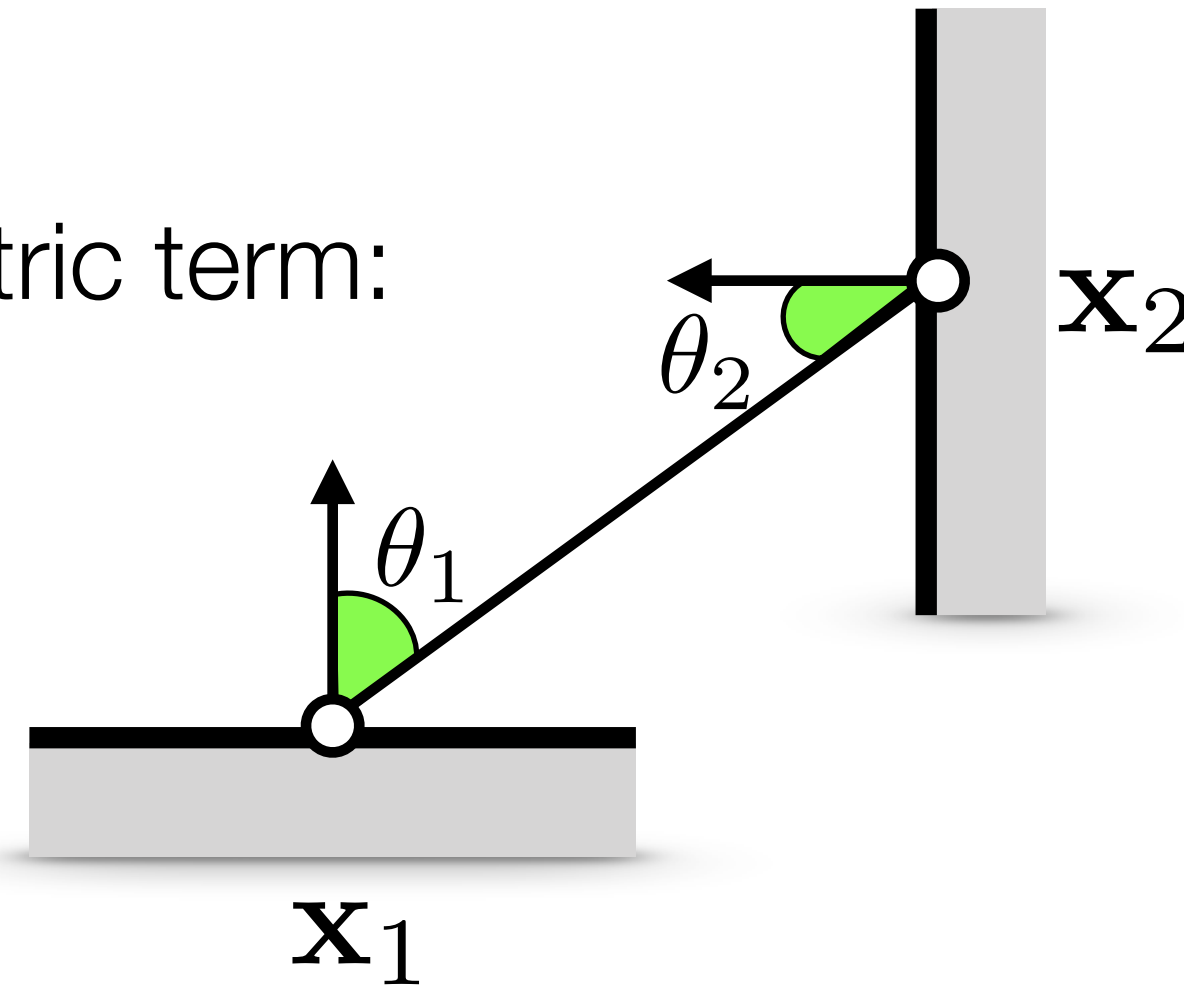


Lighting with VPLs

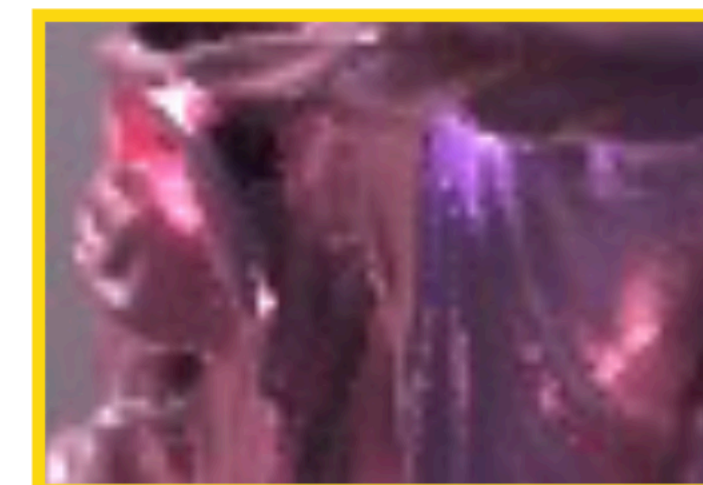
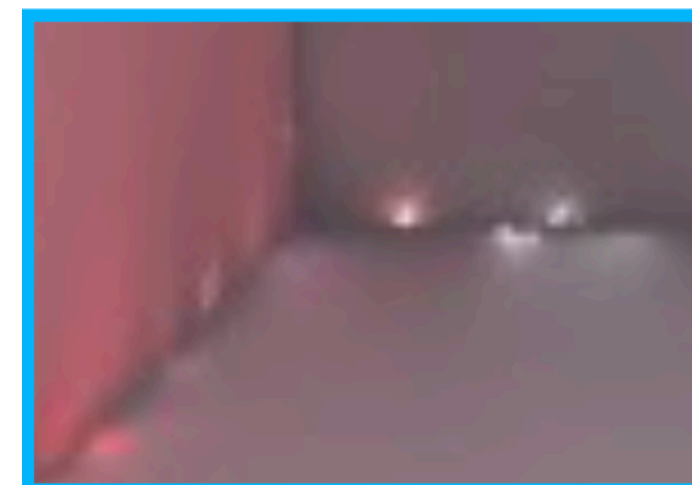
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Approximation with VPLs



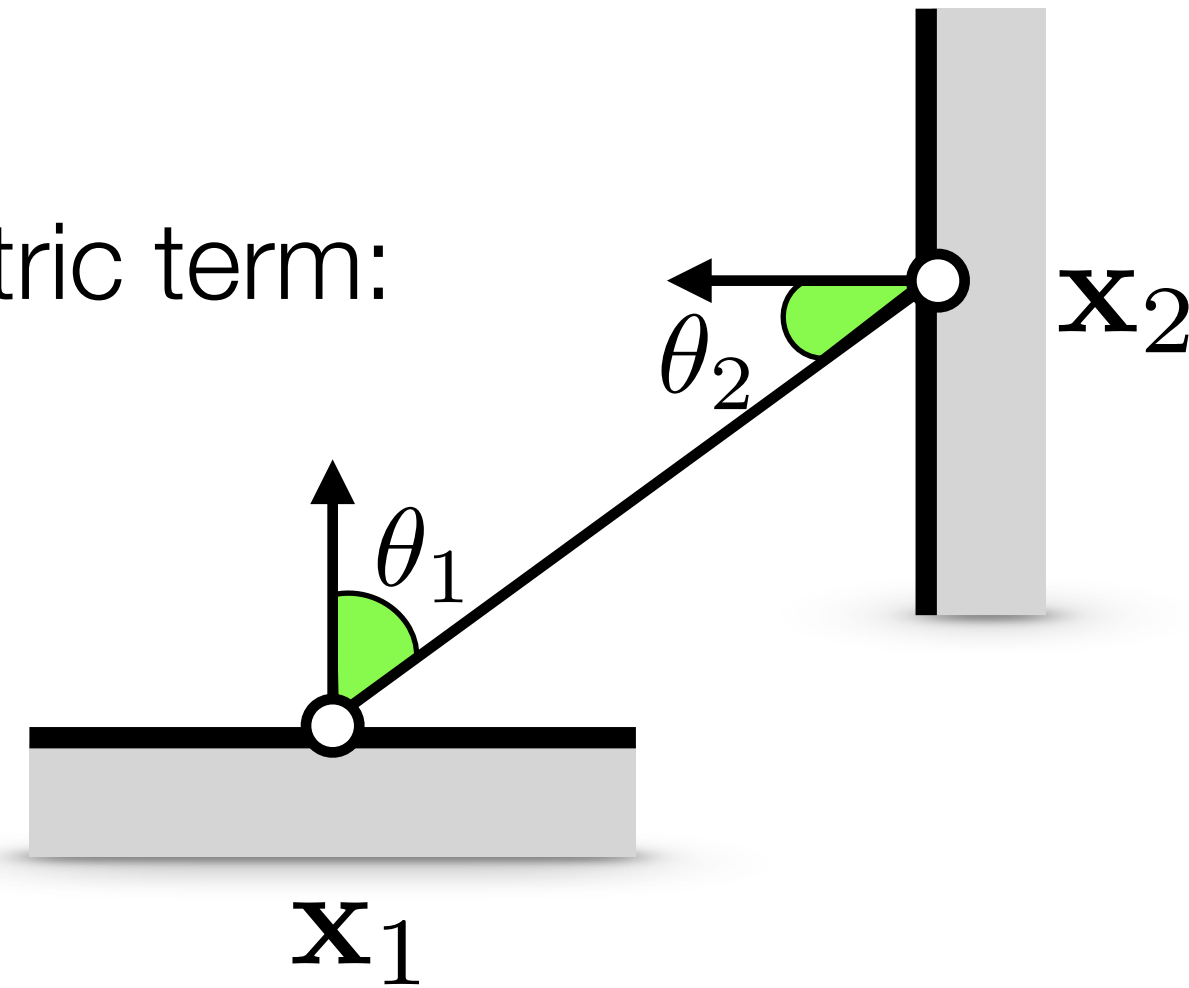
Lighting with VPLs

Why there are Splotches?

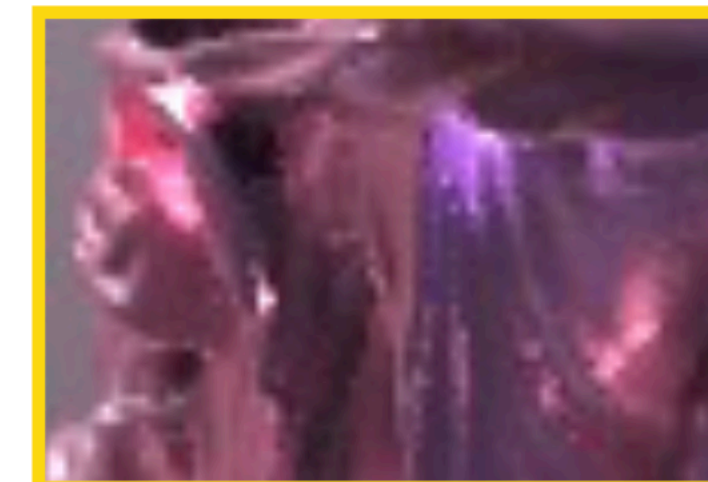
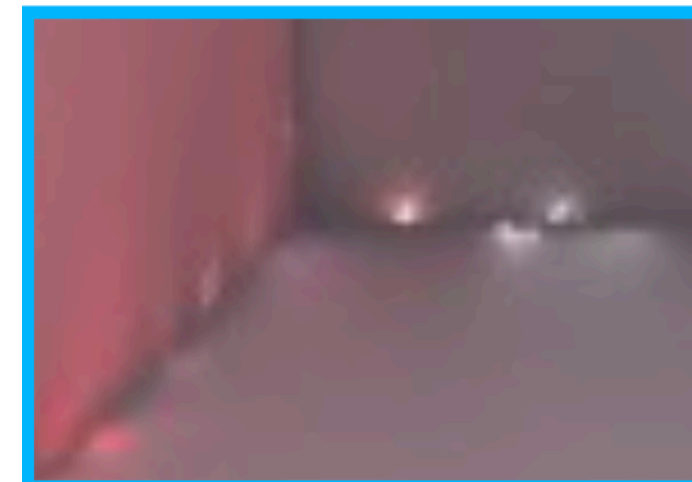
1. Have a look at the geometric term:

$$G(\mathbf{x}_1, \mathbf{x}_2) = \frac{\cos \theta_1 \cos \theta_2}{\|\mathbf{x}_1 - \mathbf{x}_2\|^2}$$

Singularity



Approximation with VPLs



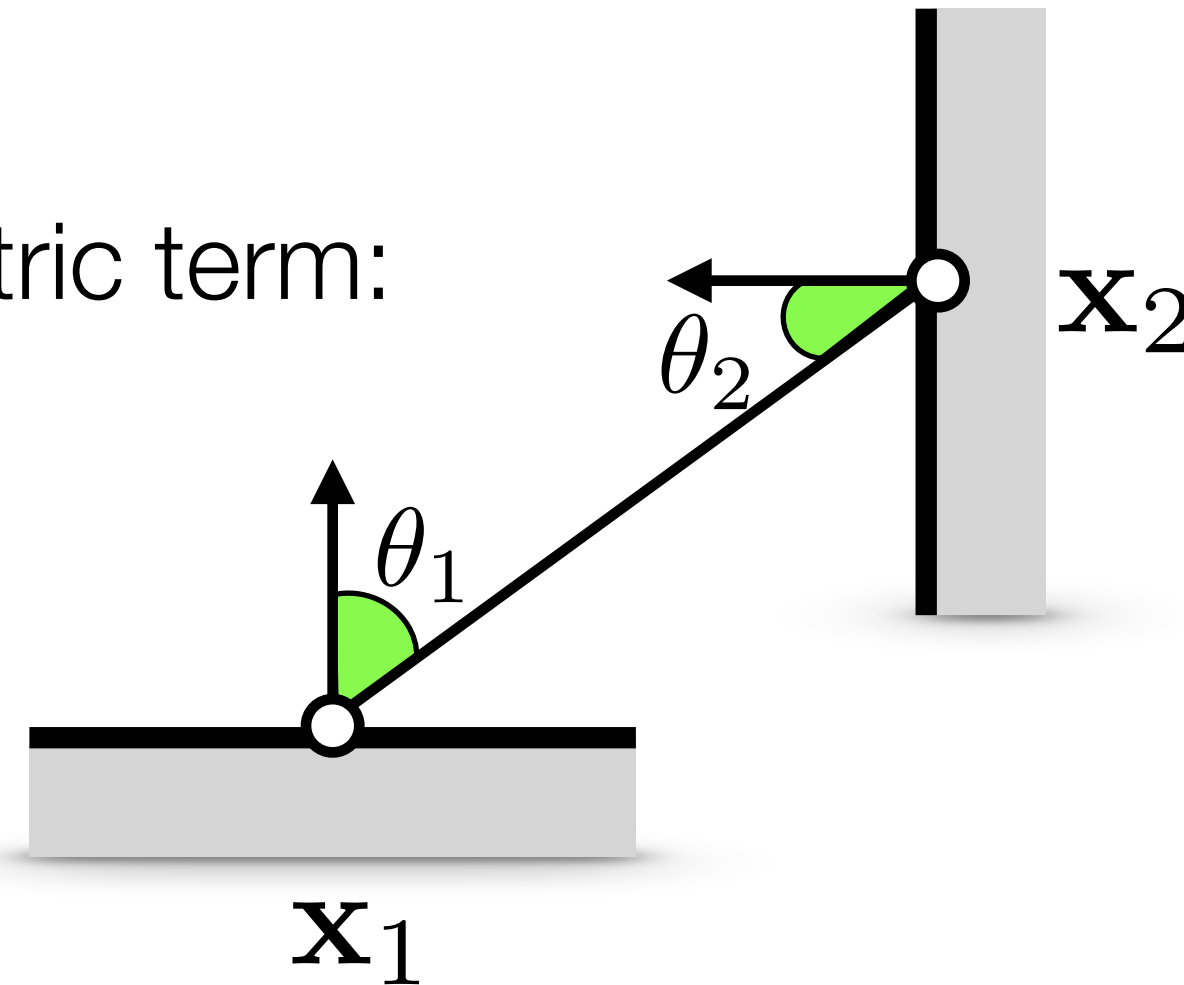
Lighting with VPLs

Why there are Splotches?

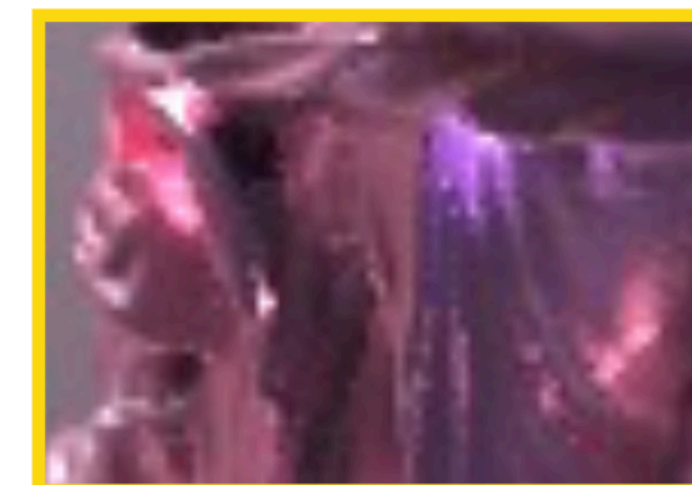
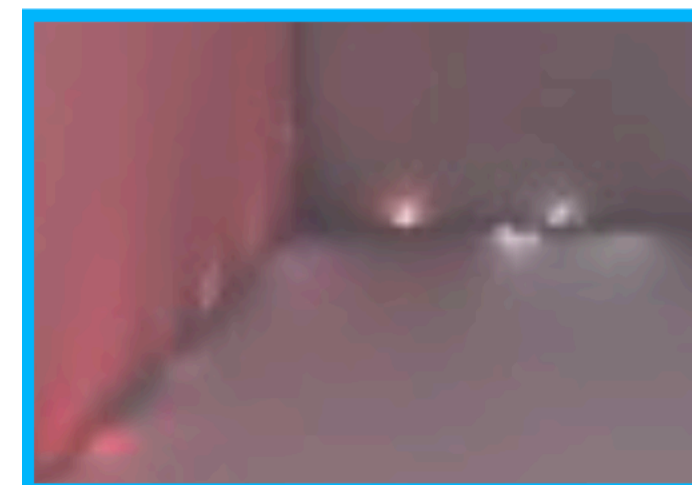
1. Have a look at the geometric term:

$$G(\mathbf{x}_1, \mathbf{x}_2) = \frac{\cos \theta_1 \cos \theta_2}{\|\mathbf{x}_1 - \mathbf{x}_2\|^2}$$

Singularity



Approximation with VPLs



2. All points are lit by the same set of VPLs
- introduce bad correlations

Lighting with VPLs

How to avoid Splotches?

Solutions:

1) Bound the geometry

- remove energy, darkens the image
- to get unbiased results, we need to compensate for the bounding

2) Distribute the flux of a VPL over area (volume)

- redistributes energy, blurs the illumination
- to get consistent results, progressively reduce the blurring

Lighting with VPLs

How to avoid Splotches?

Solutions:

1) Bound the geometry

- remove energy, darkens the image
- to get unbiased results, we need to compensate for the bounding

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- redistributes energy, blurs the illumination
- to get consistent results, progressively reduce the blurring

Lighting with VPLs

1) Bound the geometry

- prevent G from being very high
- user-defined maximum value

$$G_b(\mathbf{x}_1, \mathbf{x}_2) = \min(G(\mathbf{x}_1, \mathbf{x}_2), b)$$

Lighting with VPLs

1) Bound the geometry

- prevent G from being very high
- user-defined maximum value

$$G_b(\mathbf{x}_1, \mathbf{x}_2) = \min(G(\mathbf{x}_1, \mathbf{x}_2), b)$$

Advantage:

- extremely simple and fast

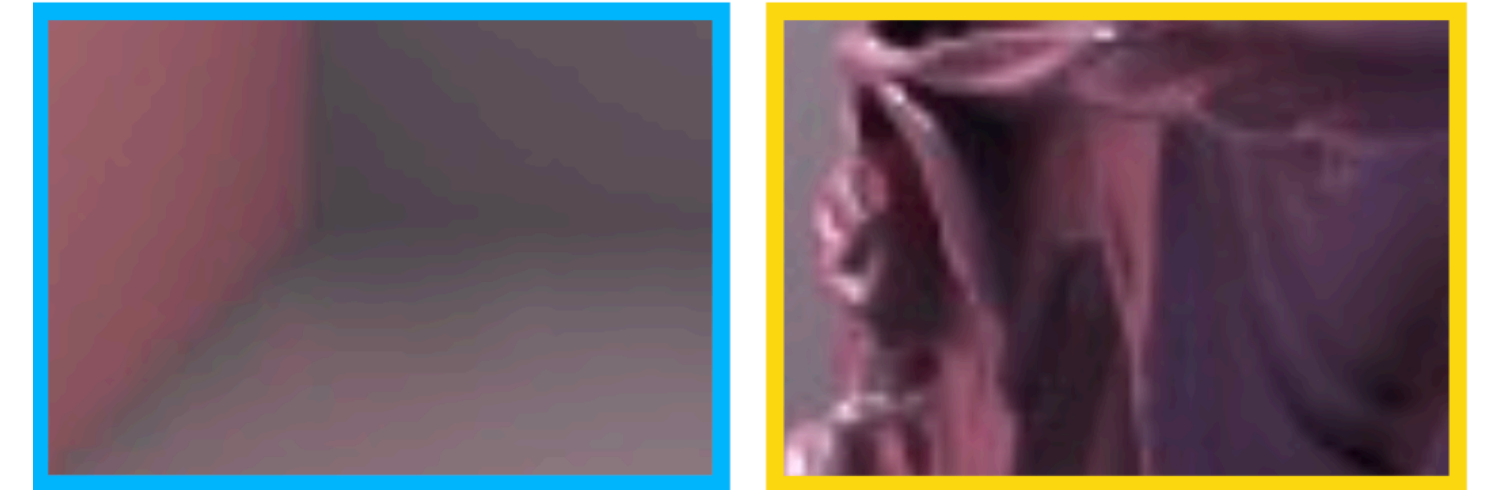
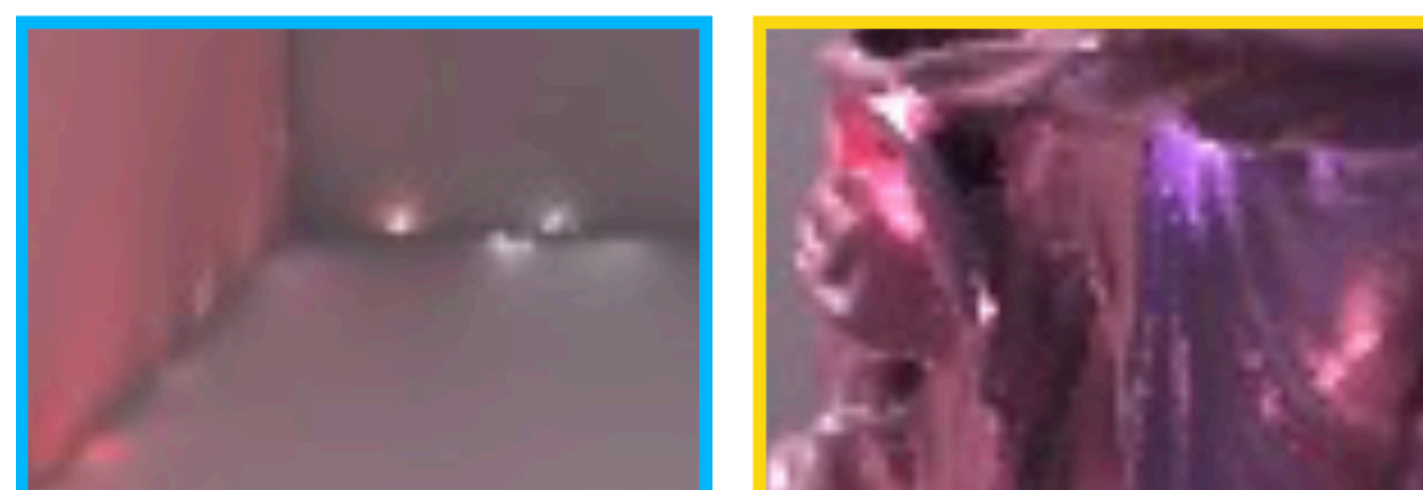
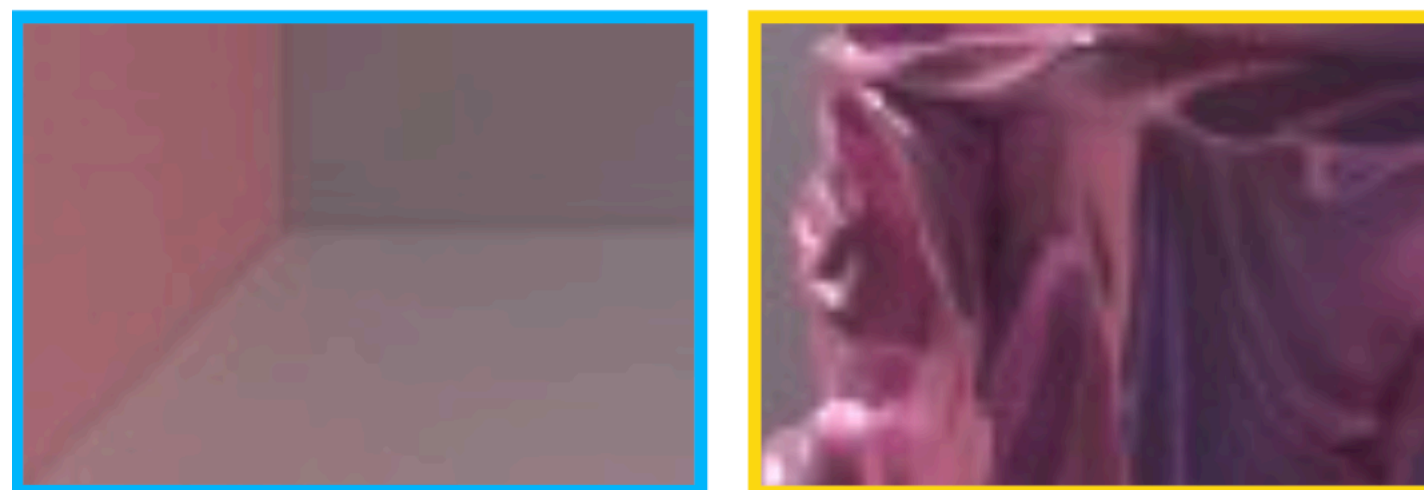
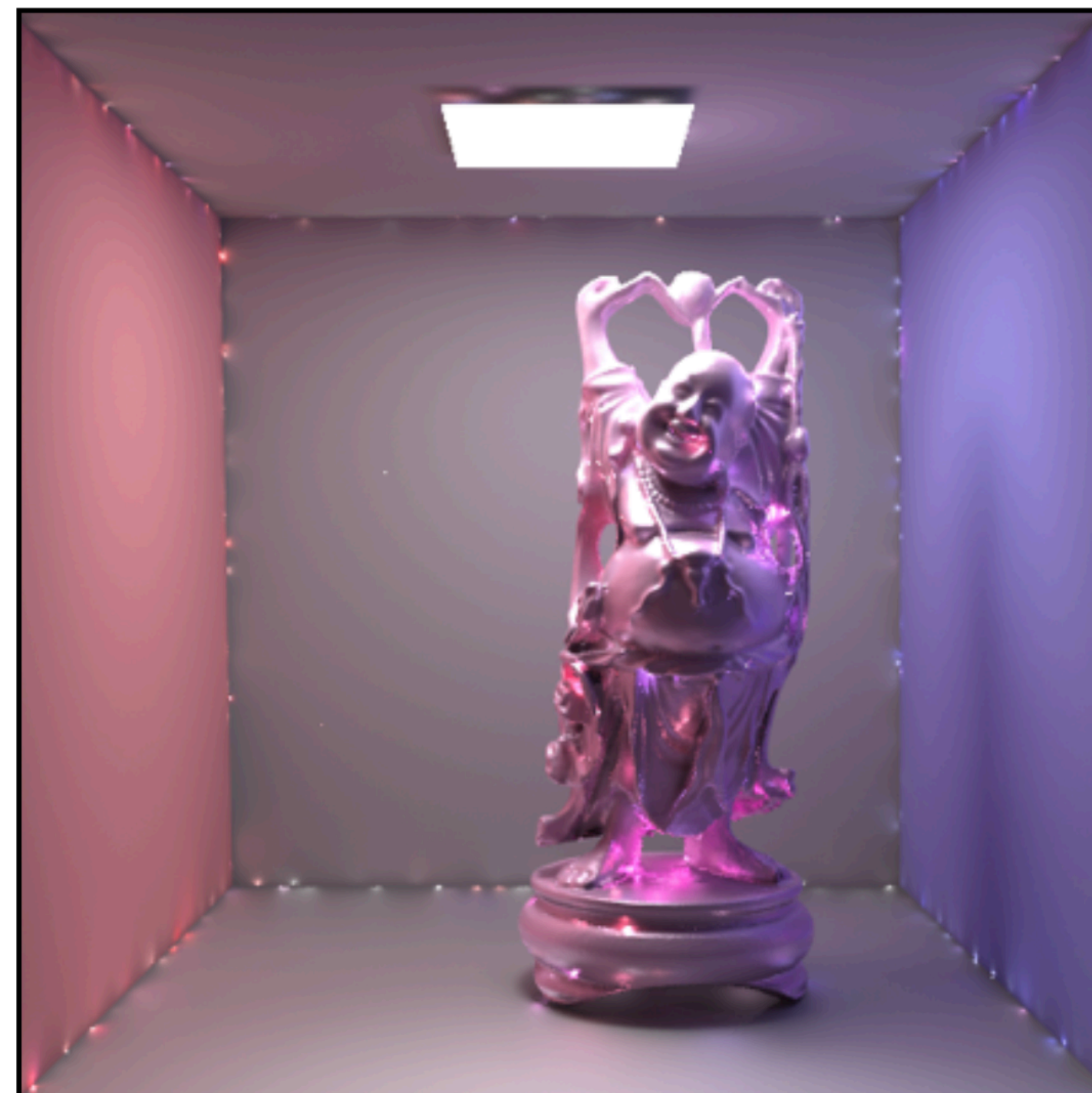
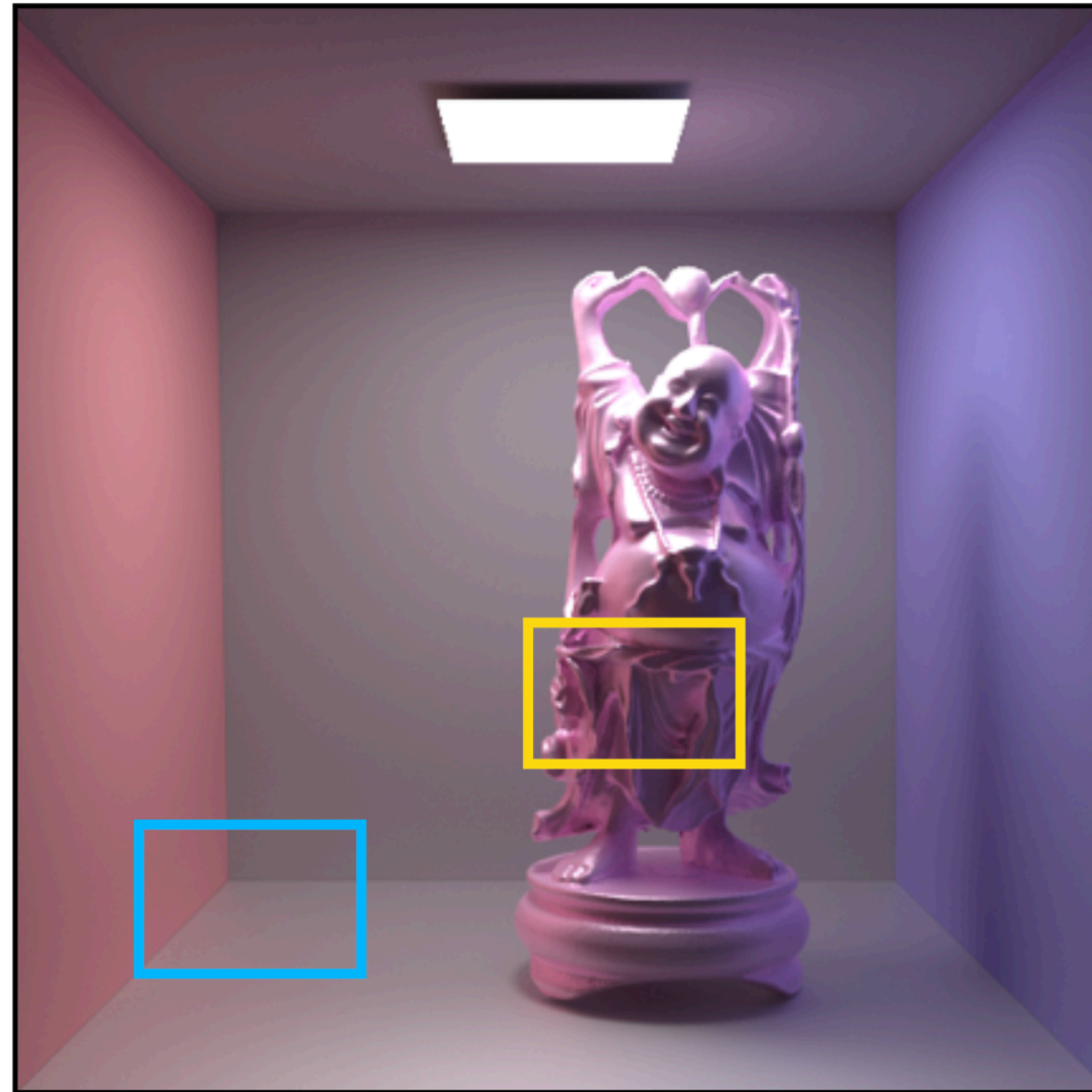
Disadvantages:

- removes energy, darkens the image

Reference

VPLs

VPLs with bounded G



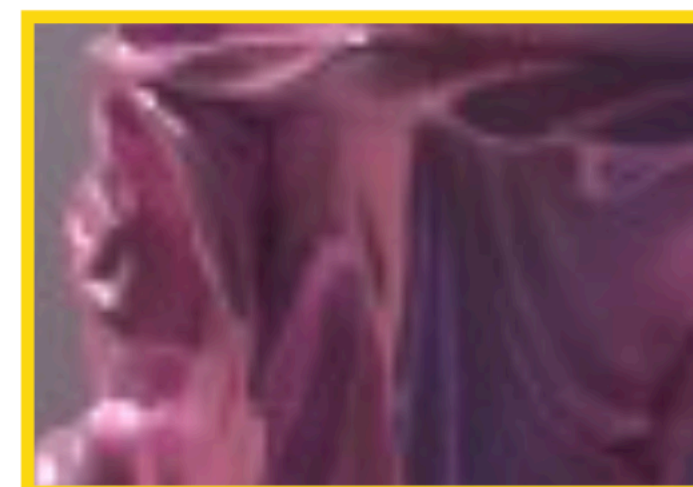
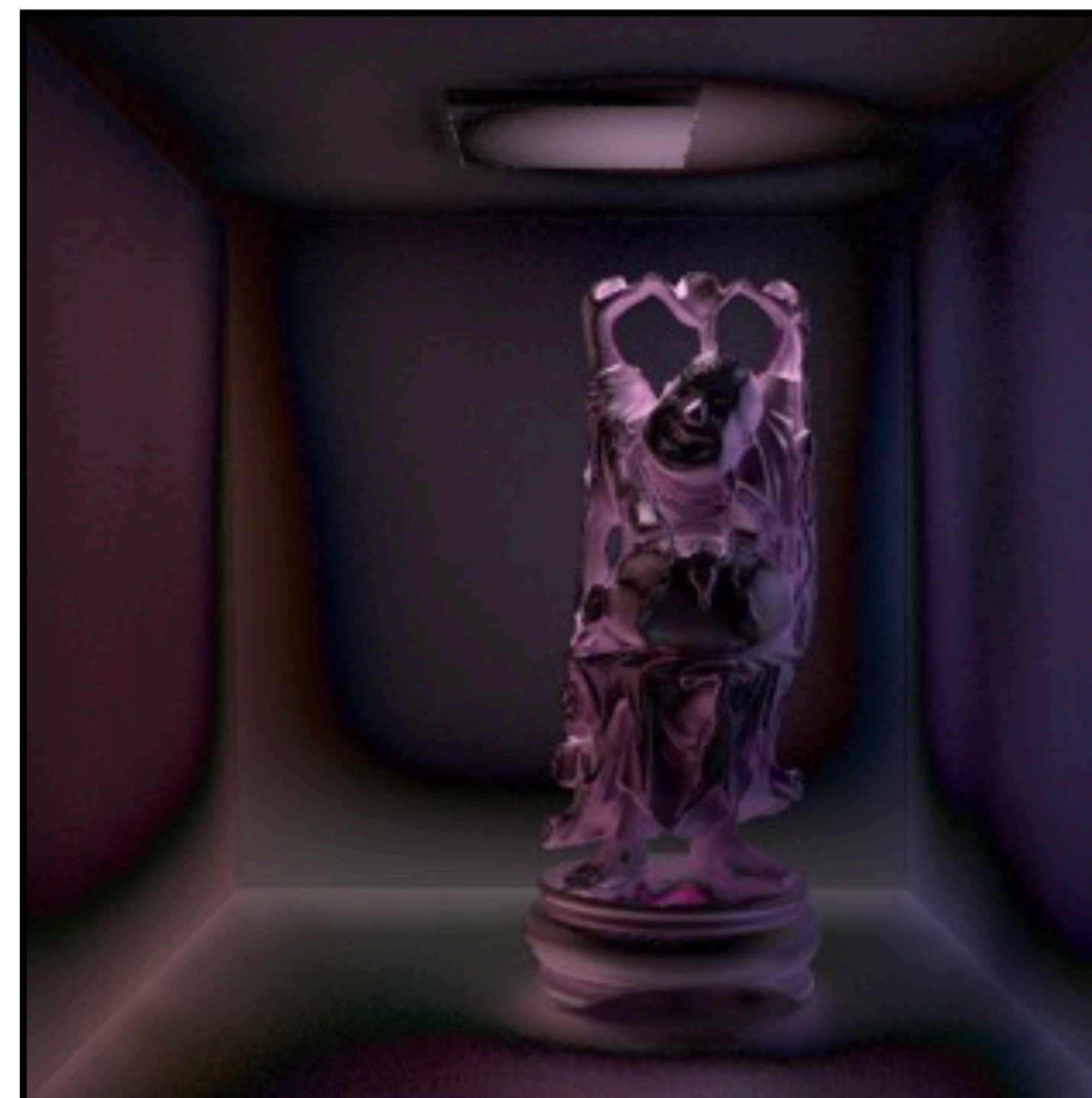
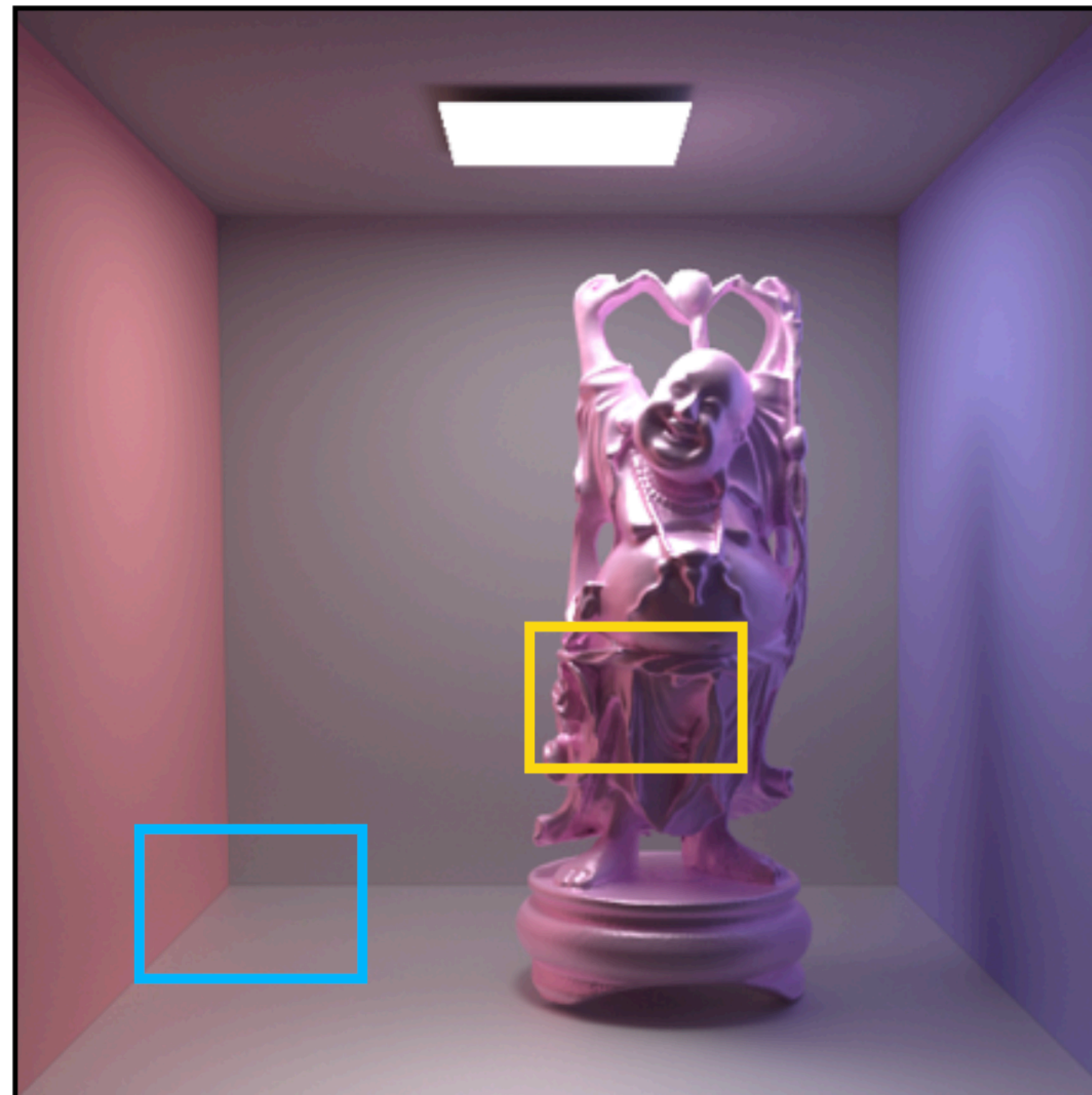
using $G(\mathbf{x}_1, \mathbf{x}_2)$

using $G_b(\mathbf{x}_1, \mathbf{x}_2)$

Reference

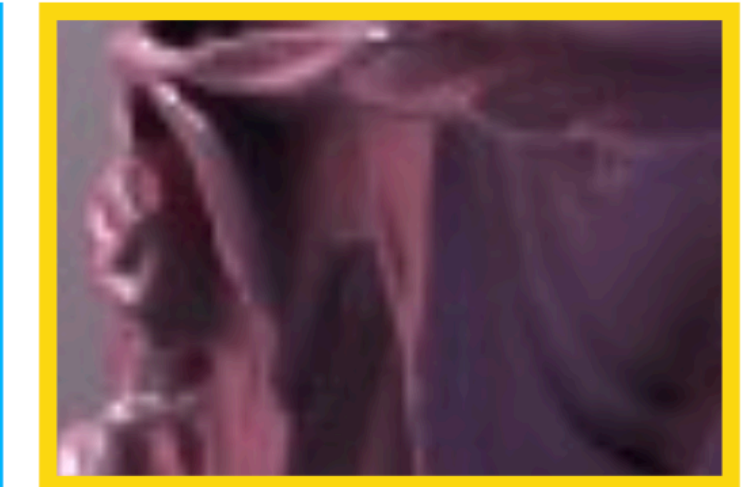
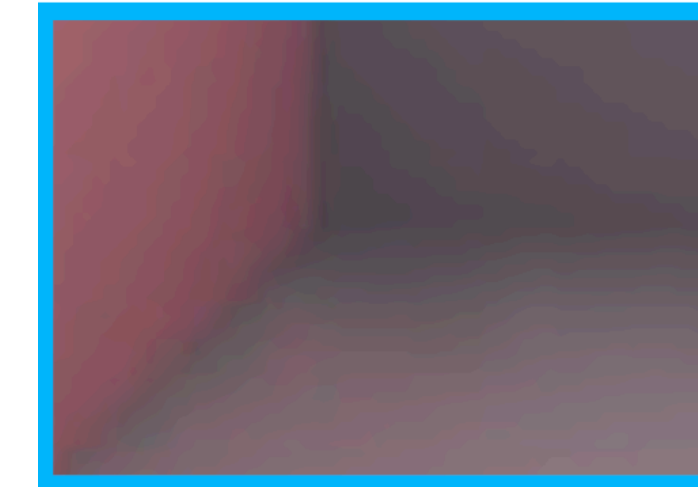
Difference

VPLs with bounded G'



$$G(\mathbf{x}_1, \mathbf{x}_2) - G_b(\mathbf{x}_1, \mathbf{x}_2)$$

**We need to compensate
for the energy loss!**



using $G_b(\mathbf{x}_1, \mathbf{x}_2)$

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1)G(\mathbf{x}_1, \mathbf{x}_2)V(\mathbf{x}_1, \mathbf{x}_2)L(\mathbf{x}_2 \rightarrow \mathbf{x}_1)dA(\mathbf{x}_2)$$

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) G(\mathbf{x}_1, \mathbf{x}_2) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Bounded light transport operator \mathbf{T}_b

$$(\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) \min(G(\mathbf{x}_1, \mathbf{x}_2), b) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1)G(\mathbf{x}_1, \mathbf{x}_2)V(\mathbf{x}_1, \mathbf{x}_2)L(\mathbf{x}_2 \rightarrow \mathbf{x}_1)dA(\mathbf{x}_2)$$

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$$(\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) \min(G(\mathbf{x}_1, \mathbf{x}_2), b) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Residual light transport operator \mathbf{T}_r

$$(\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) \max(G(\mathbf{x}_1, \mathbf{x}_2) - b, 0) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1)G(\mathbf{x}_1, \mathbf{x}_2)V(\mathbf{x}_1, \mathbf{x}_2)L(\mathbf{x}_2 \rightarrow \mathbf{x}_1)dA(\mathbf{x}_2)$$

Bounded light transport operator \mathbf{T}_b

$$(\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) \min(G(\mathbf{x}_1, \mathbf{x}_2), b) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Residual light transport operator \mathbf{T}_r

$$(\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) \max(G(\mathbf{x}_1, \mathbf{x}_2) - b, 0) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = (\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + (\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0)$$

Bounded light transport operator \mathbf{T}_b

$$(\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) \min(G(\mathbf{x}_1, \mathbf{x}_2), b) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Residual light transport operator \mathbf{T}_r

$$(\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = \int_A f(\mathbf{x}_1) \max(G(\mathbf{x}_1, \mathbf{x}_2) - b, 0) V(\mathbf{x}_1, \mathbf{x}_2) L(\mathbf{x}_2 \rightarrow \mathbf{x}_1) dA(\mathbf{x}_2)$$

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = (\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + (\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0)$$

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = (\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + (\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0)$$



Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = (\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + (\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0)$$



=

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = (\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + (\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0)$$



=



Estimated
using VPLs

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = (\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + (\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0)$$



=



+

Estimated
using VPLs

Bounding and Compensation

Light transport operator \mathbf{T}

$$(\mathbf{T}L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) = (\mathbf{T}_b L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0) + (\mathbf{T}_r L)(\mathbf{x}_1 \rightarrow \mathbf{x}_0)$$

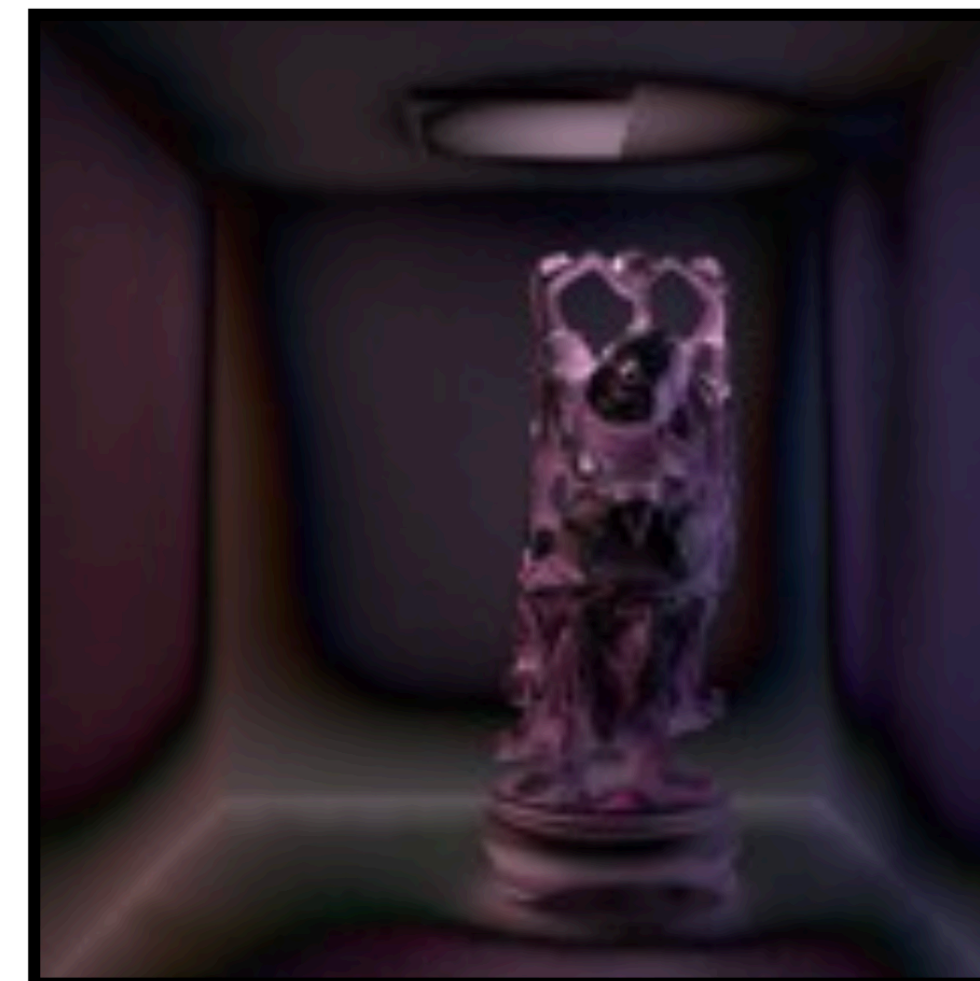


=



Estimated
using VPLs

+



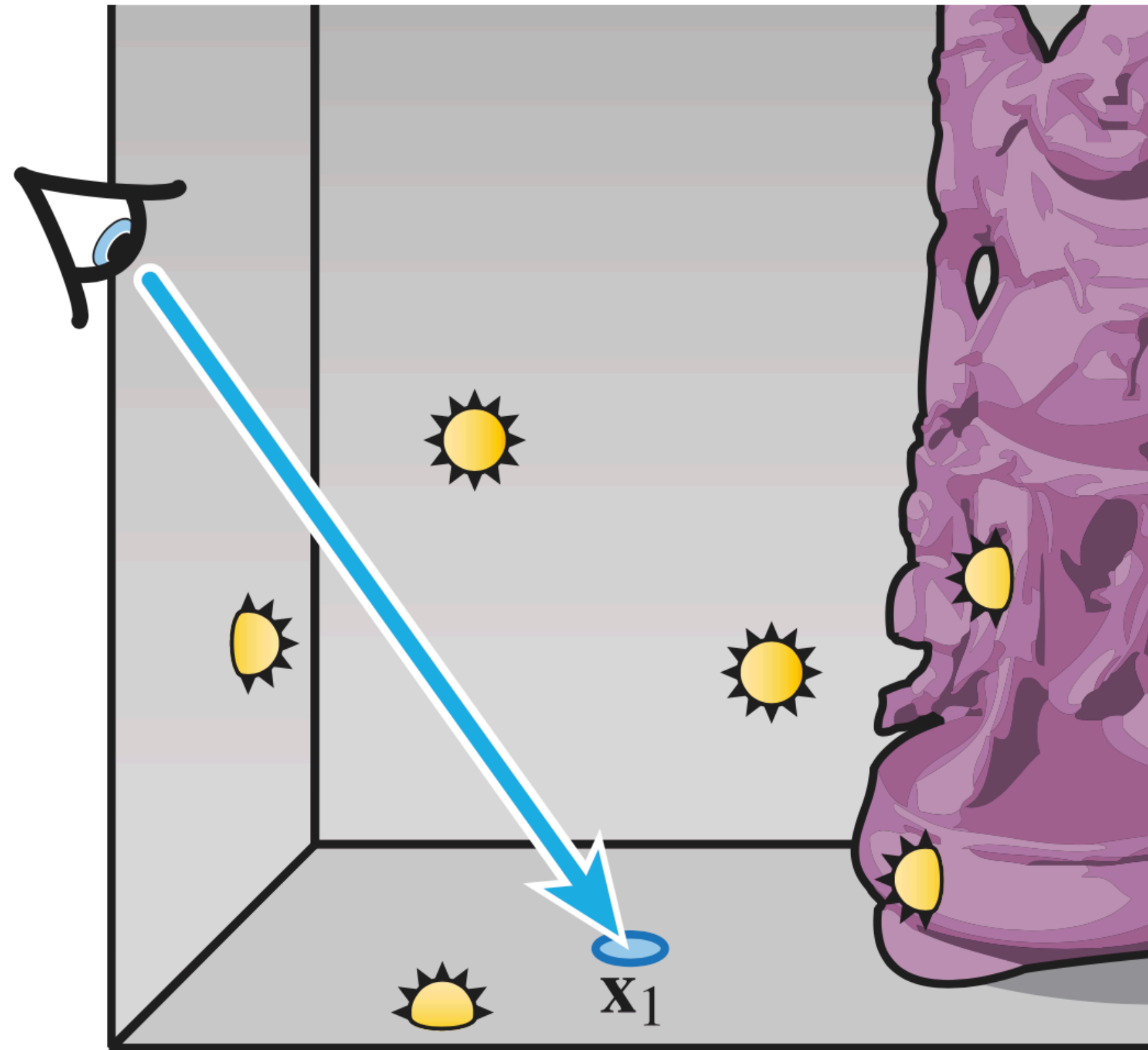
Estimated differently

How to compute residual transport?

Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

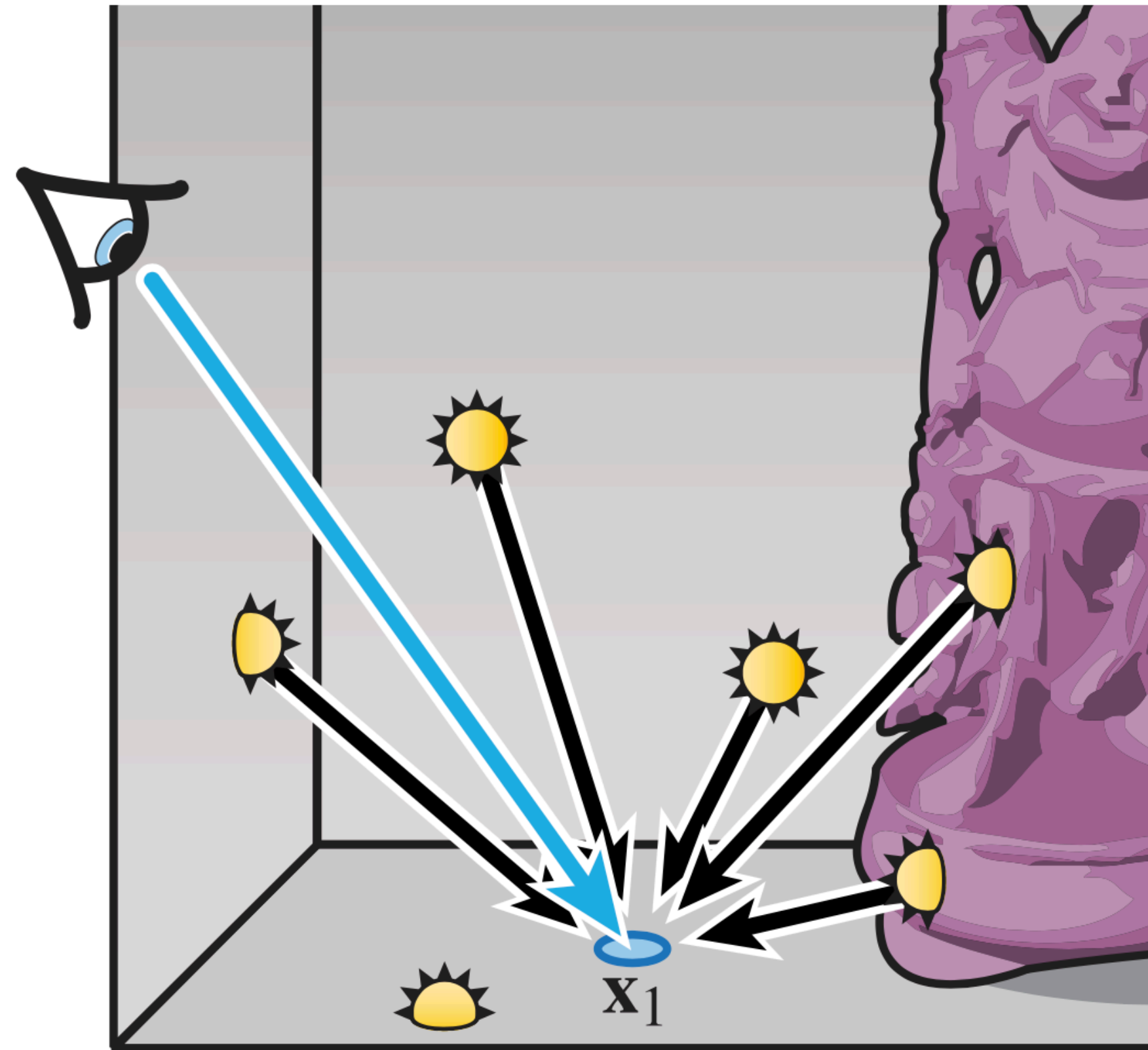
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

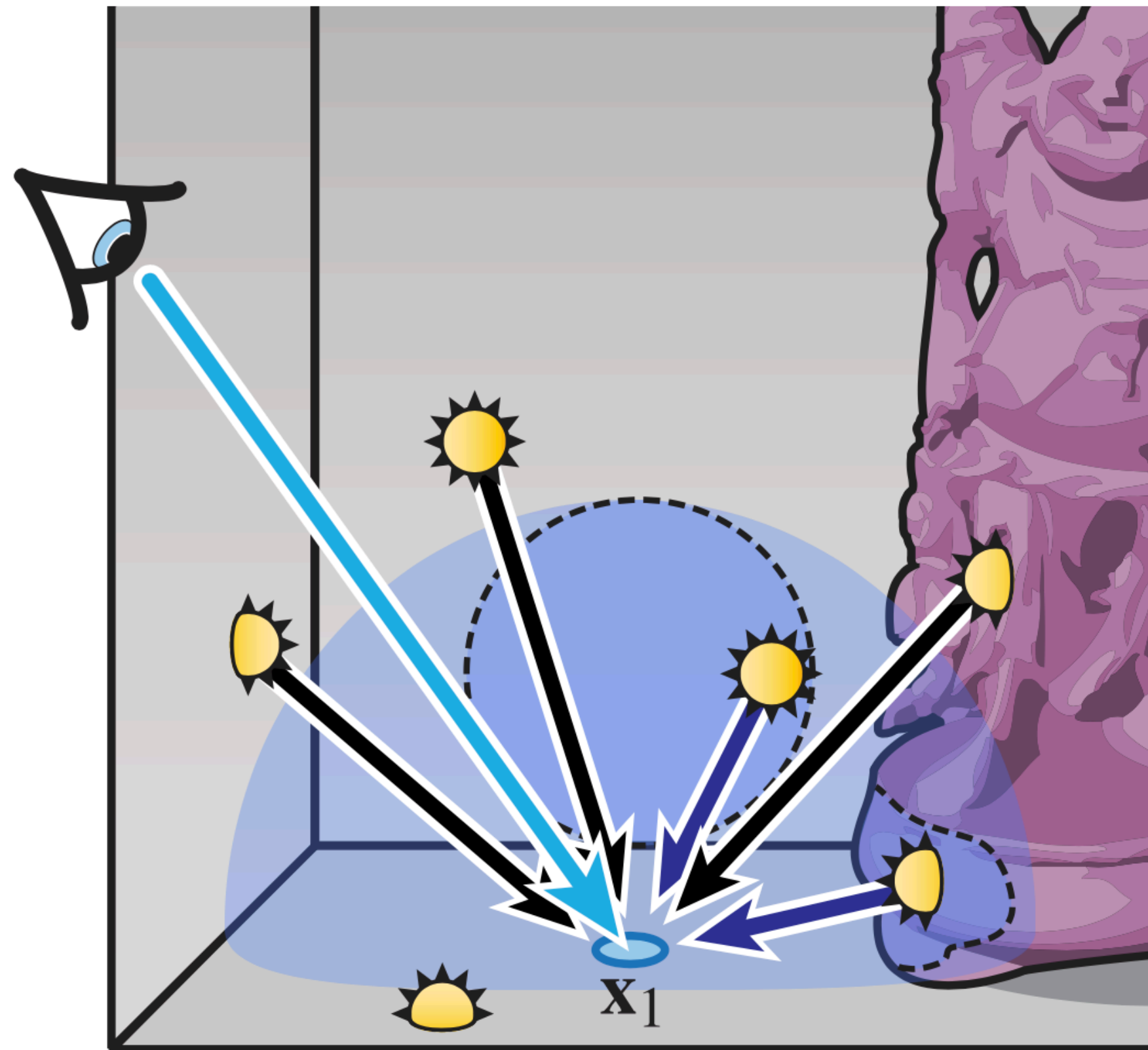
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

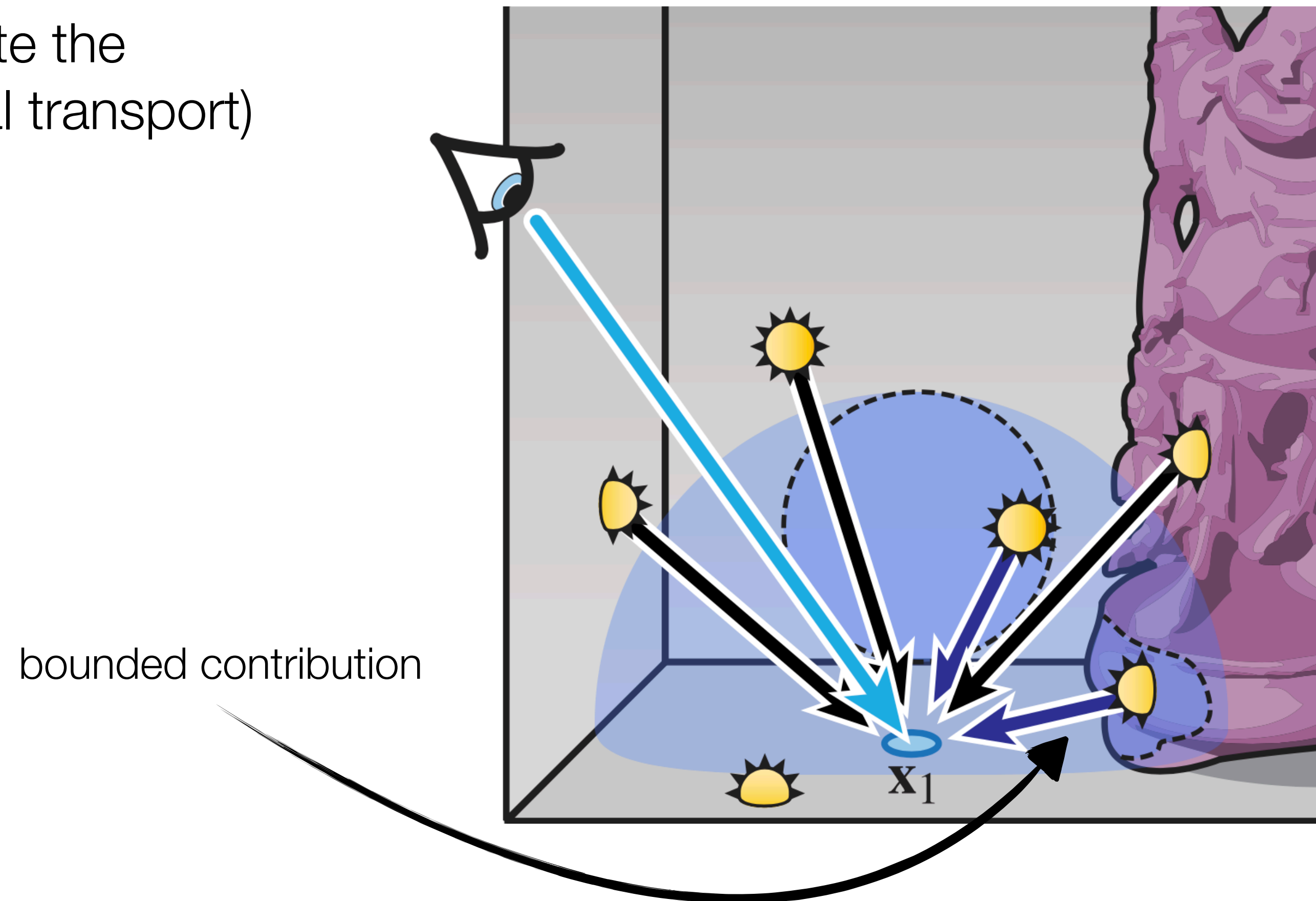
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

Trace paths to compute the compensation term (residual transport)

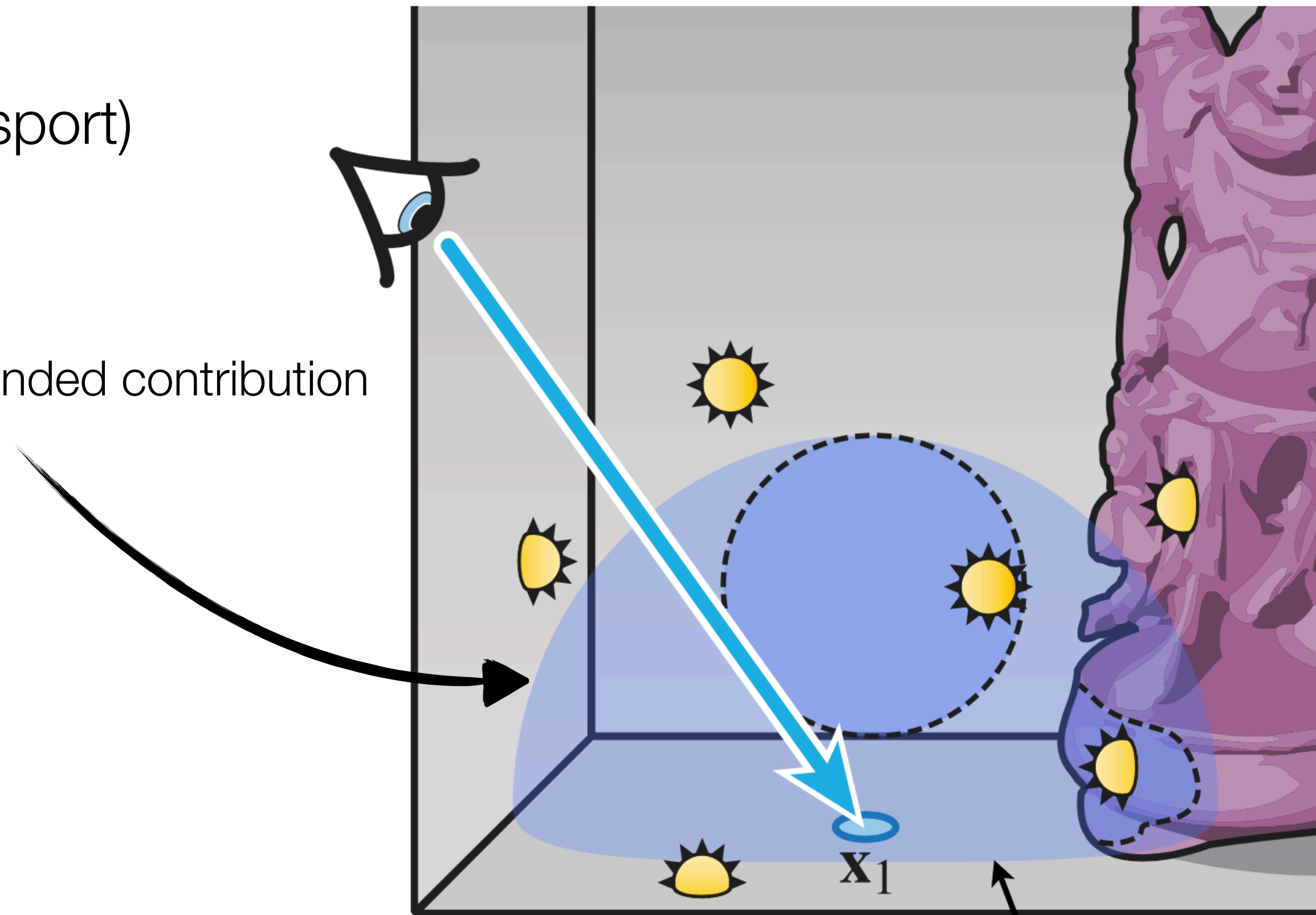


Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

Trace paths to compute the compensation term (residual transport)

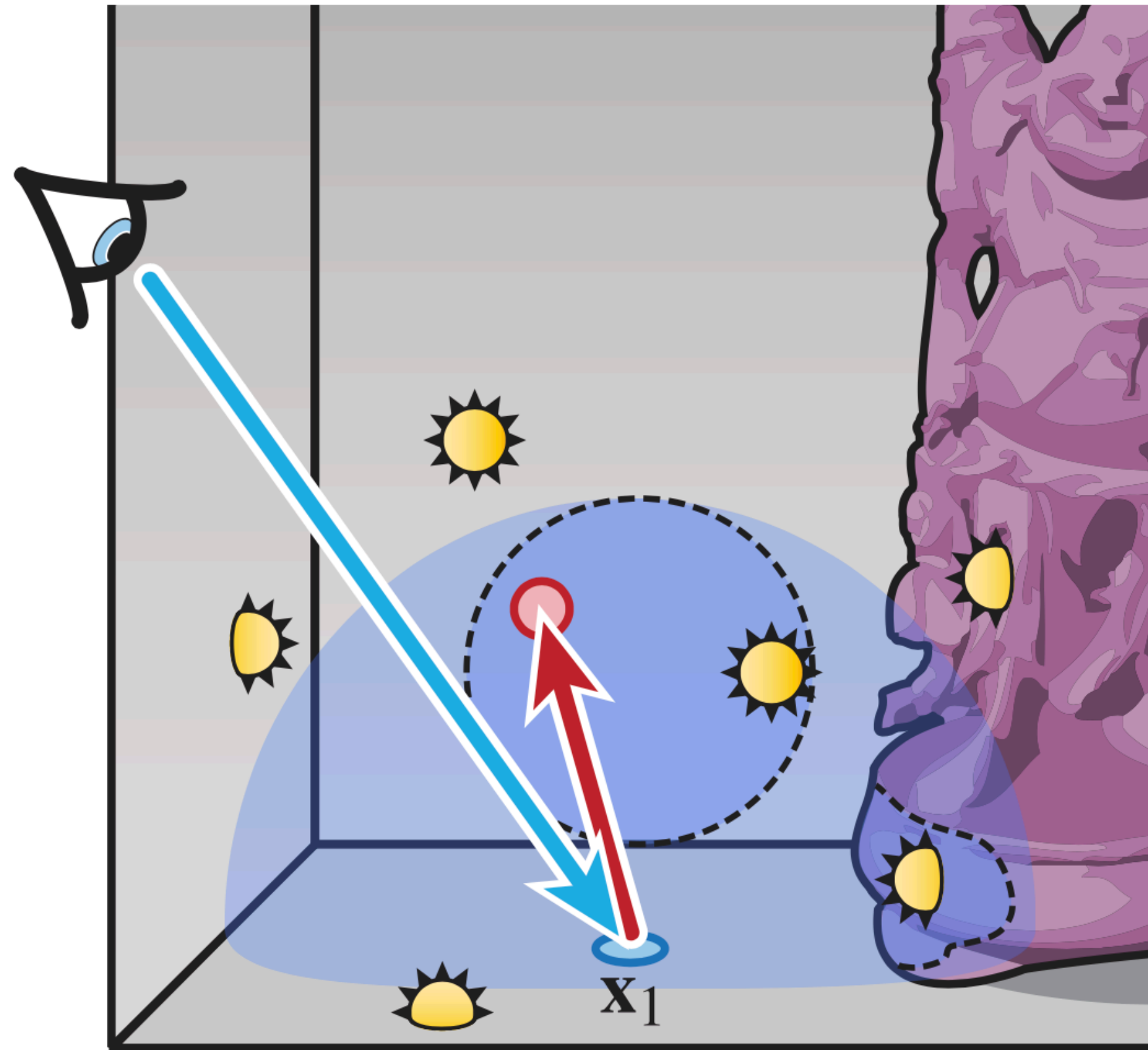
Region with bounded contribution



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

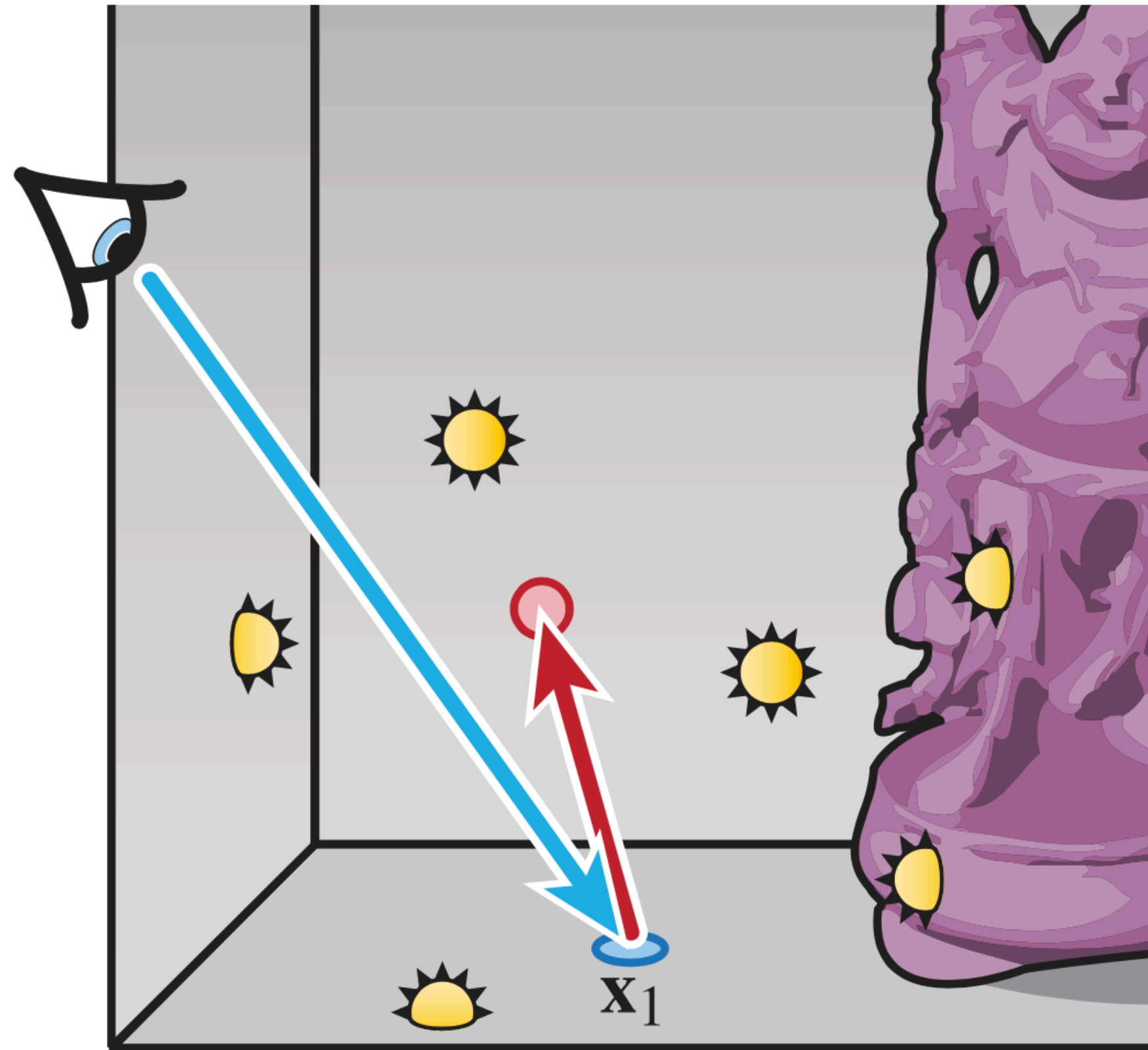
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

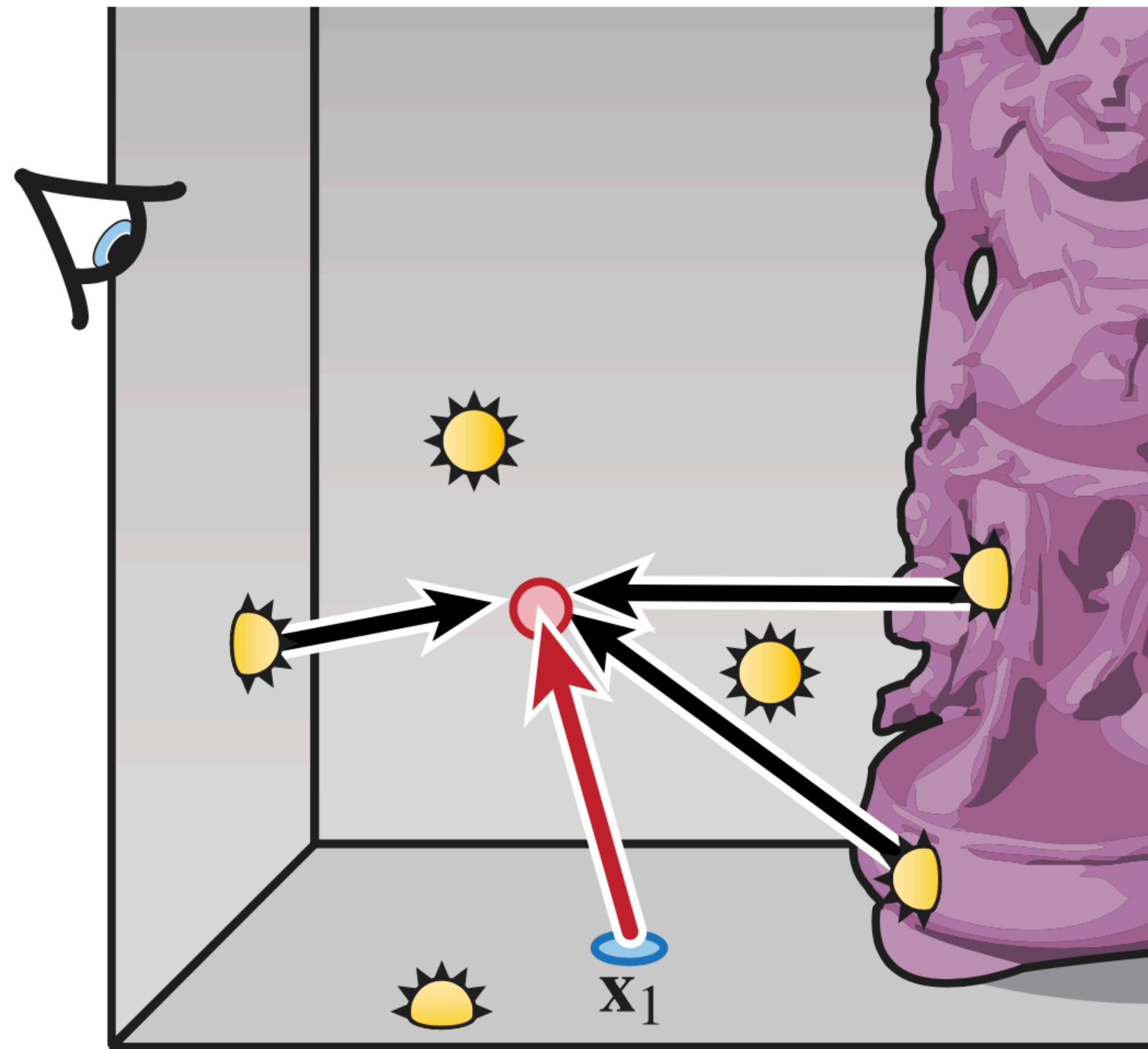
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

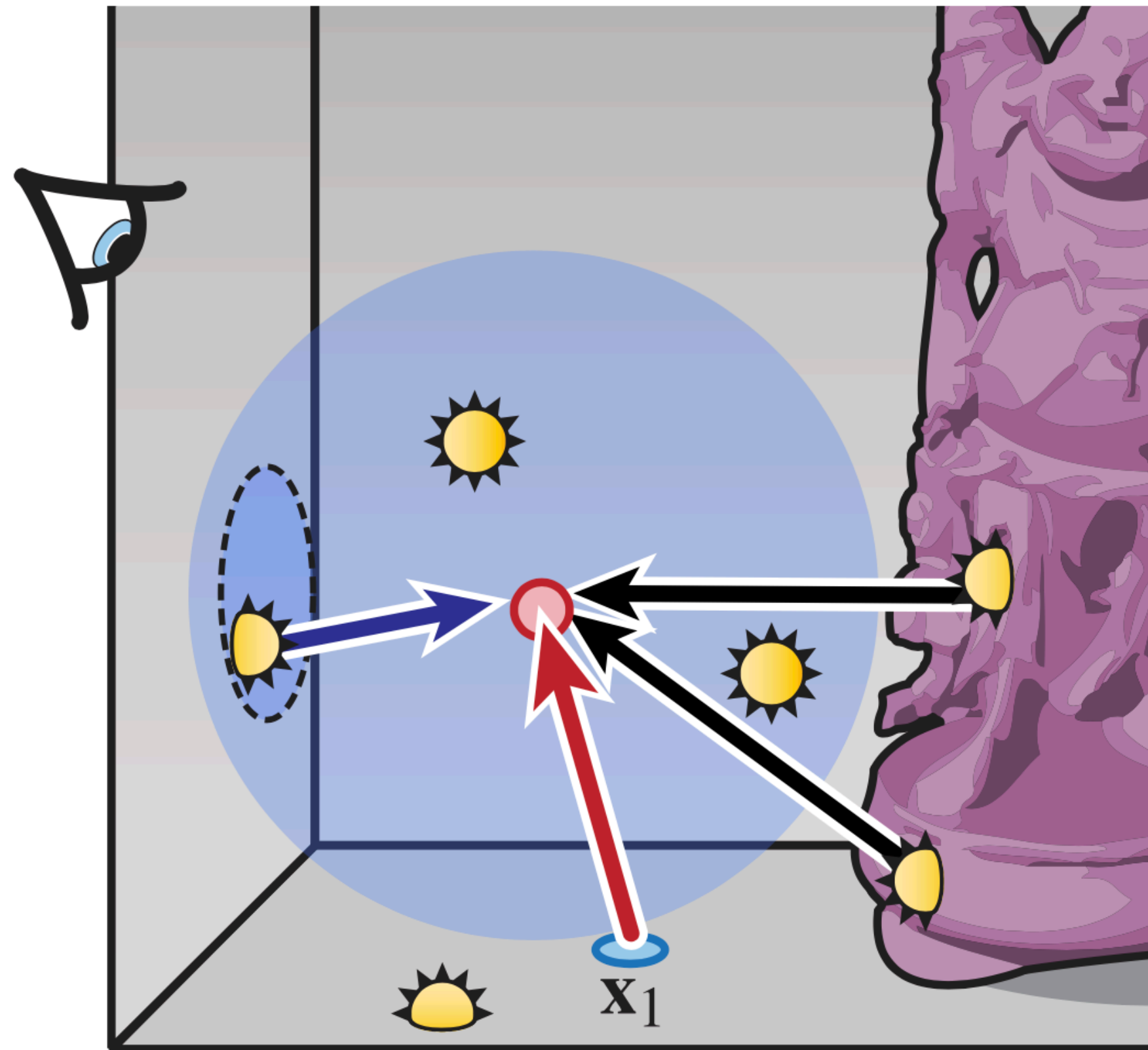
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

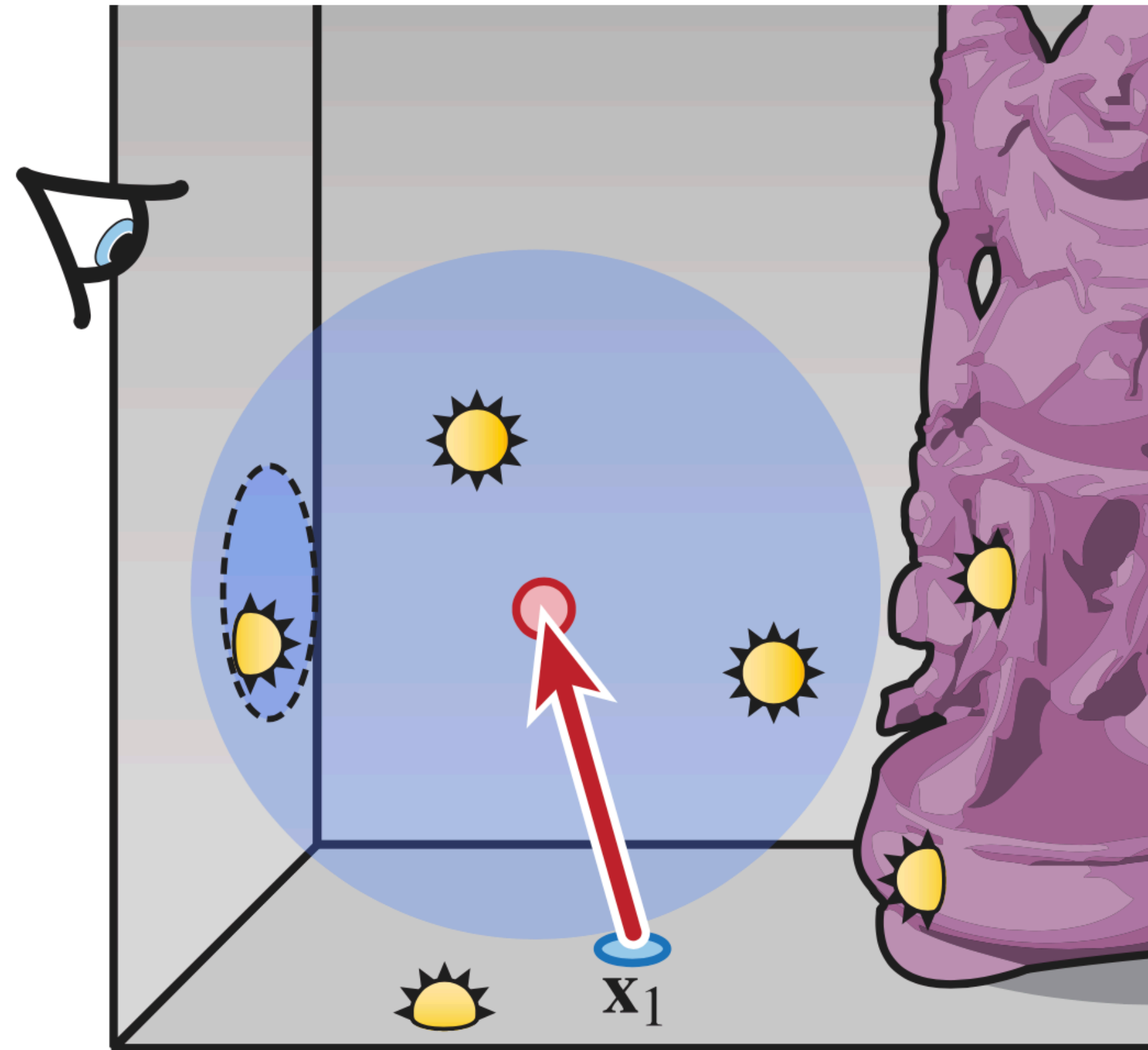
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

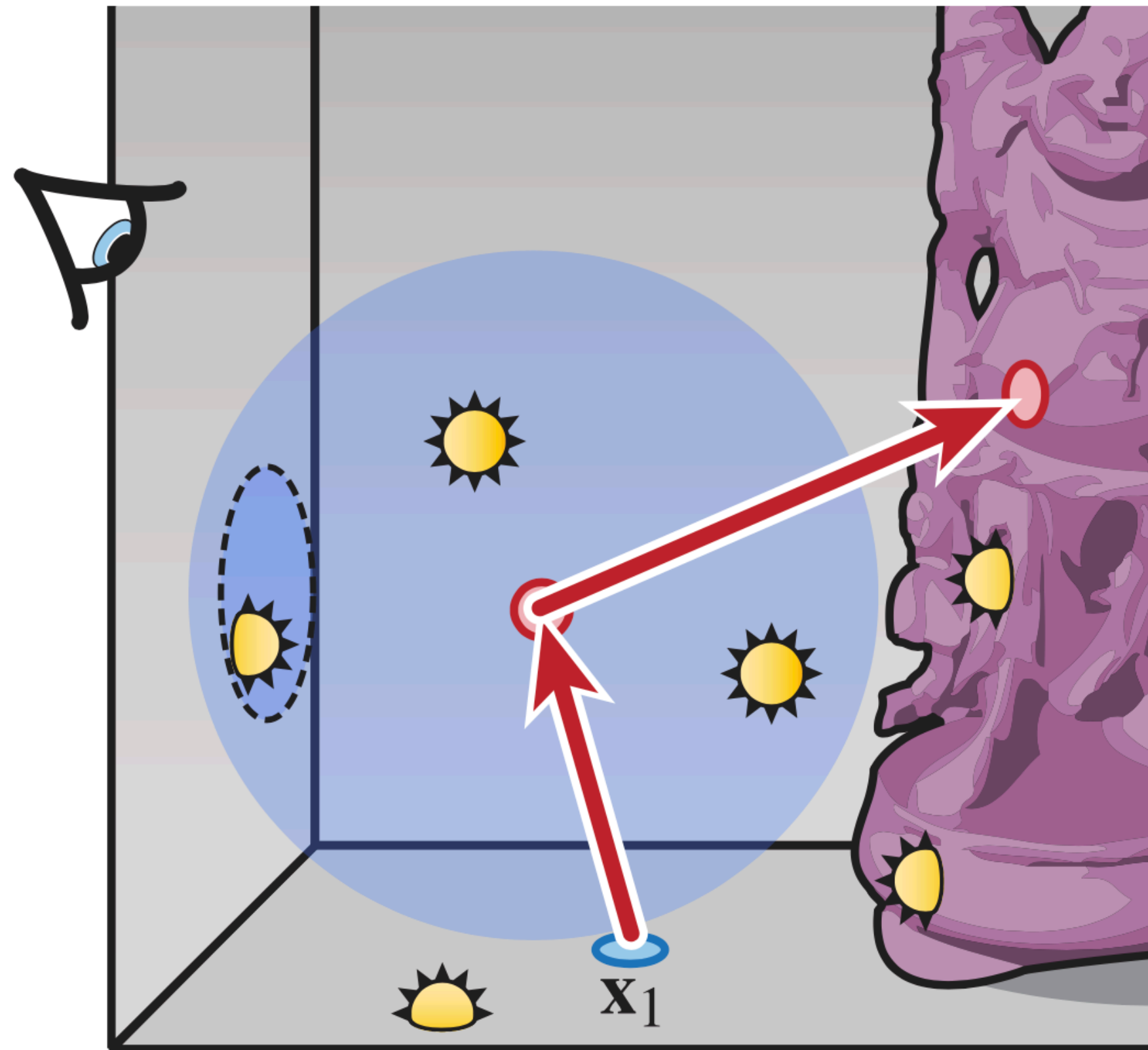
Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

Trace paths to compute the compensation term (residual transport)



Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

Advantages:

- Recover all missing energy

- Makes the algorithm unbiased

Disadvantages:

- Recursive, degenerate to path tracing

- Very expensive: recovering 10% of energy may take 90% of the rendering time

Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

Bounding only



Bounding and Compensation



Image courtesy Kollig and Keller

Bounding and Compensation

Bias Compensation [Kollig and Keller 2004] [Raab et al. 2008]

Bounding only



Bounding and Compensation



Image courtesy Kollig and Keller

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

Rendering Equation:

$$L = L_e + \mathbf{T}L$$

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

Rendering Equation:

$$\begin{aligned} L &= L_e + \mathbf{T}L \\ &\approx L_e + \mathbf{T}L_e + \mathbf{T}\hat{L} \end{aligned}$$

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

Rendering Equation:

$$L = L_e + \mathbf{T}L$$

$$\approx L_e + \mathbf{T}L_e + \mathbf{T}\hat{L}$$

$$\approx L_e + \mathbf{T}L_e + \mathbf{T}_b\hat{L} + \mathbf{T}_r\hat{L}$$

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

Rendering Equation:

$$\begin{aligned} L &= L_e + \mathbf{T}L \\ &\approx L_e + \mathbf{T}L_e + \mathbf{T}\hat{L} \\ &\approx L_e + \mathbf{T}L_e + \mathbf{T}_b\hat{L} + \mathbf{T}_r\hat{L} \\ &\approx L_e + \mathbf{T}L_e + \mathbf{T}_b\hat{L} + \mathbf{T}_r(L - L_e) \end{aligned}$$

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

Rendering Equation:

$$\begin{aligned} L &= L_e + \mathbf{T}L \\ &\approx L_e + \mathbf{T}L_e + \mathbf{T}\hat{L} \\ &\approx L_e + \mathbf{T}L_e + \mathbf{T}_b\hat{L} + \mathbf{T}_r\hat{L} \\ &\approx L_e + \mathbf{T}L_e + \mathbf{T}_b\hat{L} + \mathbf{T}_r(L - L_e) \\ &\approx L_e + \sum_{i=0}^{\infty} \mathbf{T}_r^i \underbrace{(\mathbf{T}L_e + \mathbf{T}_b\hat{L})}_{\text{compute once and store}} \end{aligned}$$

iteratively apply \mathbf{T}_r

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

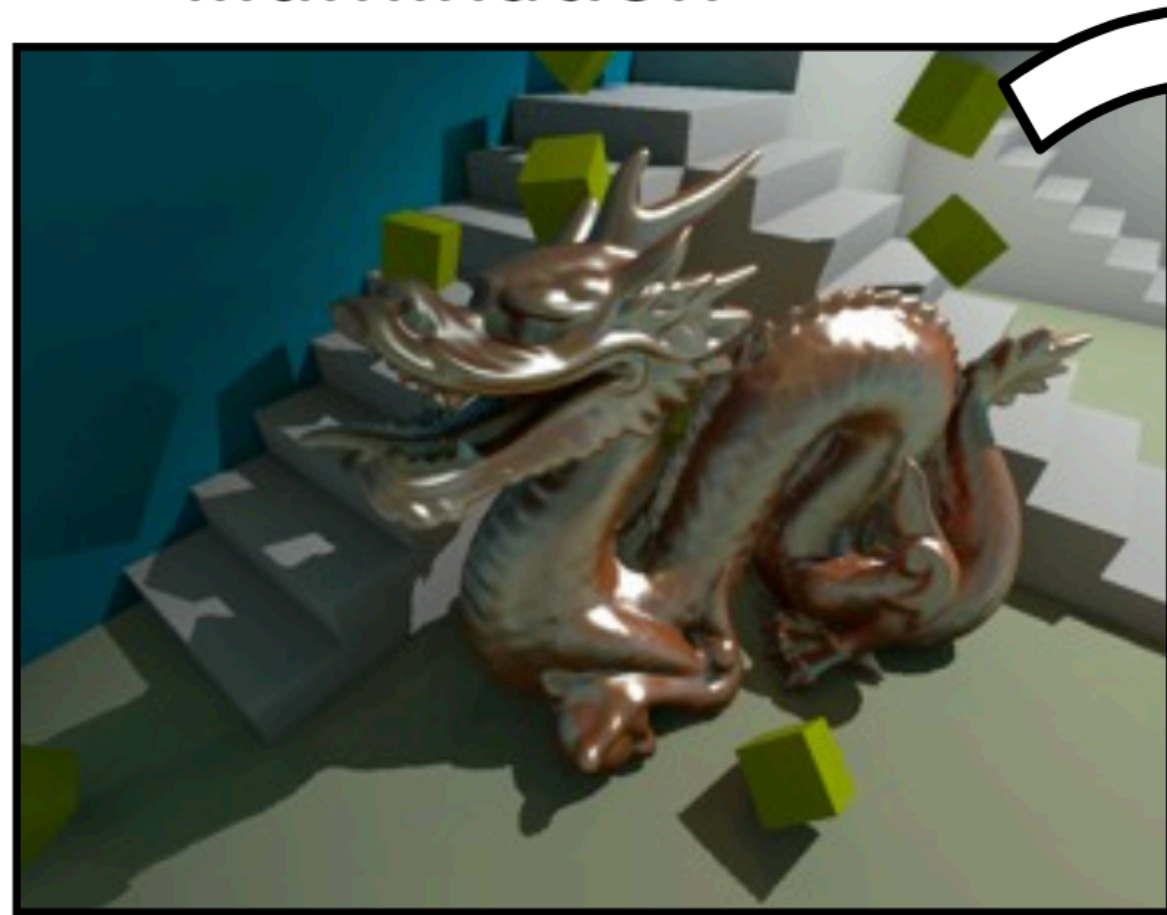
Rendering Equation:

$$\approx L_e + \sum_{i=0}^{\infty} \mathbf{T}_{\mathbf{r}}^i (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$

direct +
bounded indirect
illumination

residual transport
in screen-space

residual transport
in screen-space



$$\mathbf{T}_{\mathbf{r}}^0 (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$

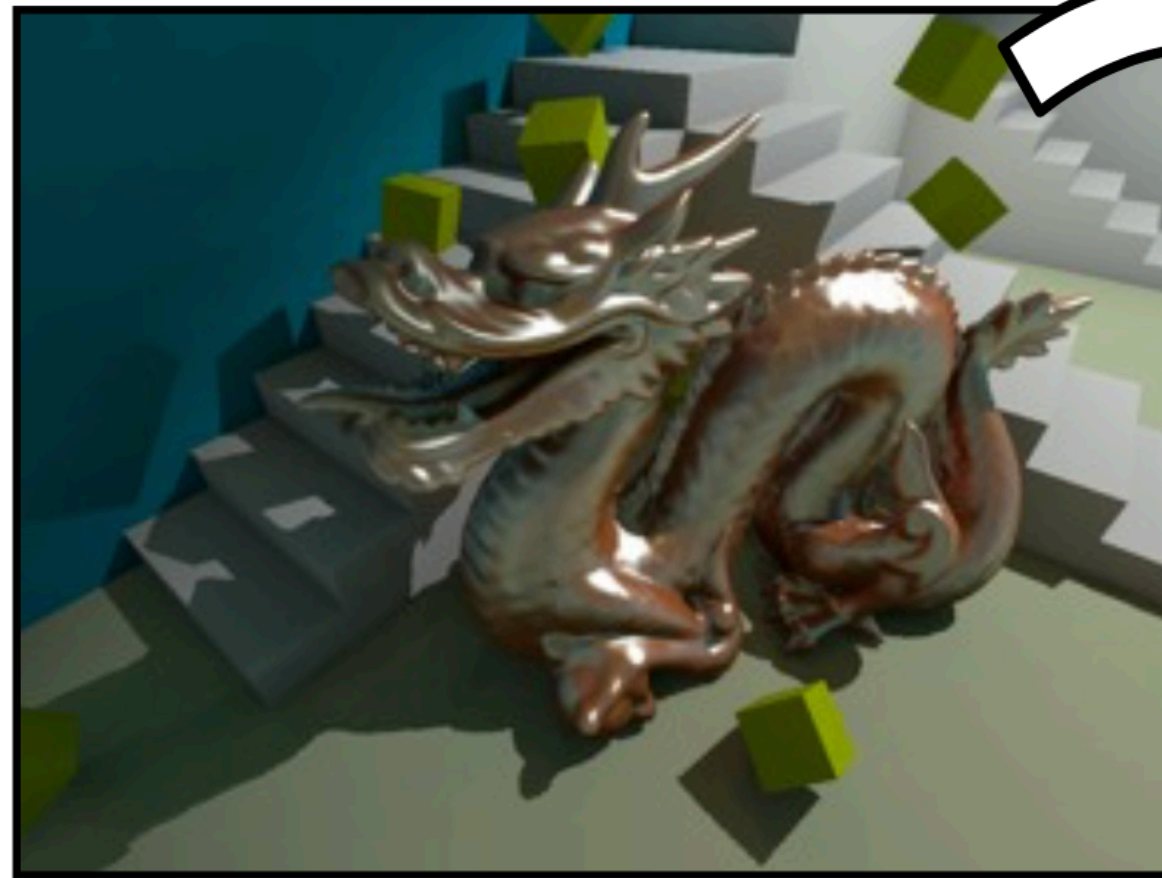
Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

Rendering Equation:

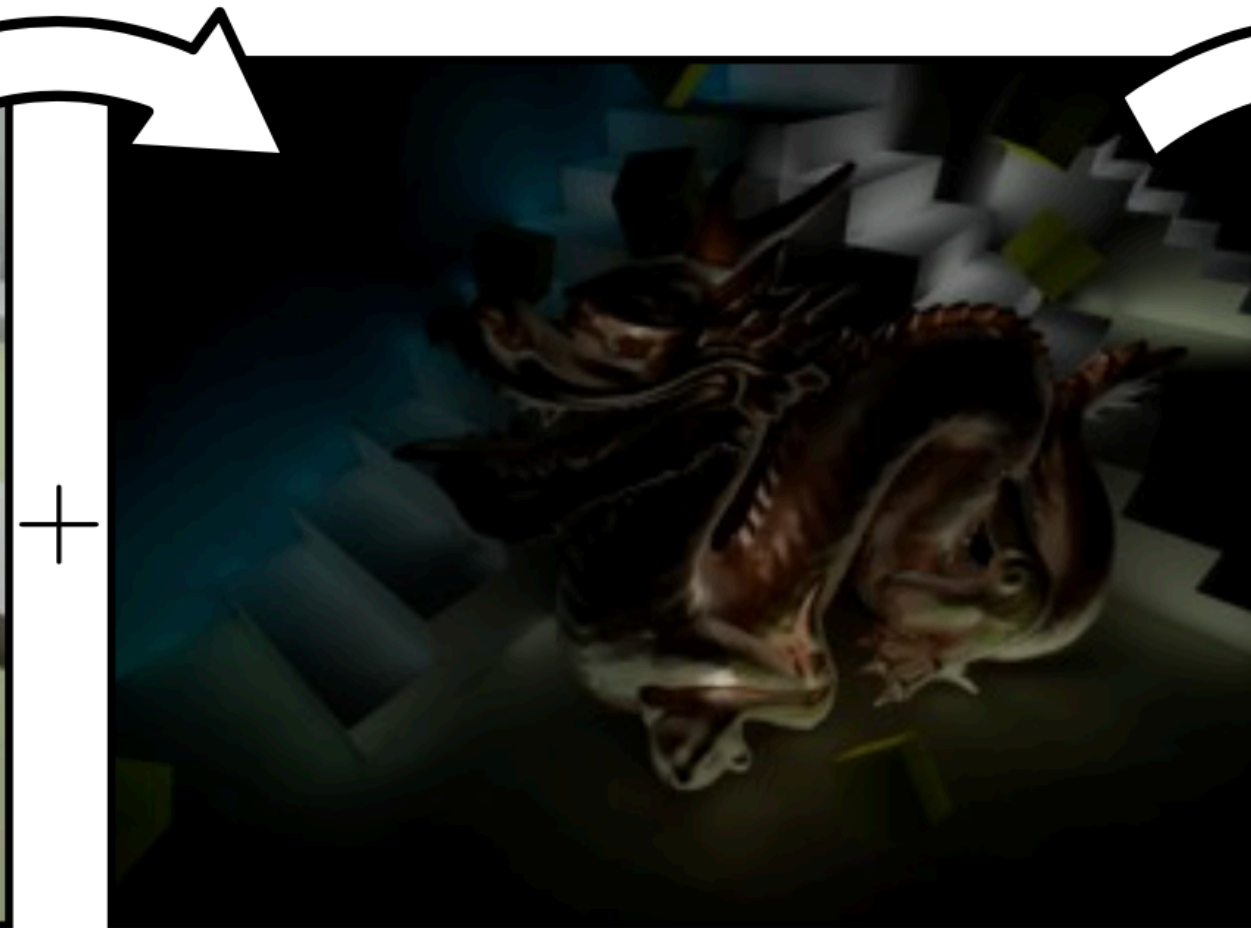
$$\approx L_e + \sum_{i=0}^{\infty} \mathbf{T}_{\mathbf{r}}^i (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$

direct +
bounded indirect
illumination



$$\mathbf{T}_{\mathbf{r}}^0 (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$

residual transport
in screen-space



$$\mathbf{T}_{\mathbf{r}}^1 (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$

residual transport
in screen-space

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

Rendering Equation:
$$\approx L_e + \sum_{i=0}^{\infty} \mathbf{T}_{\mathbf{r}}^i (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$

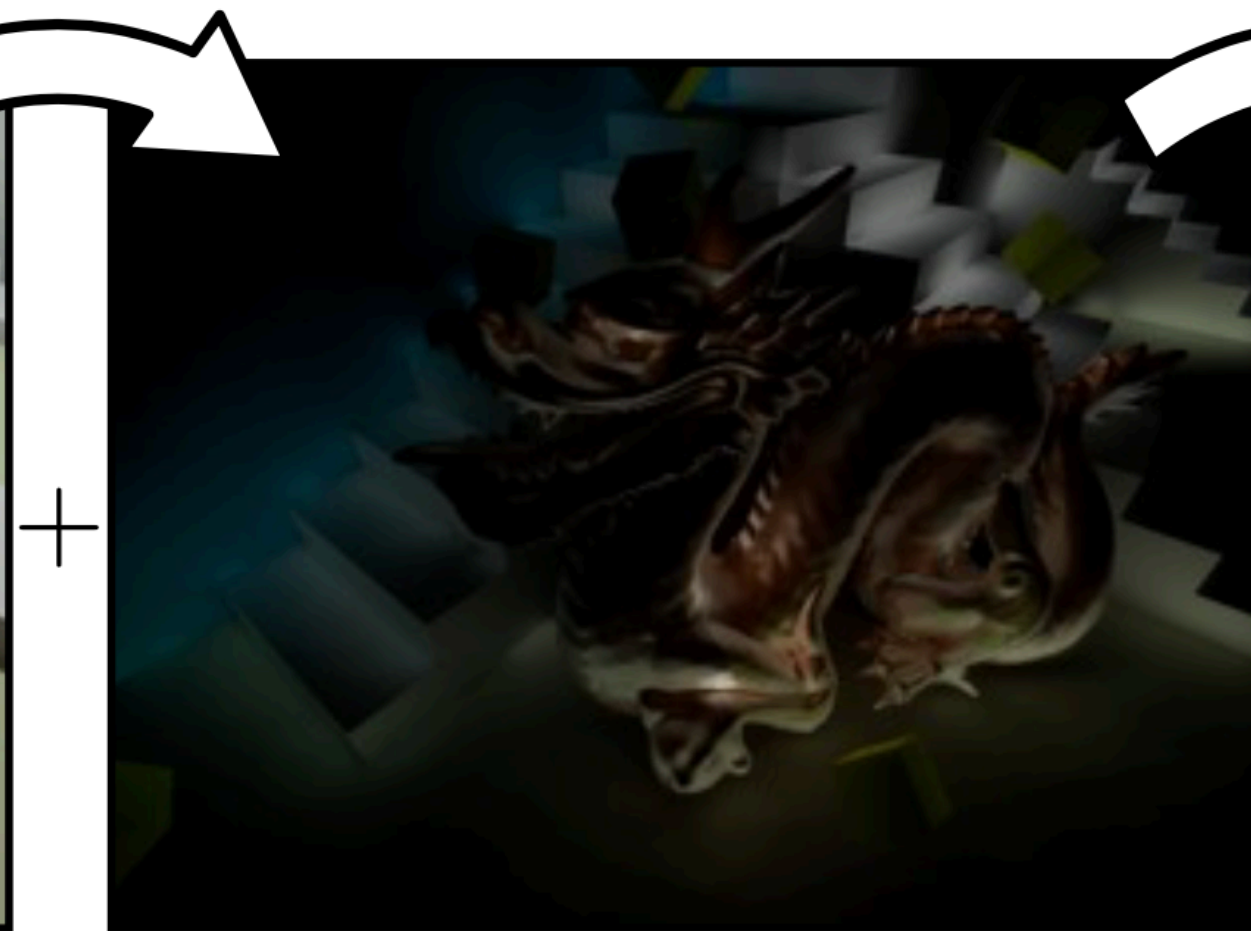
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$$\mathbf{T}_{\mathbf{r}}^0 (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$



$$\mathbf{T}_{\mathbf{r}}^1 (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$



$$\mathbf{T}_{\mathbf{r}}^2 (\mathbf{T} L_e + \mathbf{T}_{\mathbf{b}} \hat{L})$$

+ ...

Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

**Direct +
bounded indirect**



+

**1- and 2-bounce
residual**



Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

**Direct +
bounded indirect**



+

**1- and 2-bounce
residual**



=

Composited



Bounding and Compensation

Screen space bias compensation [Novak et al. 2011]

**Direct +
bounded indirect**



**1- and 2-bounce
residual**



Composited



Bounding and Compensation

Approximate bias compensation [Engelhardt et al. 2012]

- efficient compensation for participating media

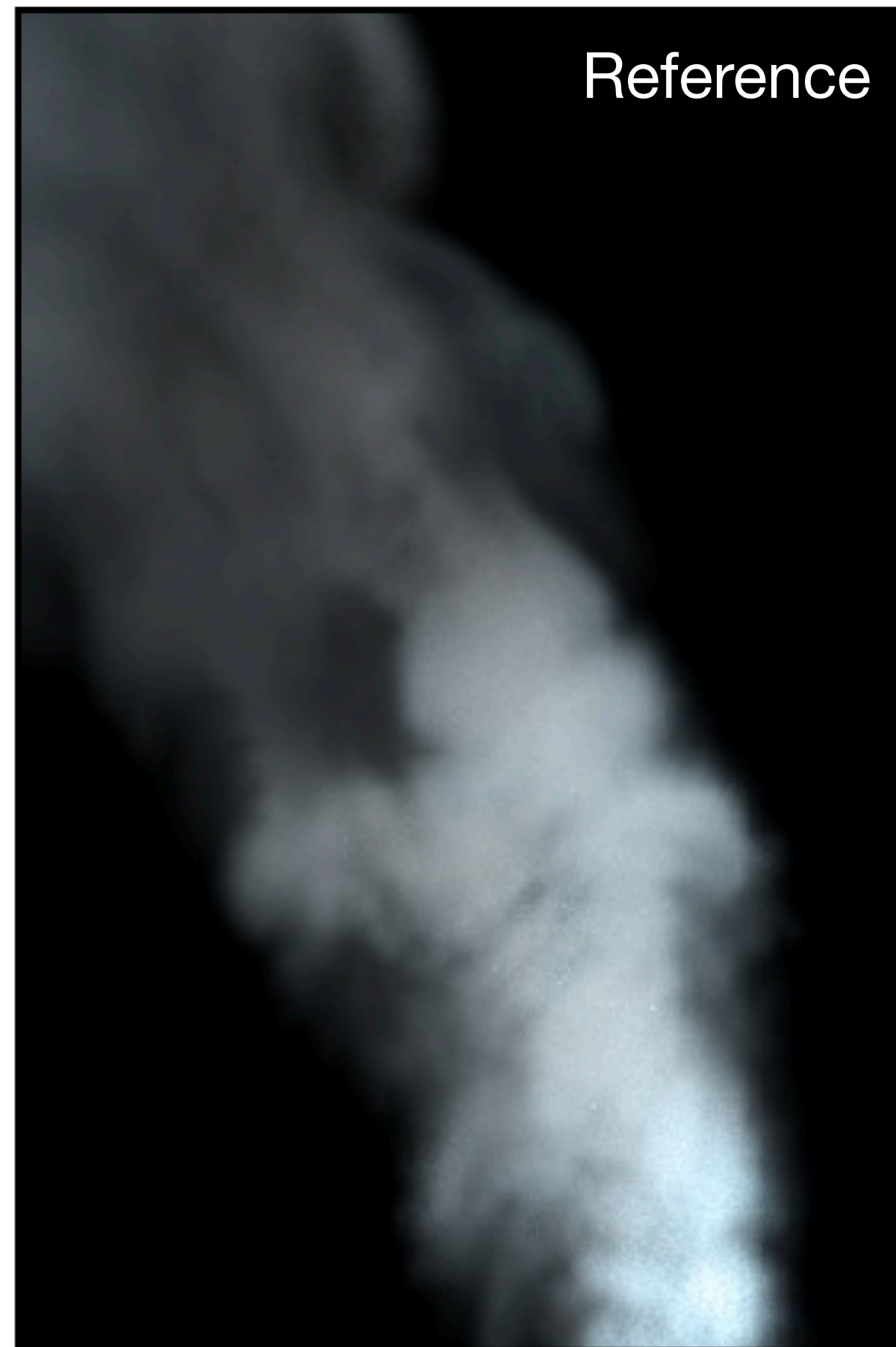


Image courtesy Engelhardt et al. [2012]

Bounding and Compensation

Approximate bias compensation [Engelhardt et al. 2012]

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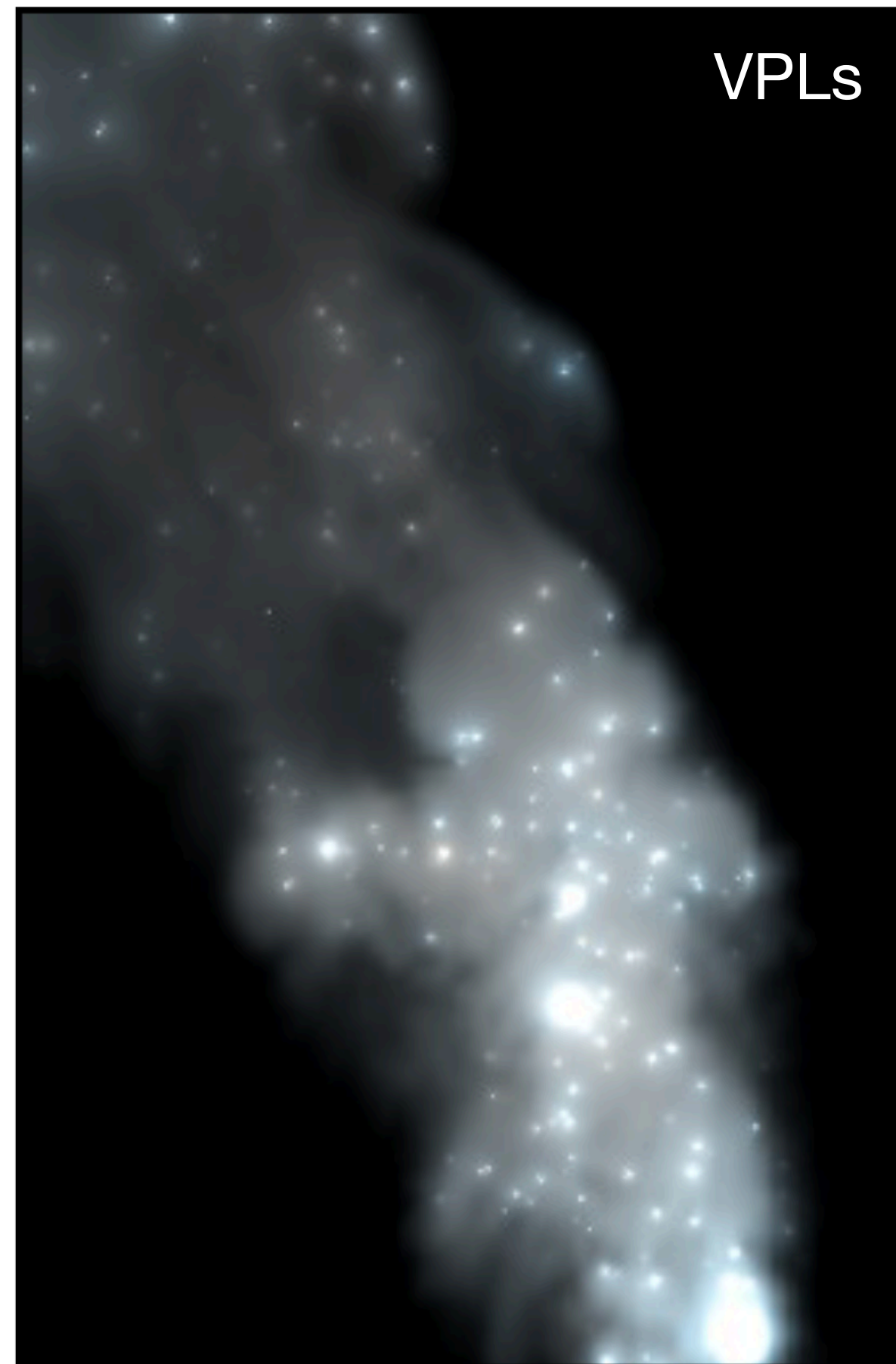
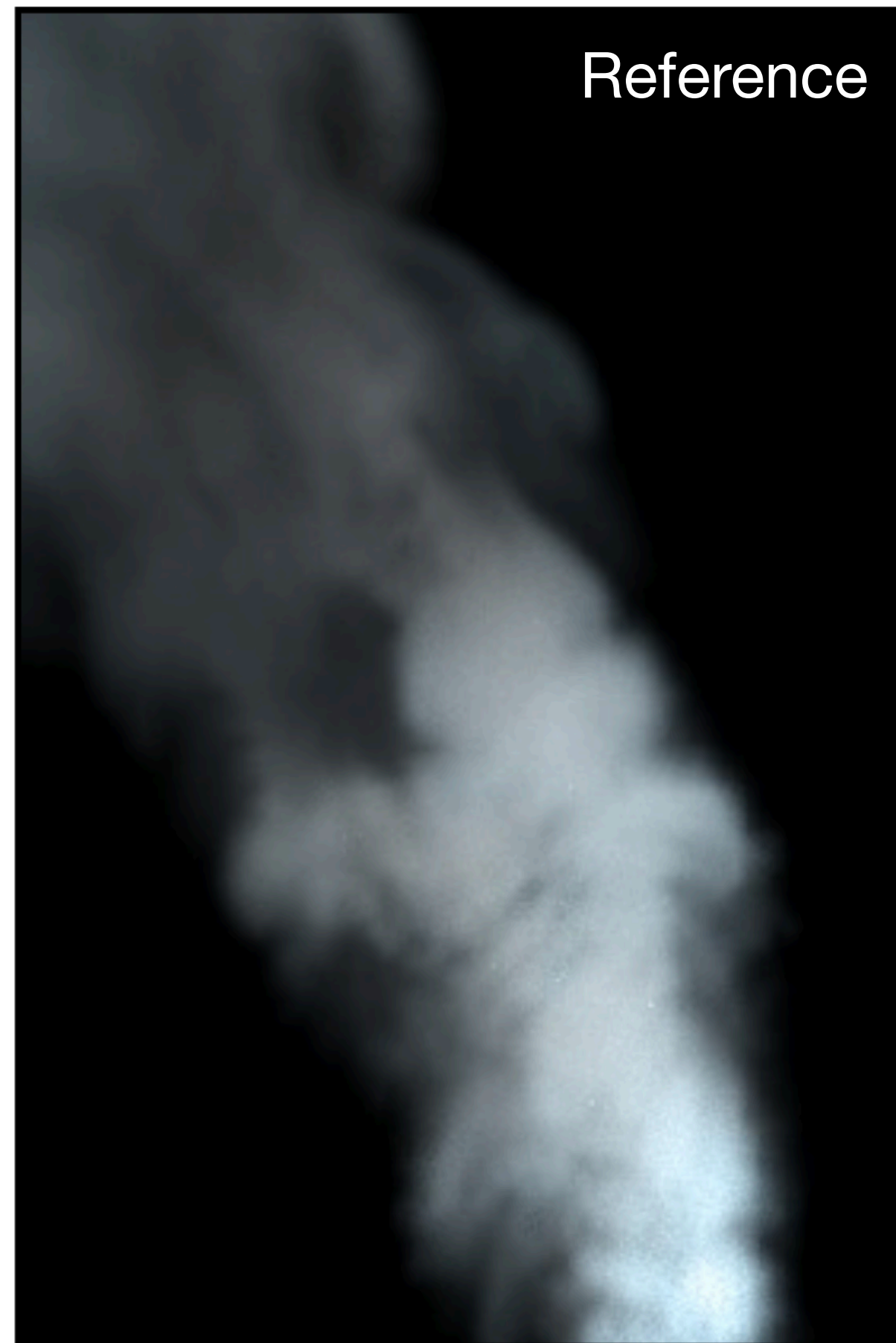


Image courtesy Engelhardt et al. [2012]

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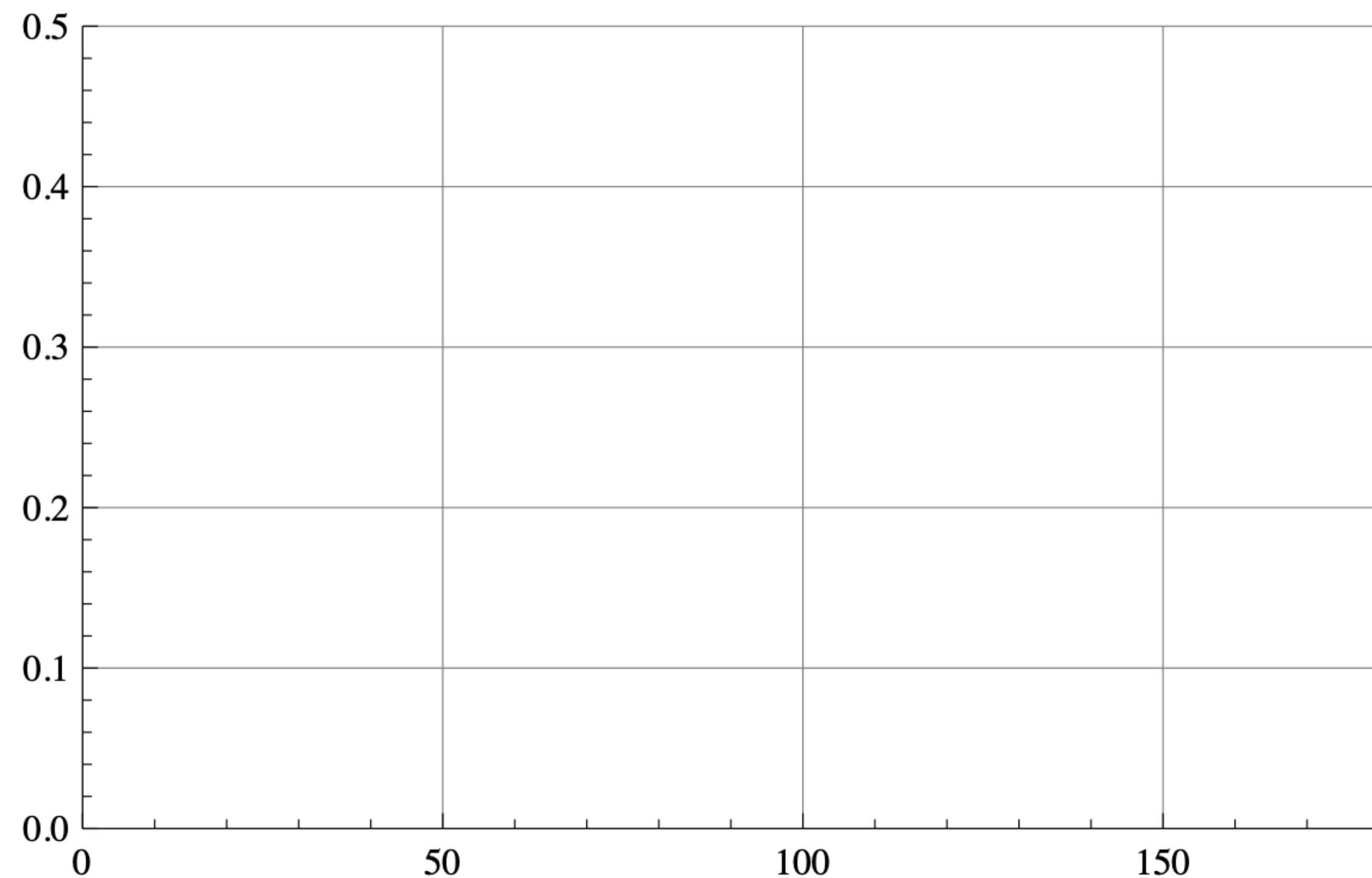
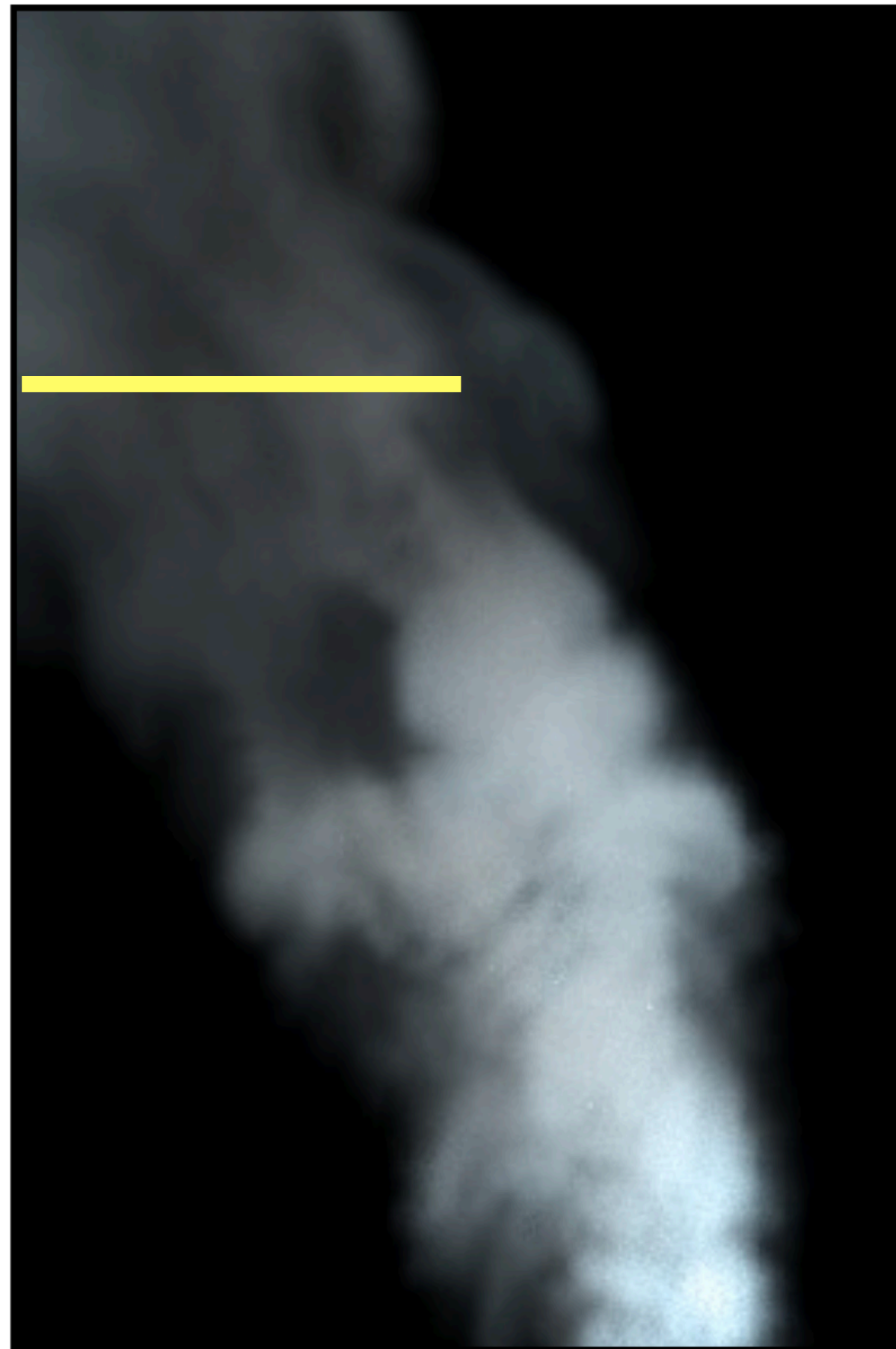


Image courtesy Engelhardt et al. [2012]

Bounding and Compensation

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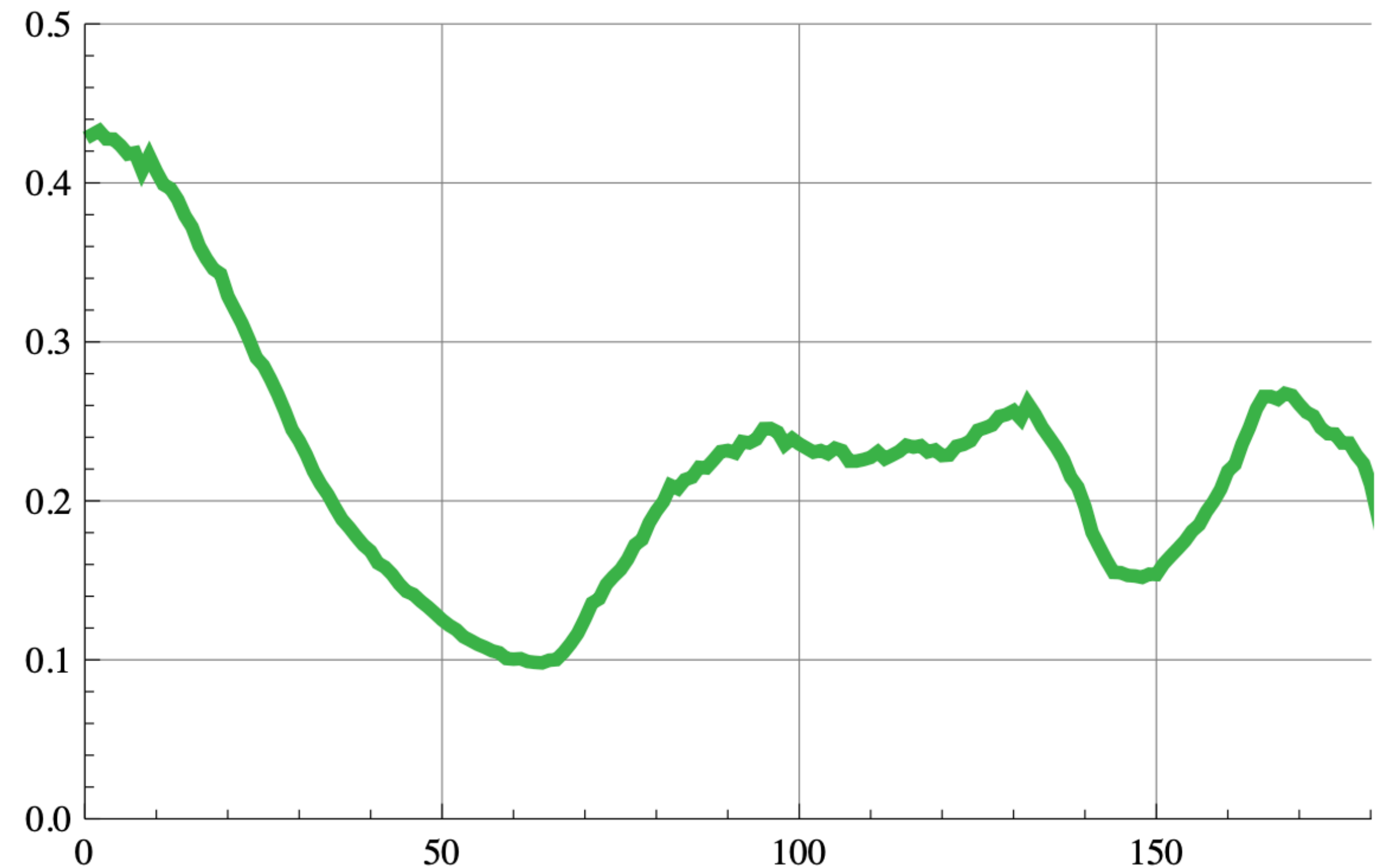
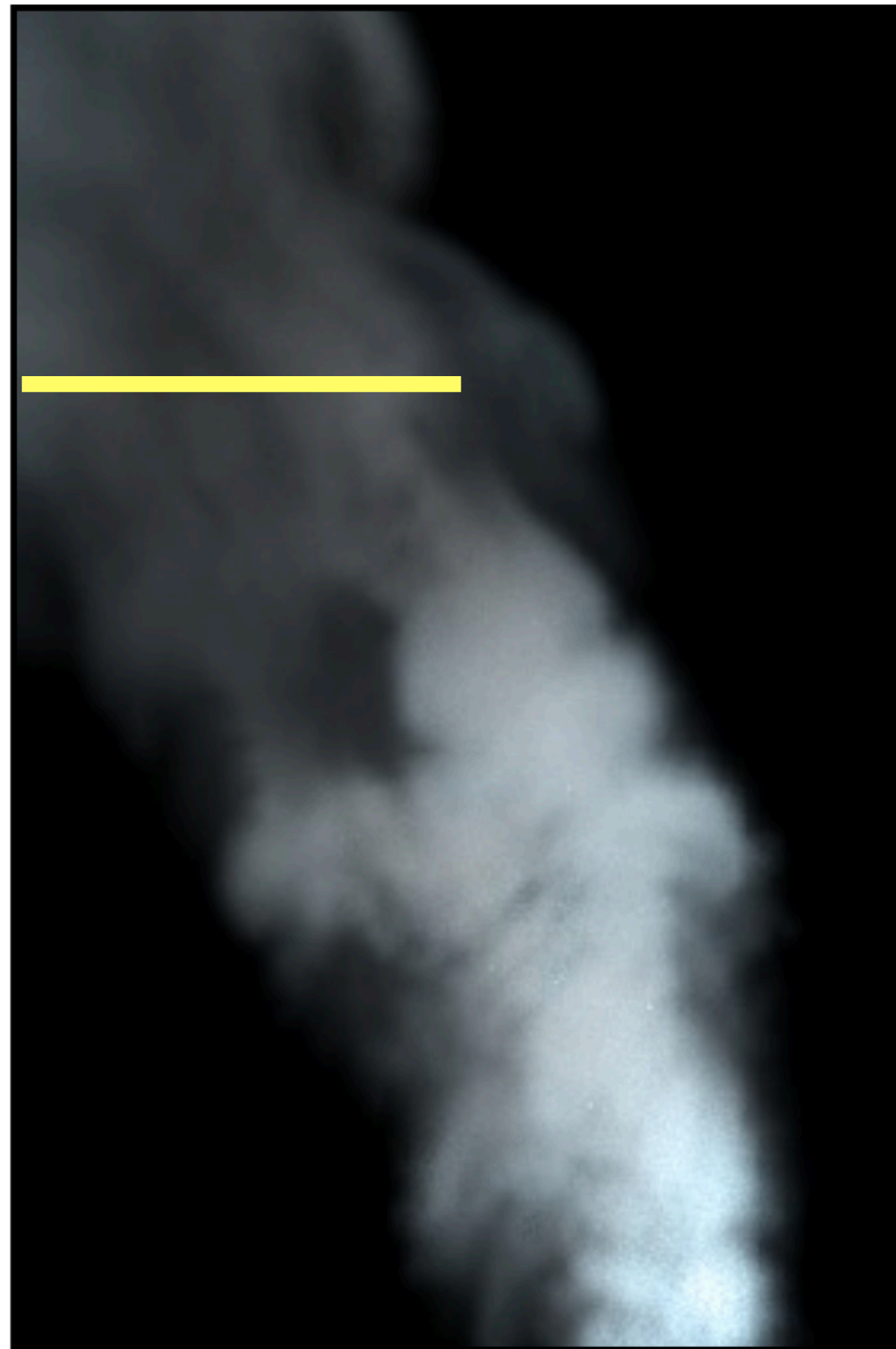


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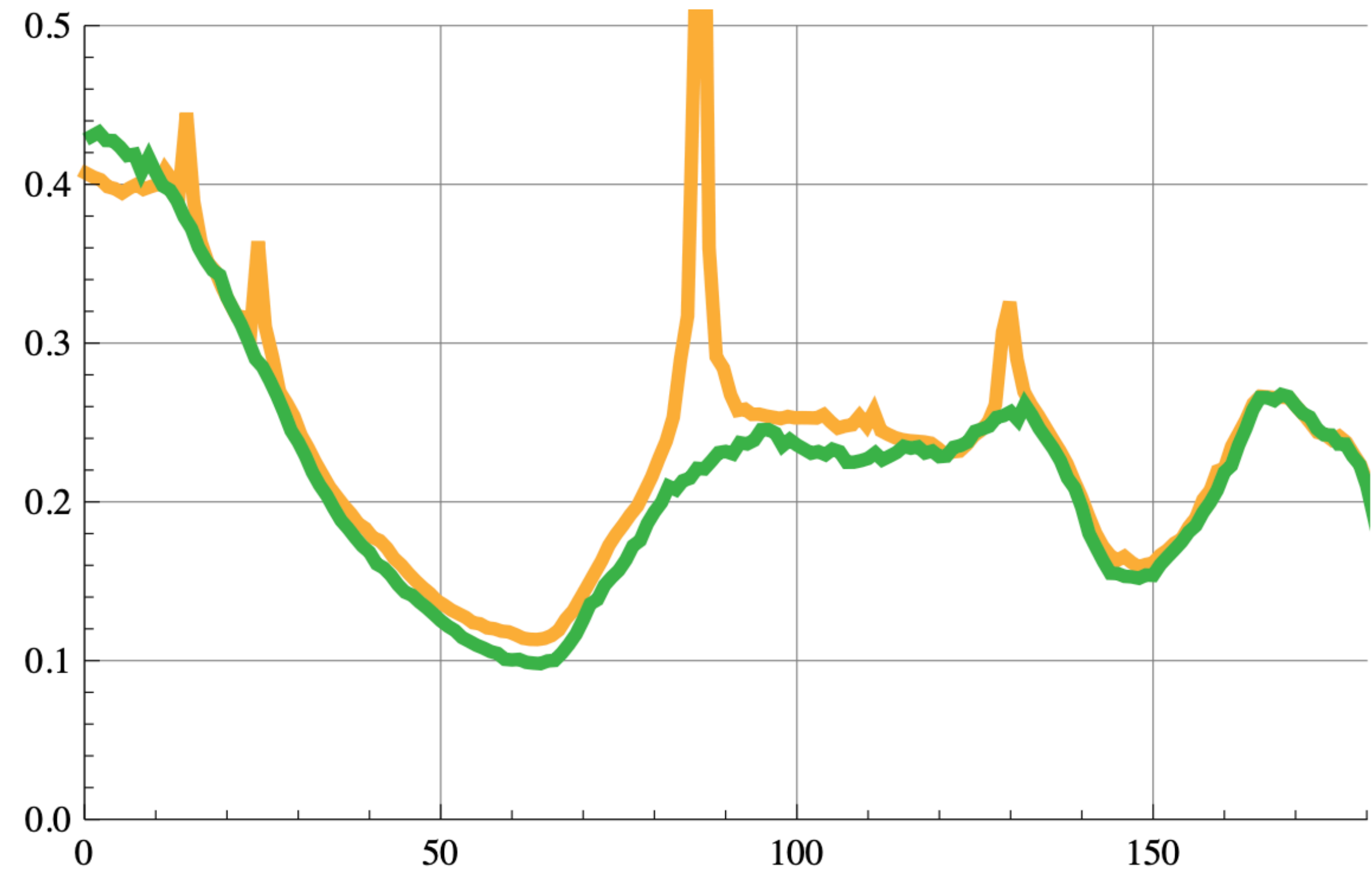
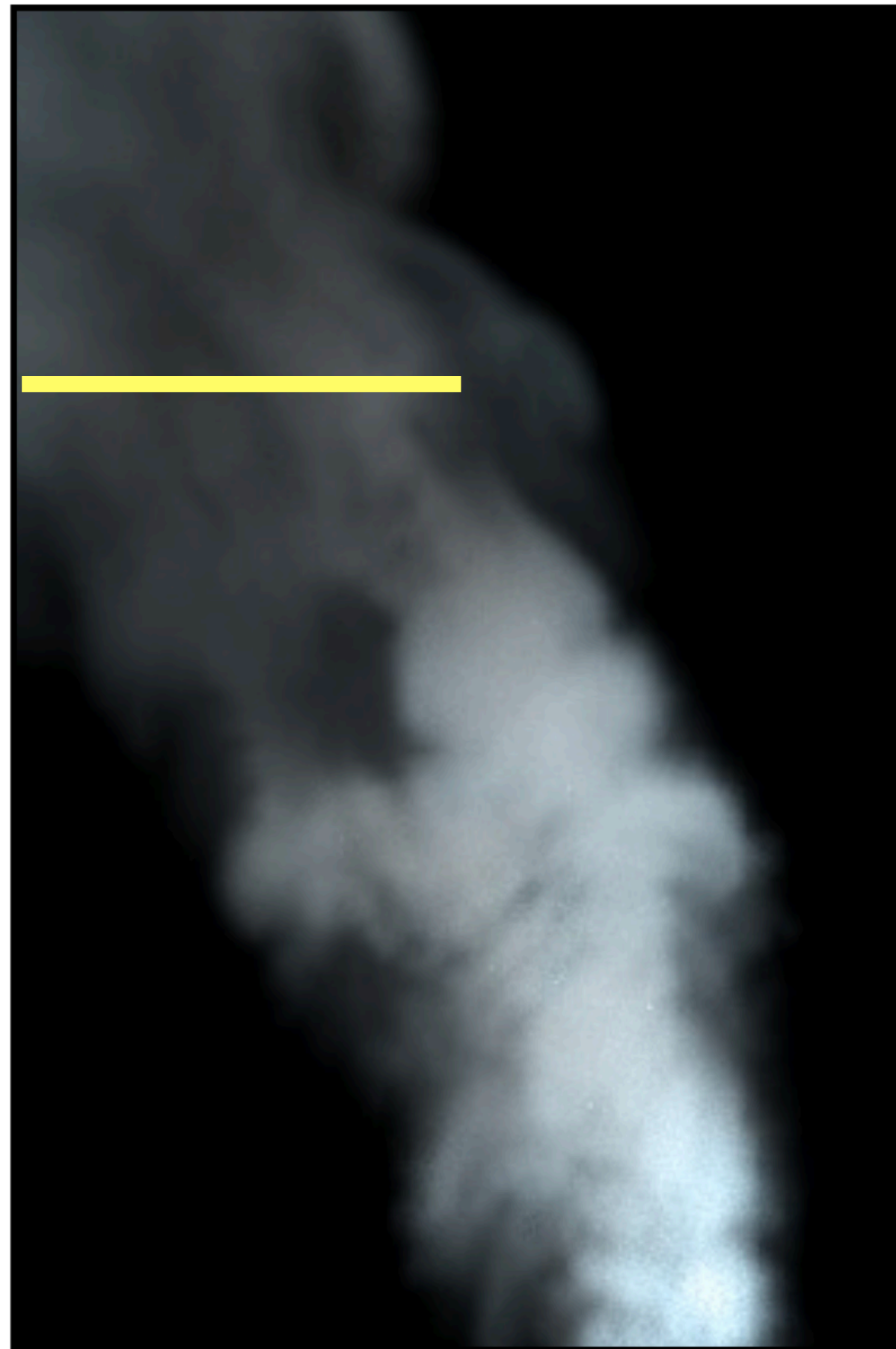


Image courtesy Engelhardt et al. [2012]

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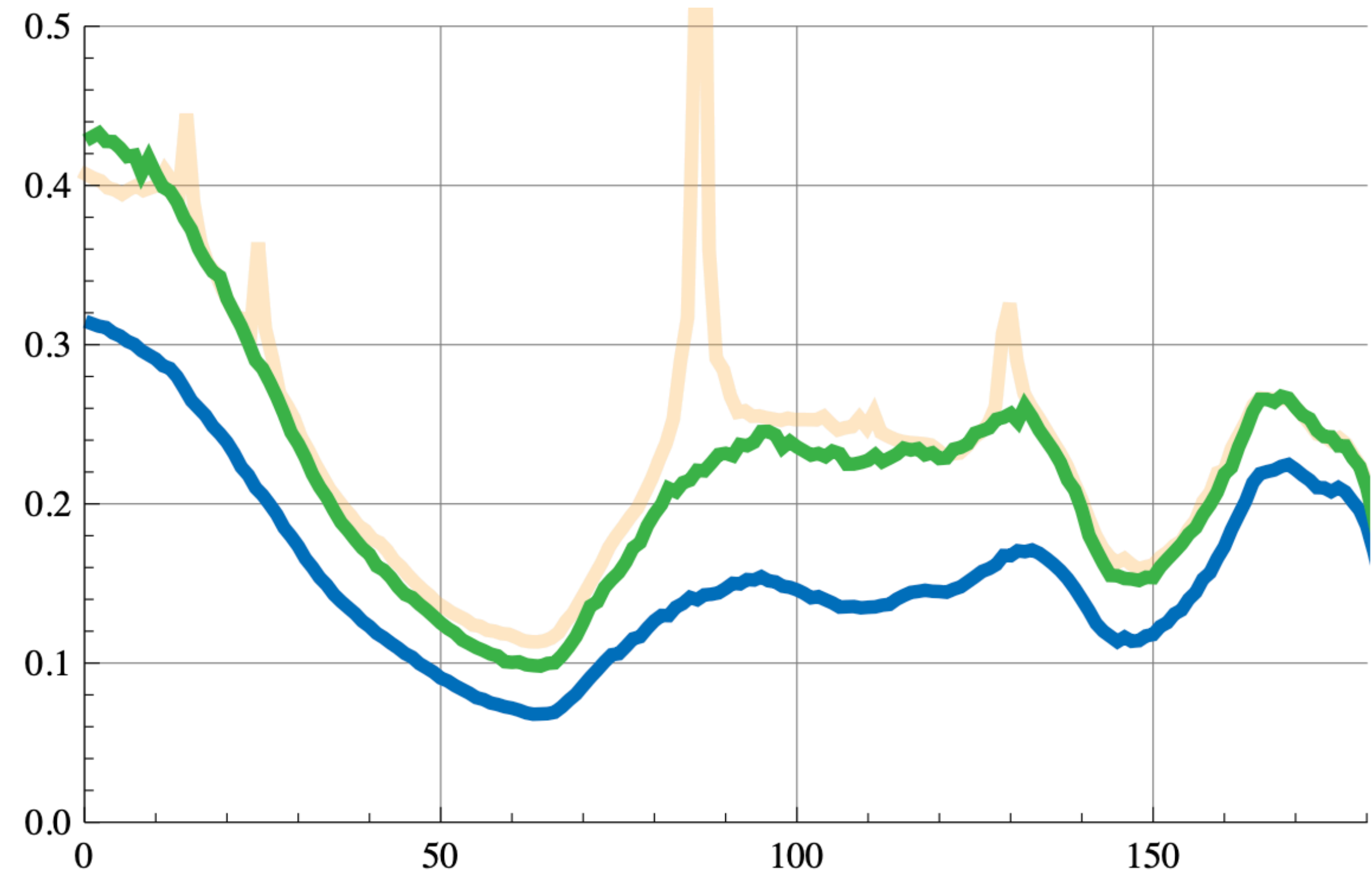
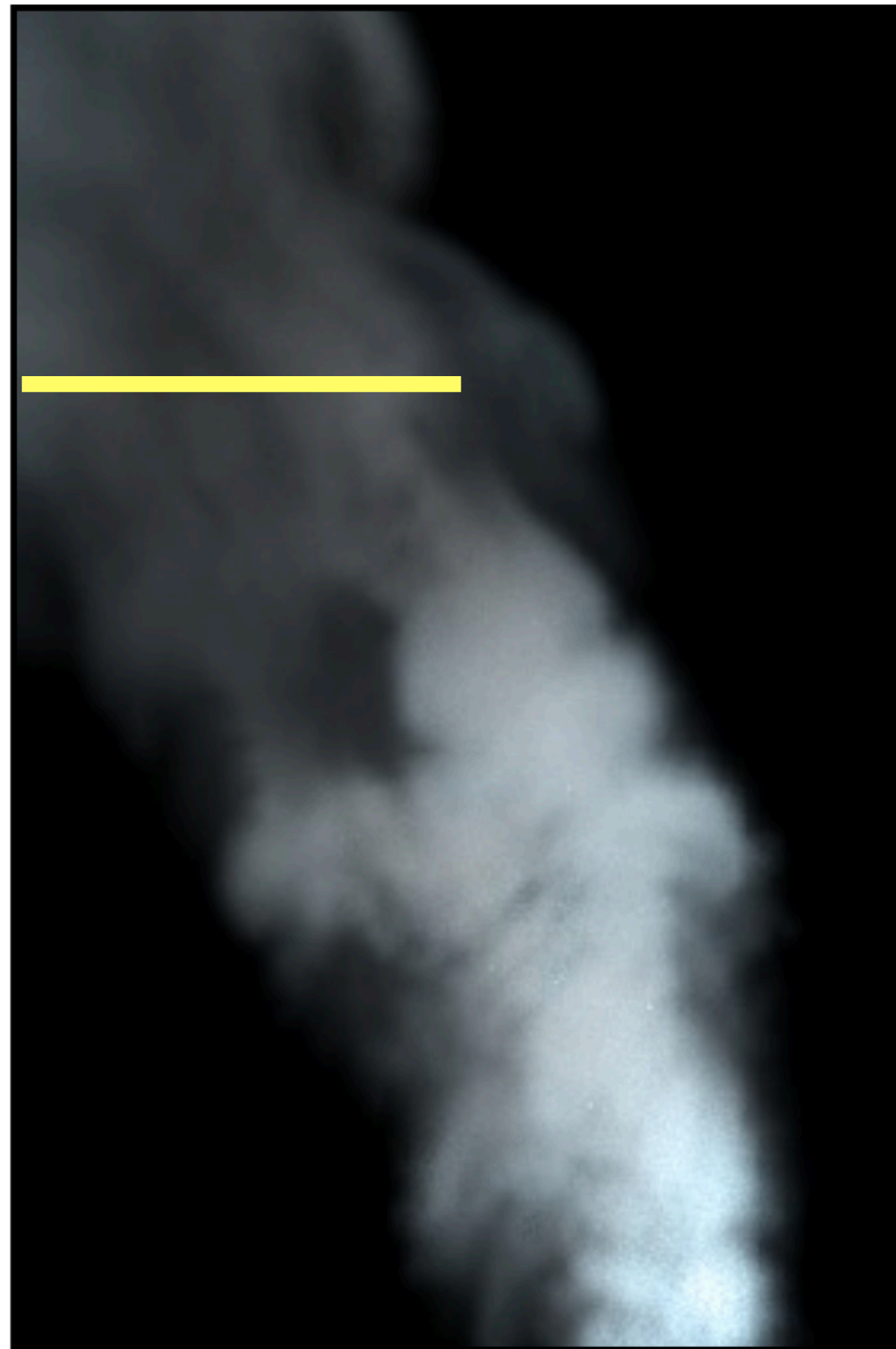


Image courtesy Engelhardt et al. [2012]

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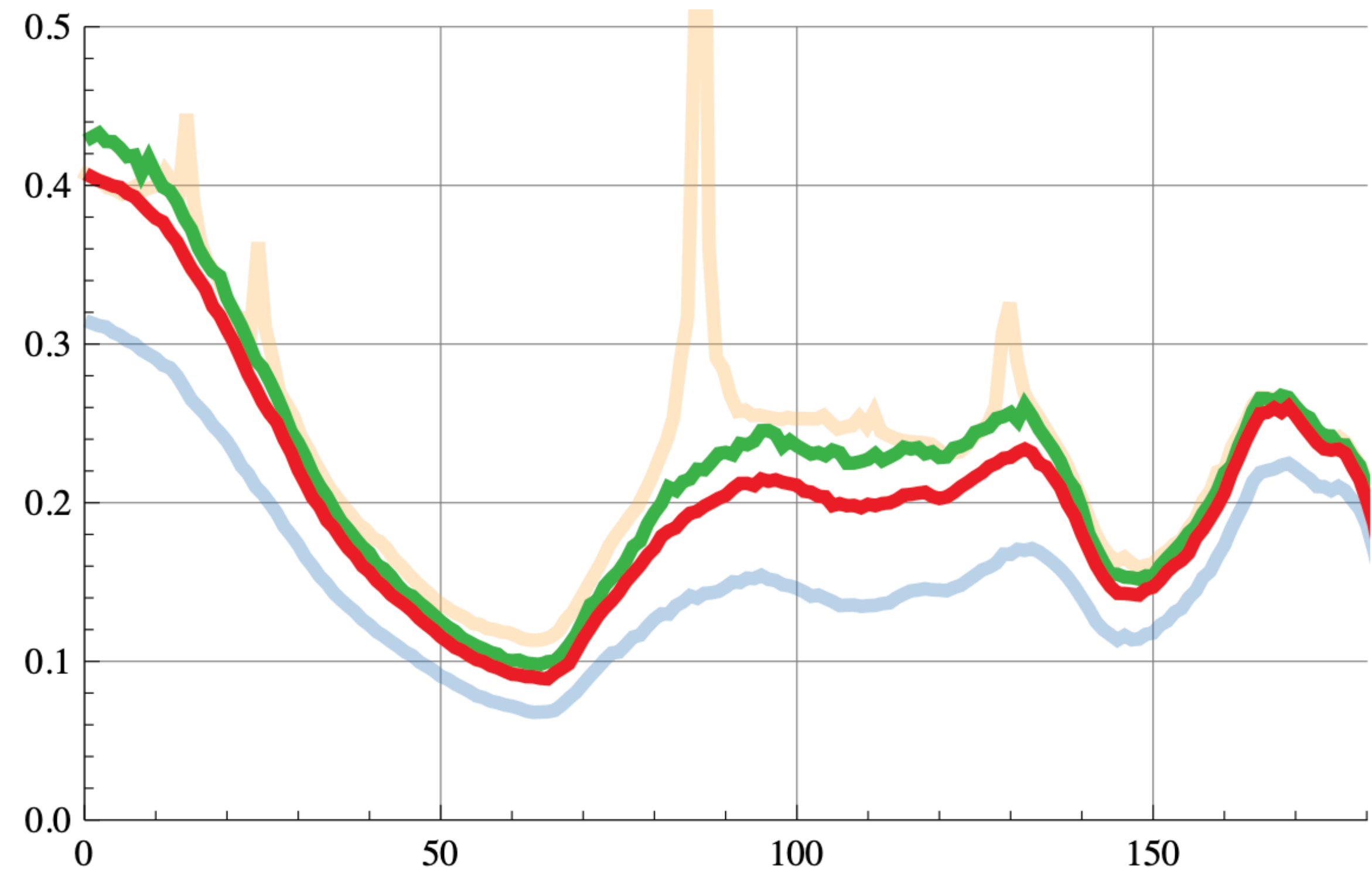
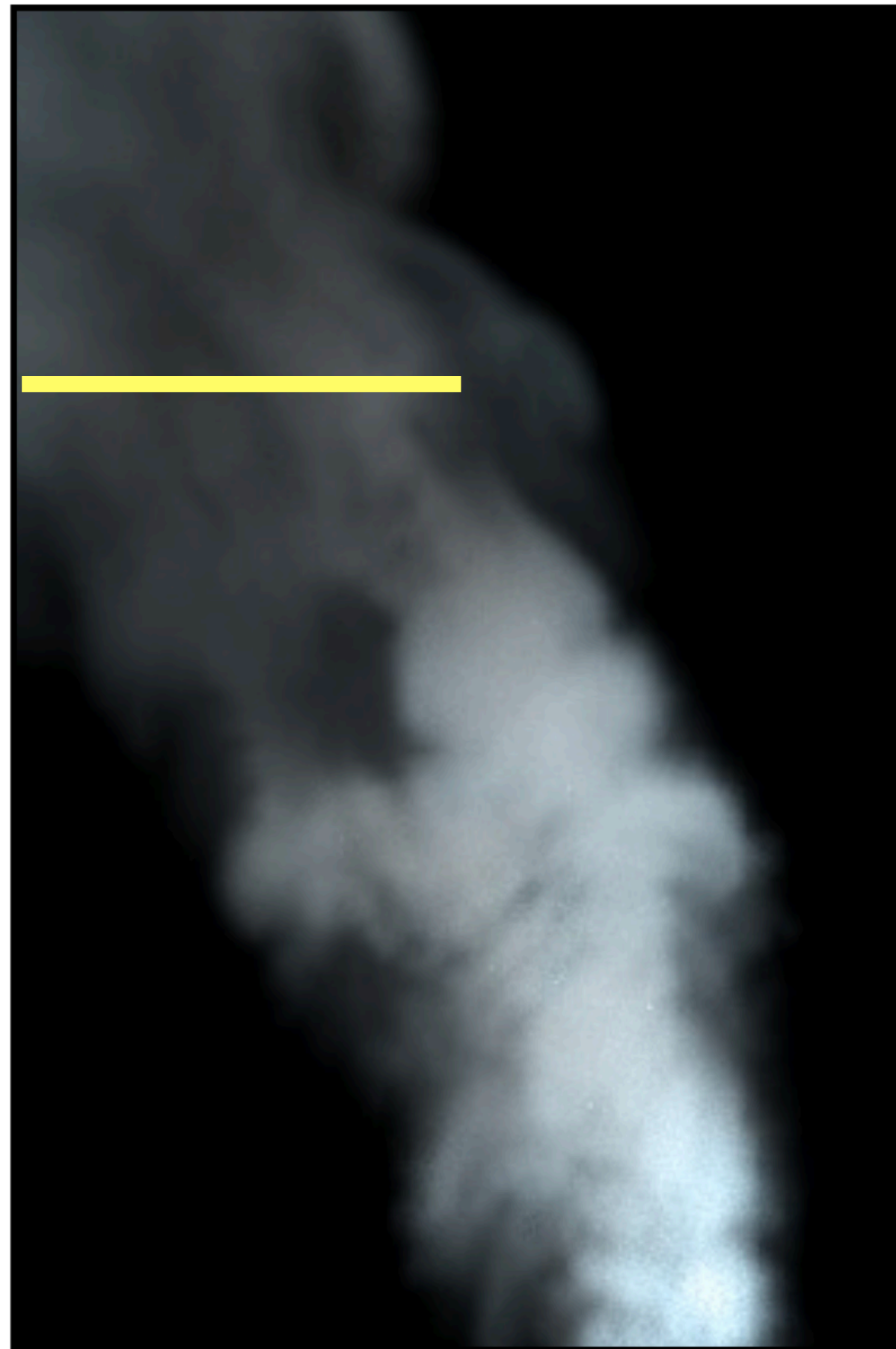


Image courtesy Engelhardt et al. [2012]

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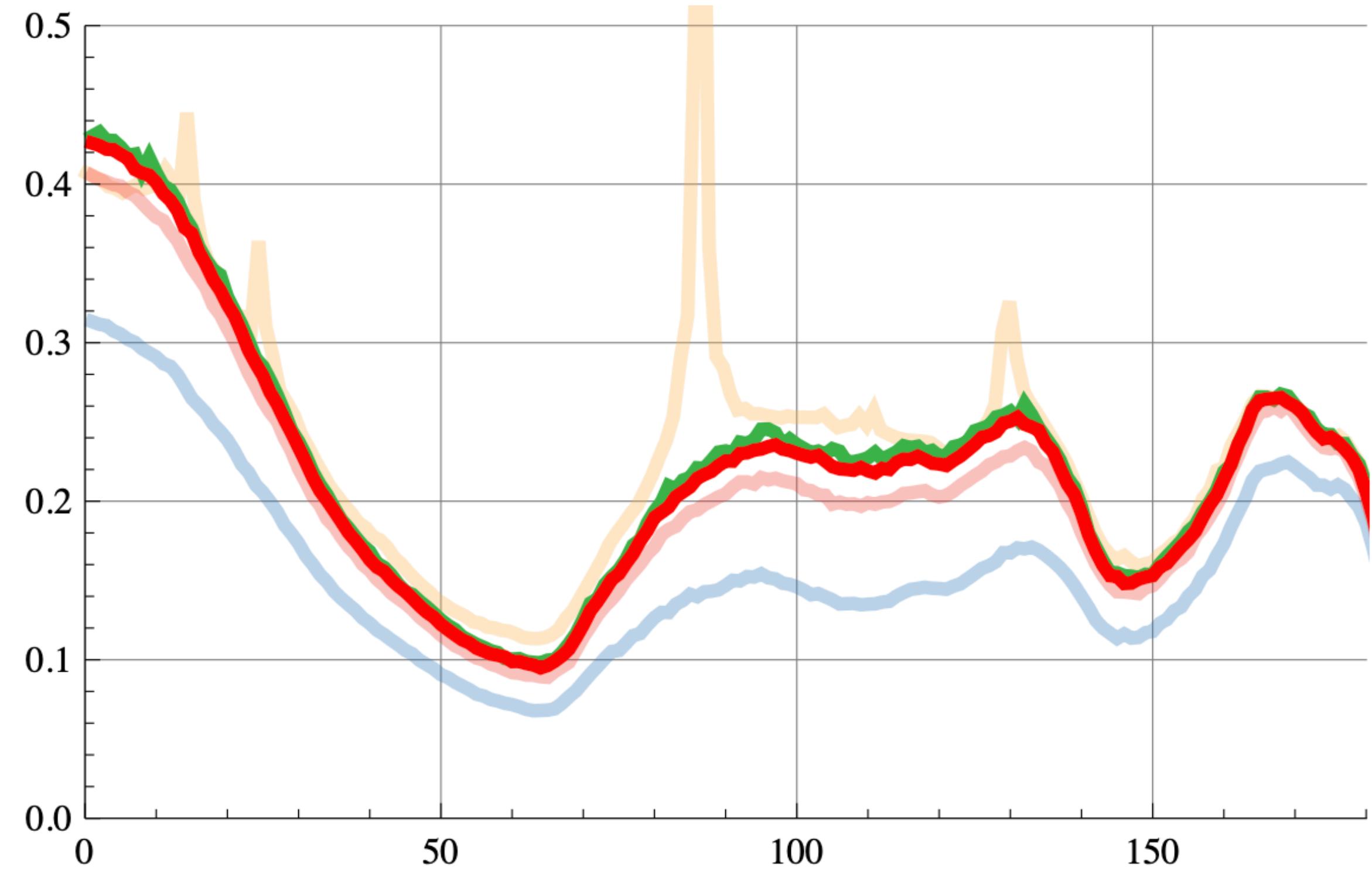
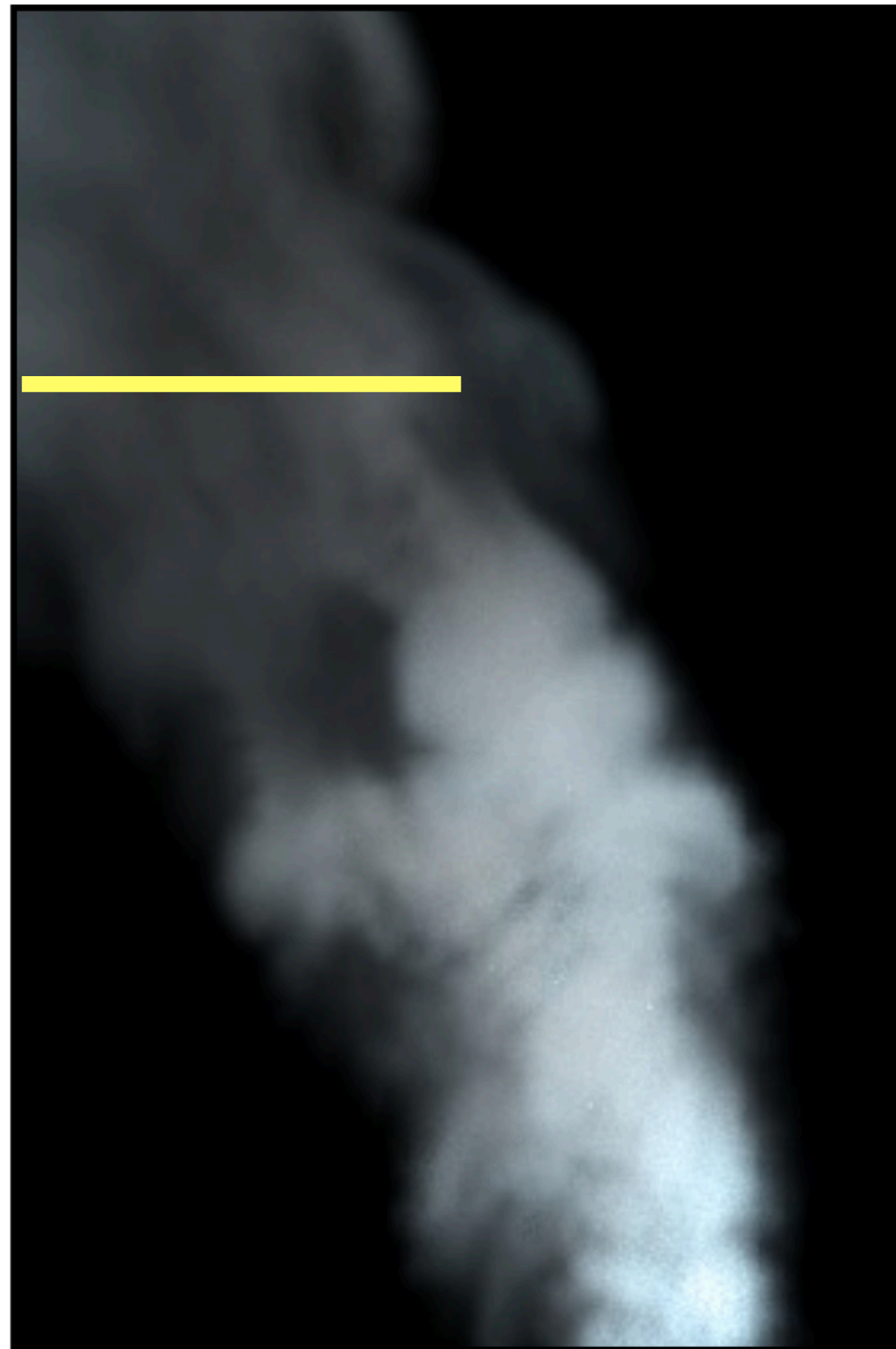


Image courtesy Engelhardt et al. [2012]

Bounding and Compensation

Approximate bias compensation [Engelhardt et al. 2012]

- efficient compensation for participating media

Optimizations used for Bias Compensation:

- Assumes locally homogeneous media
- Omit testing local visibility

Advantages:

Fast, GPU friendly

Disadvantages:

Approximate, complicated

Image courtesy Engelhardt et al. [2012]

Bounding and Compensation

Approximate bias compensation [Engelhardt et al. 2012]



Bounded: 39 mins

Approximate bias compensation: 13 mins

Lighting with VPLs

How to avoid Splotches?

Solutions:

1) Bound the geometry

- remove energy, darkens the image
- to get unbiased results, we need to compensate for the bounding

2) Distribute the flux of a VPL over area (volume)

- redistributes energy, blurs the illumination
- to get consistent results, progressively reduce the blurring

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Spreading the Energy

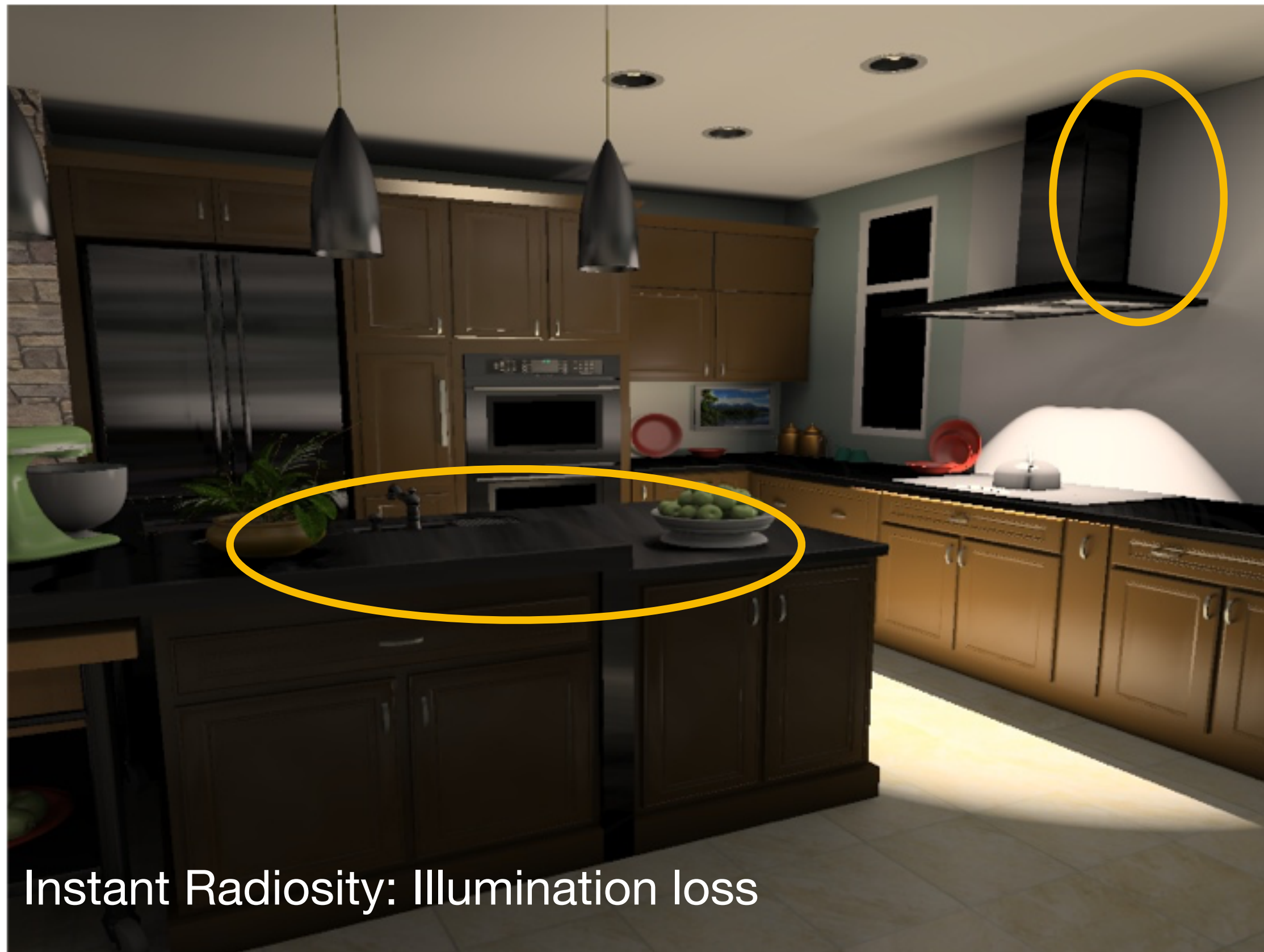
Problems with Instant Radiosity

Instant Radiosity does not handle glossy surfaces



Problems with Instant Radiosity

Instant Radiosity does not handle glossy surfaces



Bounding & Compensation

Compute the missing components by path tracing [Kollig and Keller 2004]

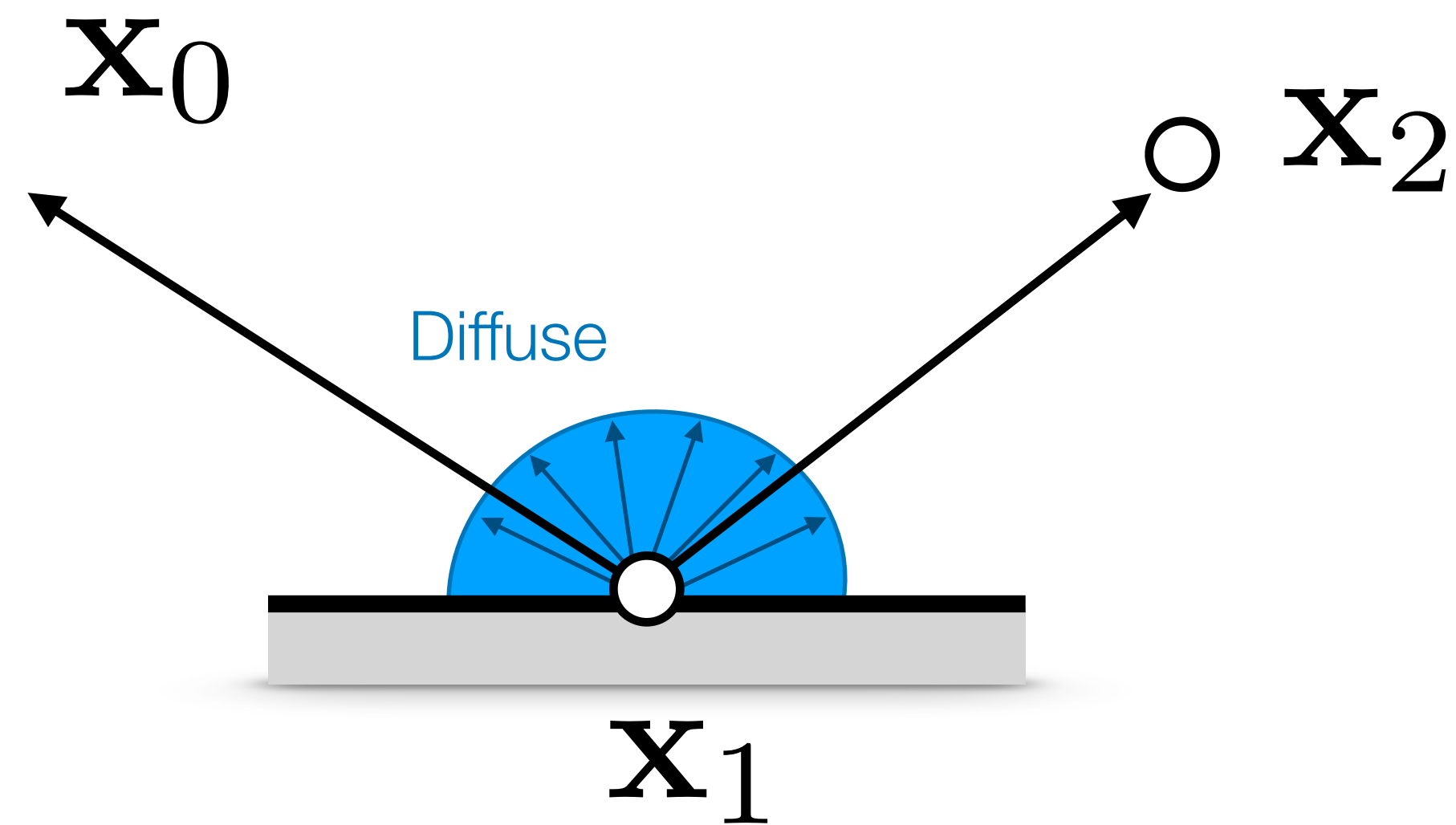


Virtual Spherical Lights



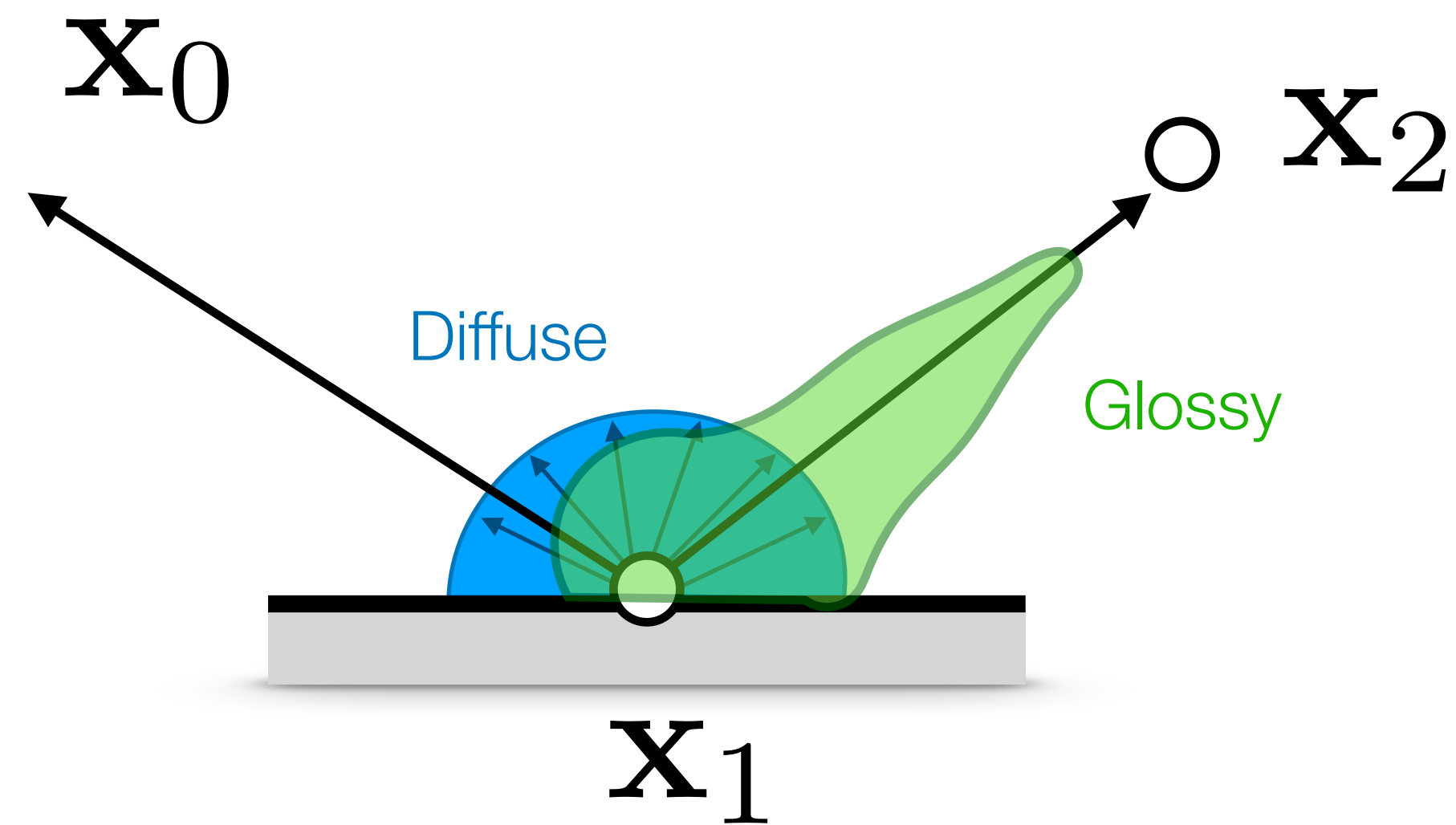
Instant Radiosity: Only Diffuse

Instant radiosity assumes all surfaces are diffuse

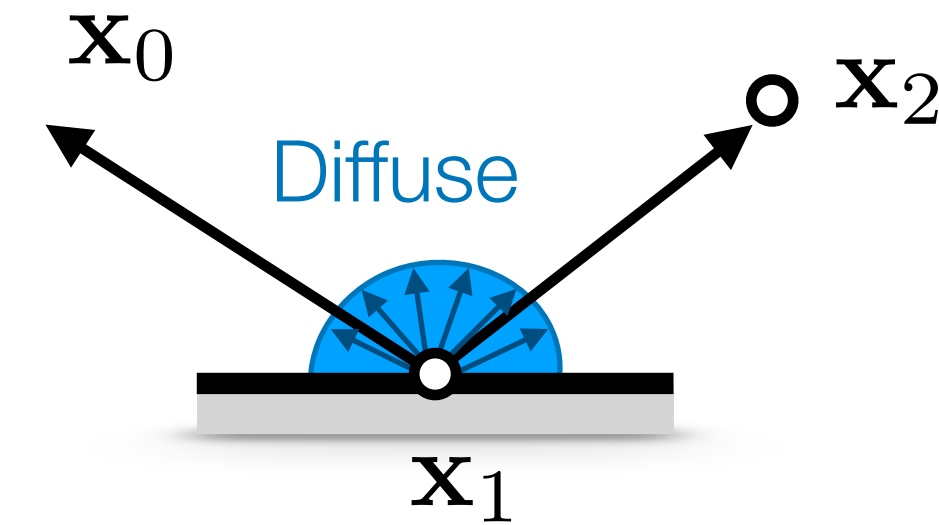


Instant Radiosity: Only Diffuse

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Glossy VPL Emission: Illumination Spikes

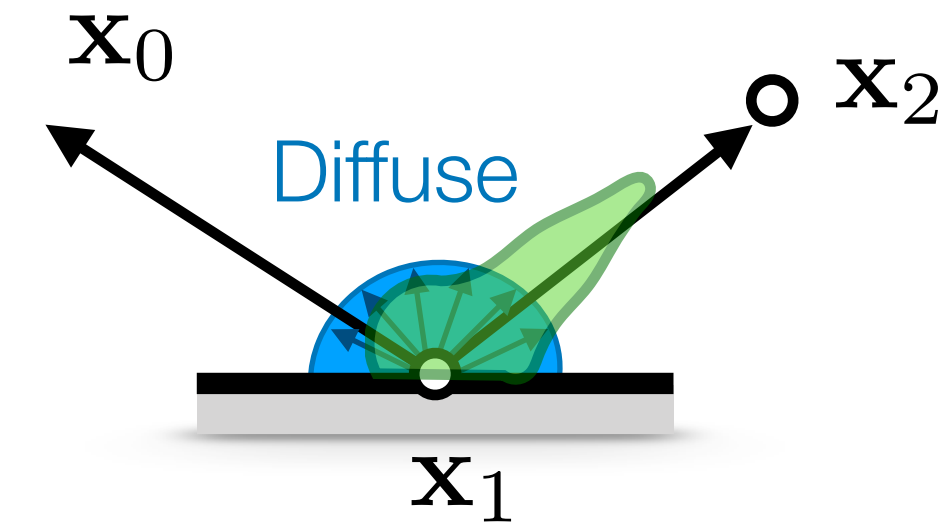


Common solution:

Only diffuse BRDF at light locations

Streak on the ceiling is caused by a VPL located on a highly anisotropic glossy surface.

Glossy VPL Emission: Illumination Spikes



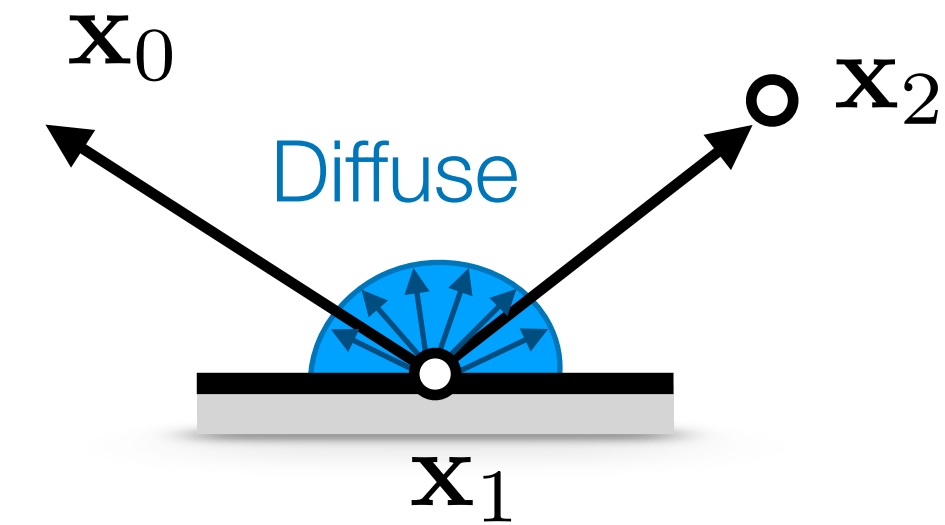
Common solution:

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Hasan et al. 2009

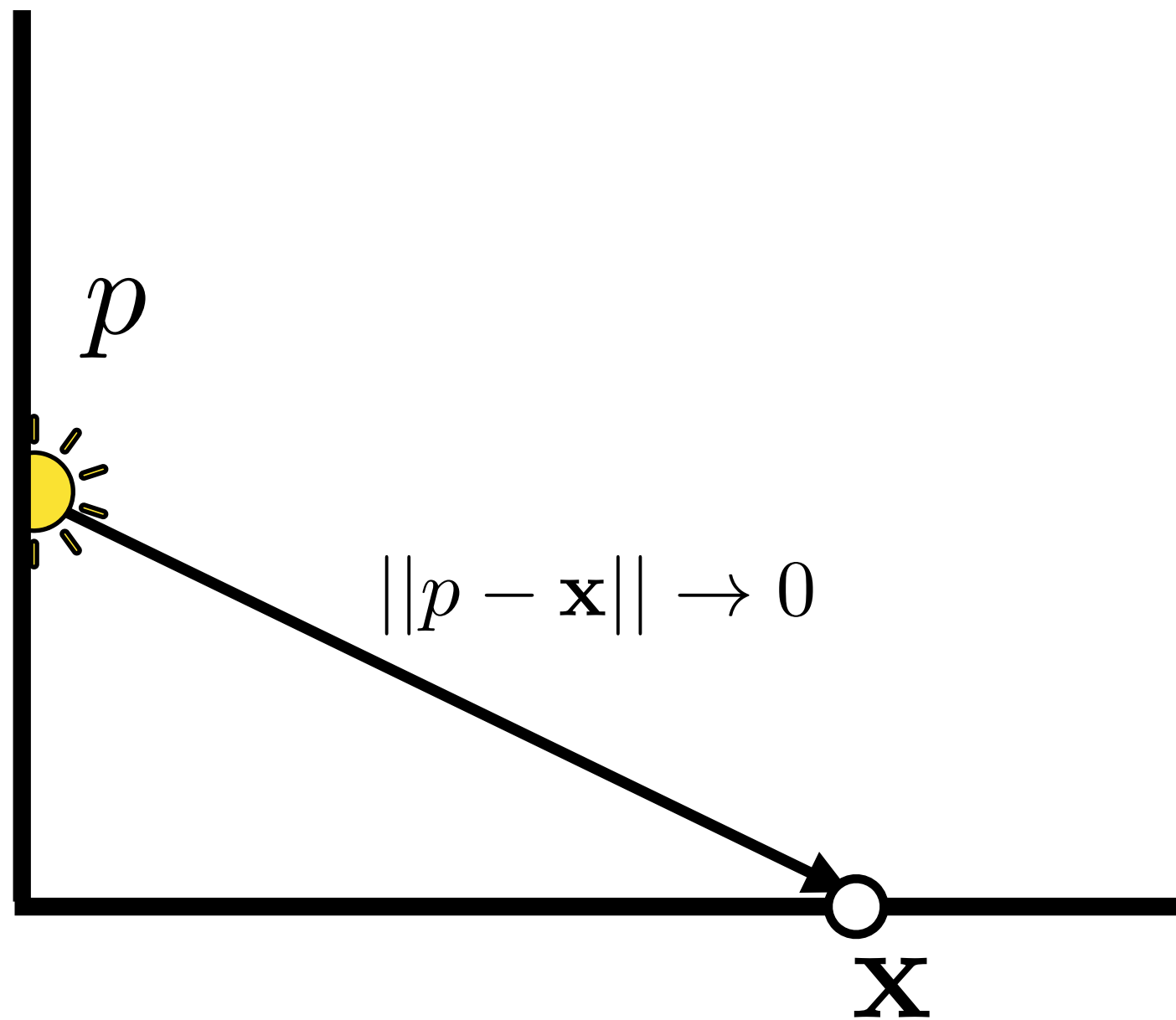
Remaining Spikes



Common solution:

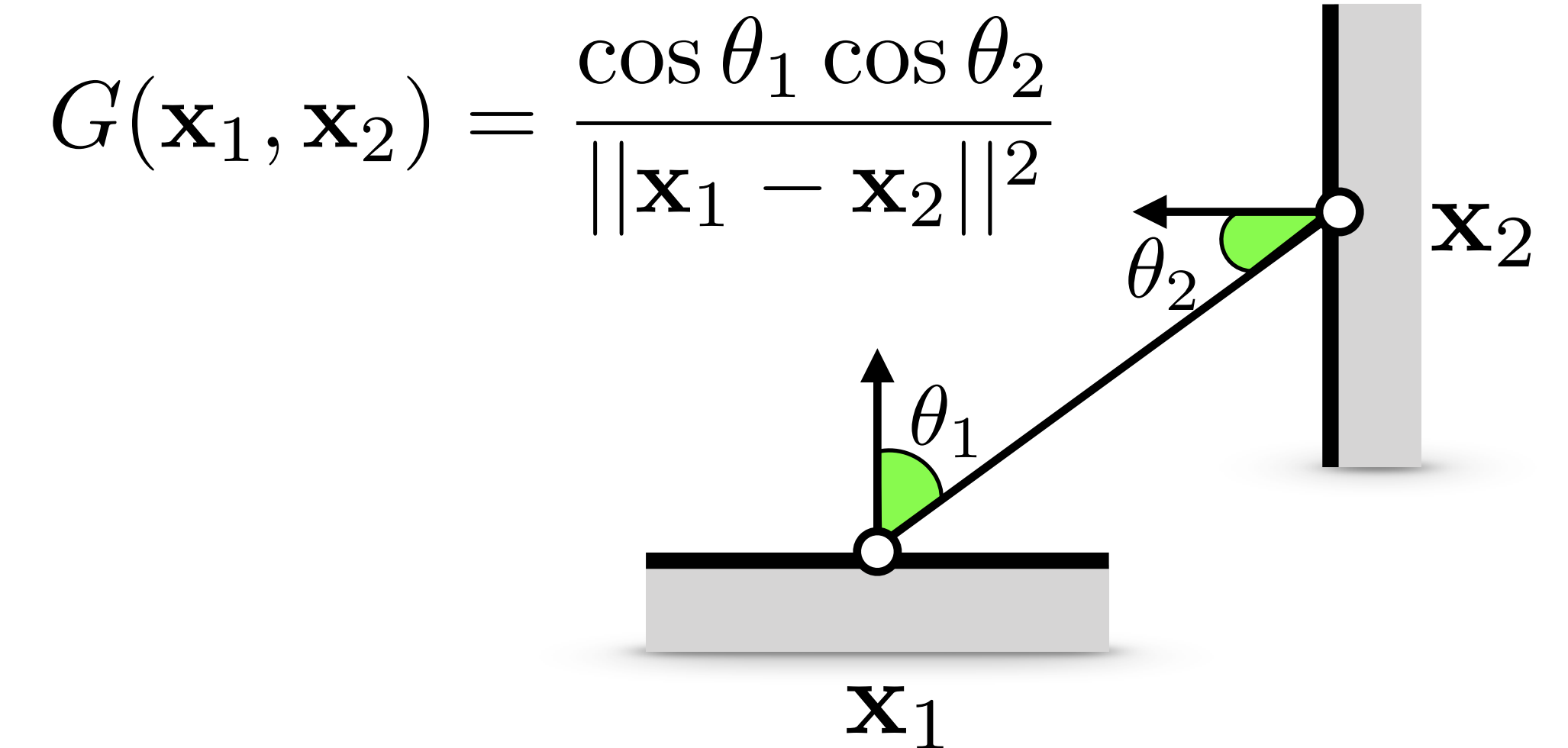
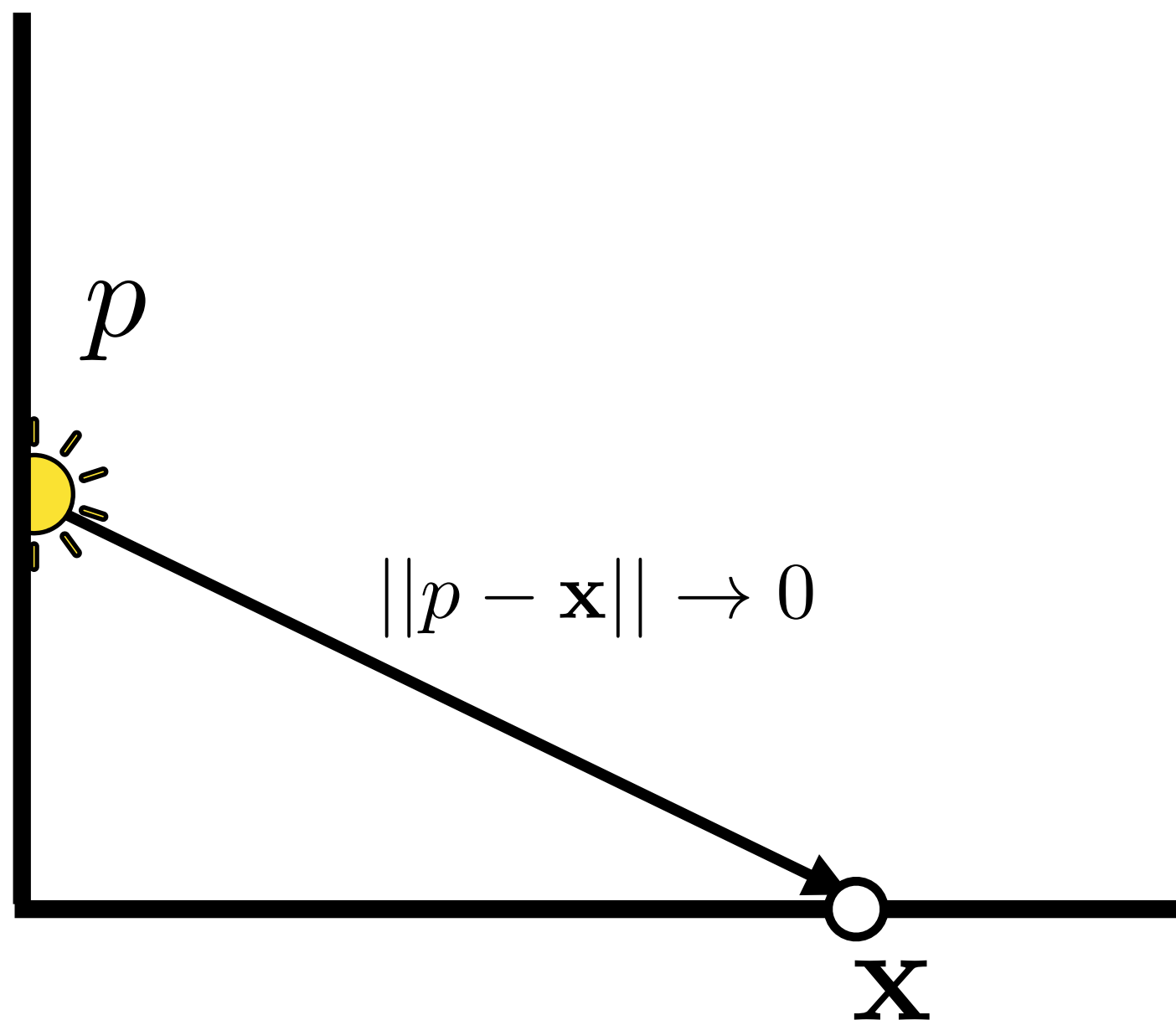
Only diffuse BRDF at light locations

VPL contribution affected by distance

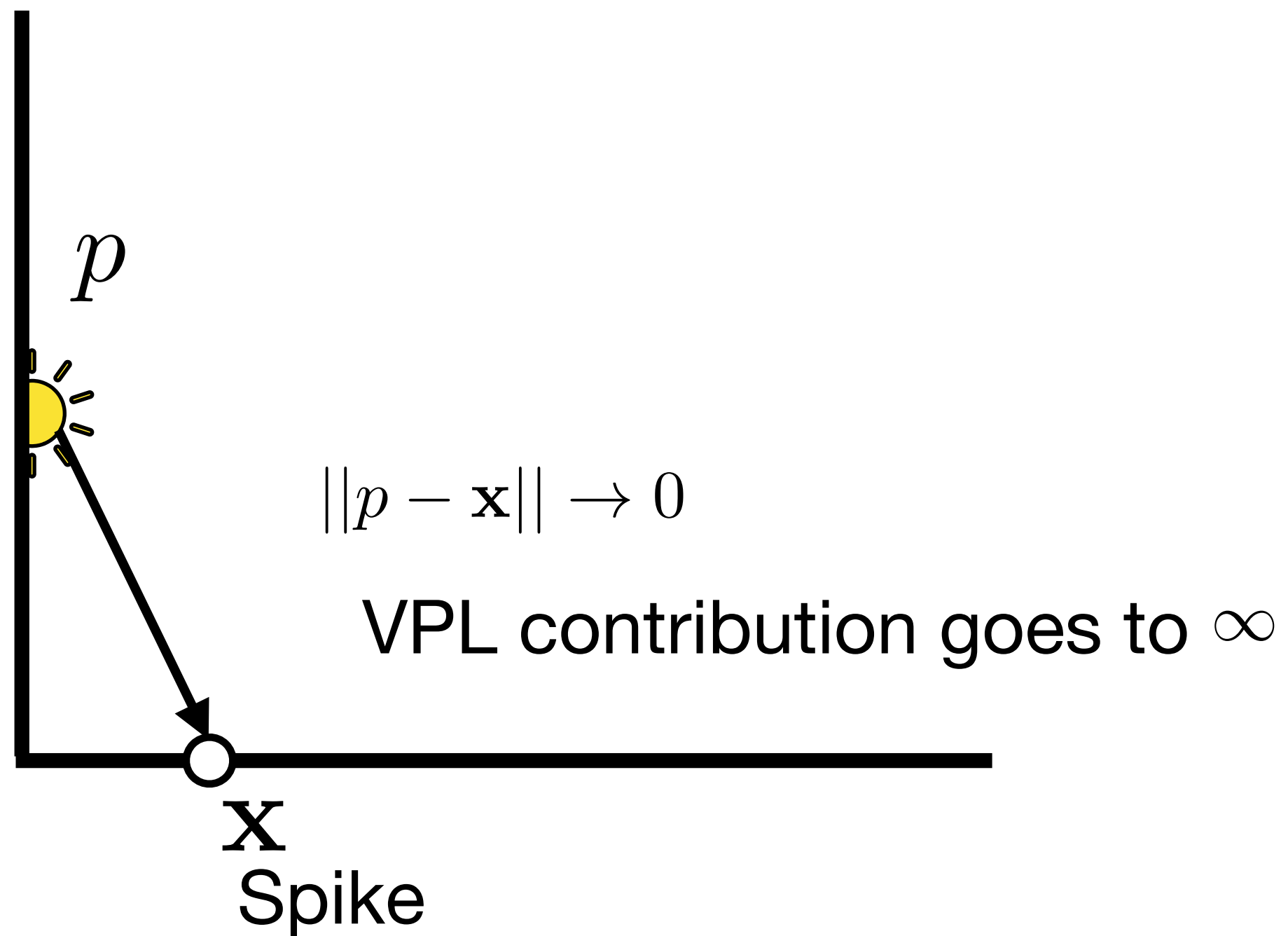


Hasan et al. 2009

VPL contribution affected by distance



VPL contribution affected by distance

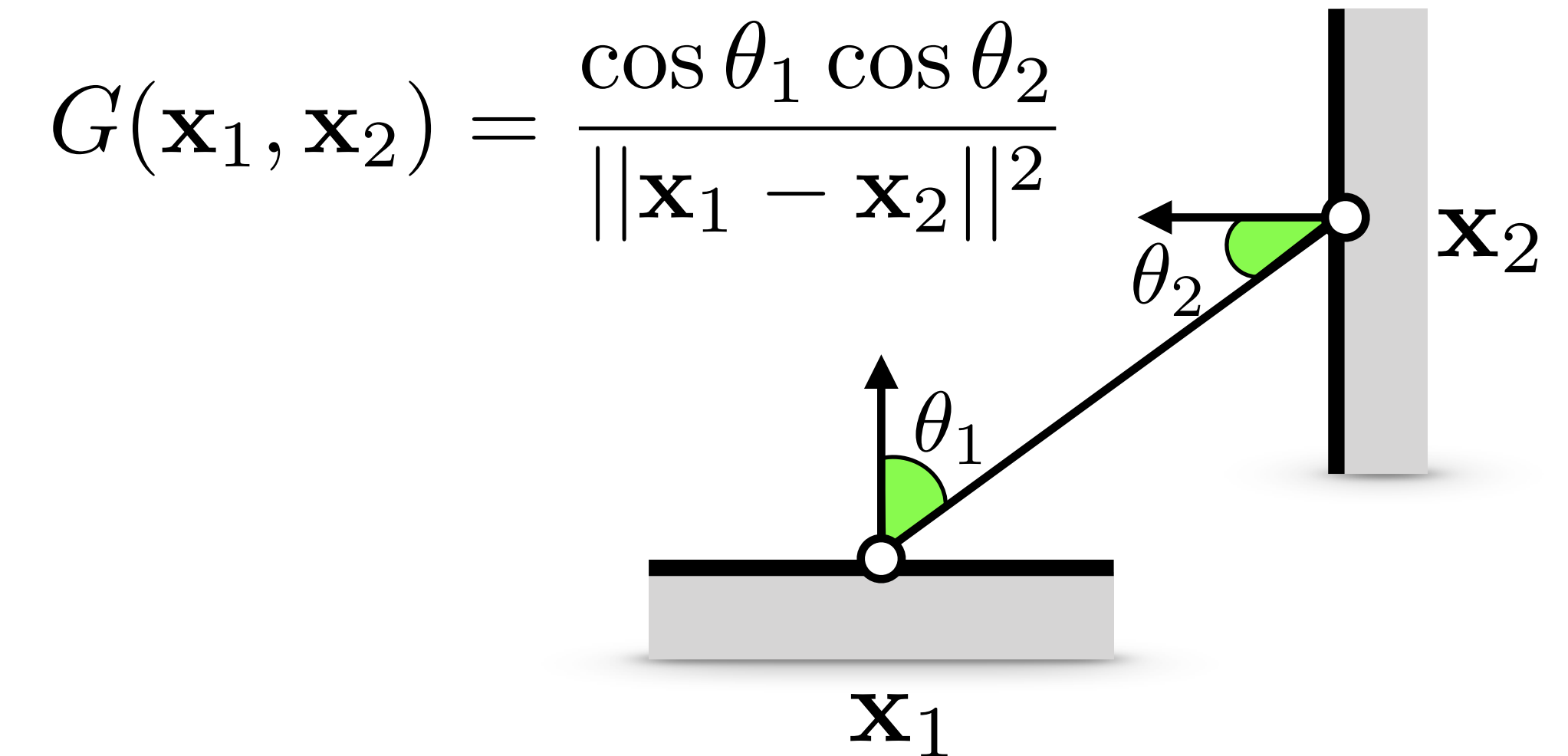
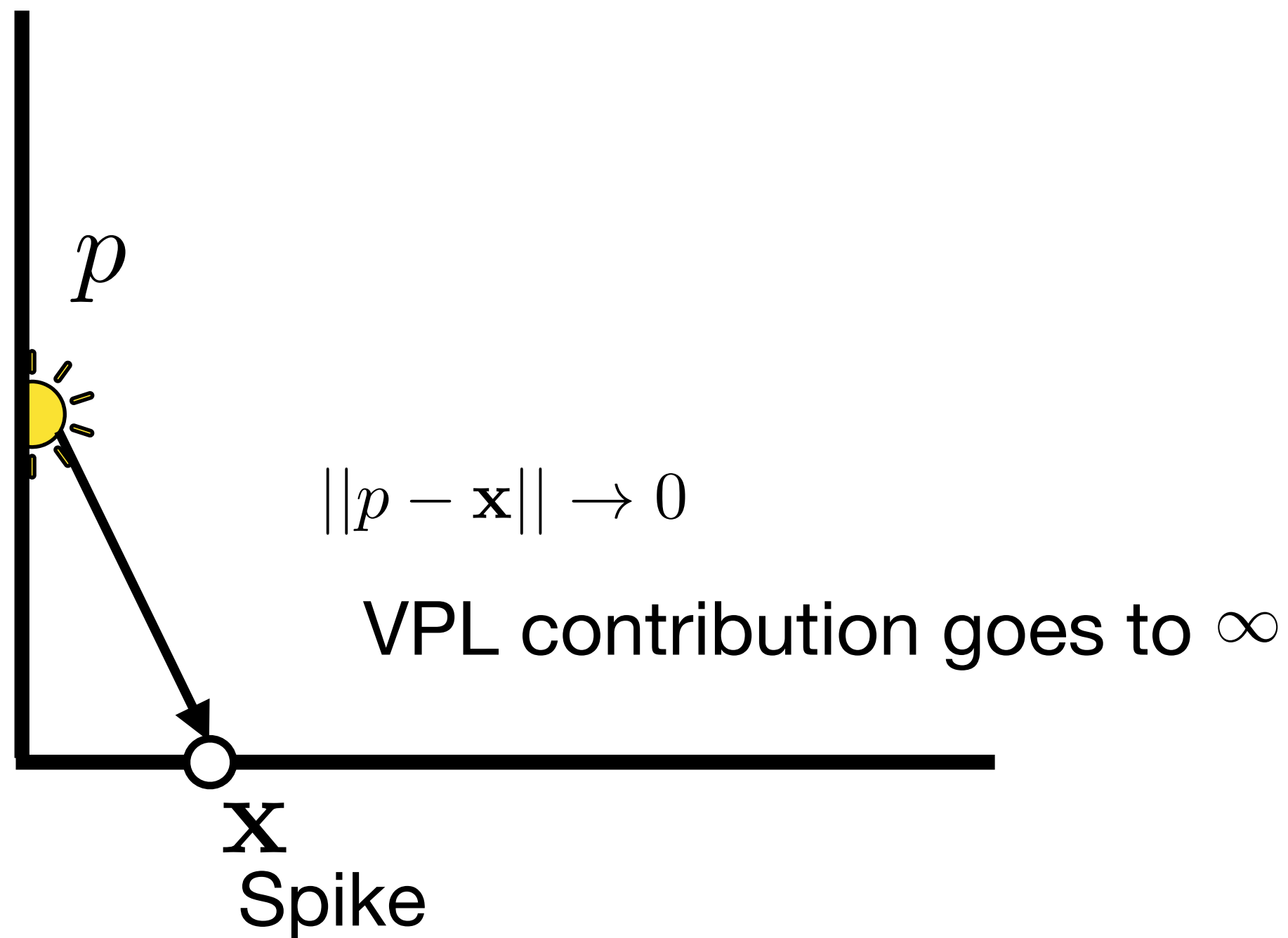


$$G(\mathbf{x}_1, \mathbf{x}_2) = \frac{\cos \theta_1 \cos \theta_2}{\|\mathbf{x}_1 - \mathbf{x}_2\|^2}$$

A diagram illustrating the geometry of the Goussain function $G(\mathbf{x}_1, \mathbf{x}_2)$. It shows two points, \mathbf{x}_1 and \mathbf{x}_2 , on a horizontal surface. \mathbf{x}_1 is on the left, and \mathbf{x}_2 is on the right. A vertical line represents a wall. The angle θ_1 is the angle between the normal vector at \mathbf{x}_1 (indicated by a vertical arrow) and the line segment connecting \mathbf{x}_1 and \mathbf{x}_2 . The angle θ_2 is the angle between the normal vector at \mathbf{x}_2 (indicated by a horizontal arrow pointing left) and the line segment connecting \mathbf{x}_1 and \mathbf{x}_2 . Green shaded sectors indicate the angles θ_1 and θ_2 .

VPL contribution affected by distance

Common solution: Clamp the VPL contribution



Hasan et al. 2009

Motivation

VPLs: Image splotches due to

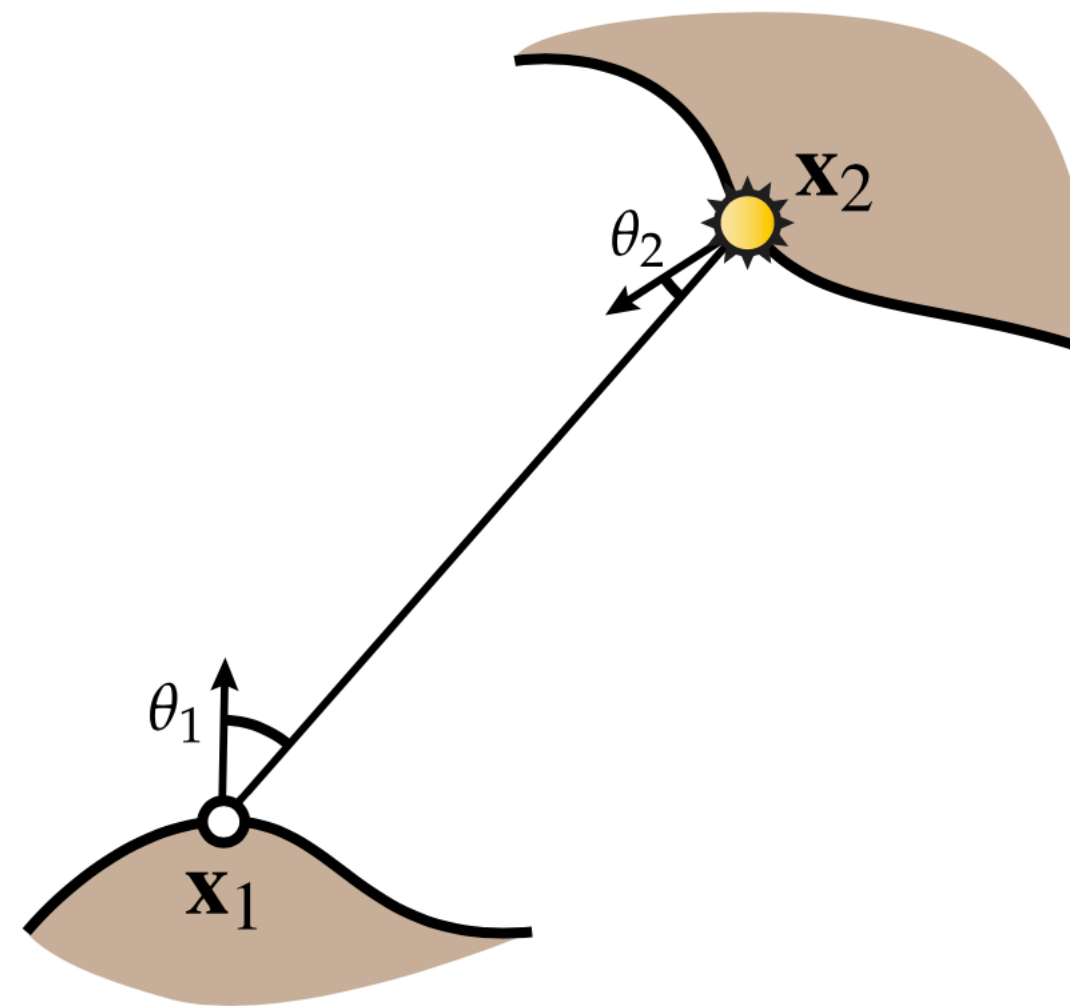
- Spikes in the VPL emission distribution
- $\frac{1}{||\mathbf{x}_1 - \mathbf{x}_2||^2}$ term

Virtual Spherical lights (VSL):

- Spread the energy of the infinitesimal VPL over a finite surface
- Computer contribution as a solid angle integral

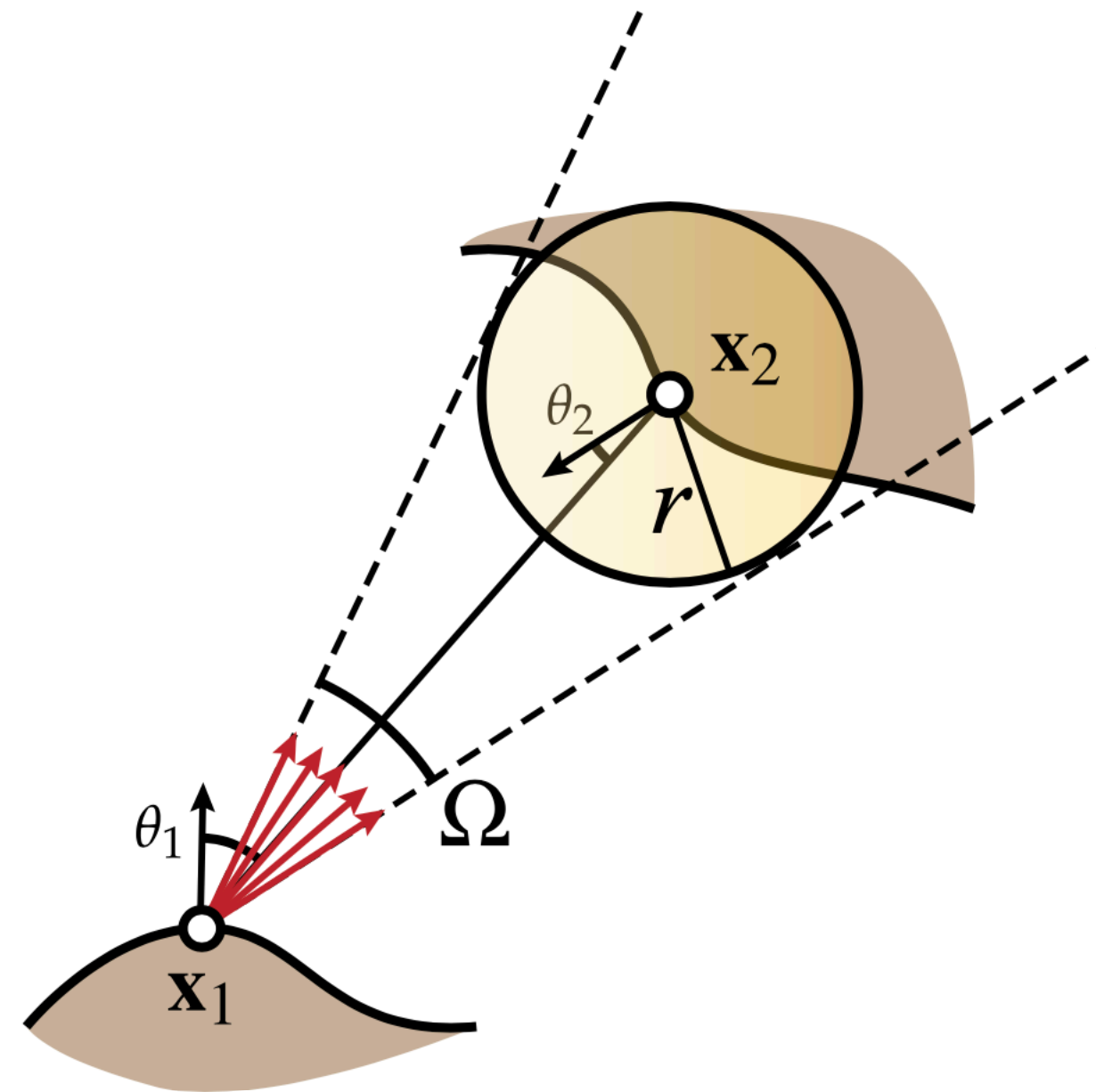
Spreading the Energy

Spread the energy of the infinitesimal VPL over a finite surface



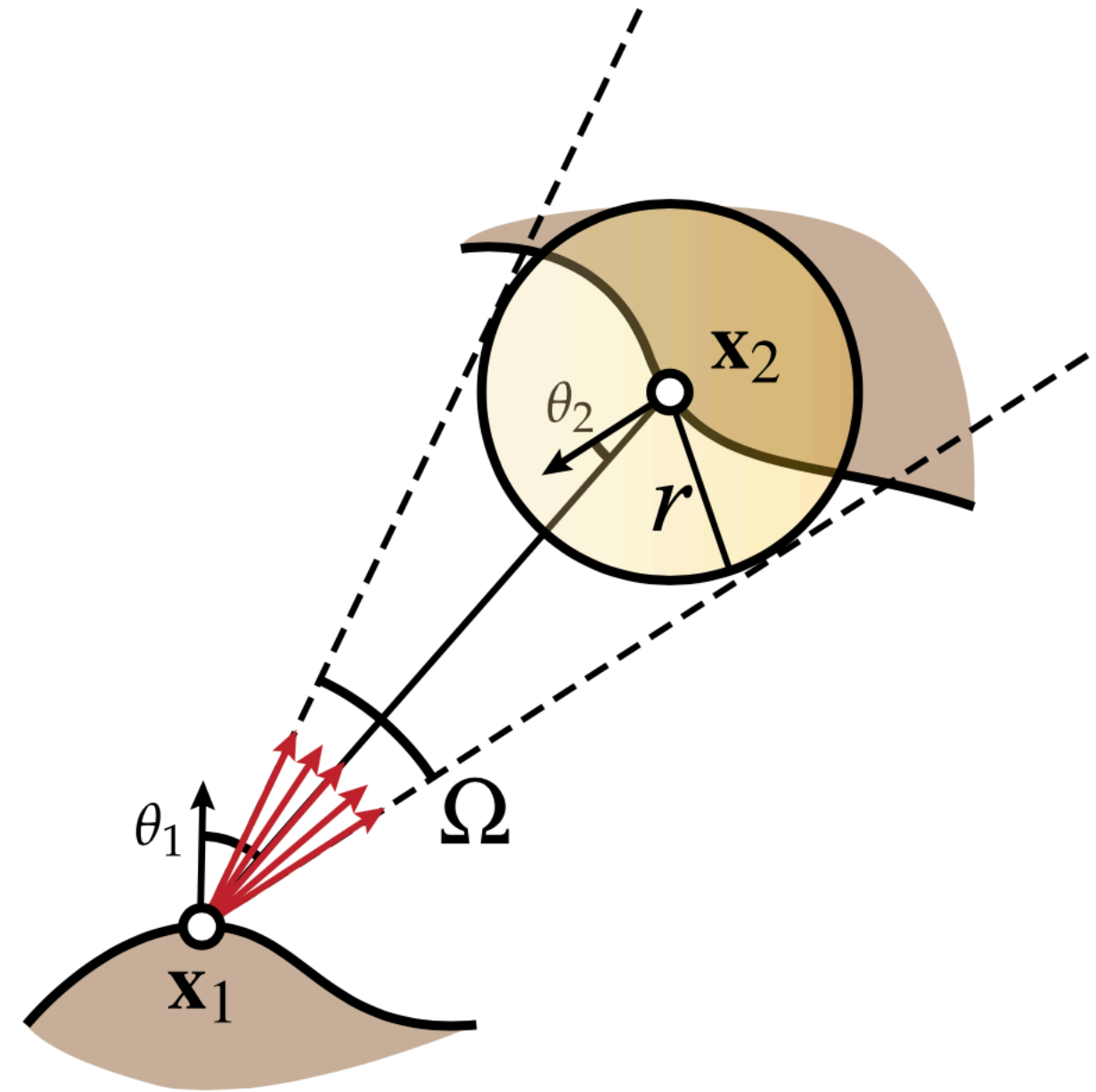
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Spreading the Energy

Spread the energy of the infinitesimal VPL over a finite surface

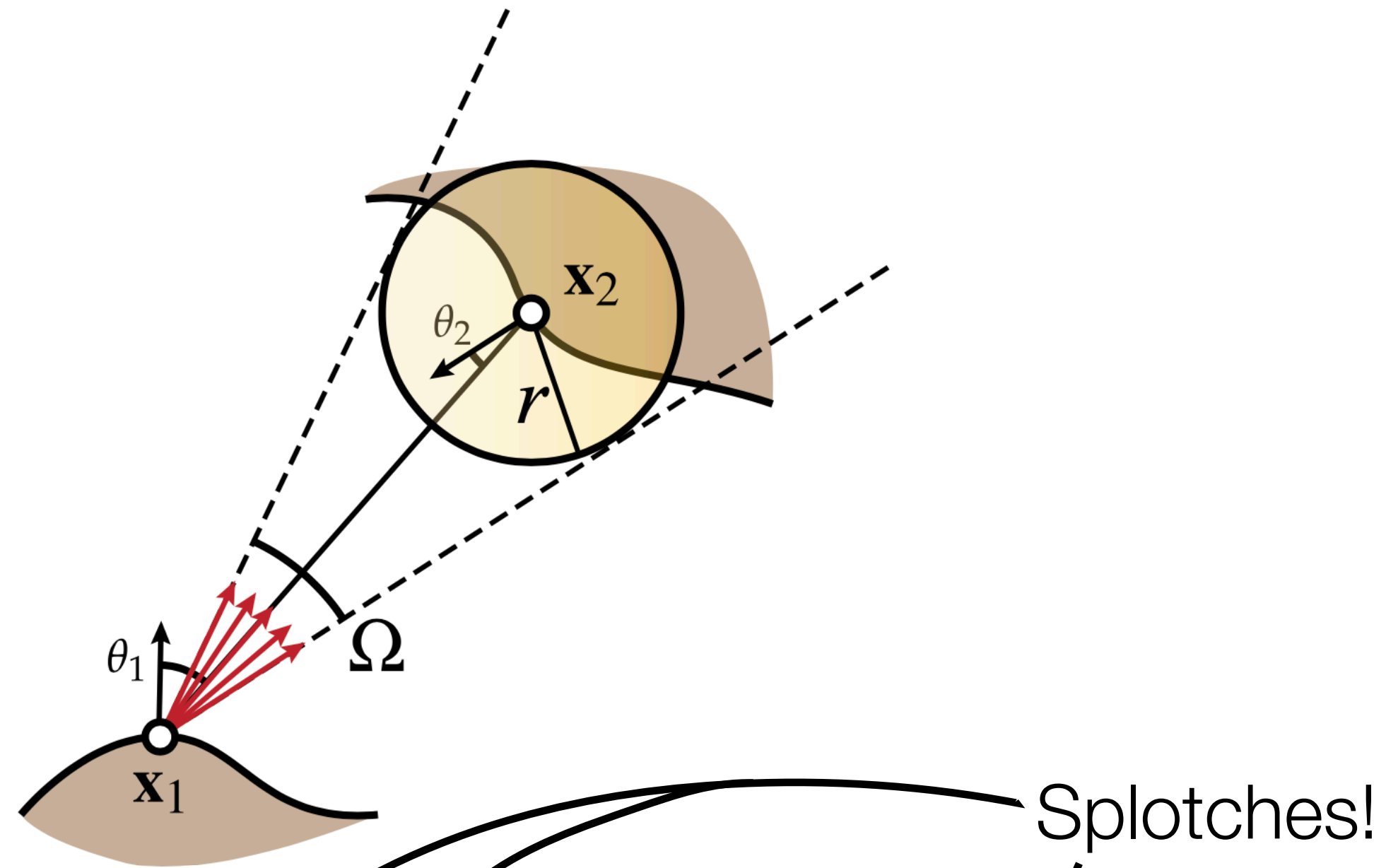


point-to-point:

$$\Phi V(\mathbf{x}_1, \mathbf{x}_2) f(\mathbf{x}_1) f(\mathbf{x}_2) \frac{\cos \theta_1 \cos \theta_2}{\|\mathbf{x}_1 - \mathbf{x}_2\|^2}$$

Spreading the Energy

Spread the energy of the infinitesimal VPL over a finite surface

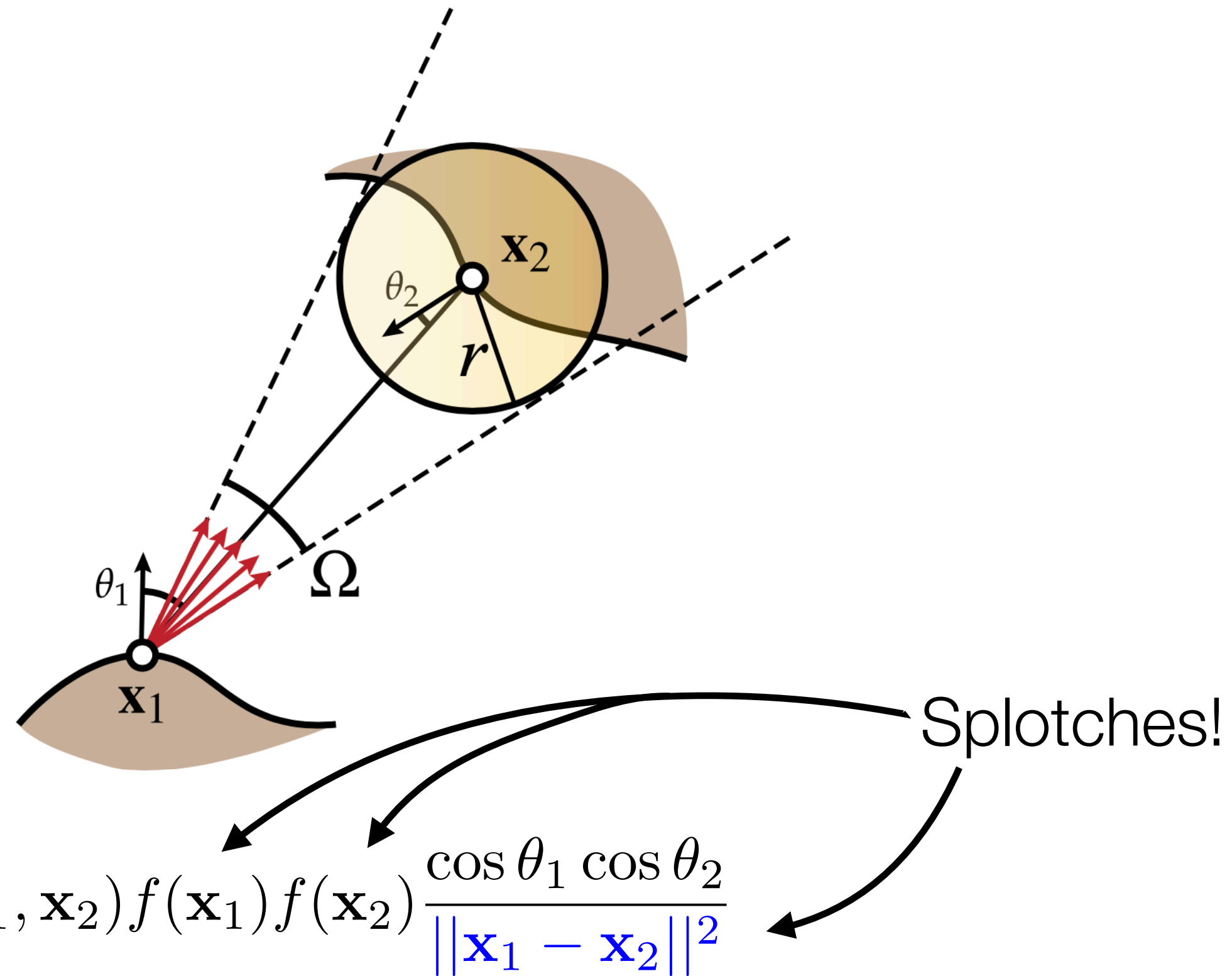


point-to-point:

$$\Phi V(\mathbf{x}_1, \mathbf{x}_2) f(\mathbf{x}_1) f(\mathbf{x}_2) \frac{\cos \theta_1 \cos \theta_2}{\|\mathbf{x}_1 - \mathbf{x}_2\|^2}$$

Spreading the Energy

Spread the energy of the infinitesimal VPL over a finite surface



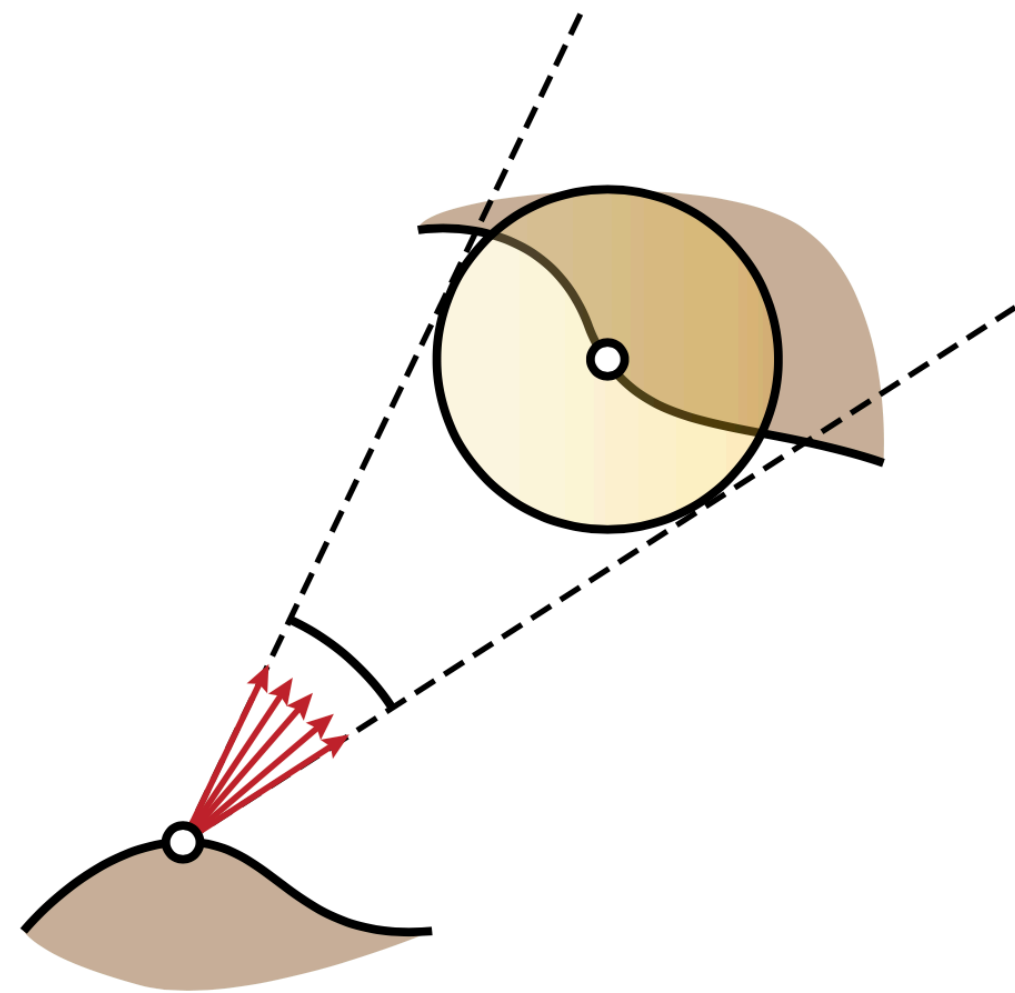
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$$\Phi V(\mathbf{x}_1, \mathbf{x}_2) f(\mathbf{x}_1) f(\mathbf{x}_2) \frac{\cos \theta_1 \cos \theta_2}{\|\mathbf{x}_1 - \mathbf{x}_2\|^2}$$

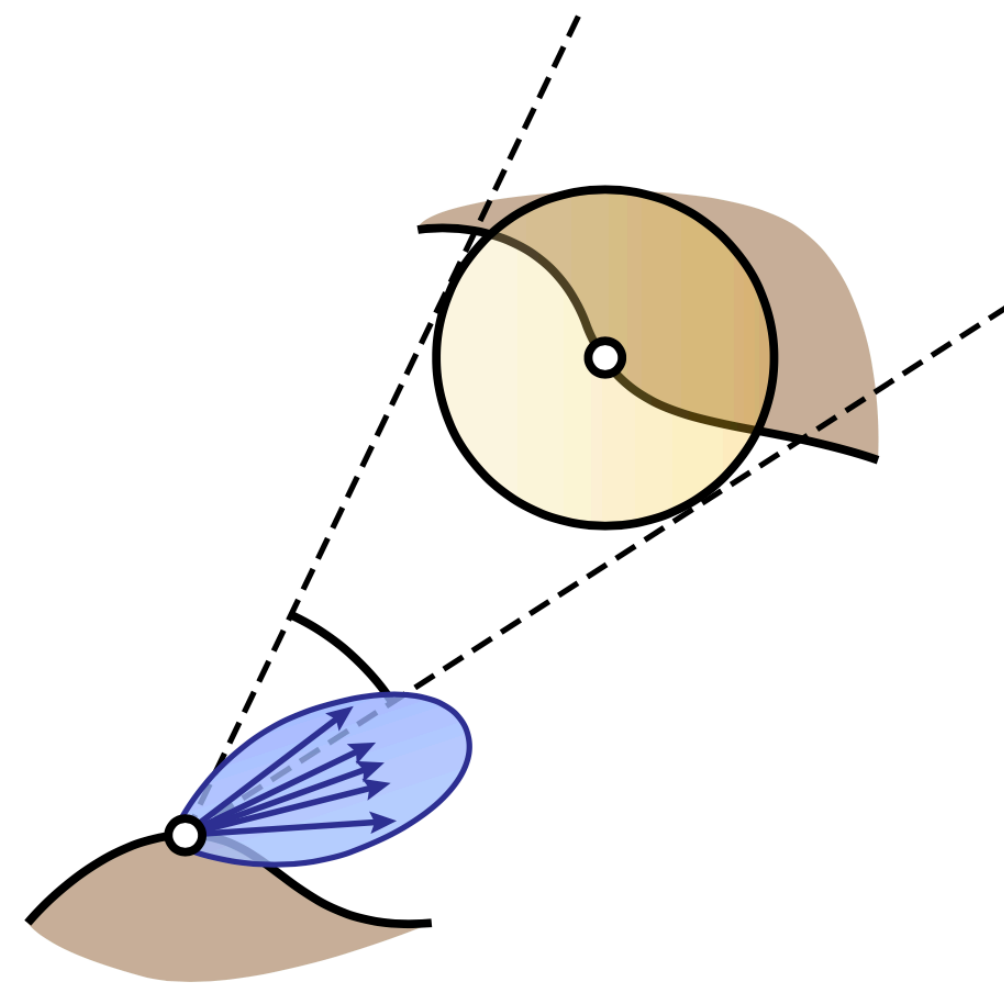
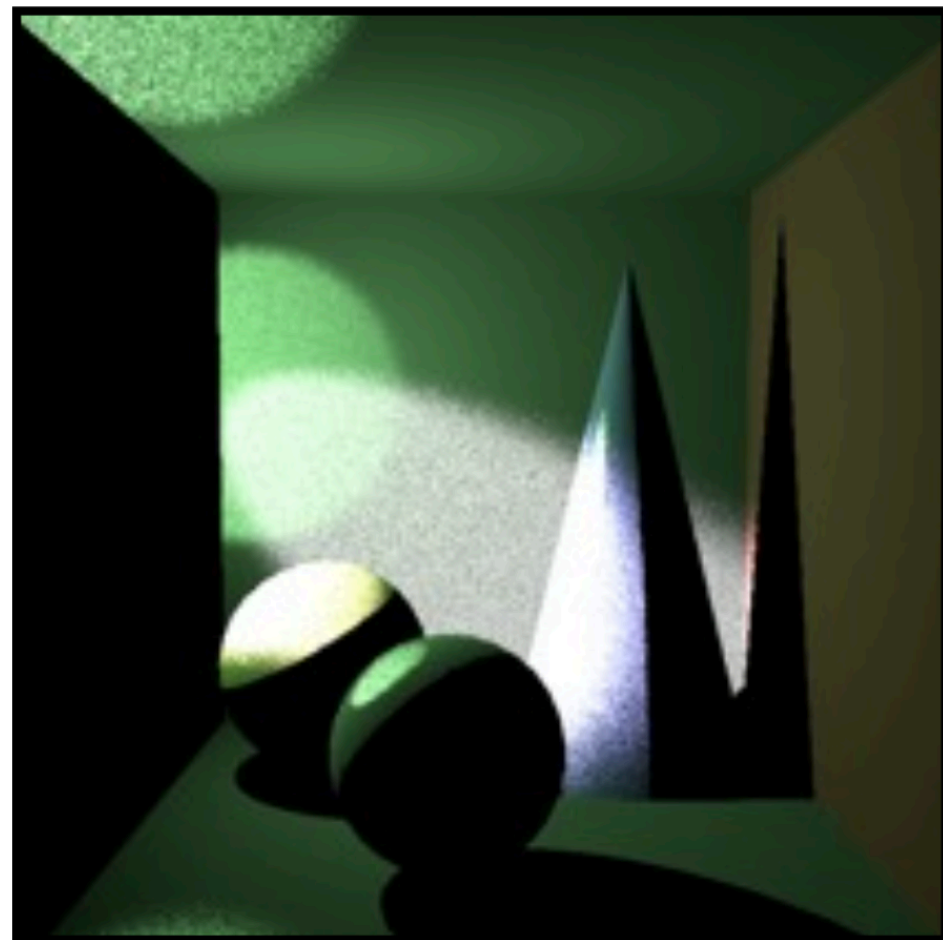
Approx. sphere-to-point:

$$\frac{\Phi}{\pi r^2} V(\mathbf{x}_1, \mathbf{x}_2) \int_{\mathcal{H}^2} f(\mathbf{x}_1) f(\mathbf{x}_2) \cos \theta_1 \cos \theta_2 d\vec{\omega}$$

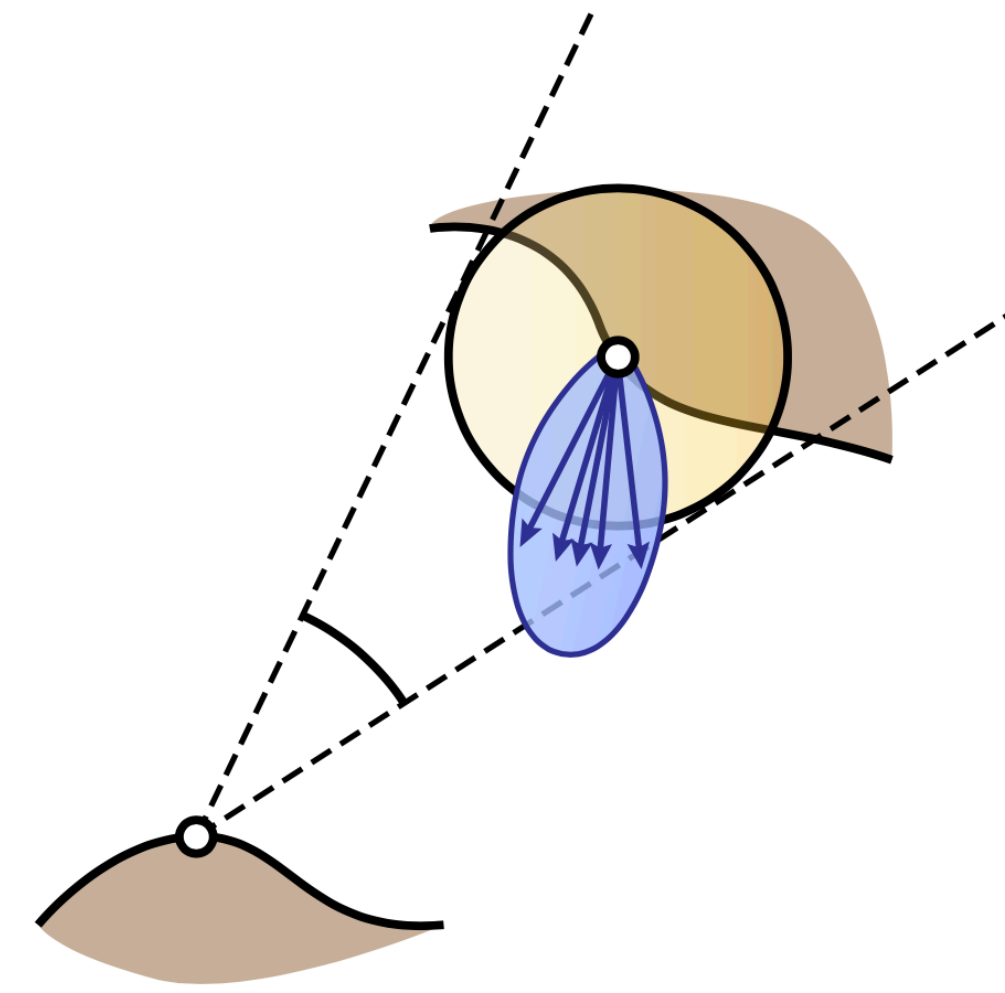
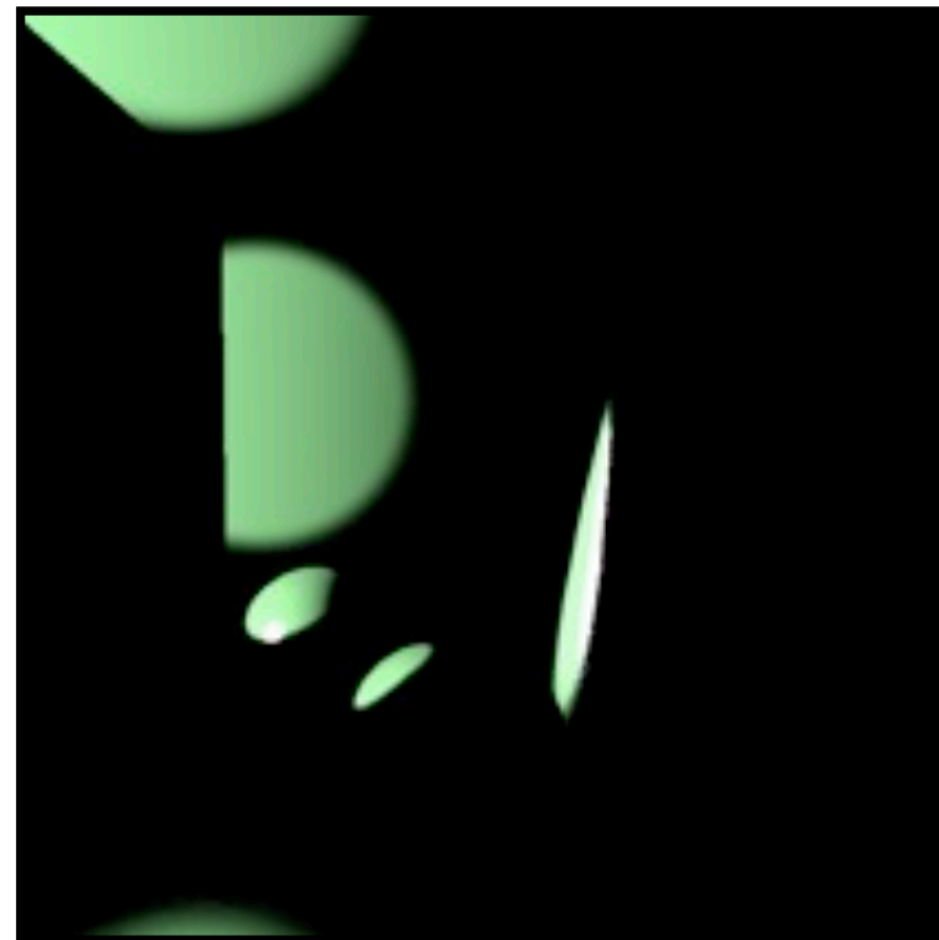
Spreading the Energy



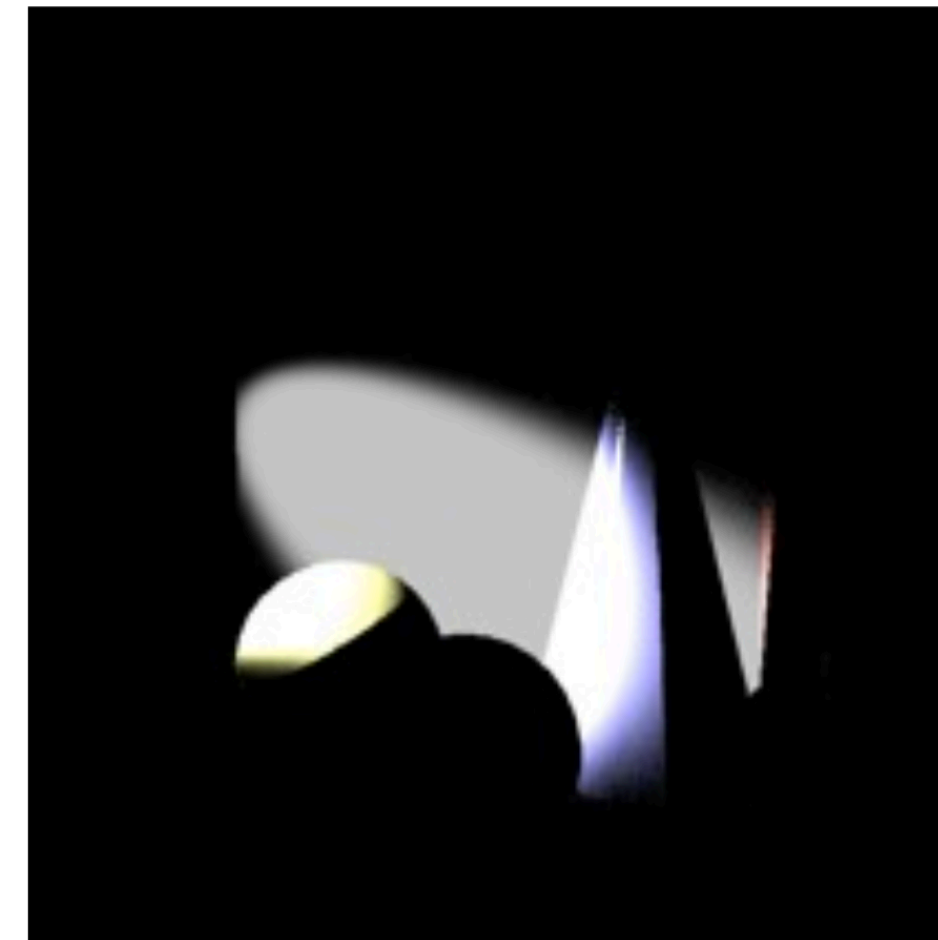
Cone sampling



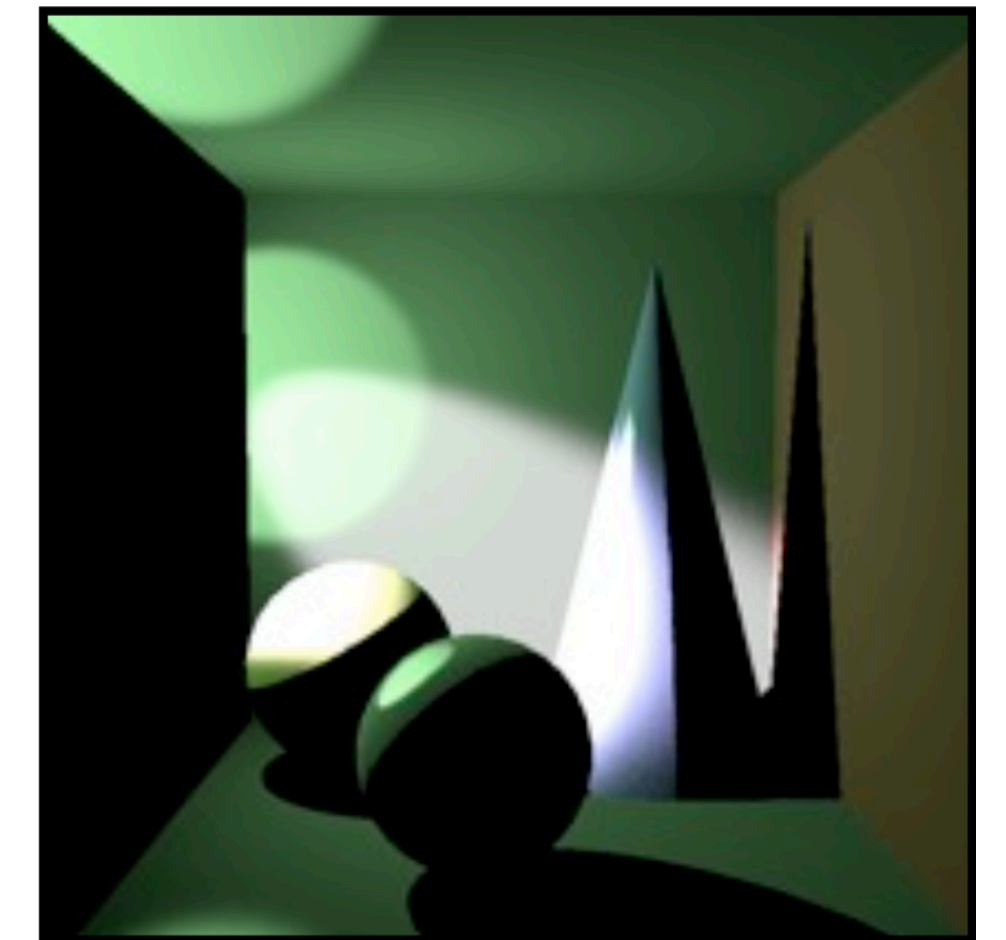
BRDF1 sampling



BRDF2 sampling



MIS sampling



Hasan et al. 2009

Spreading the Energy

Advantages:

- Energy is blurred, not clamped

Disadvantages:

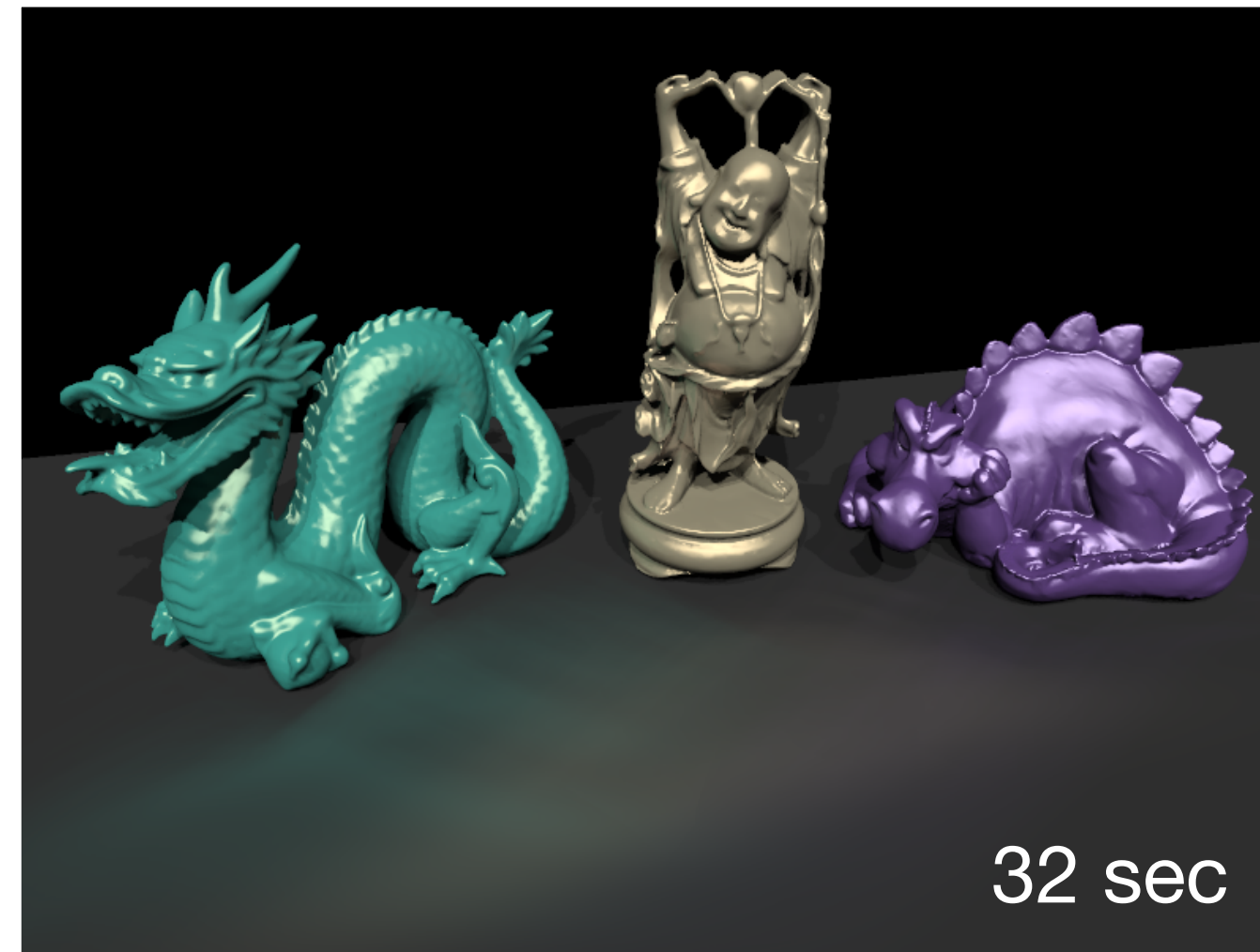
- Introduces bias
- Requires an extra integration over the solid angle

Hasan et al. 2009

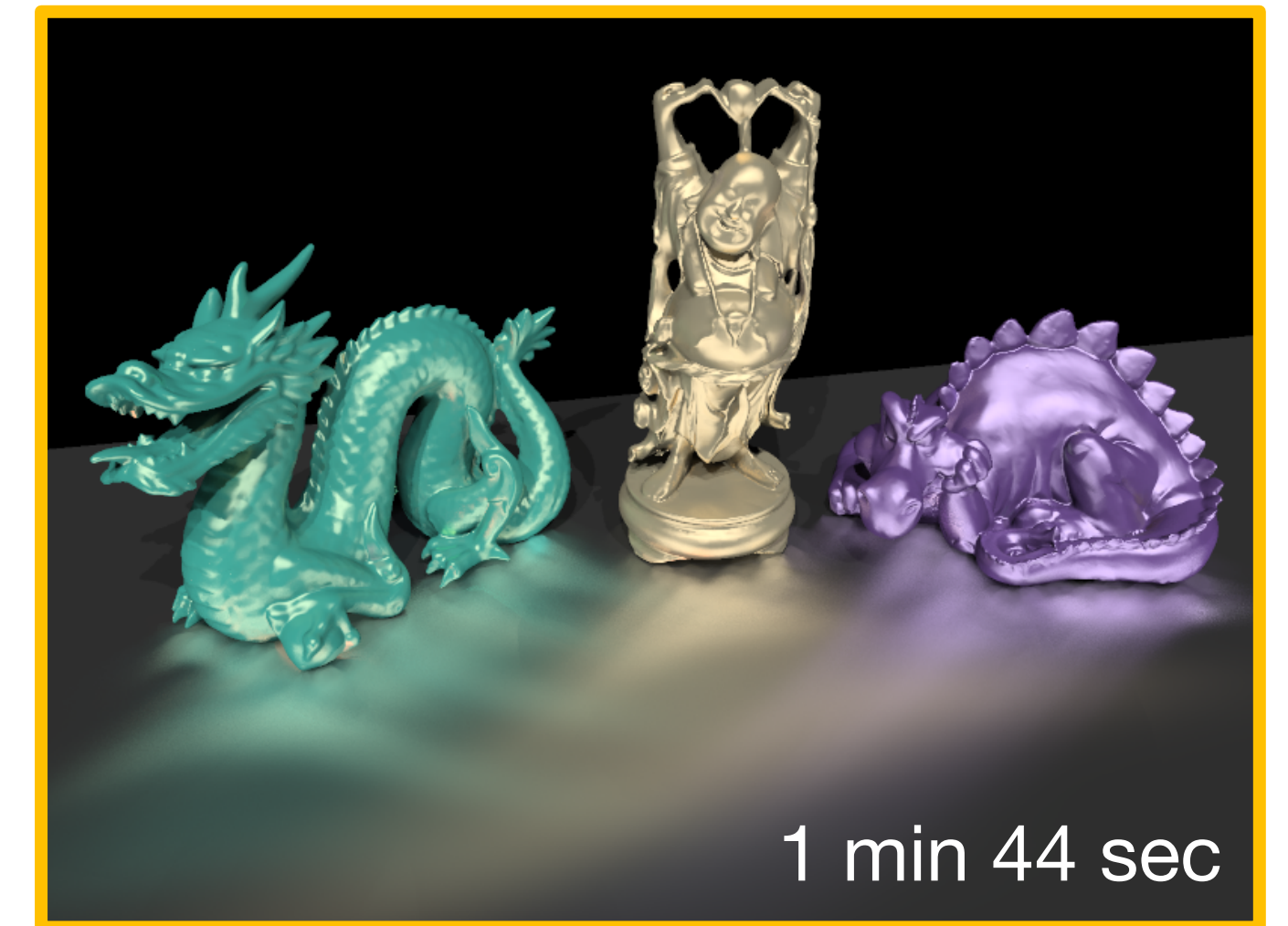
Spreading the Energy



Reference

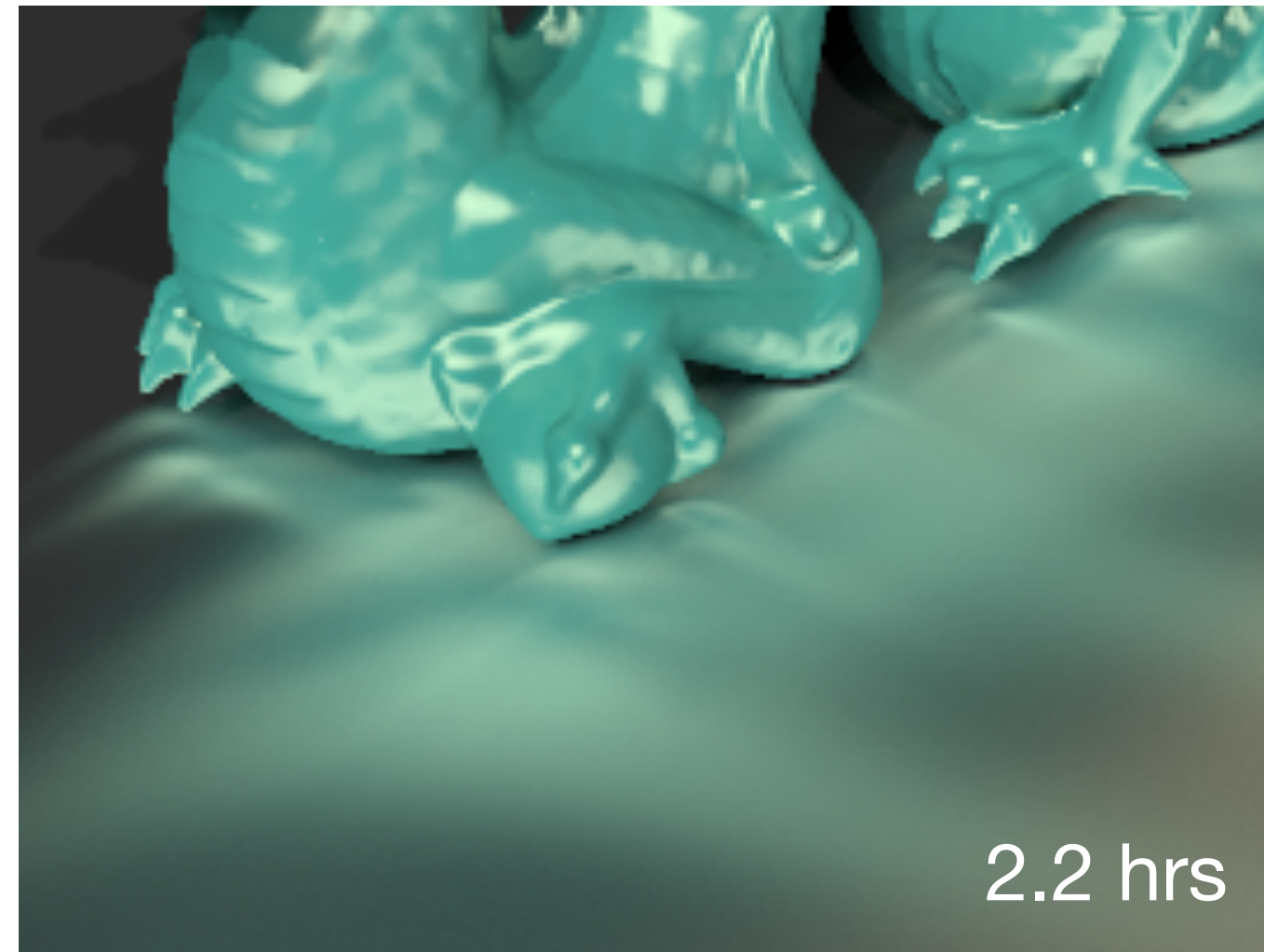


Clamped

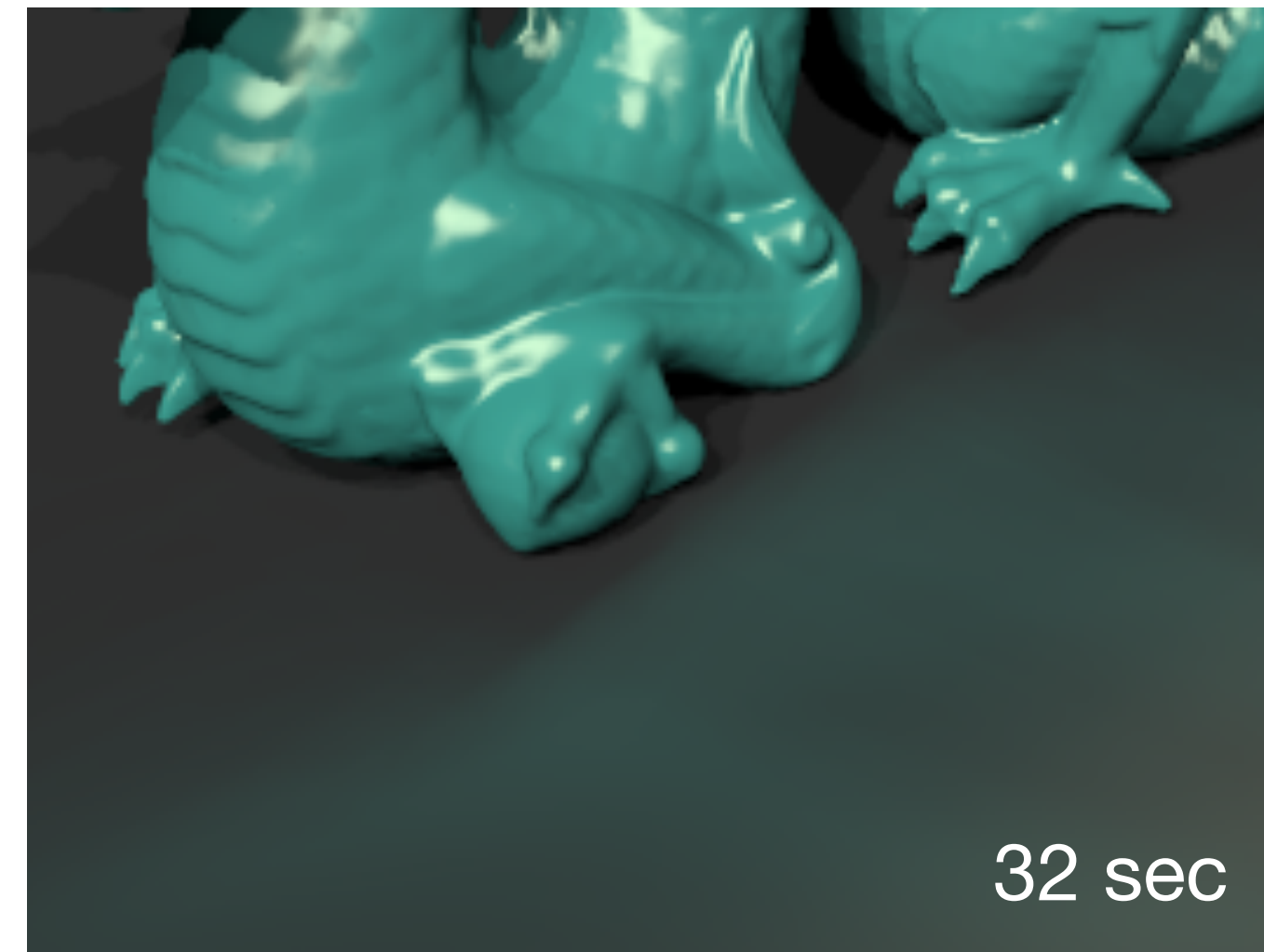


VSLs

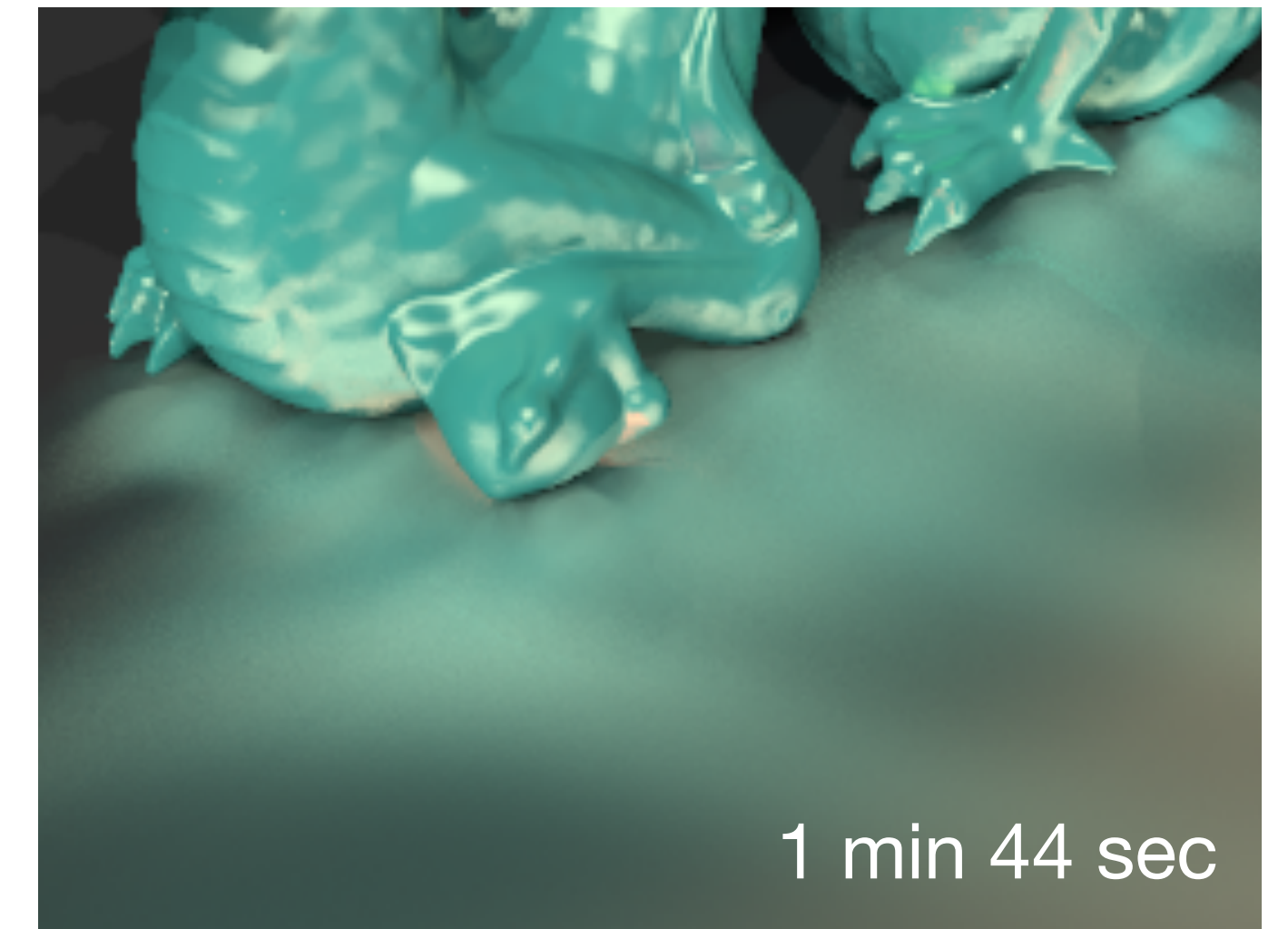
Spreading the Energy



Reference



Clamped



VSLs

Virtual Ray Lights

Motivation

Motivation



Motivation



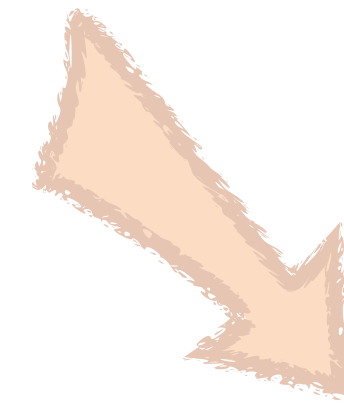
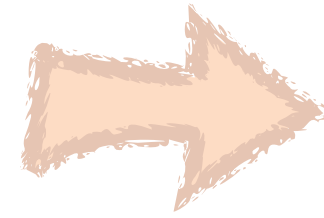
Motivation



Motivation

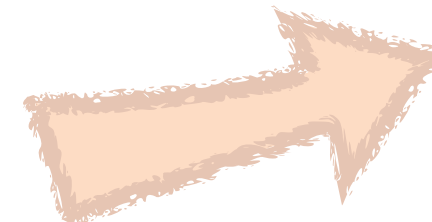
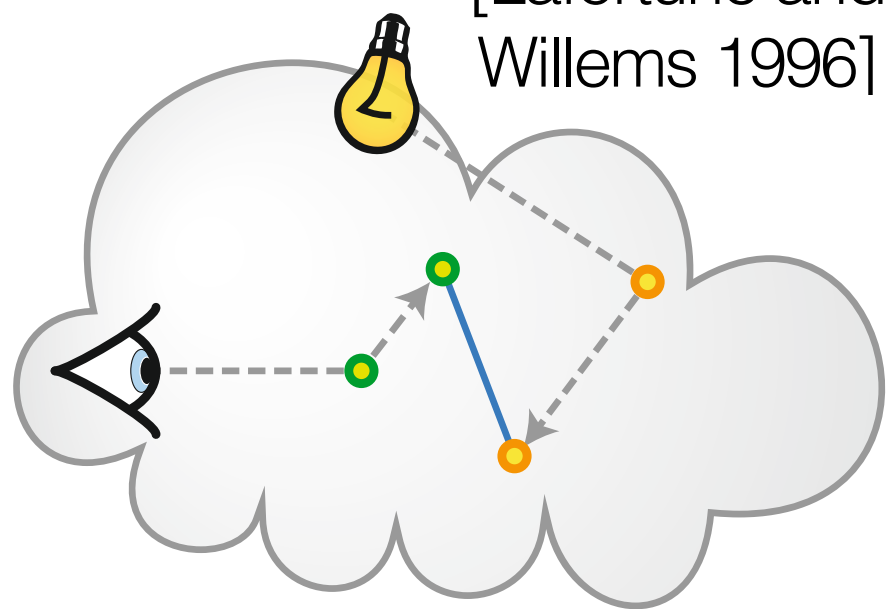


Previous work



Bidirectional Path Tracing

[Lafortune and
Willem's 1996]

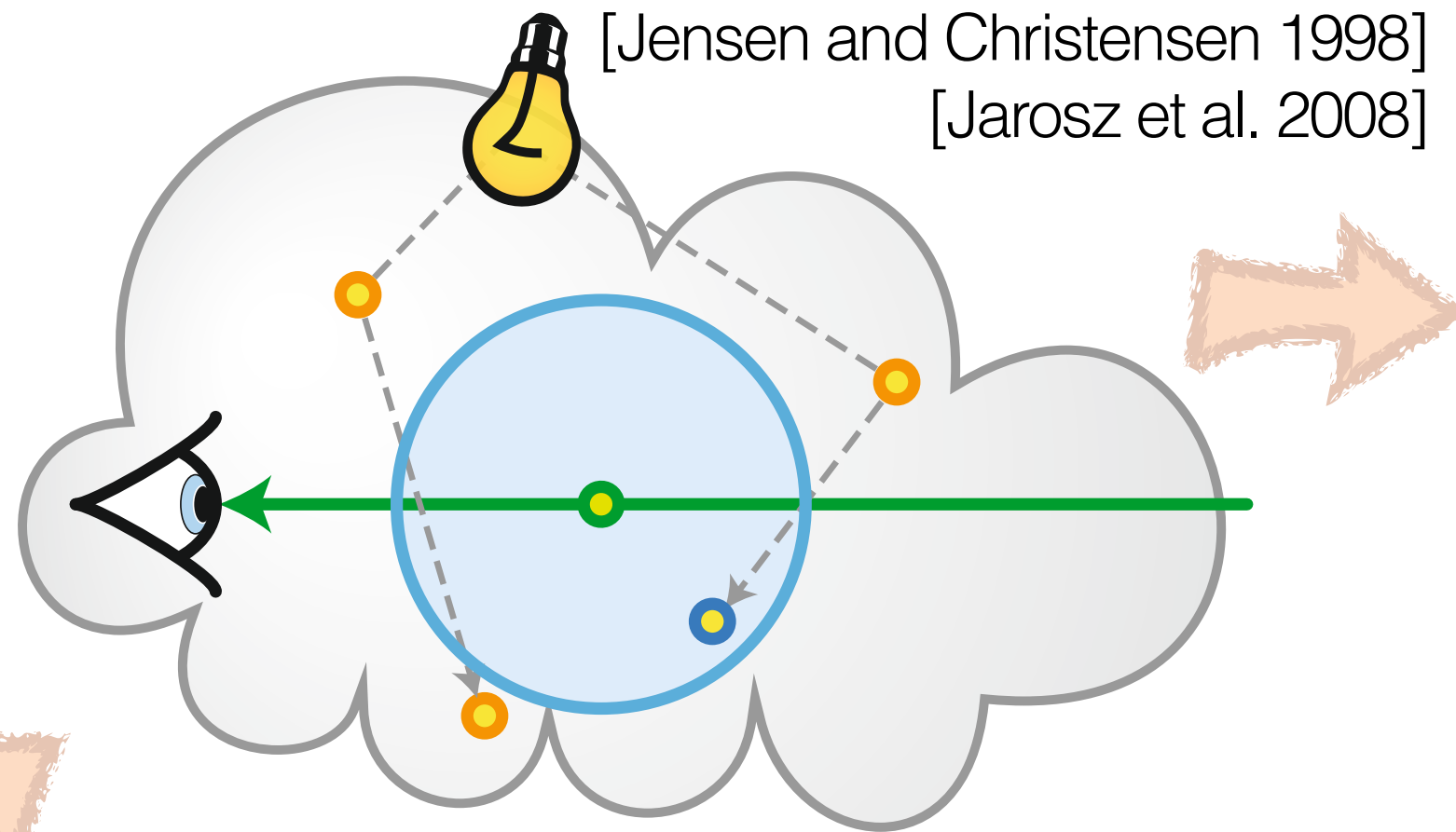


Previous work

Volumetric Photon Mapping

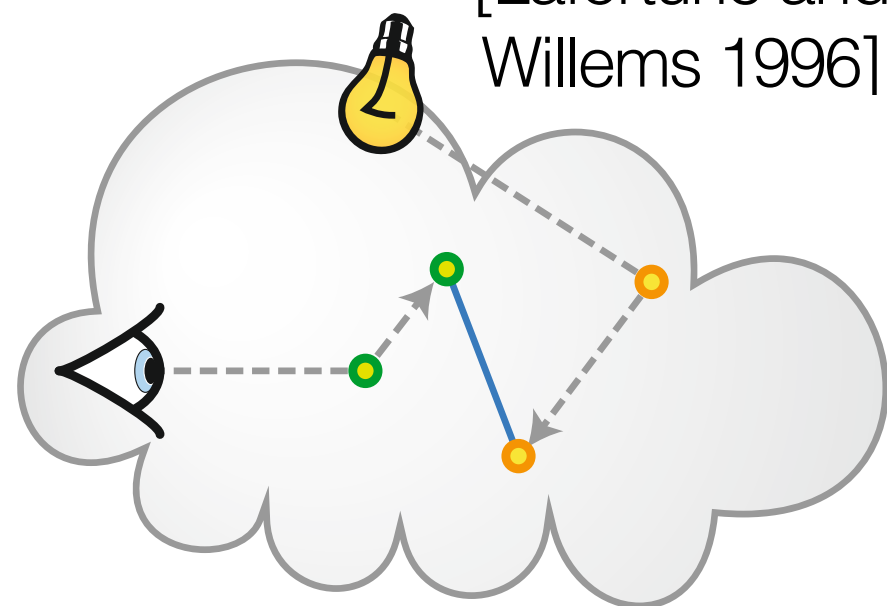
[Jensen and Christensen 1998]

[Jarosz et al. 2008]



Bidirectional Path Tracing

[Lafortune and Willem's 1996]

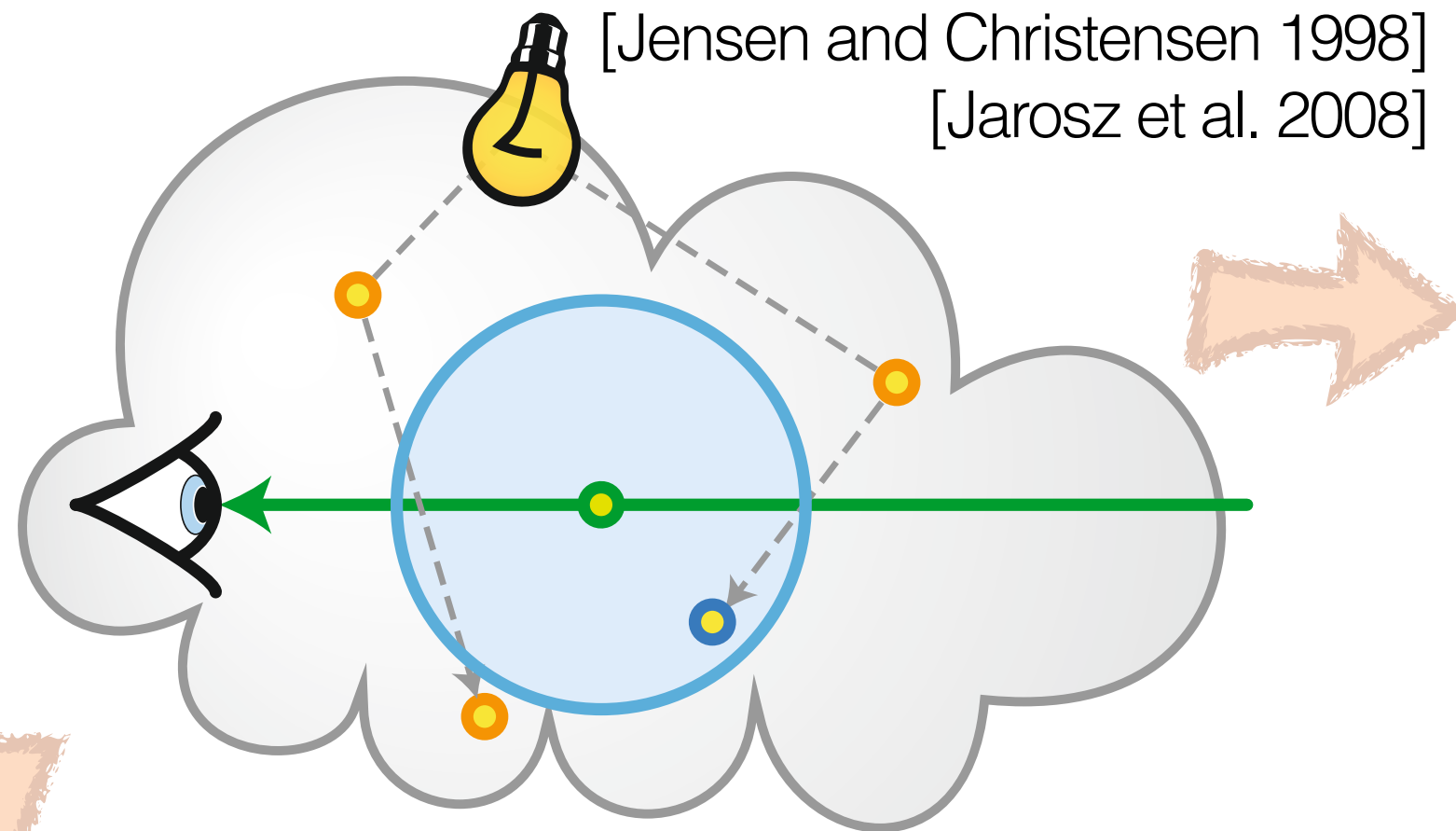


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Volumetric Photon Mapping

[Jensen and Christensen 1998]

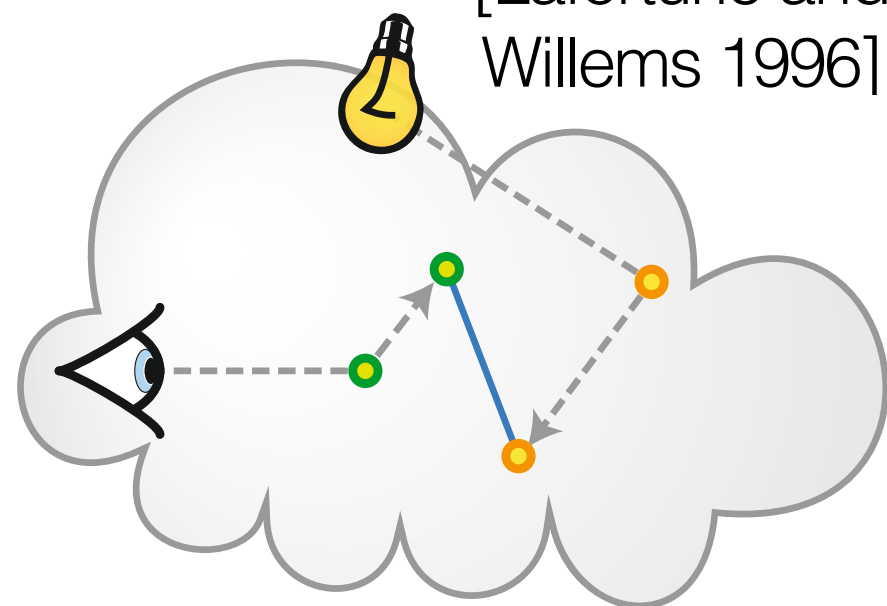
[Jarosz et al. 2008]



requires a lot of photons

Bidirectional Path Tracing

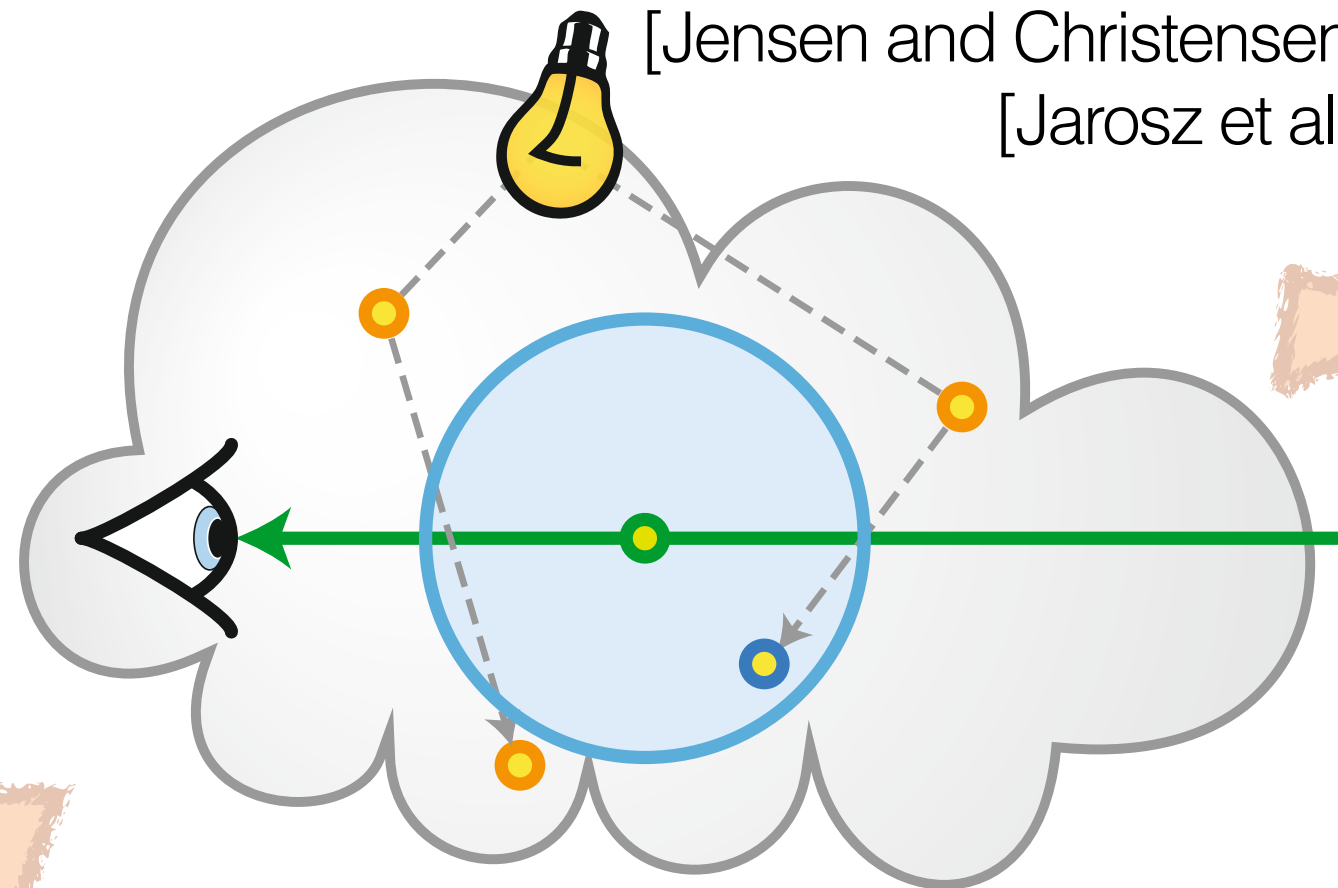
[Lafortune and Willem's 1996]



Previous work

Volumetric Photon Mapping

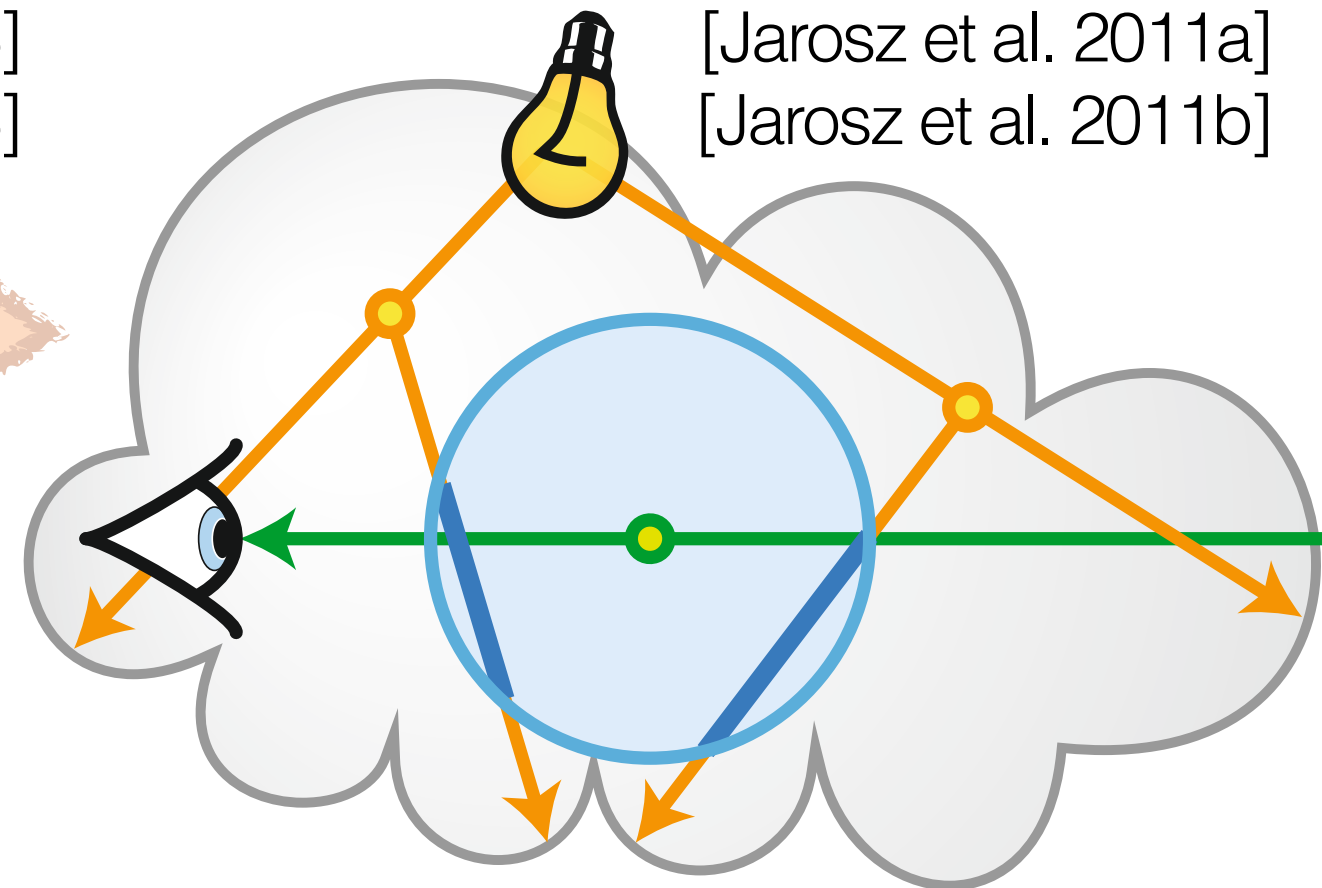
[Jensen and Christensen 1998]
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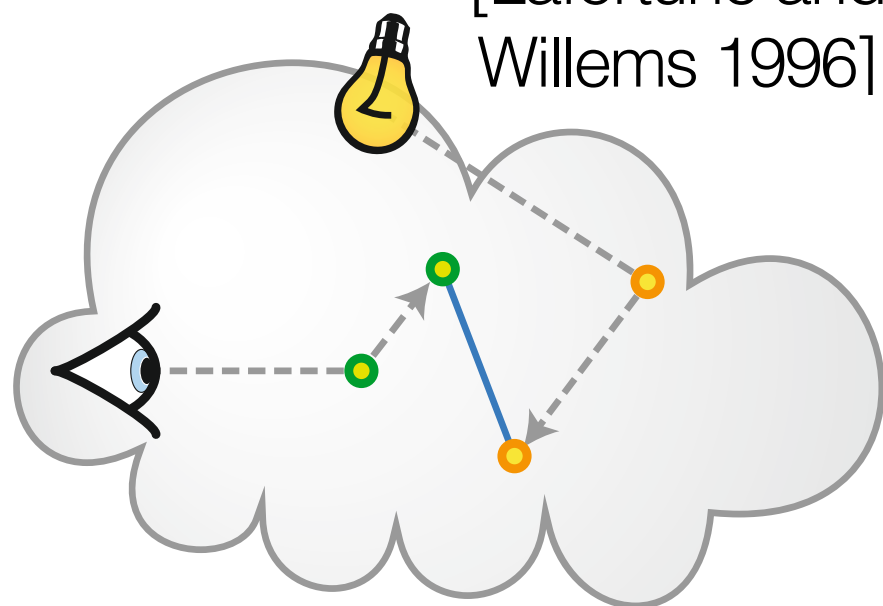
Photon Beams

[Jarosz et al. 2011a]
[Jarosz et al. 2011b]



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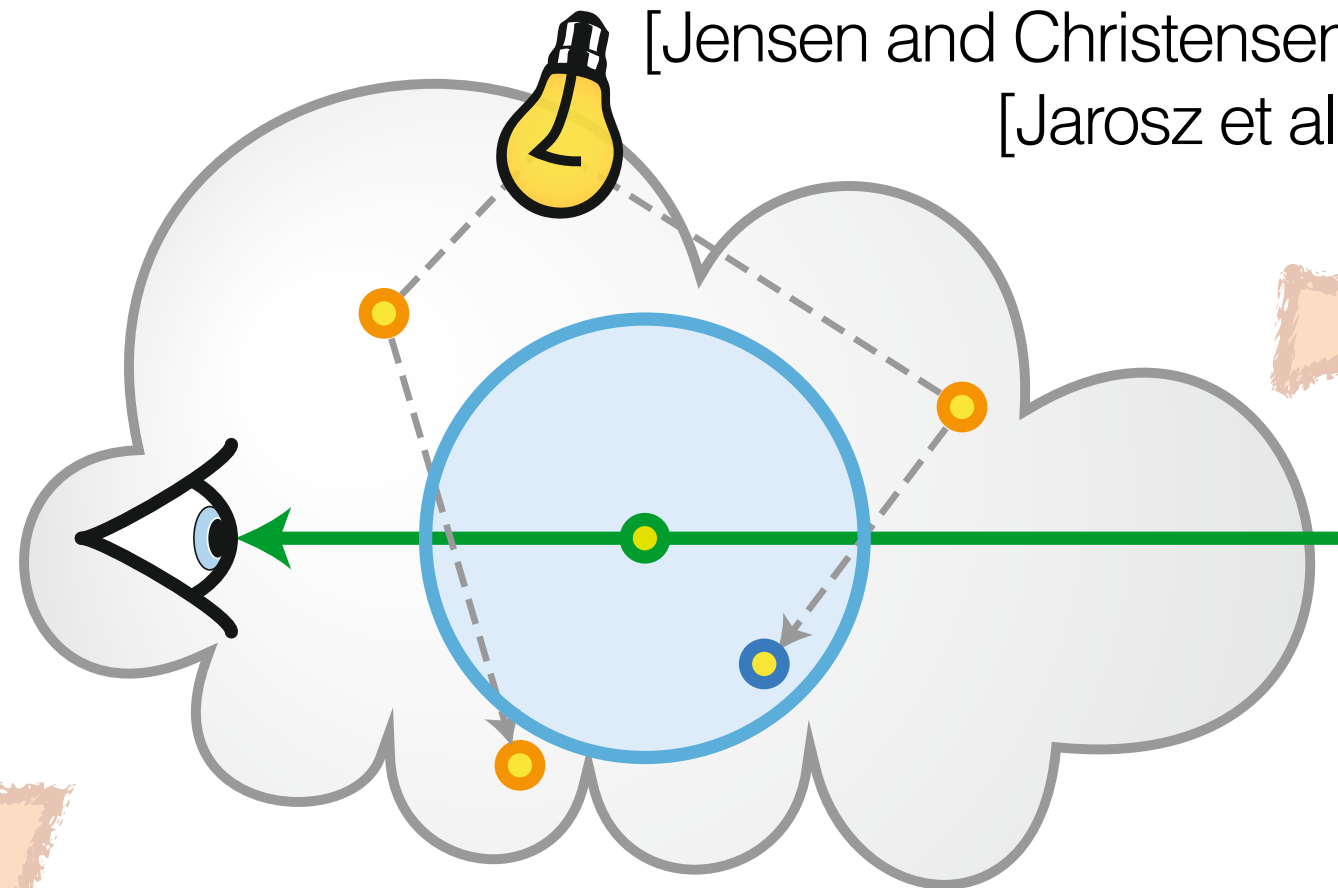
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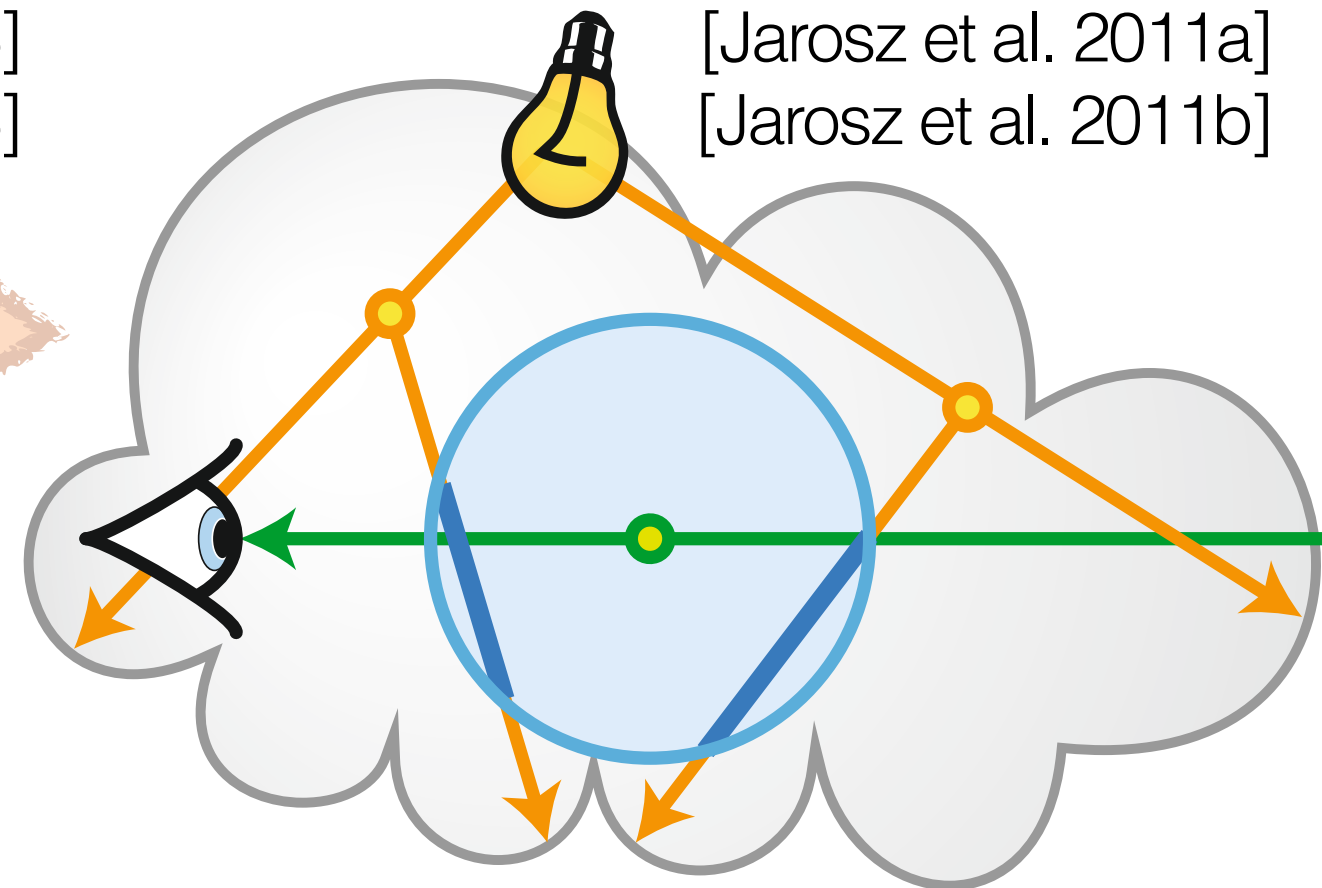
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Photon Beams

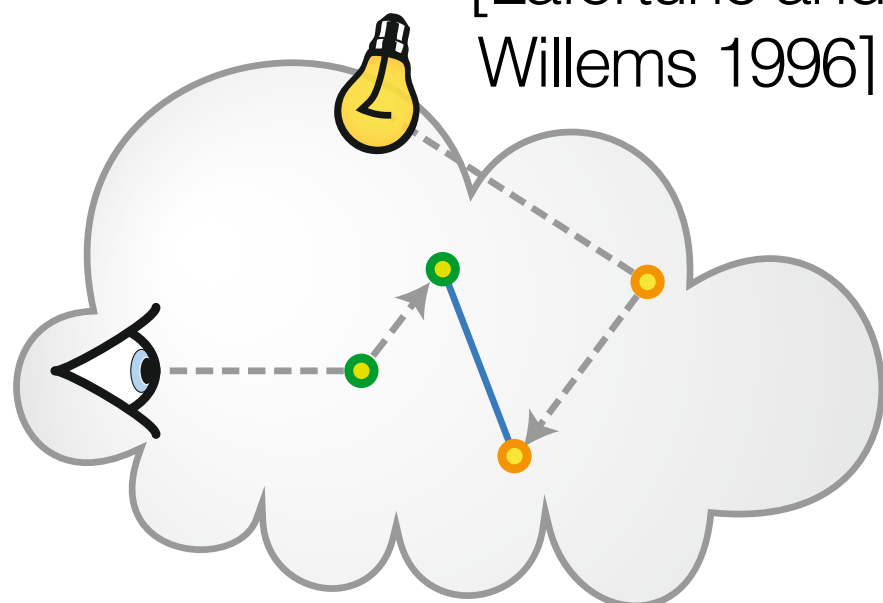
[Jarosz et al. 2011a]
[Jarosz et al. 2011b]



**great caustics,
MS not so...**

Bidirectional Path Tracing

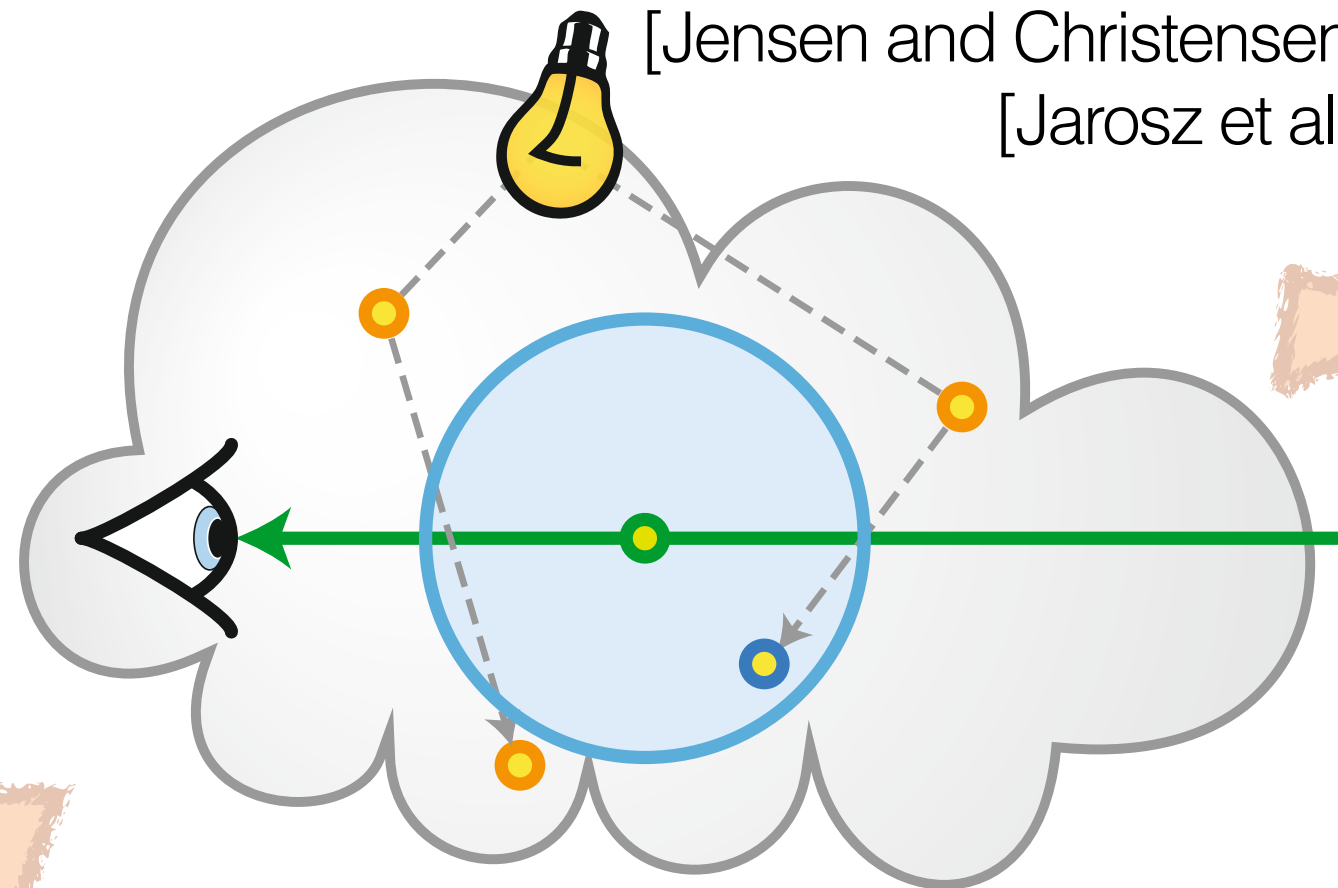
[Lafortune and
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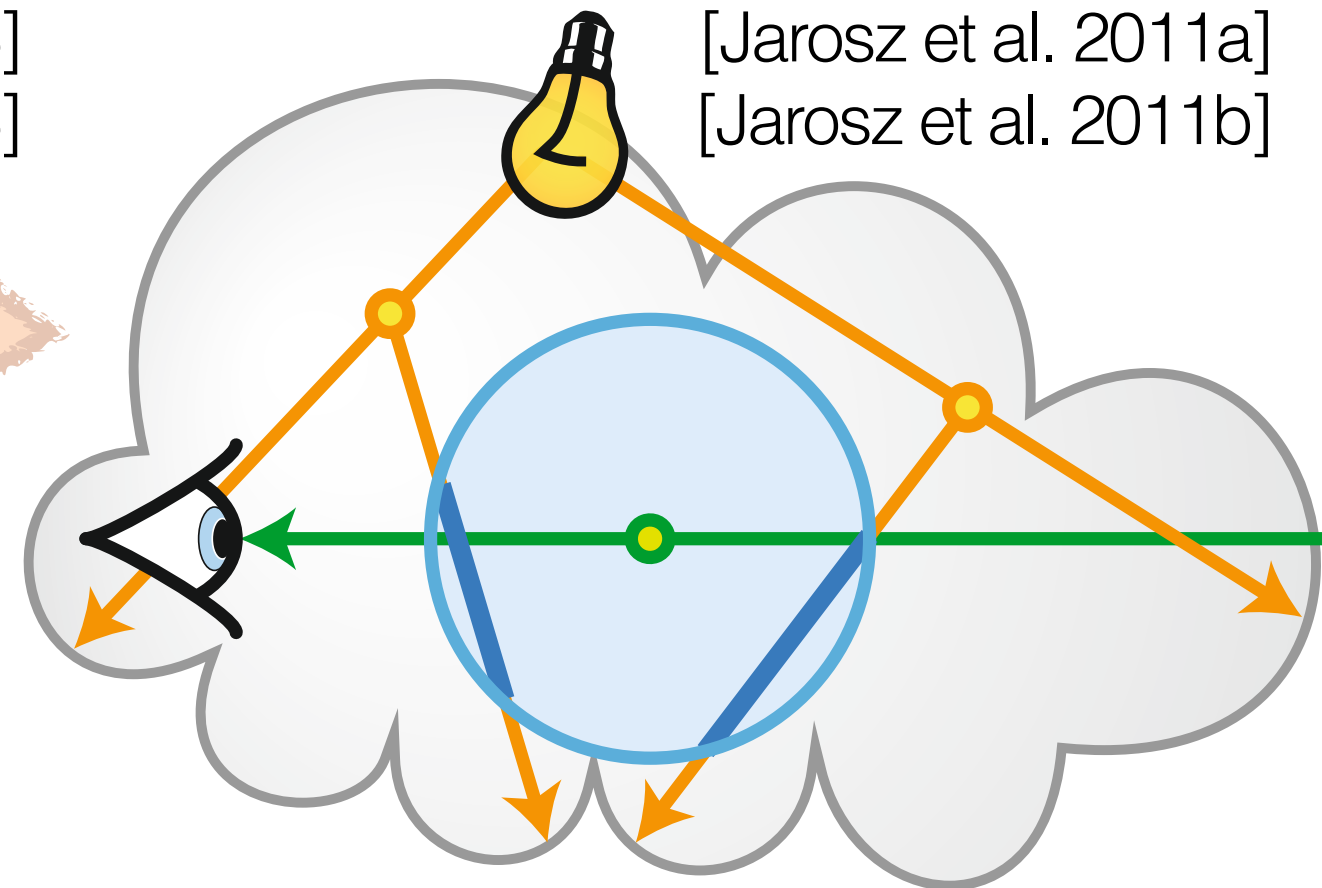
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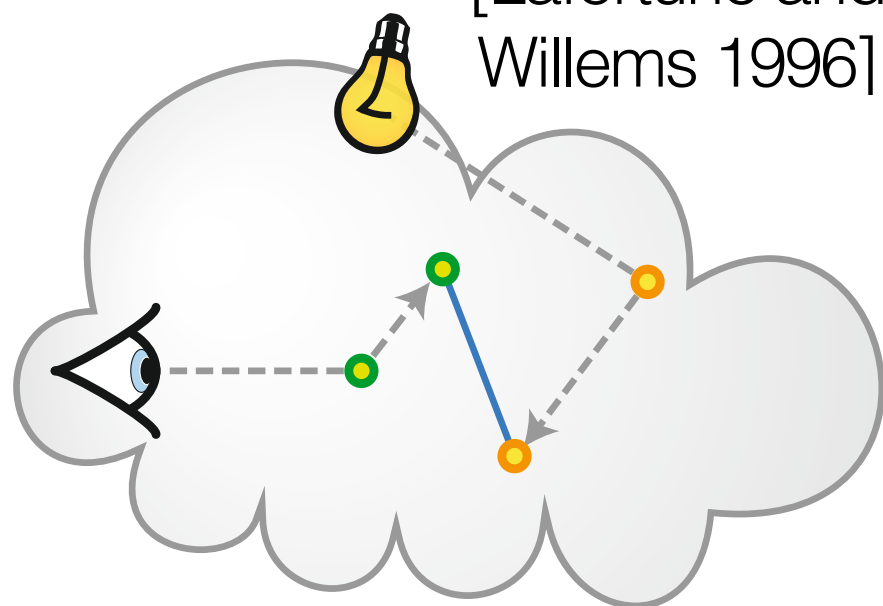
[Jarosz et al. 2011a]
[Jarosz et al. 2011b]



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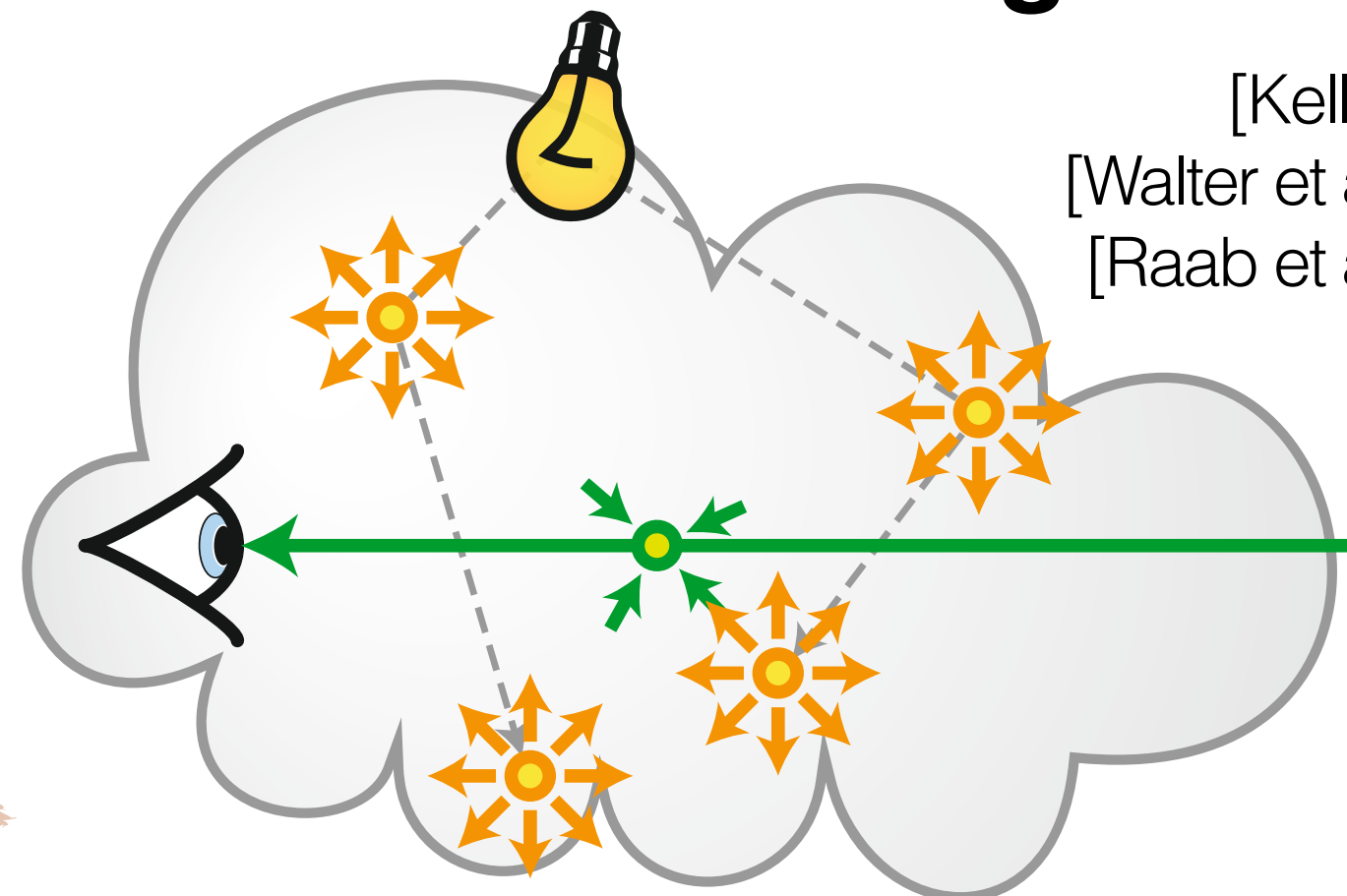
Bidirectional Path Tracing

[Lafortune and
Willem's 1996]



Virtual Point Lights

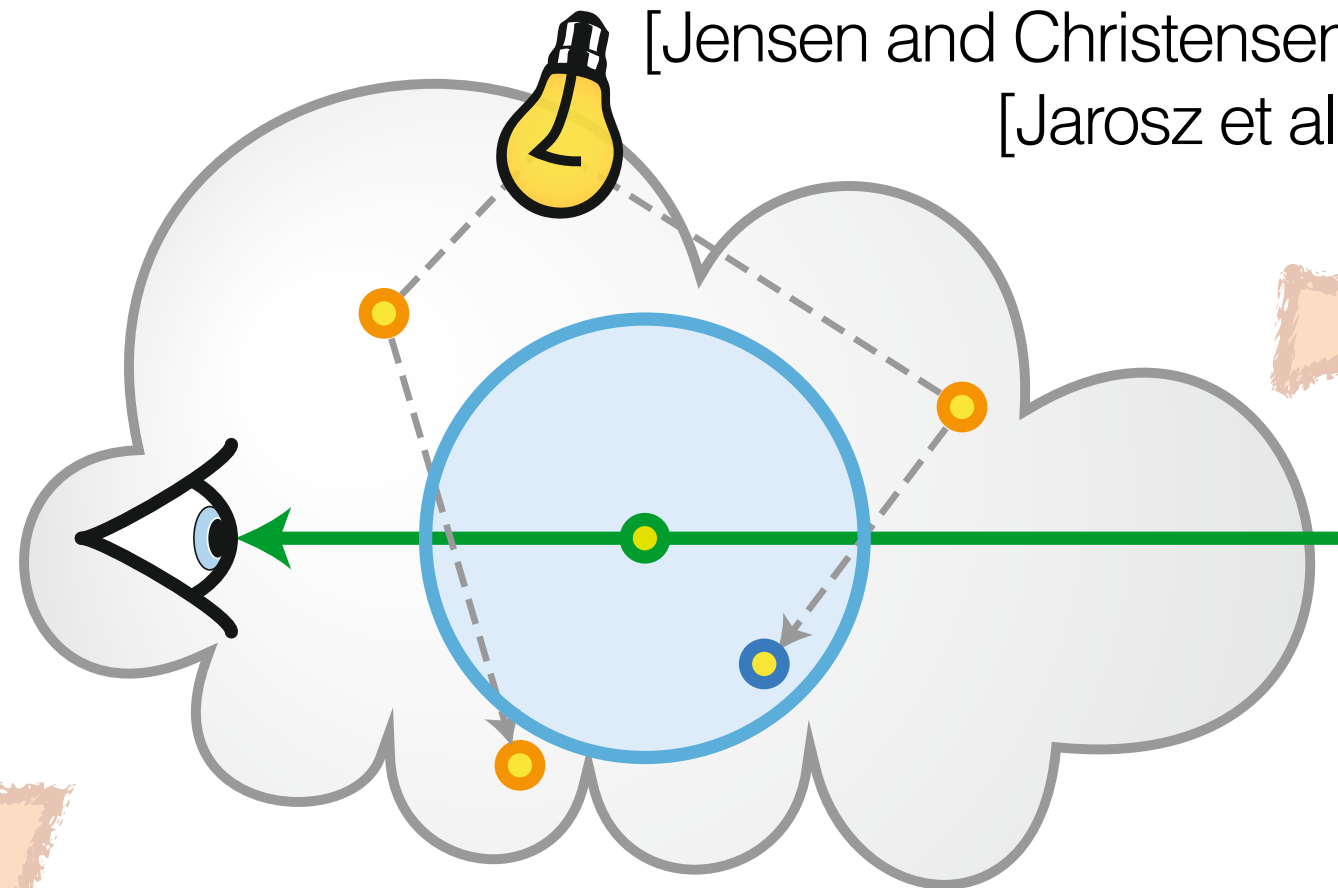
[Keller 1997]
[Walter et al. 2005]
[Raab et al. 2008]



Previous work

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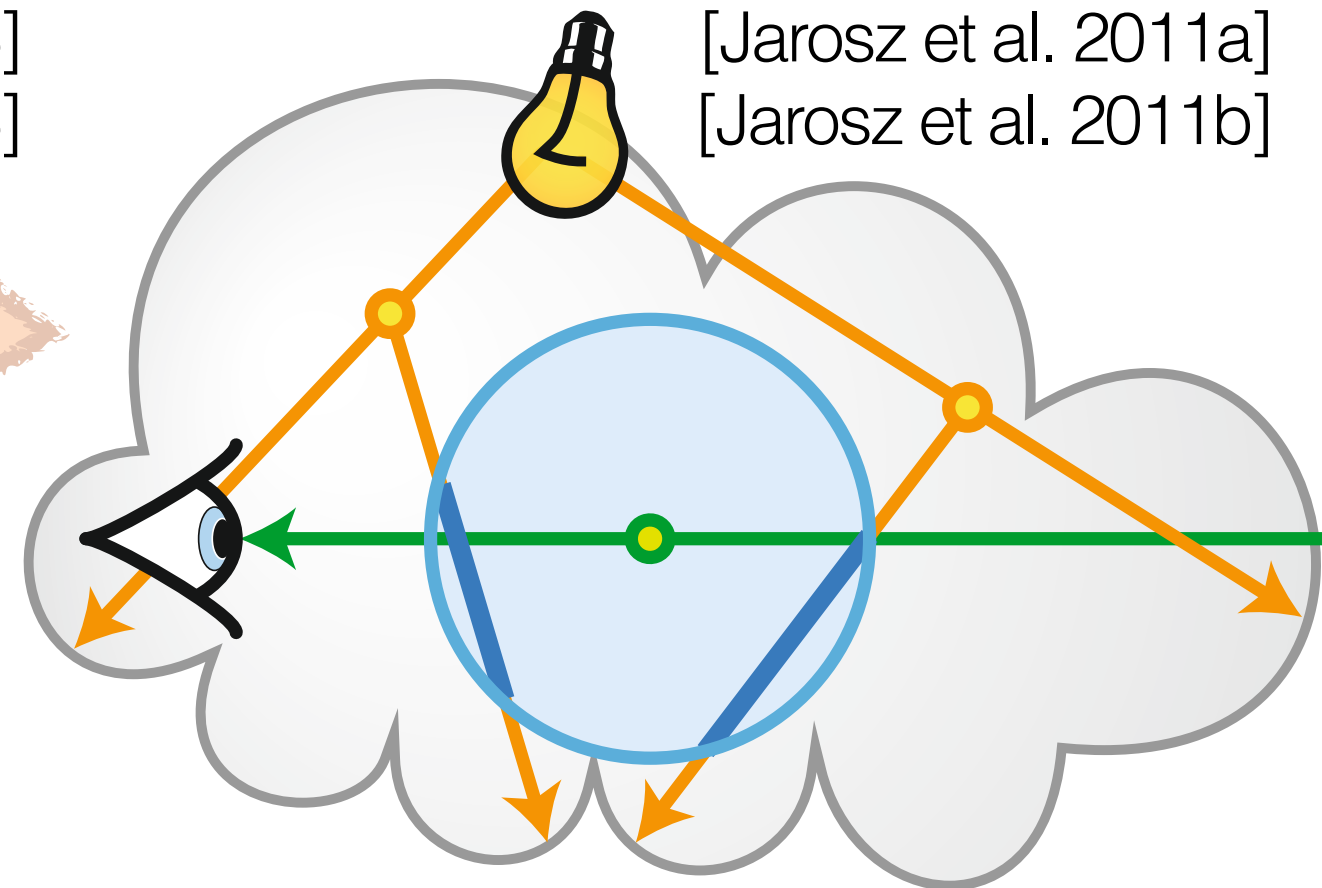
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Photon Beams

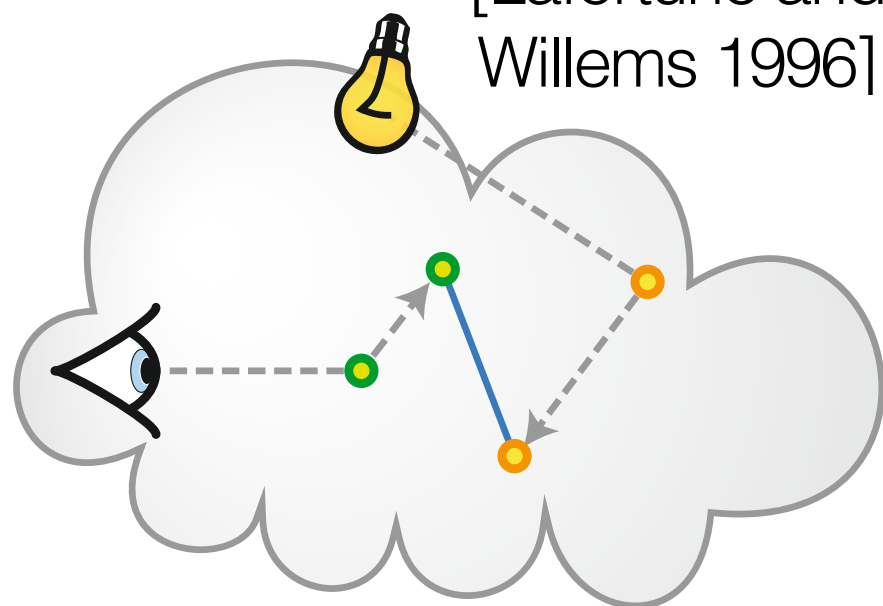
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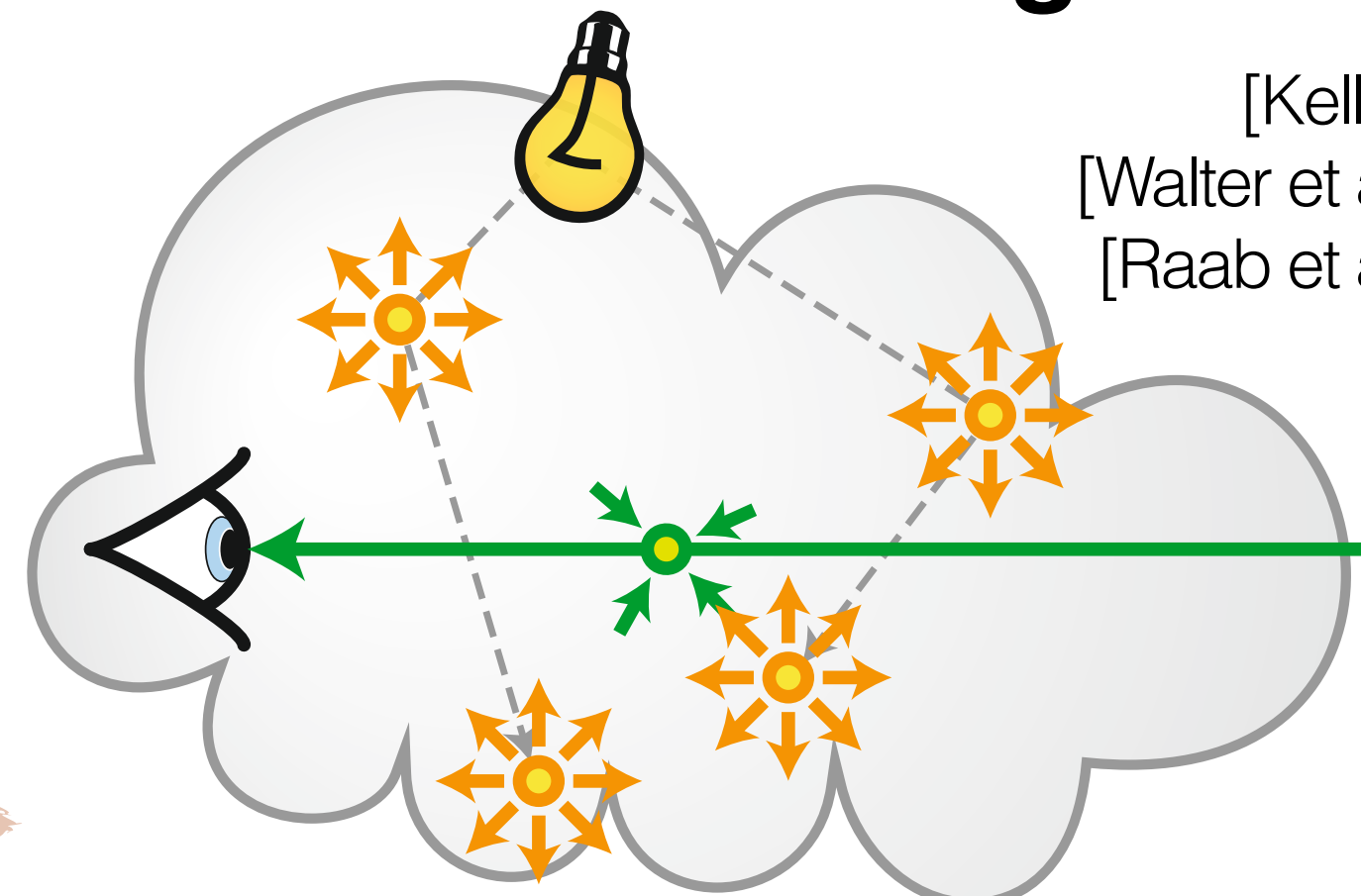
Bidirectional Path Tracing

[Lafortune and
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[Keller 1997]
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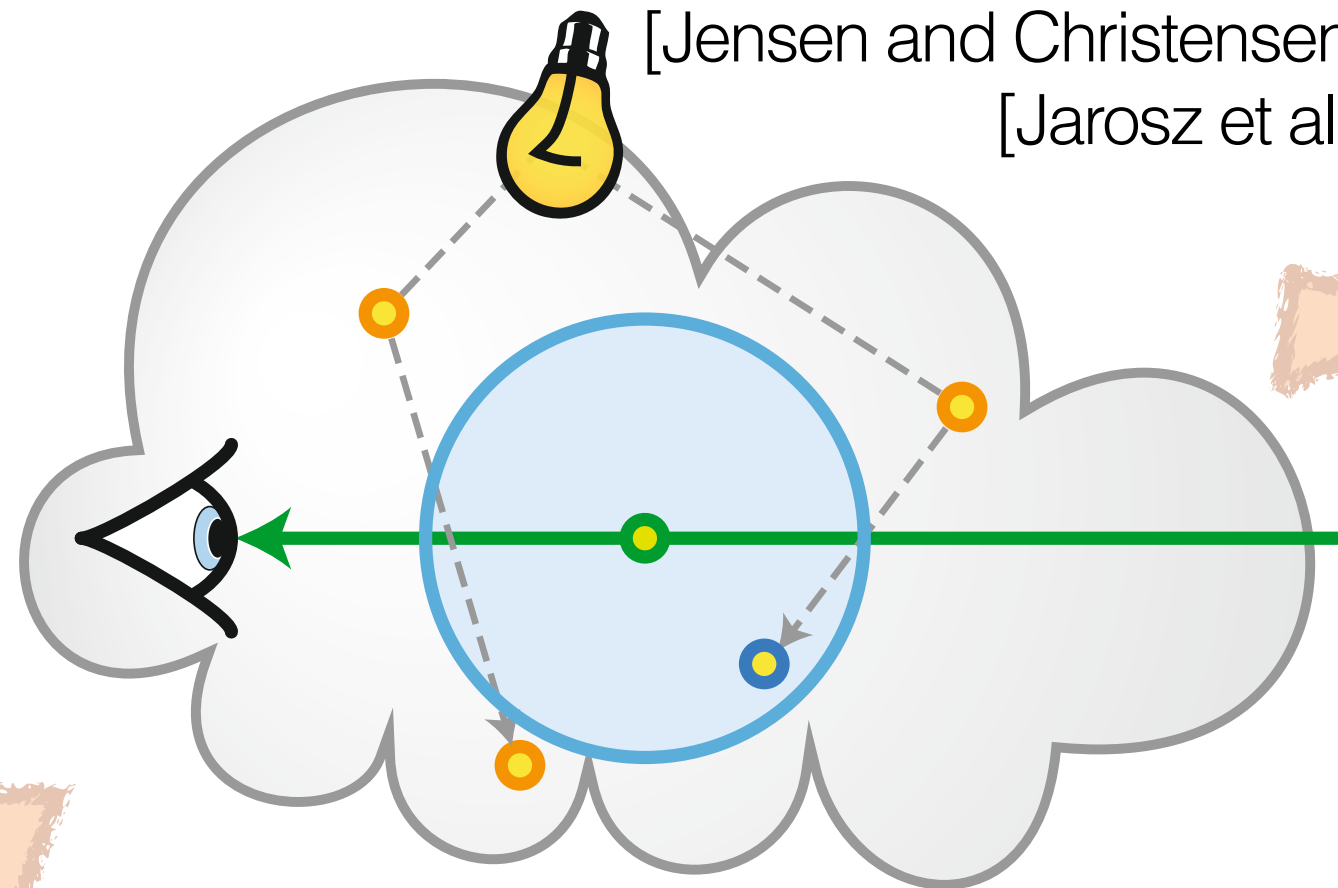


suffers from singularities

Previous work

Volumetric Photon Mapping

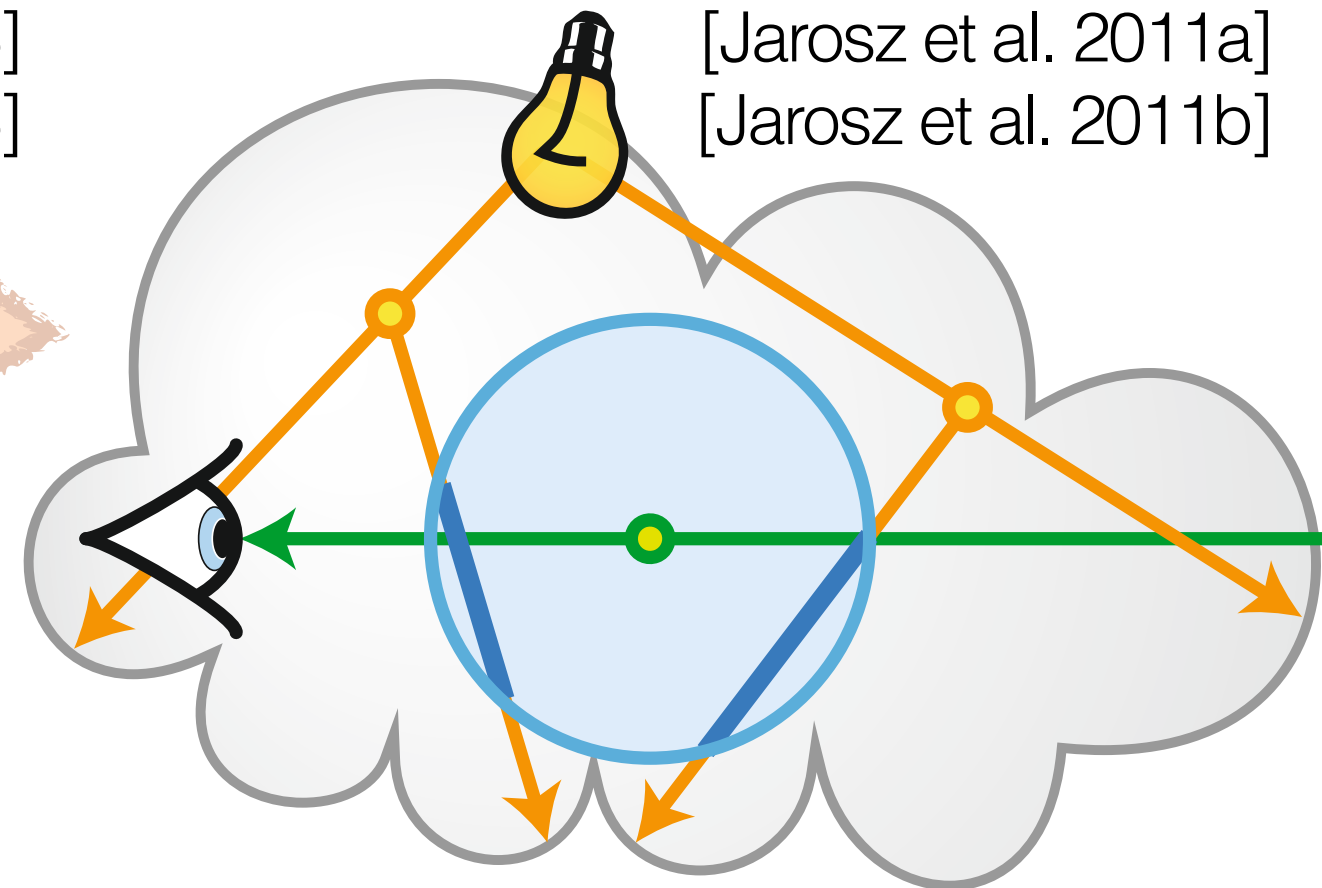
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Photon Beams

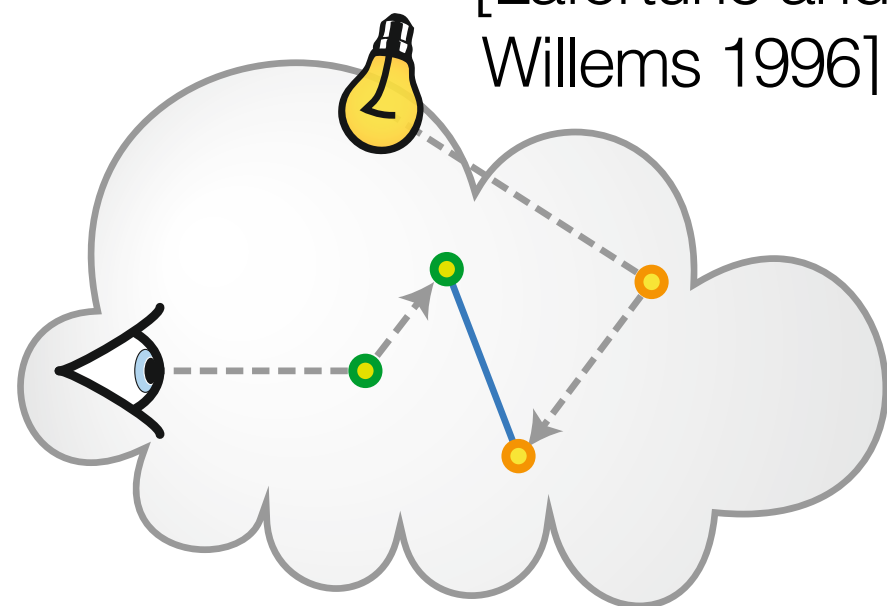
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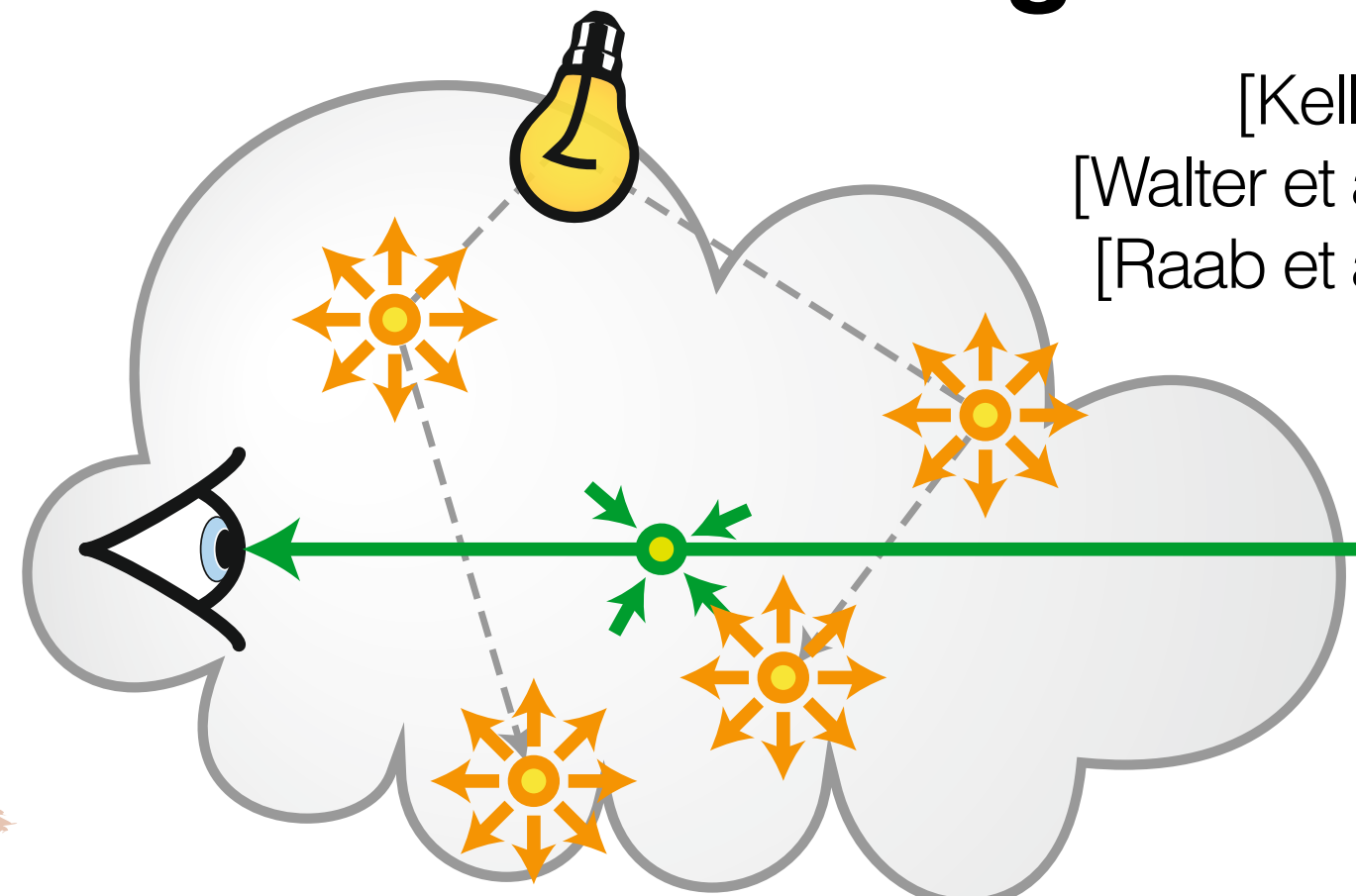
Bidirectional Path Tracing

[Lafortune and Willems 1996]



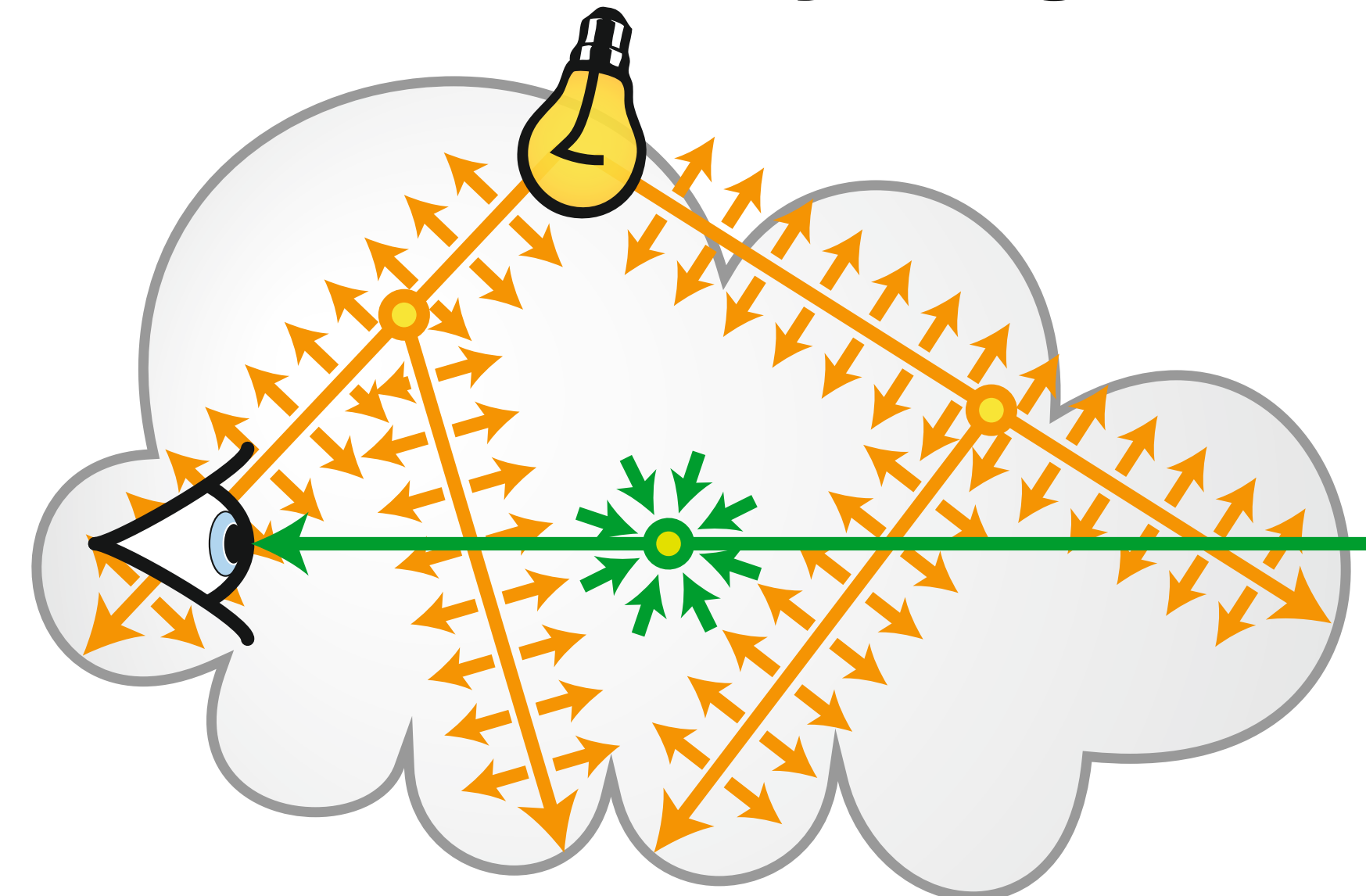
Virtual Point Lights

[Keller 1997]
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[Raab et al. 2008]



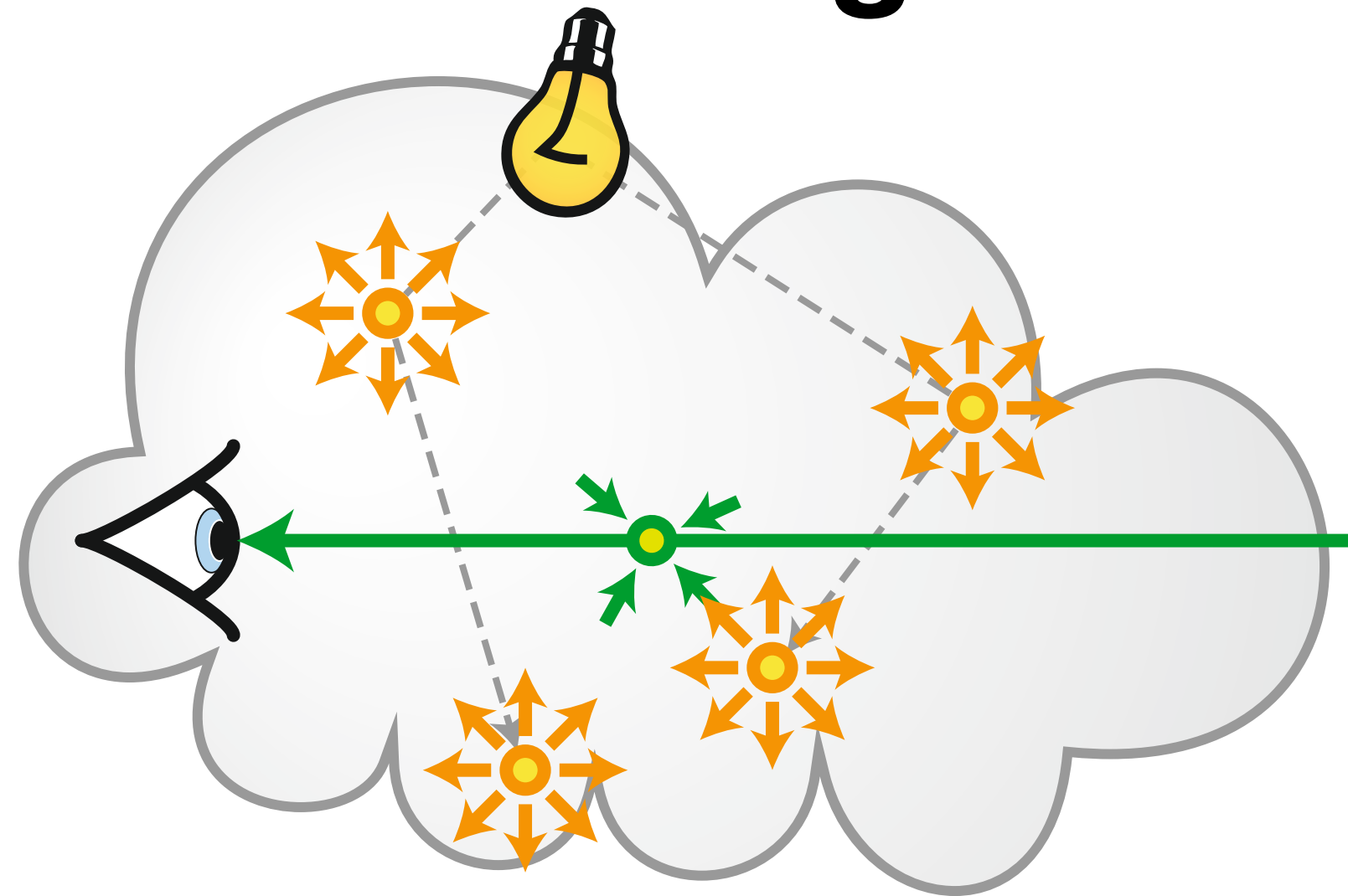
suffers from singularities

Virtual Ray Lights

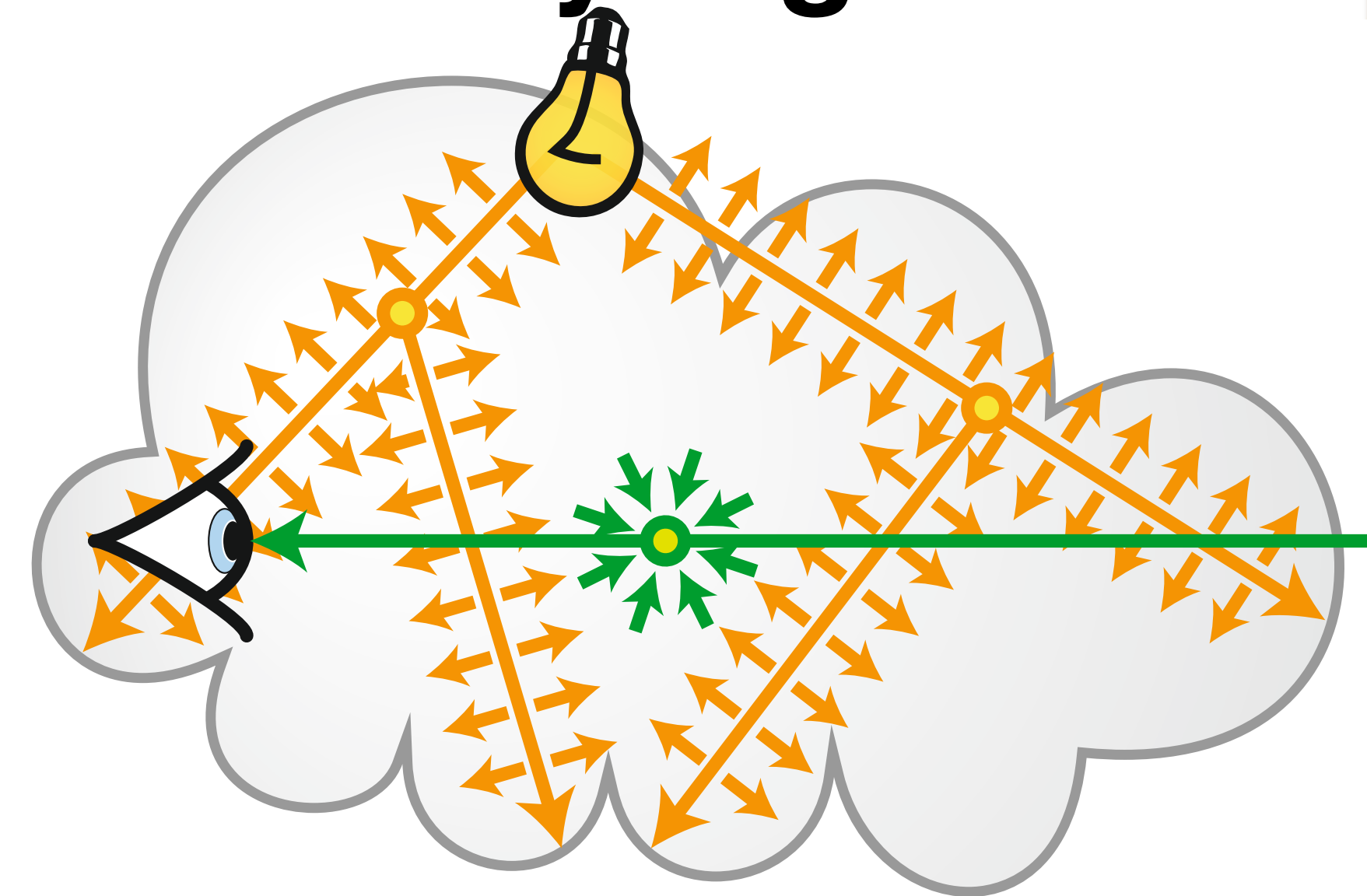


From points to rays

Point Lights

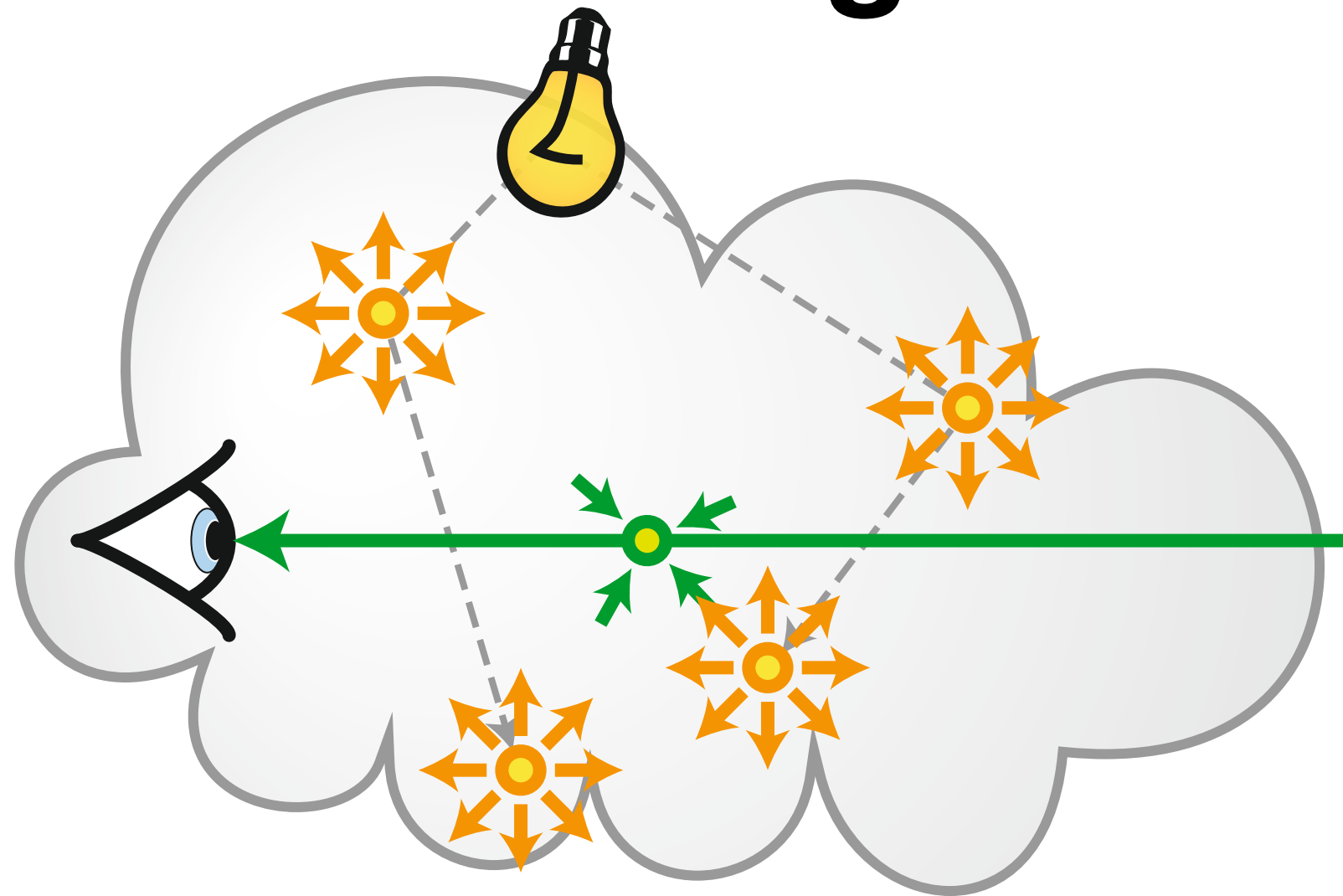


Ray Lights



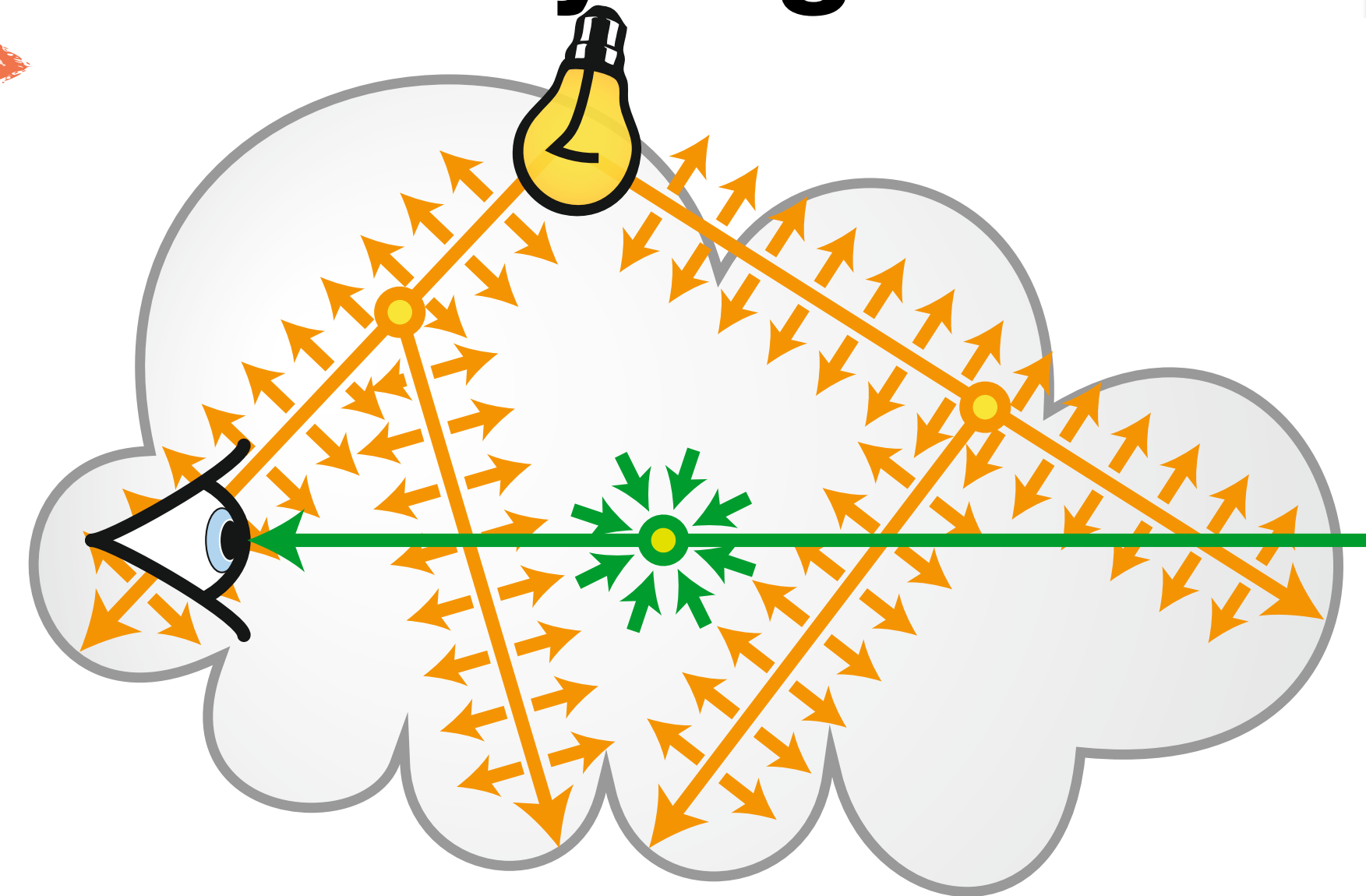
From points to rays

Point Lights



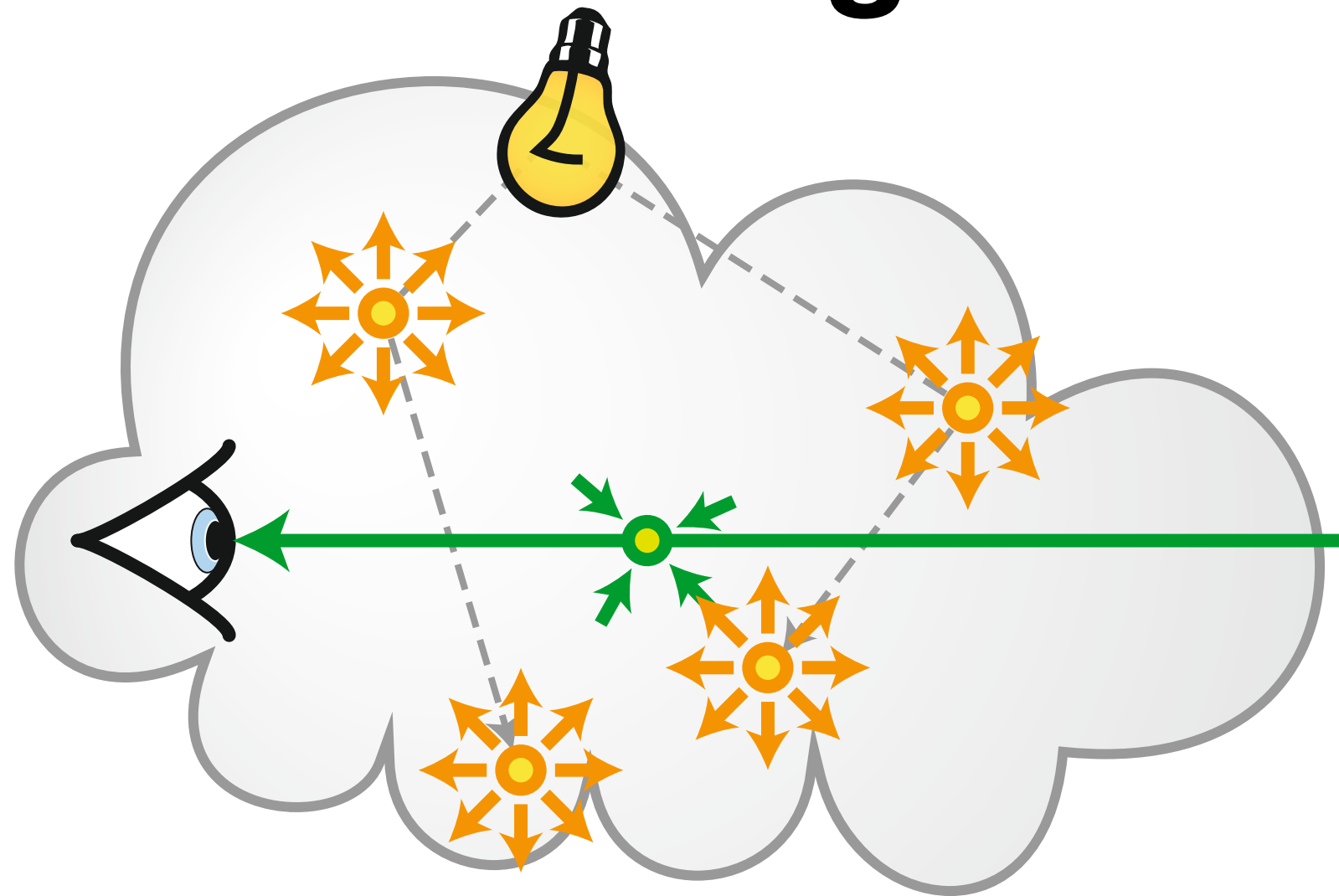
provably reduce
singularities

Ray Lights



From points to rays

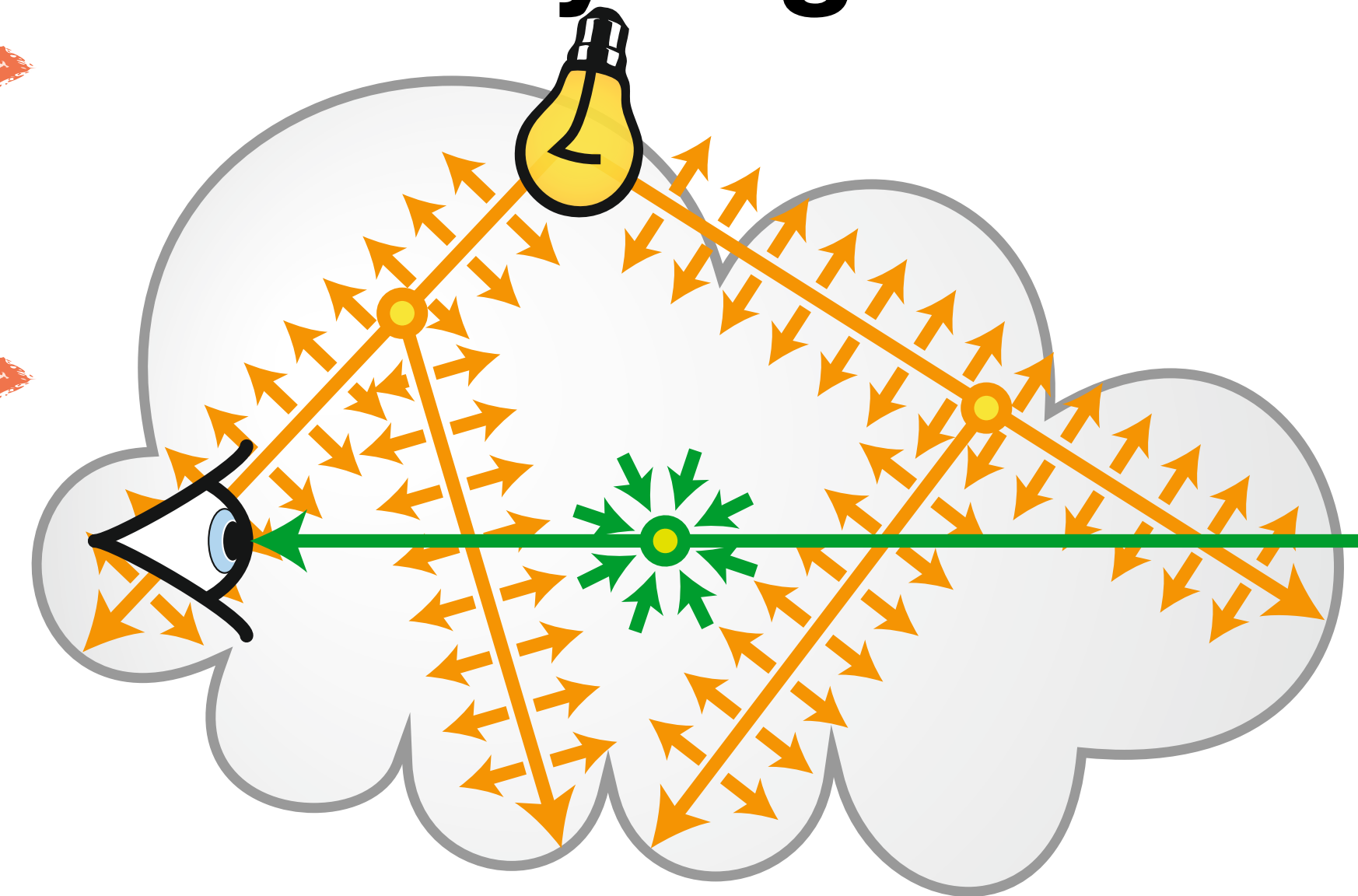
Point Lights



provably reduce
singularities

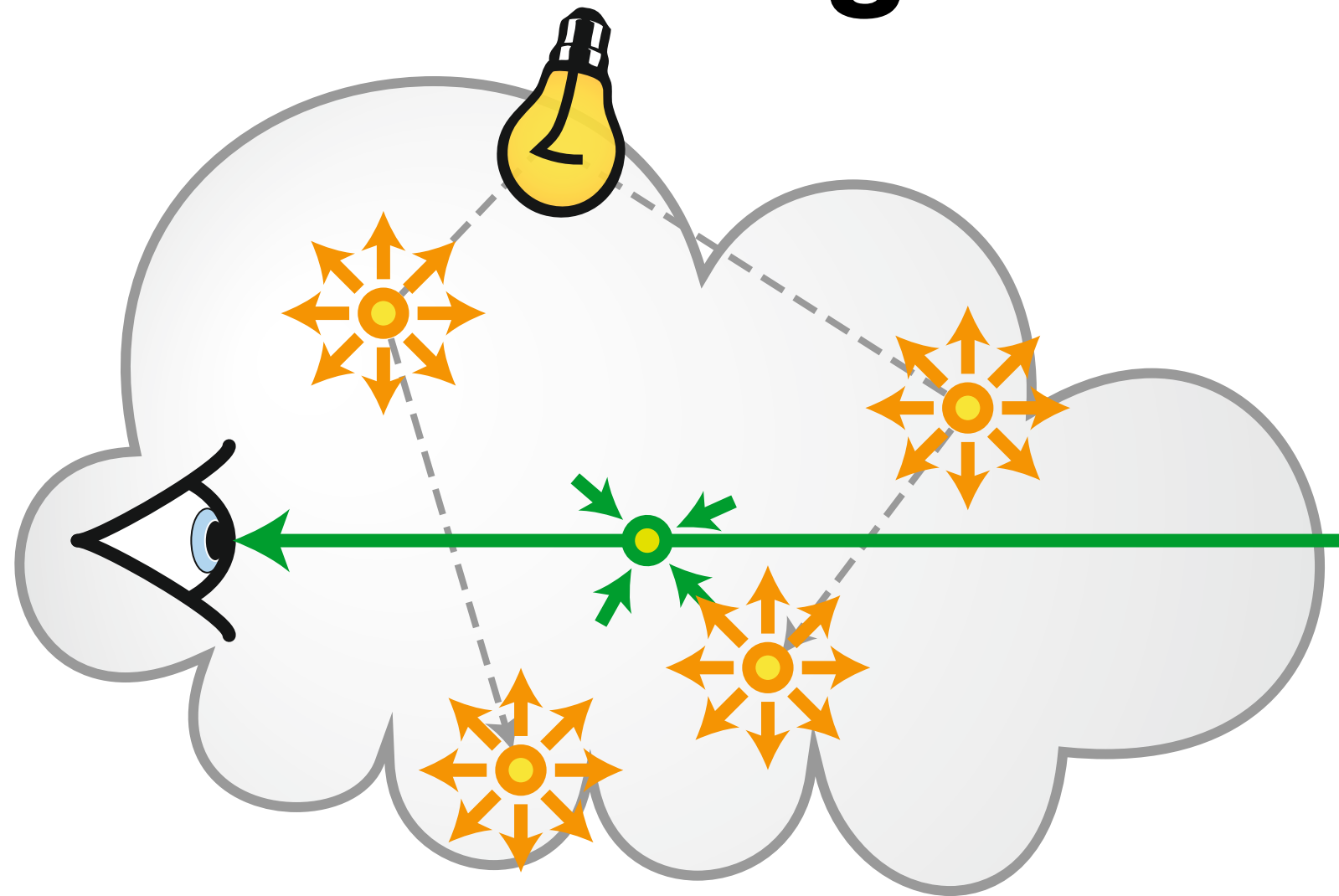
no need to clamp,
unbiased

Ray Lights



From points to rays

Point Lights

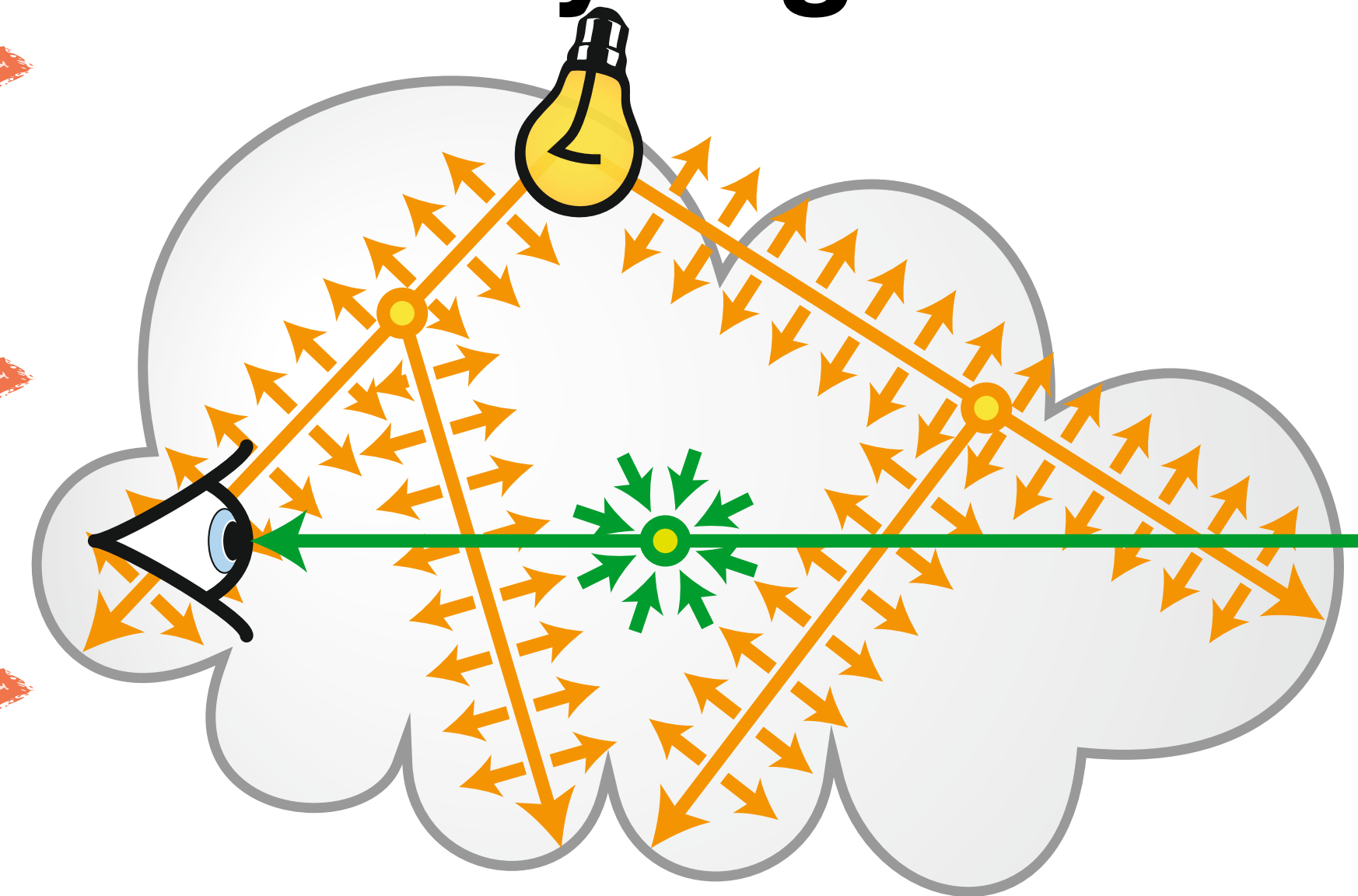


**provably reduce
singularities**

**no need to clamp,
unbiased**

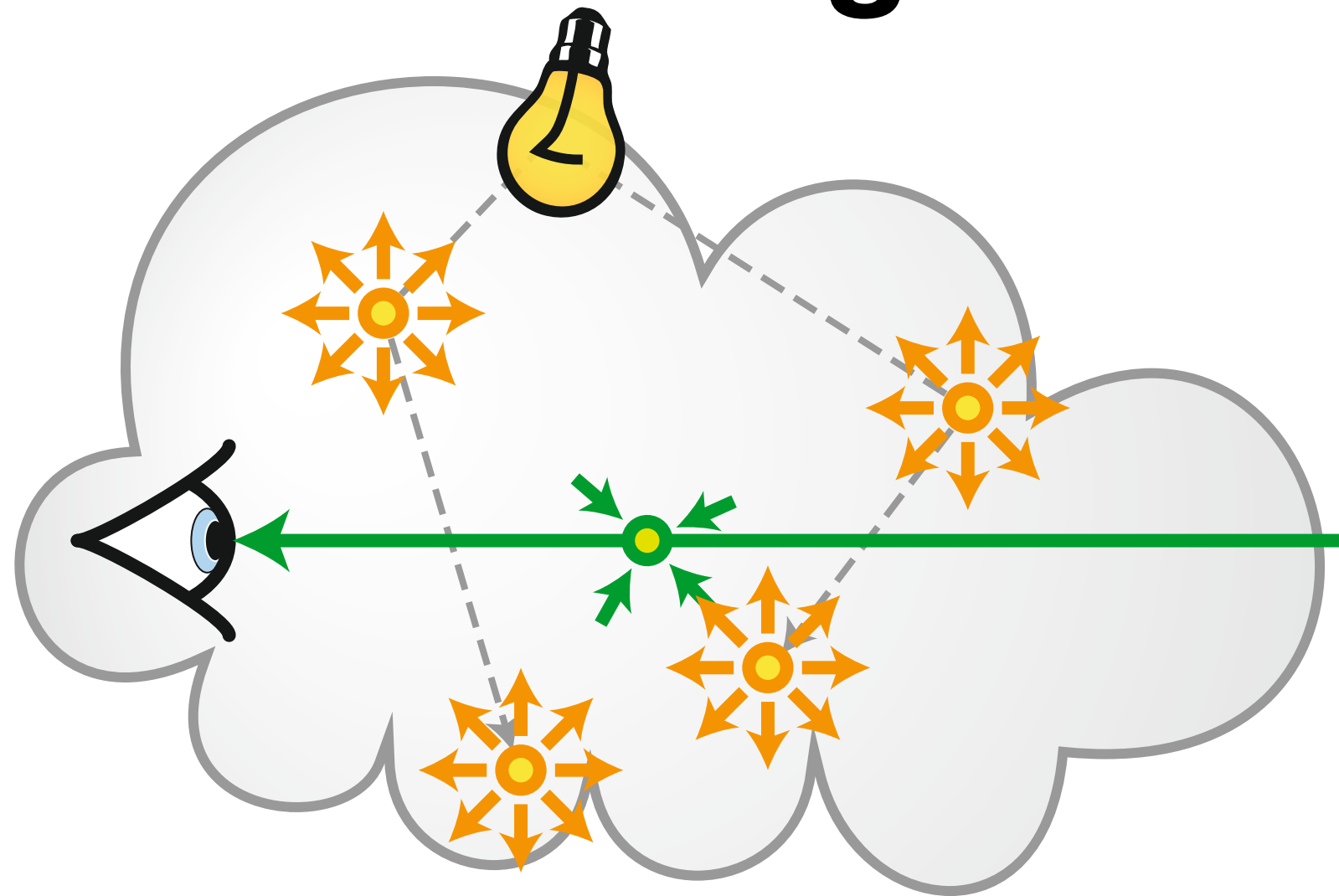
**increase sampling
of path space**

Ray Lights



From points to rays

Point Lights



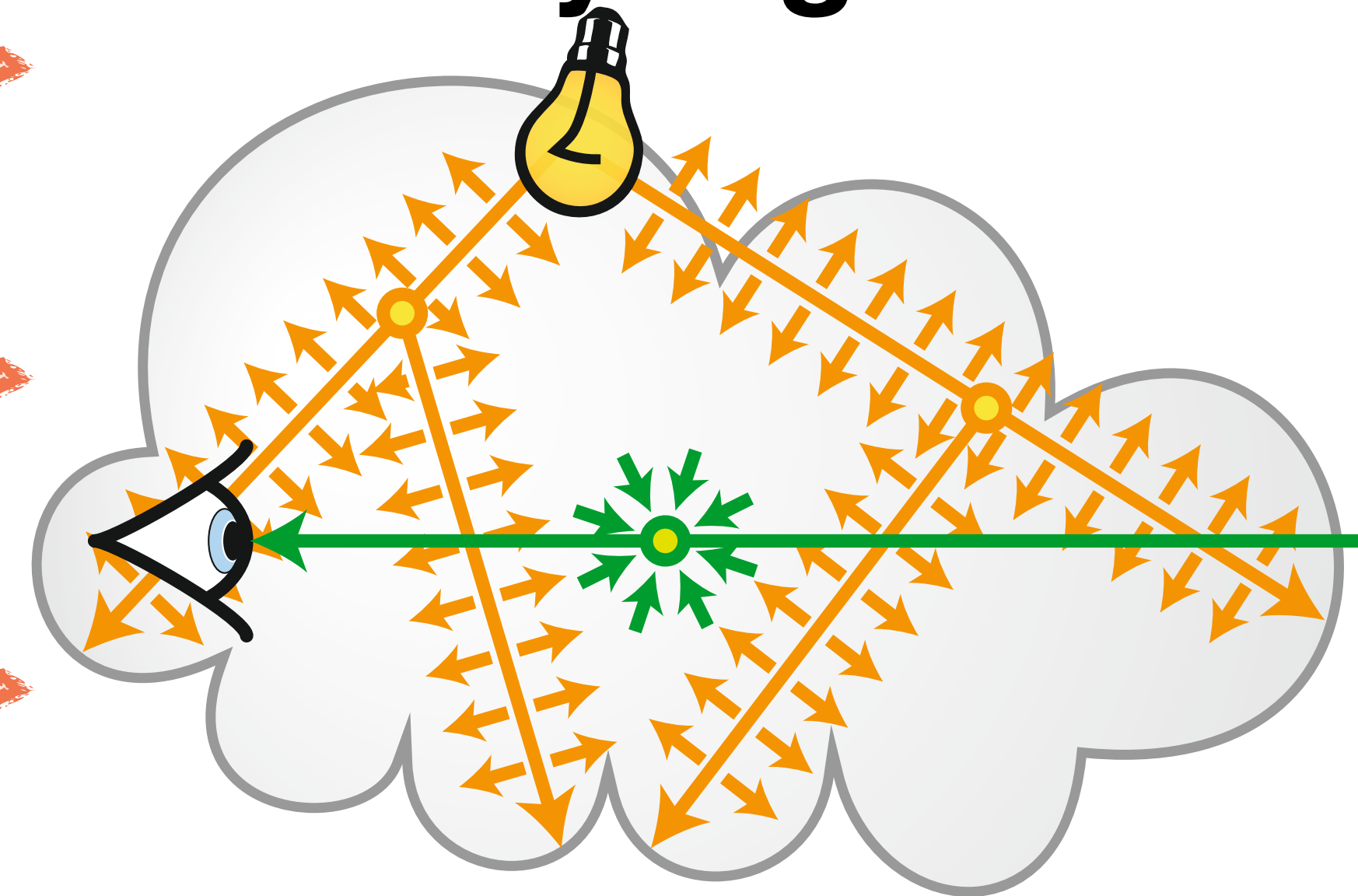
provably reduce singularities

no need to clamp, unbiased

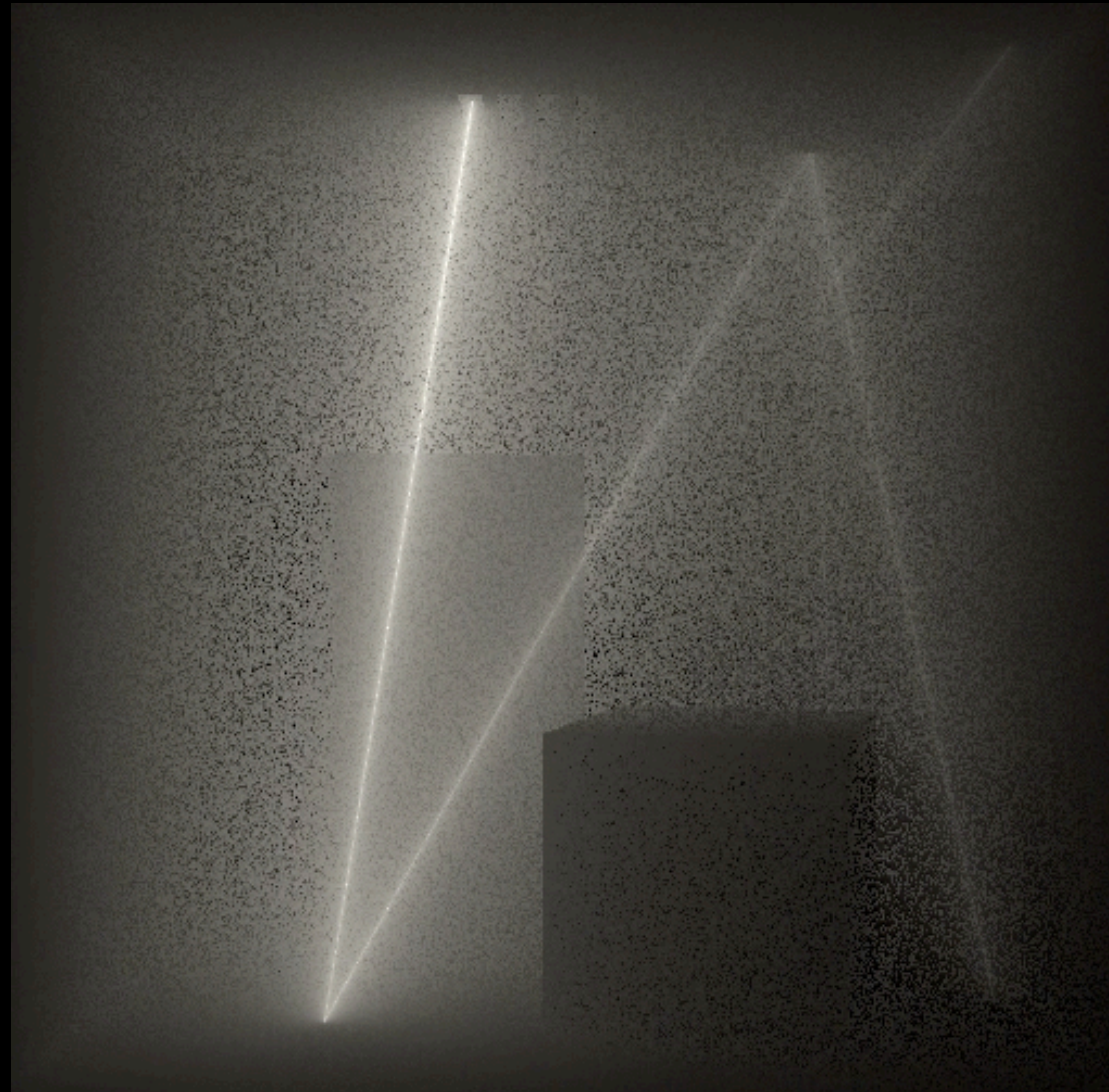
increase sampling of path space

handle anisotropic “glossy” media

Ray Lights

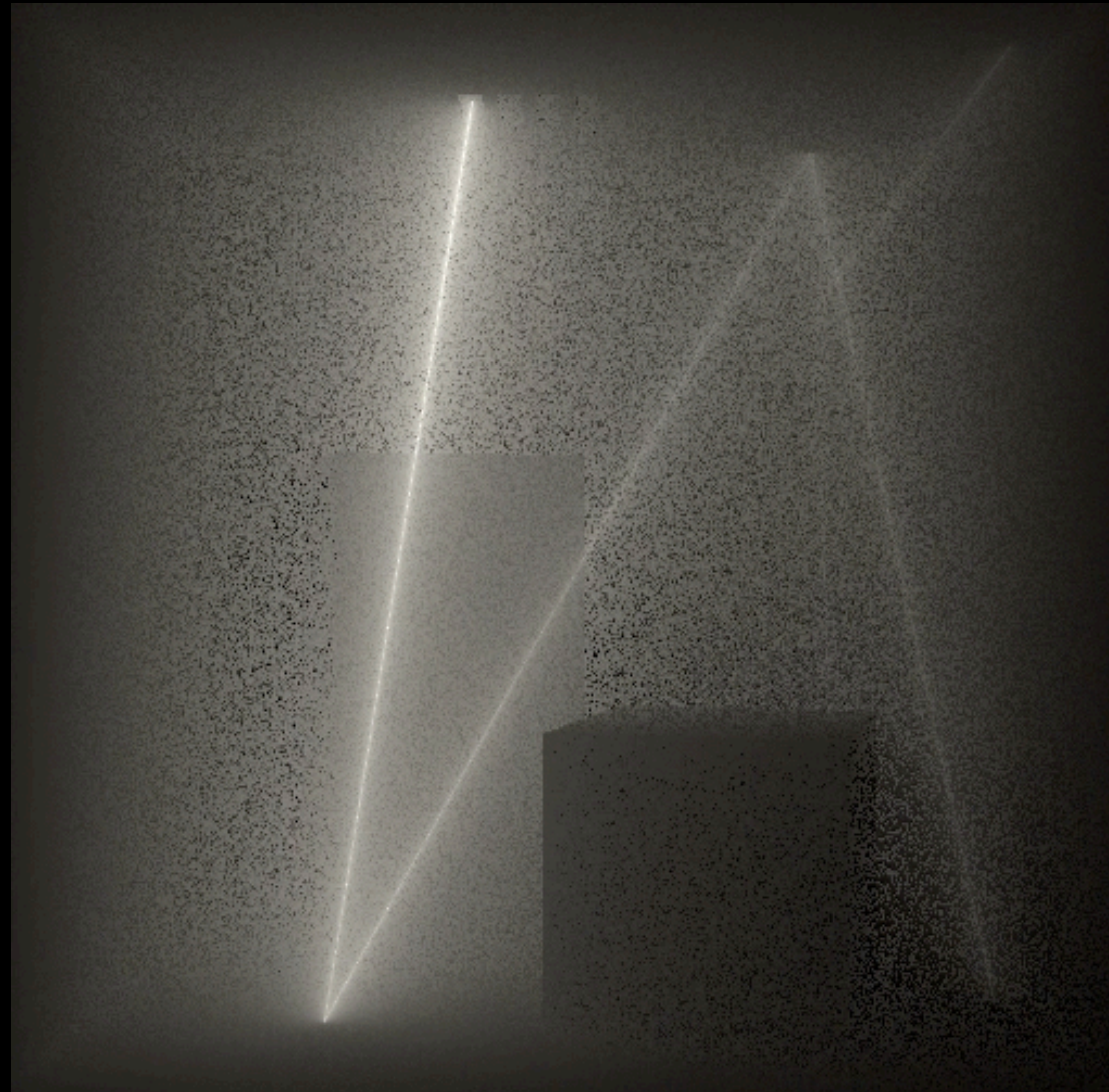


Quick demo



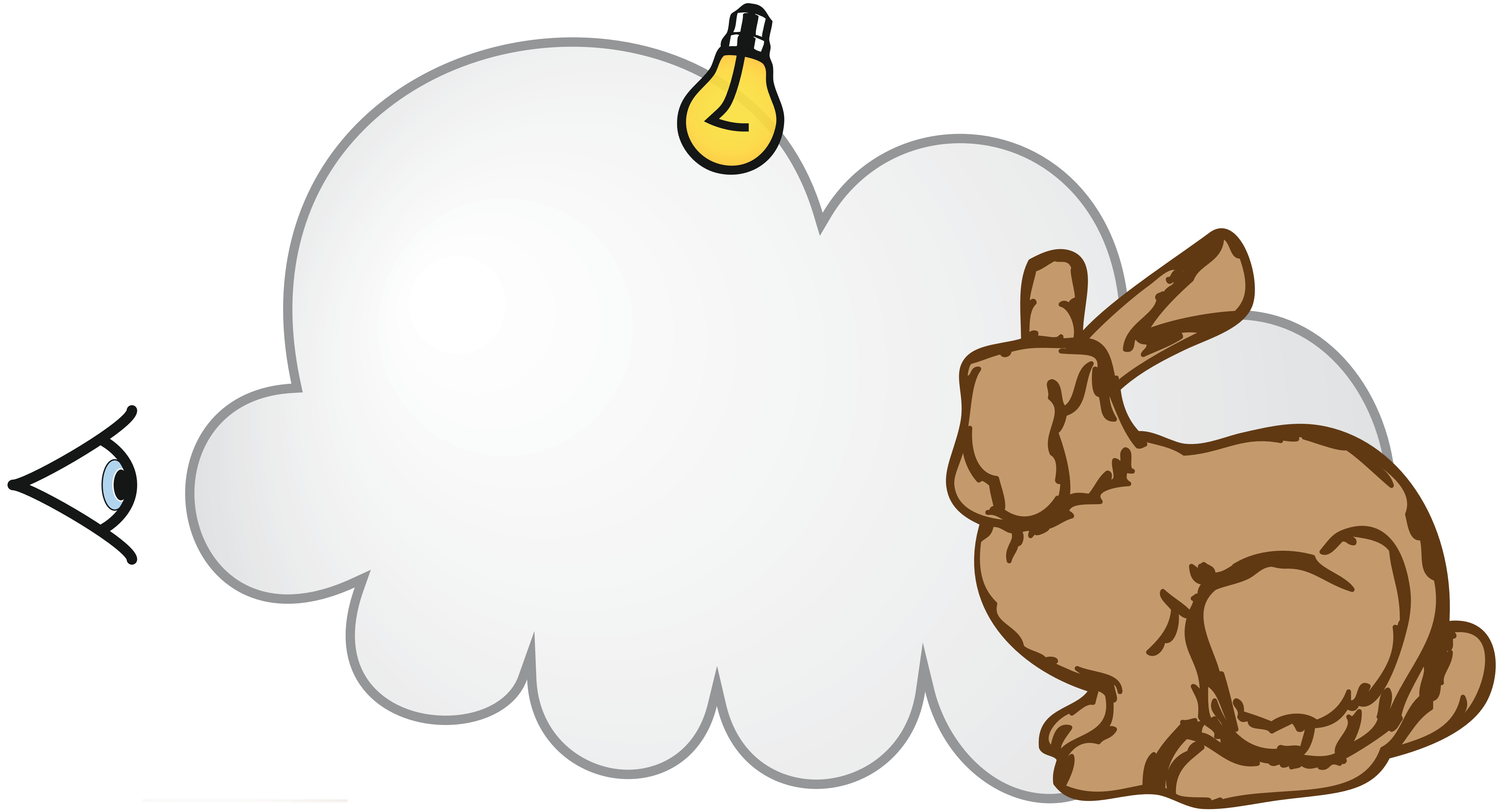
6 VRLs

Quick demo

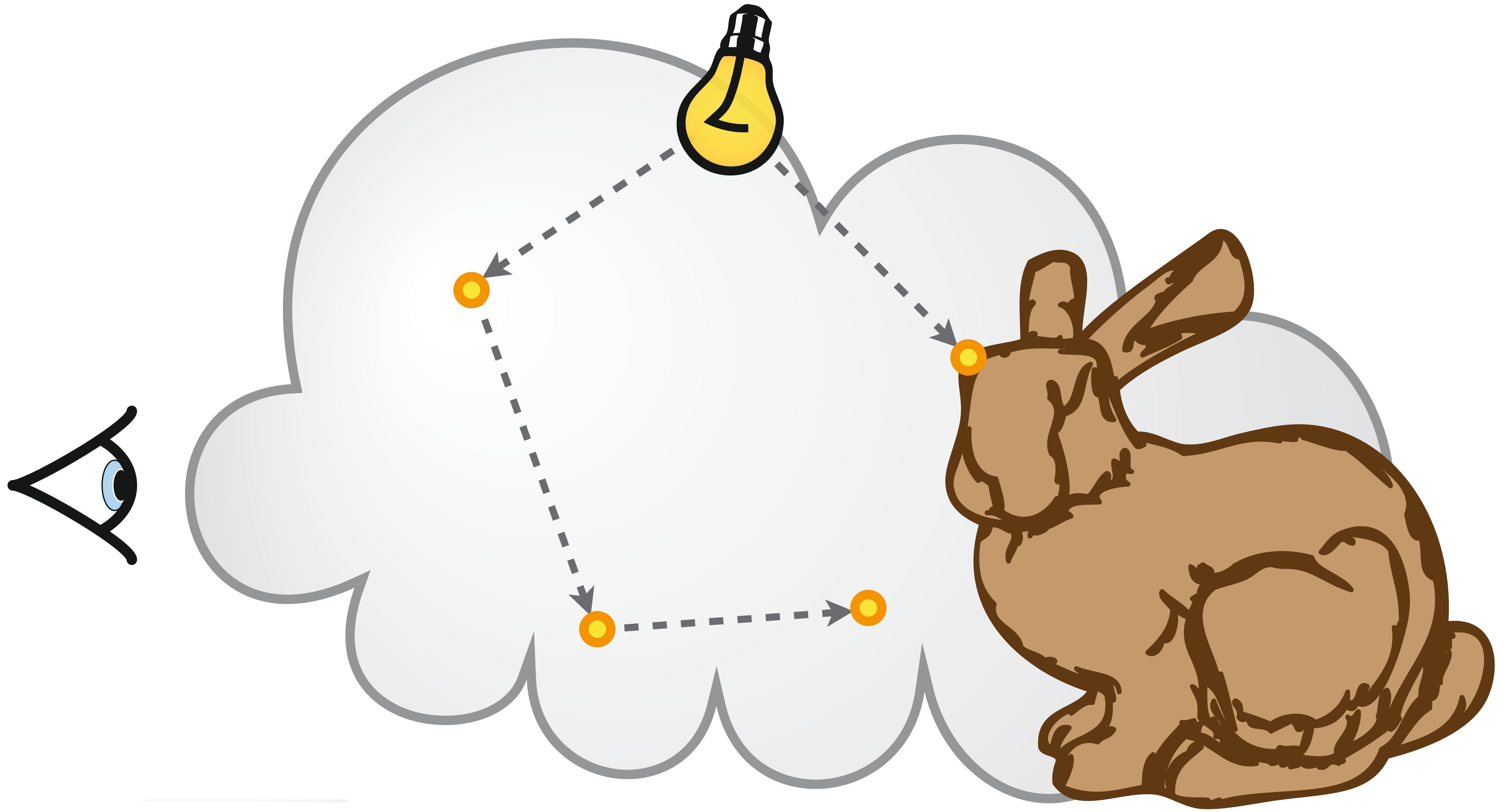


6 VRLs

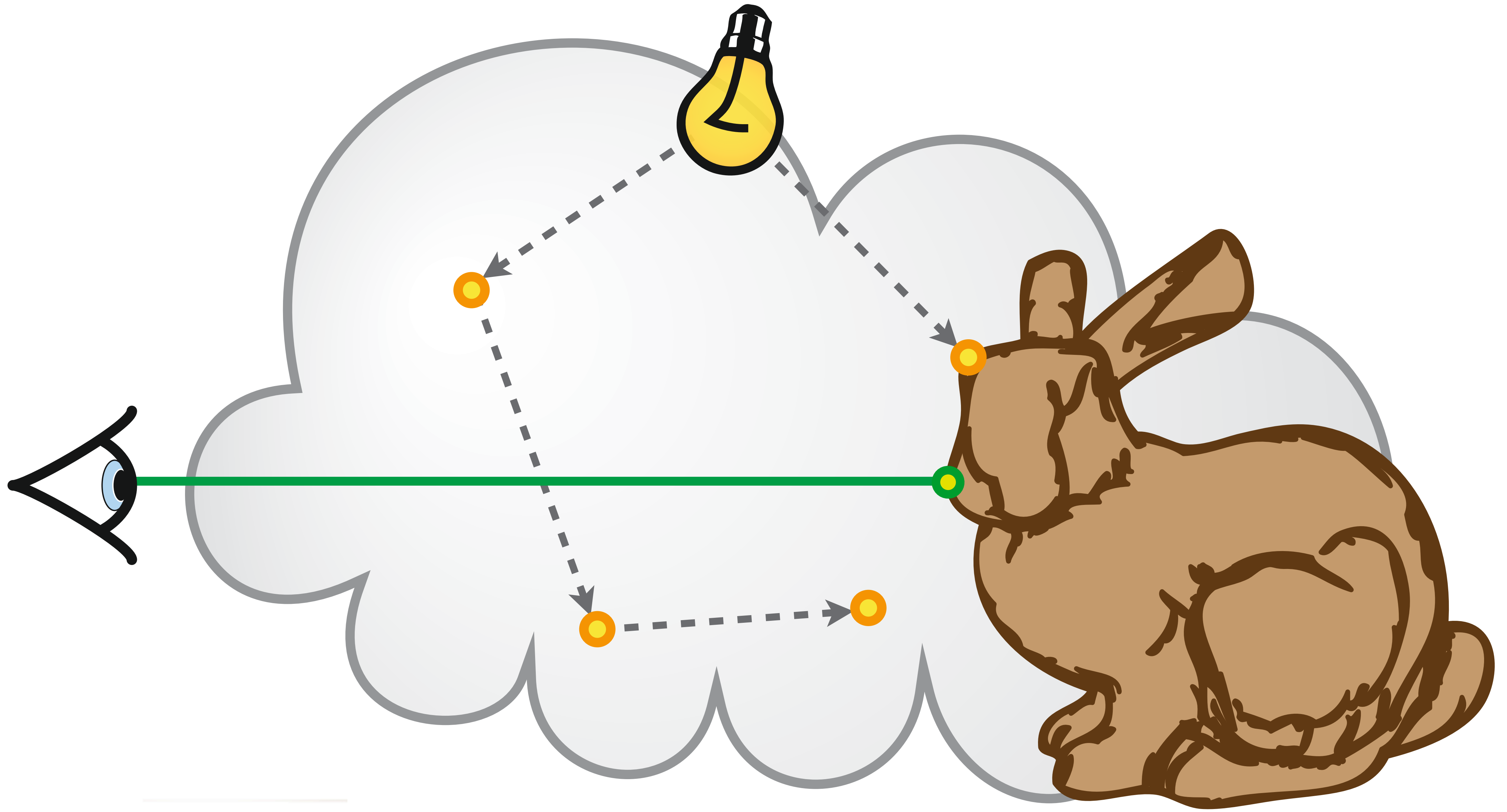
Algorithm overview



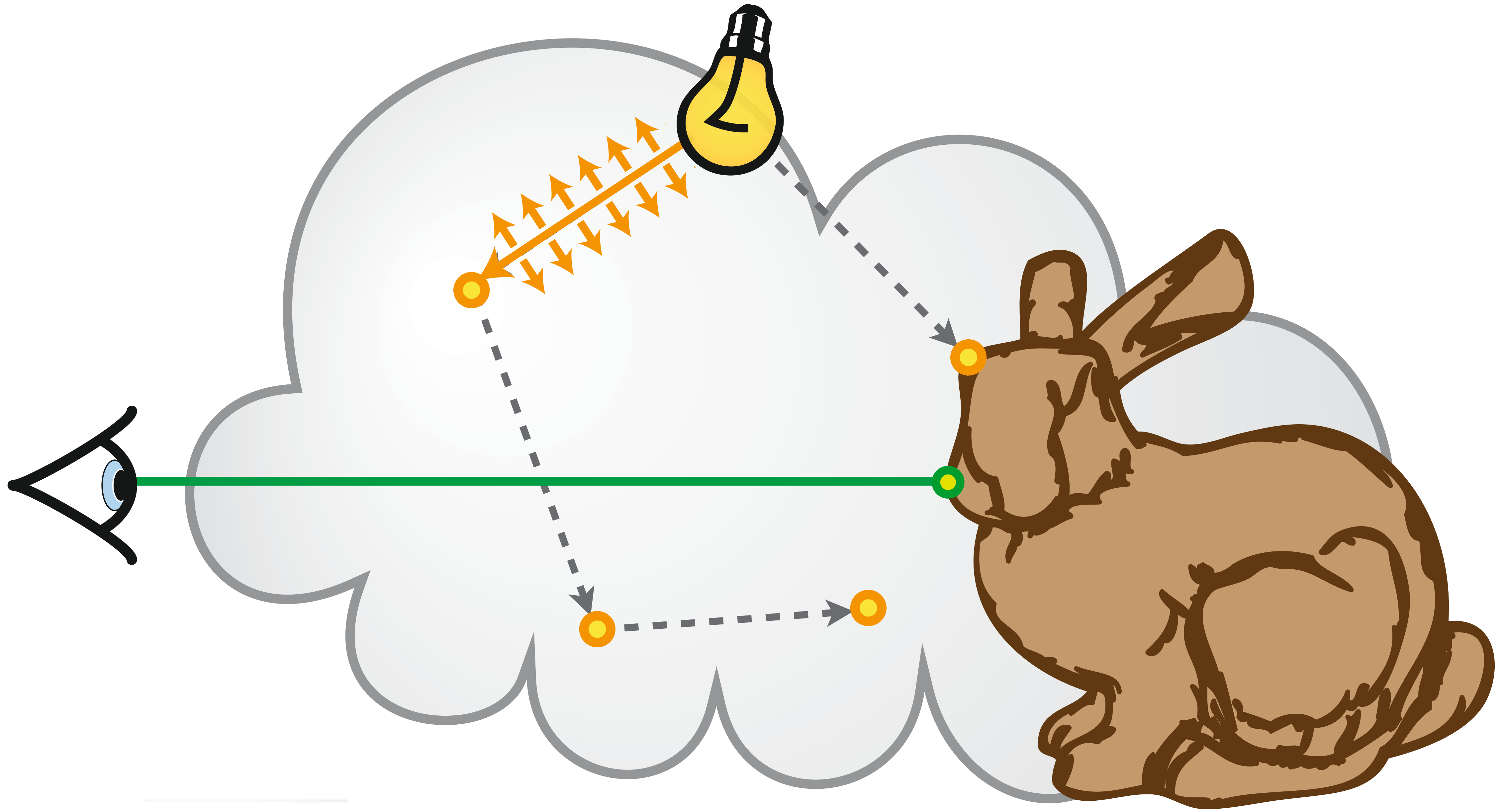
Algorithm overview



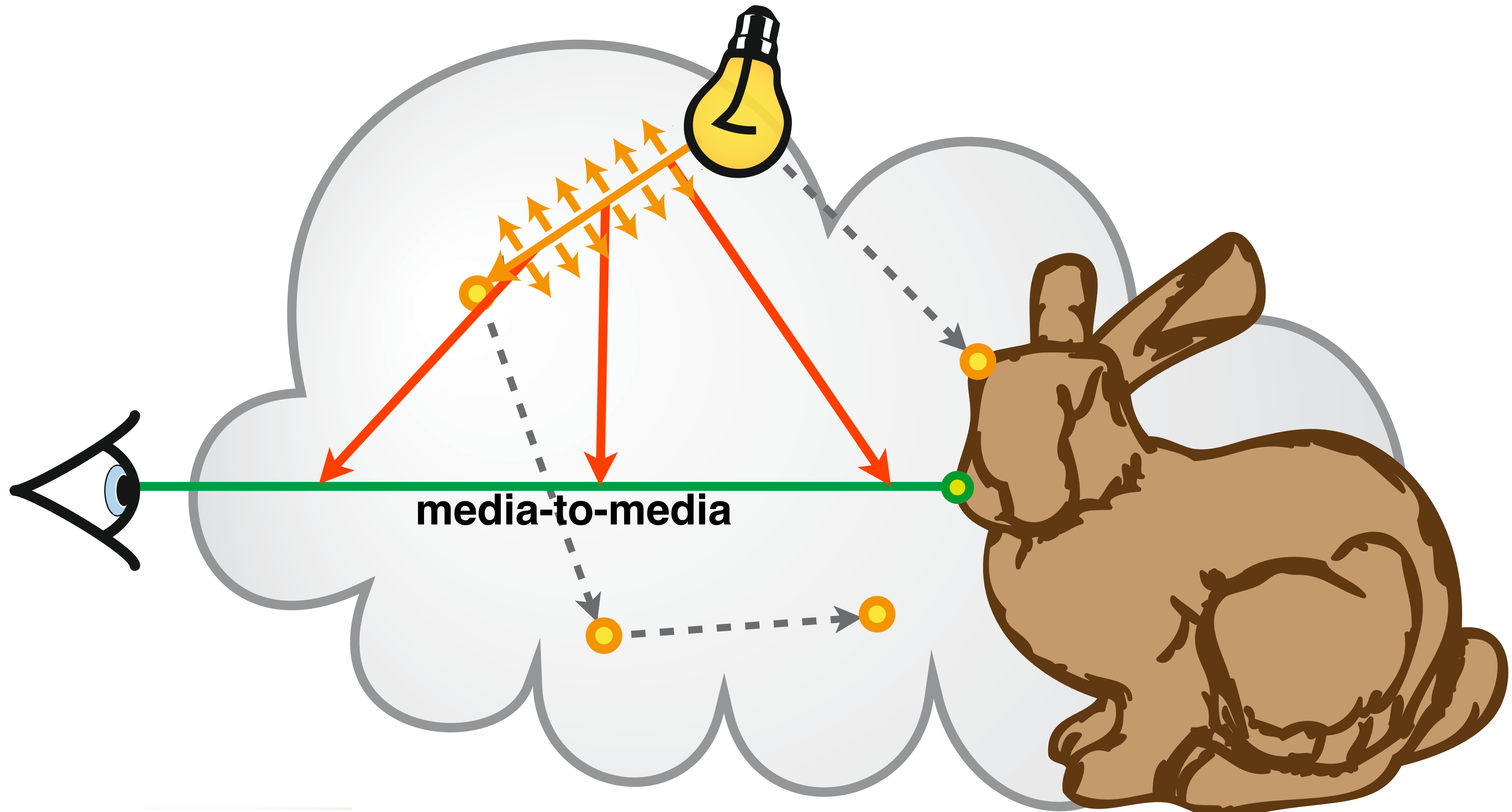
Algorithm overview



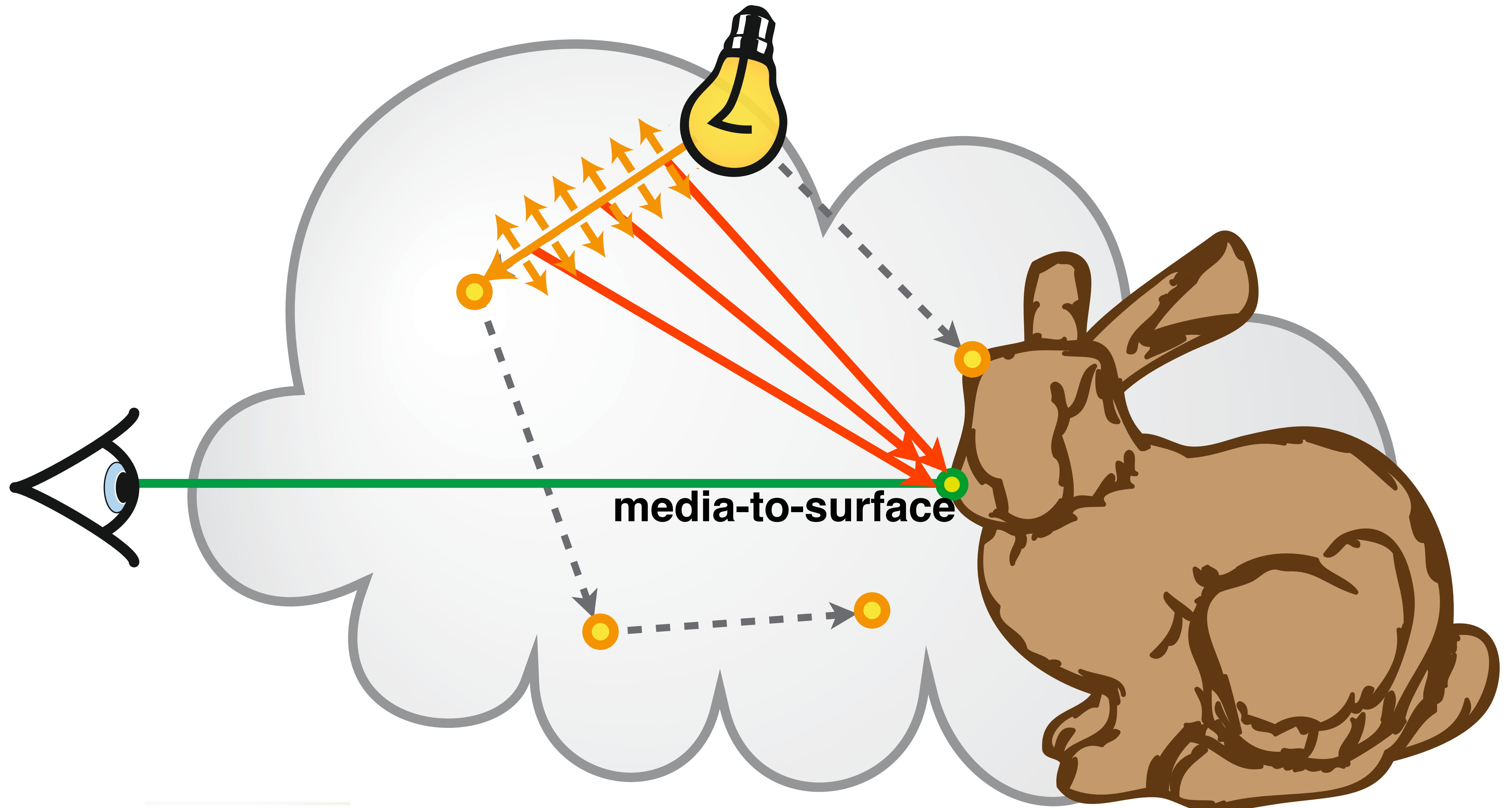
Algorithm overview



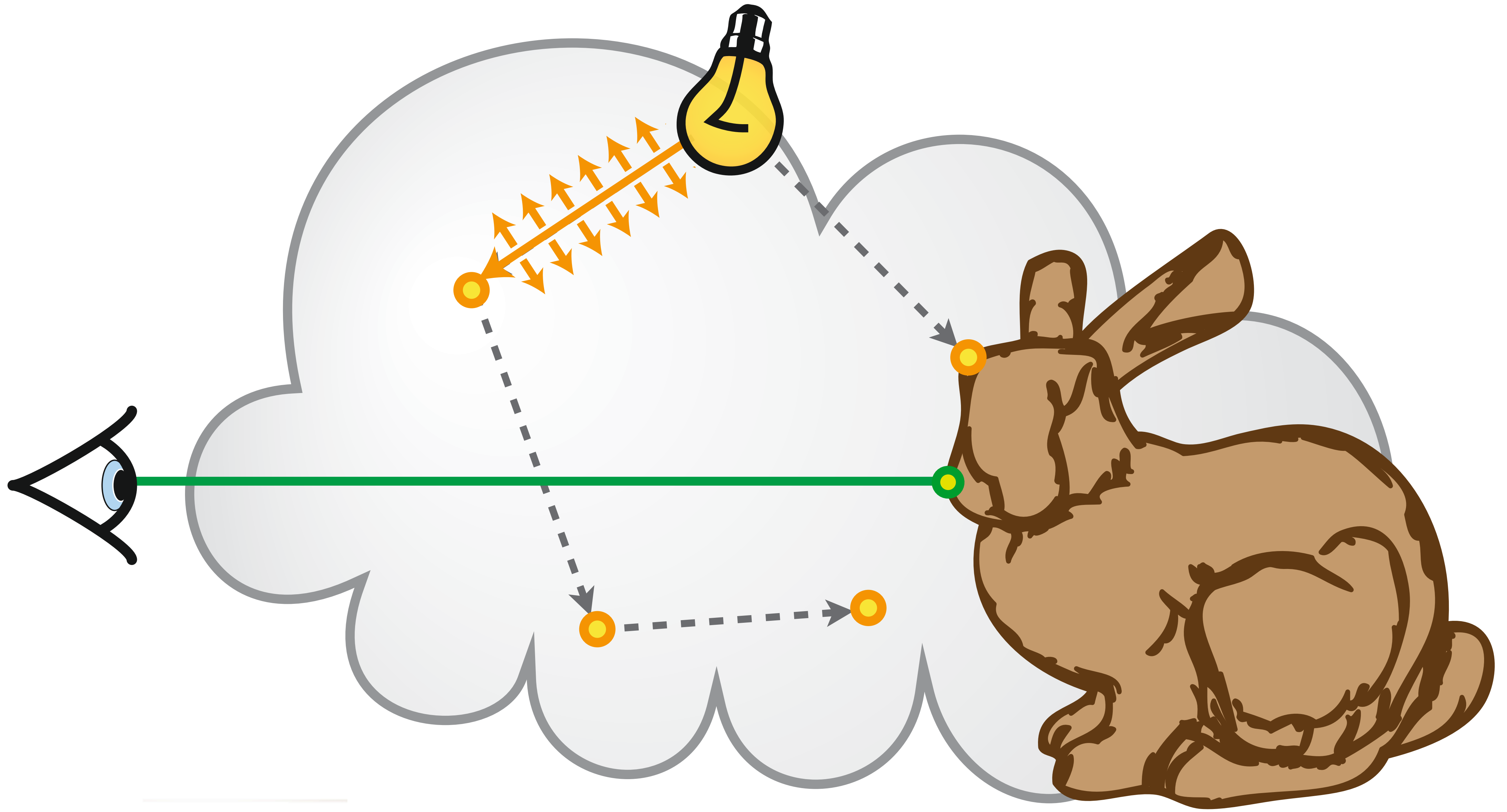
Algorithm overview



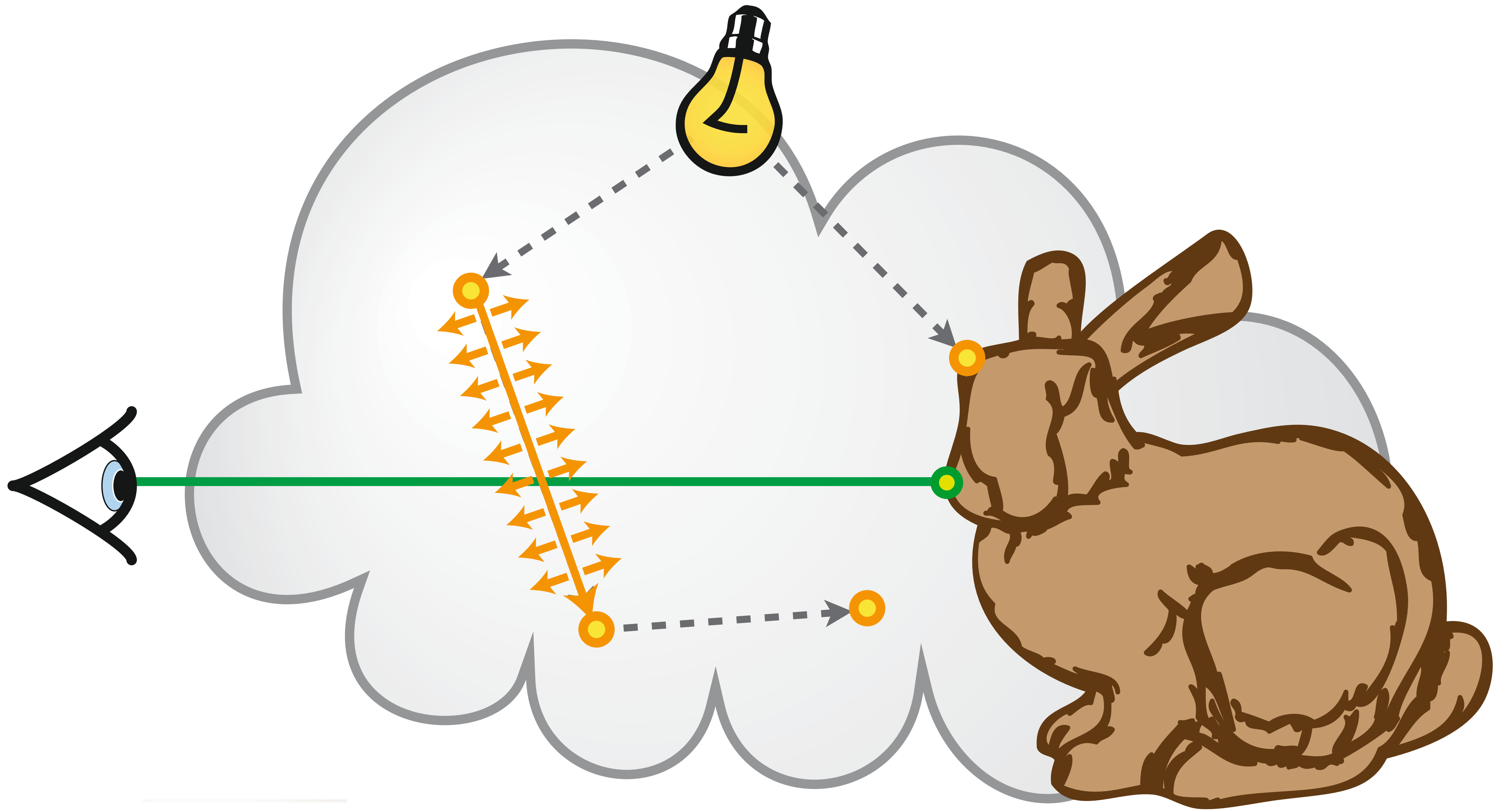
Algorithm overview



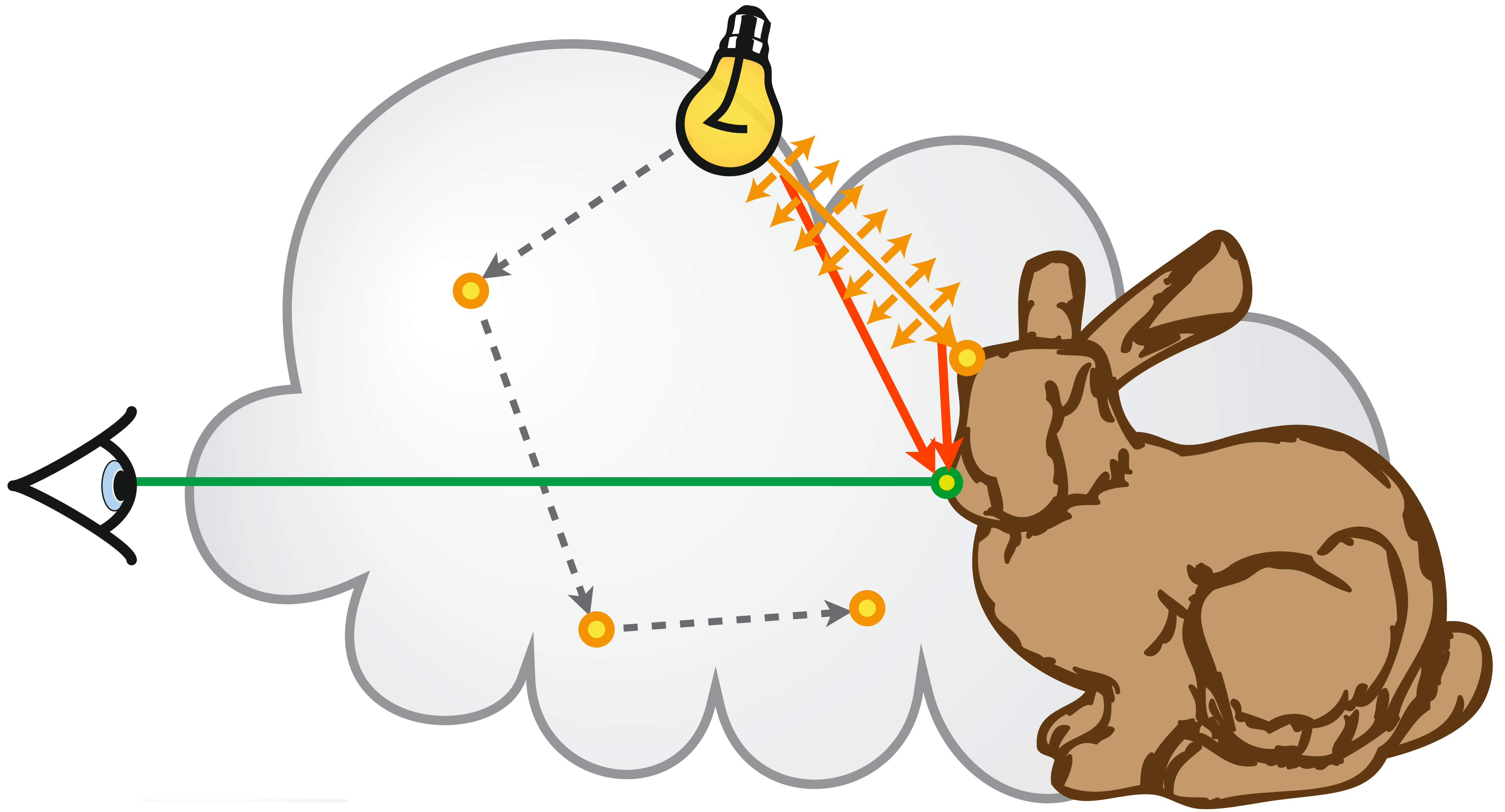
Algorithm overview



Algorithm overview

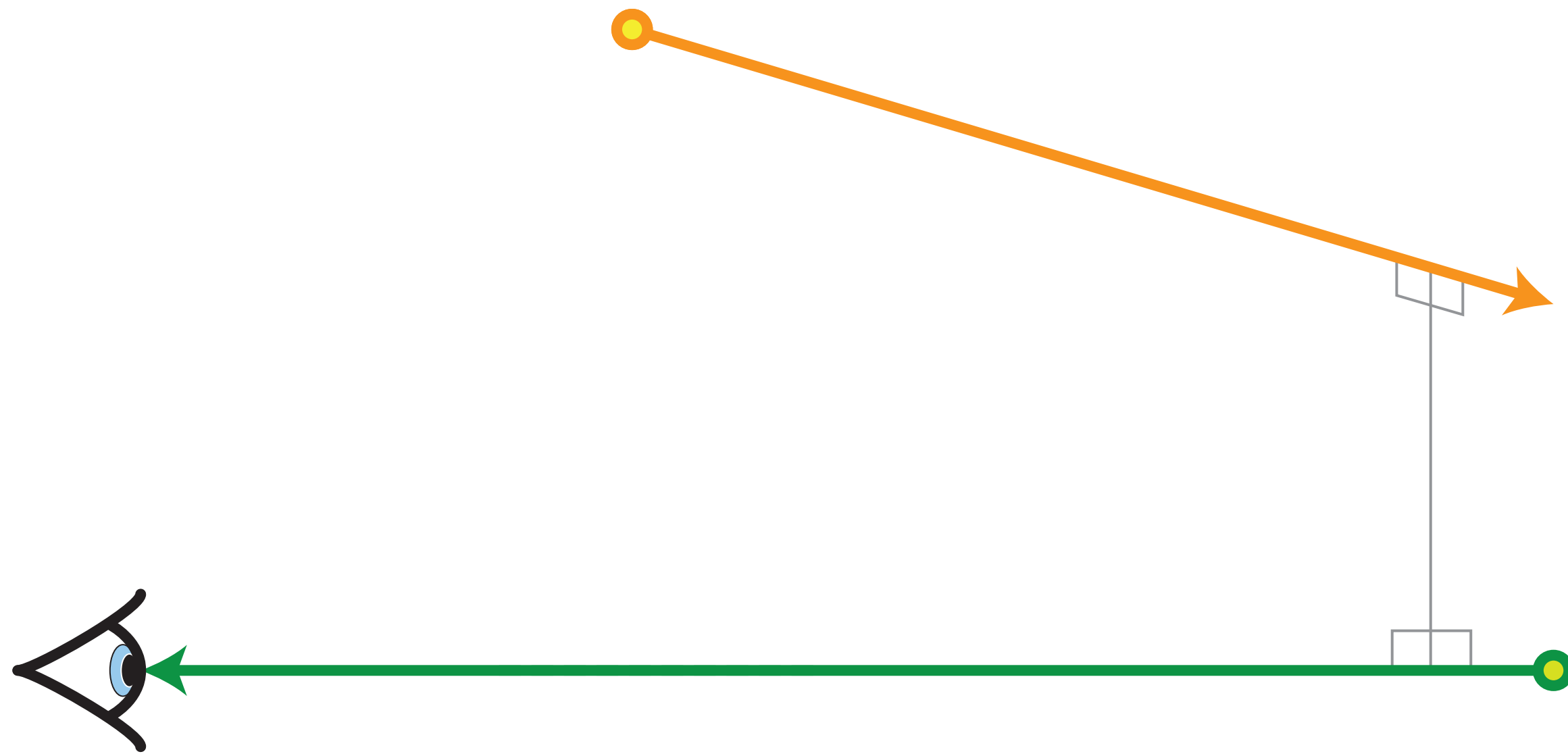


Algorithm overview

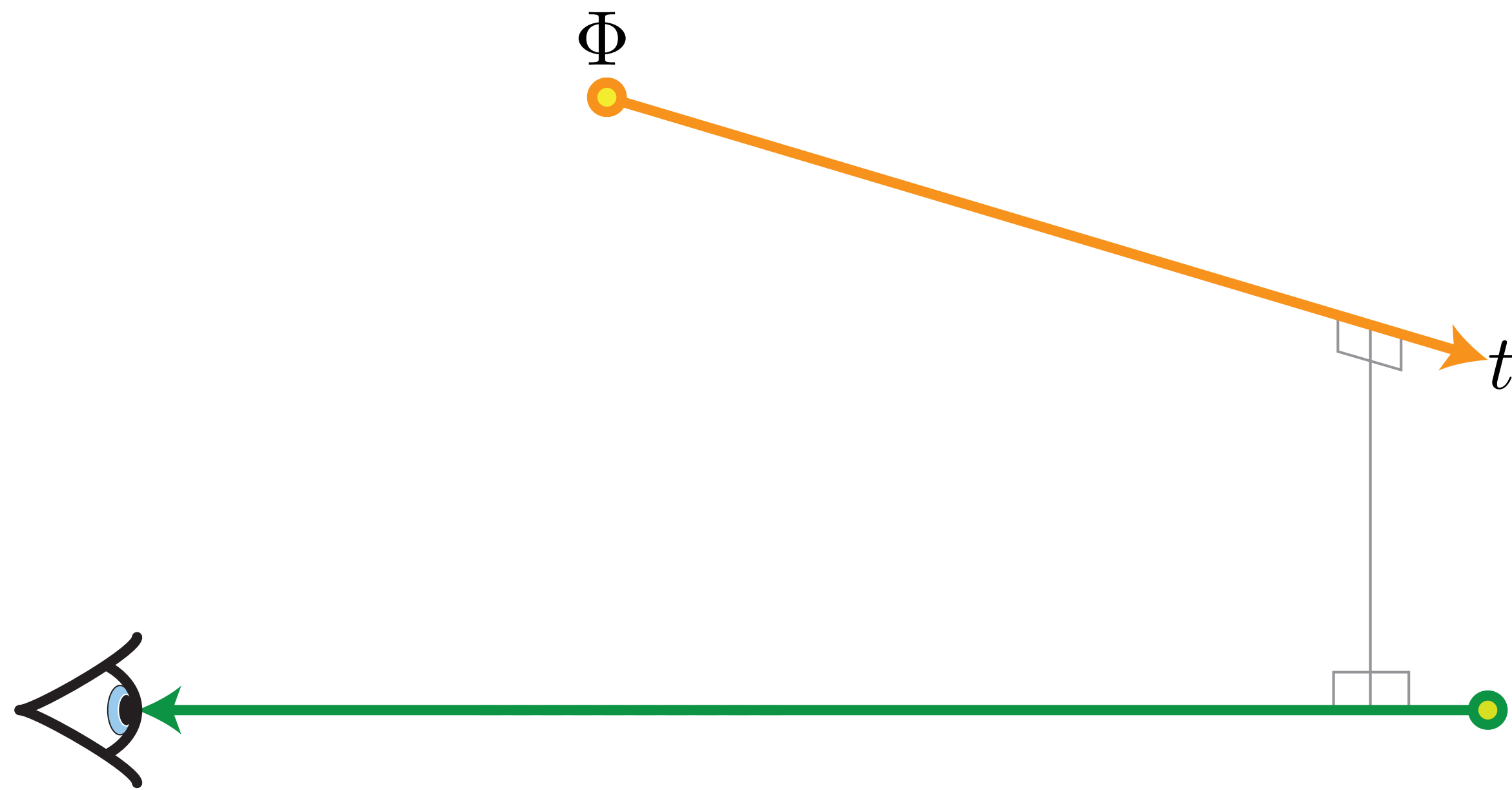


Ray-to-Ray transport

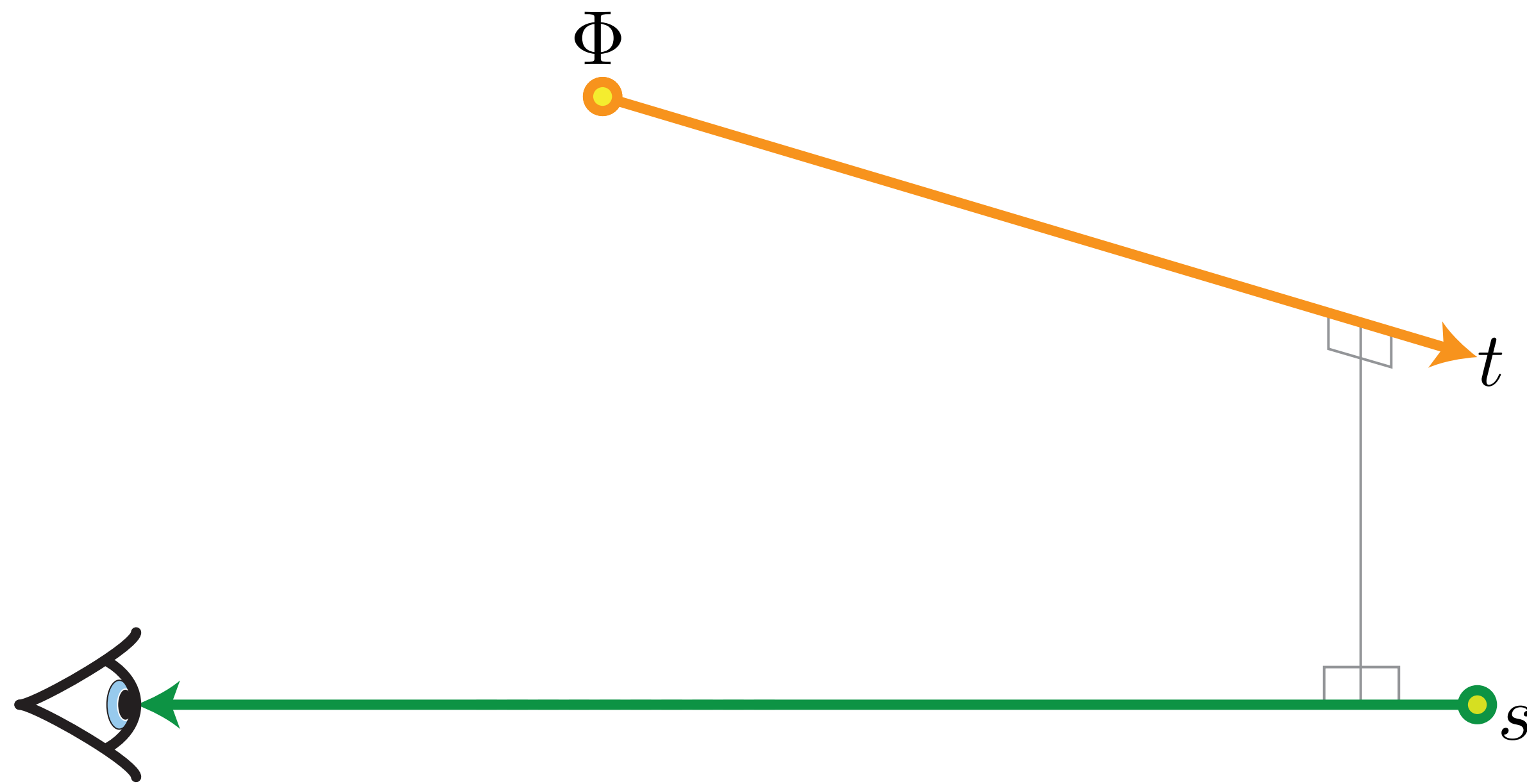
Ray-to-Ray transport



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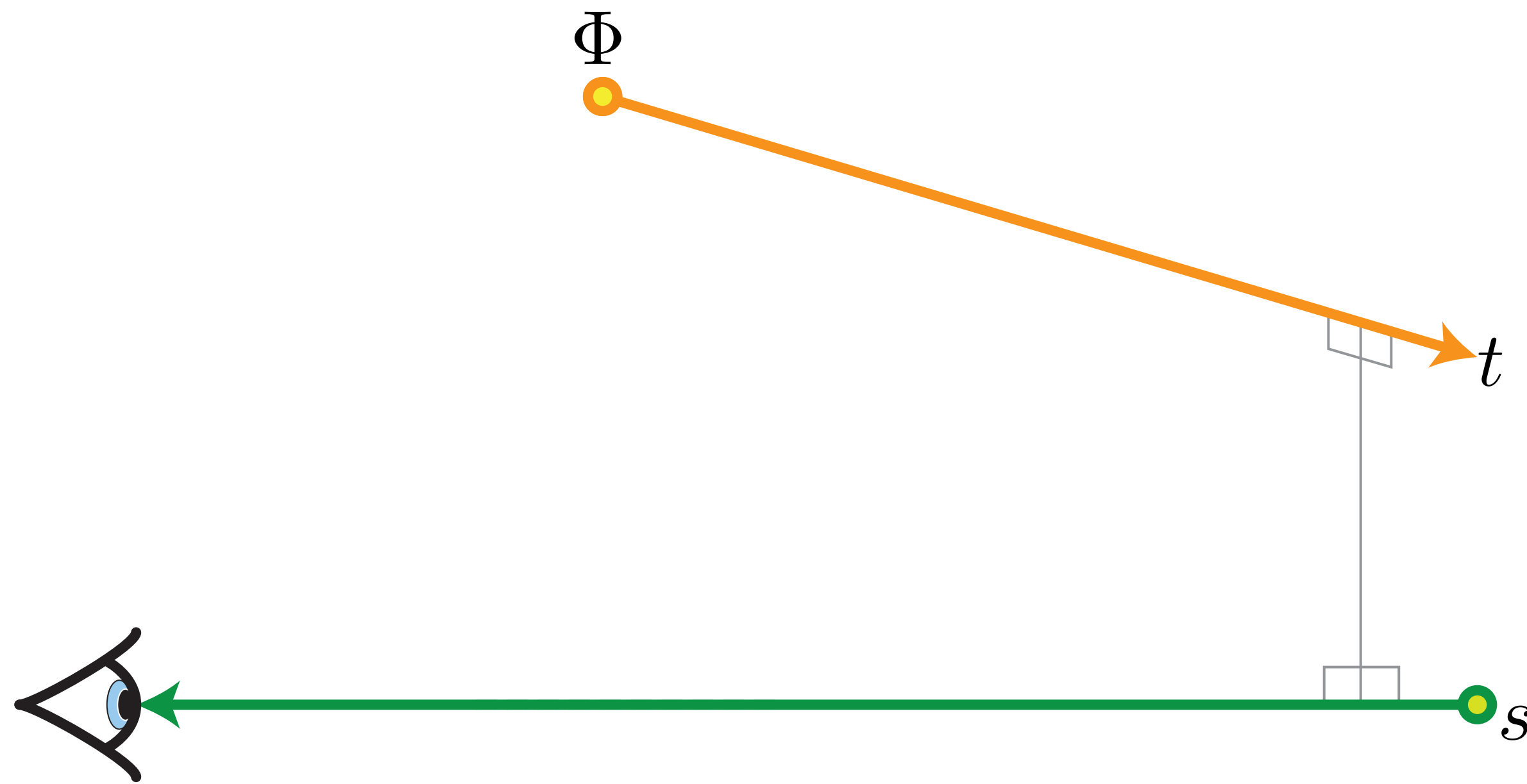


Ray-to-Ray transport



Ray-to-Ray transport

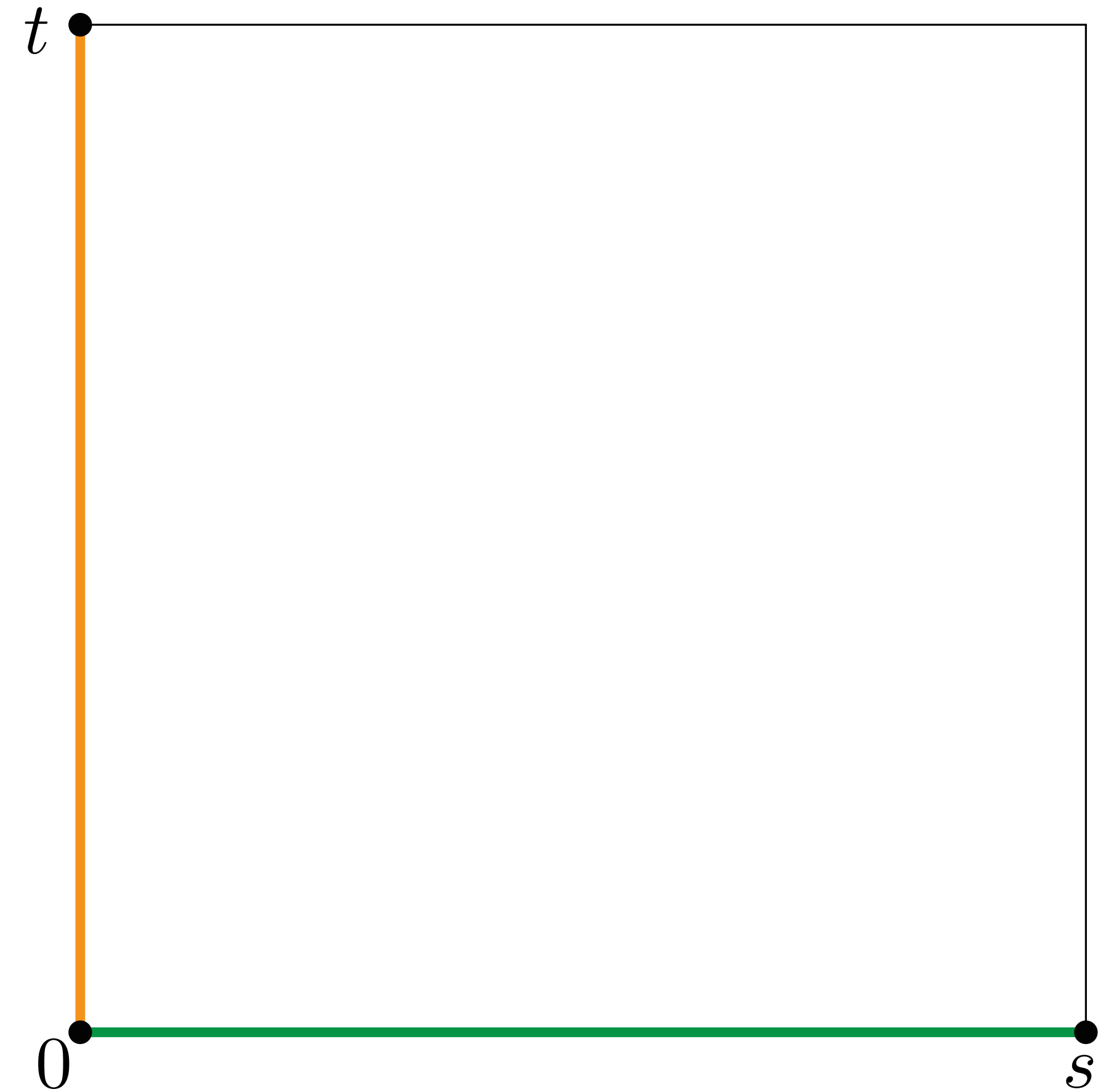
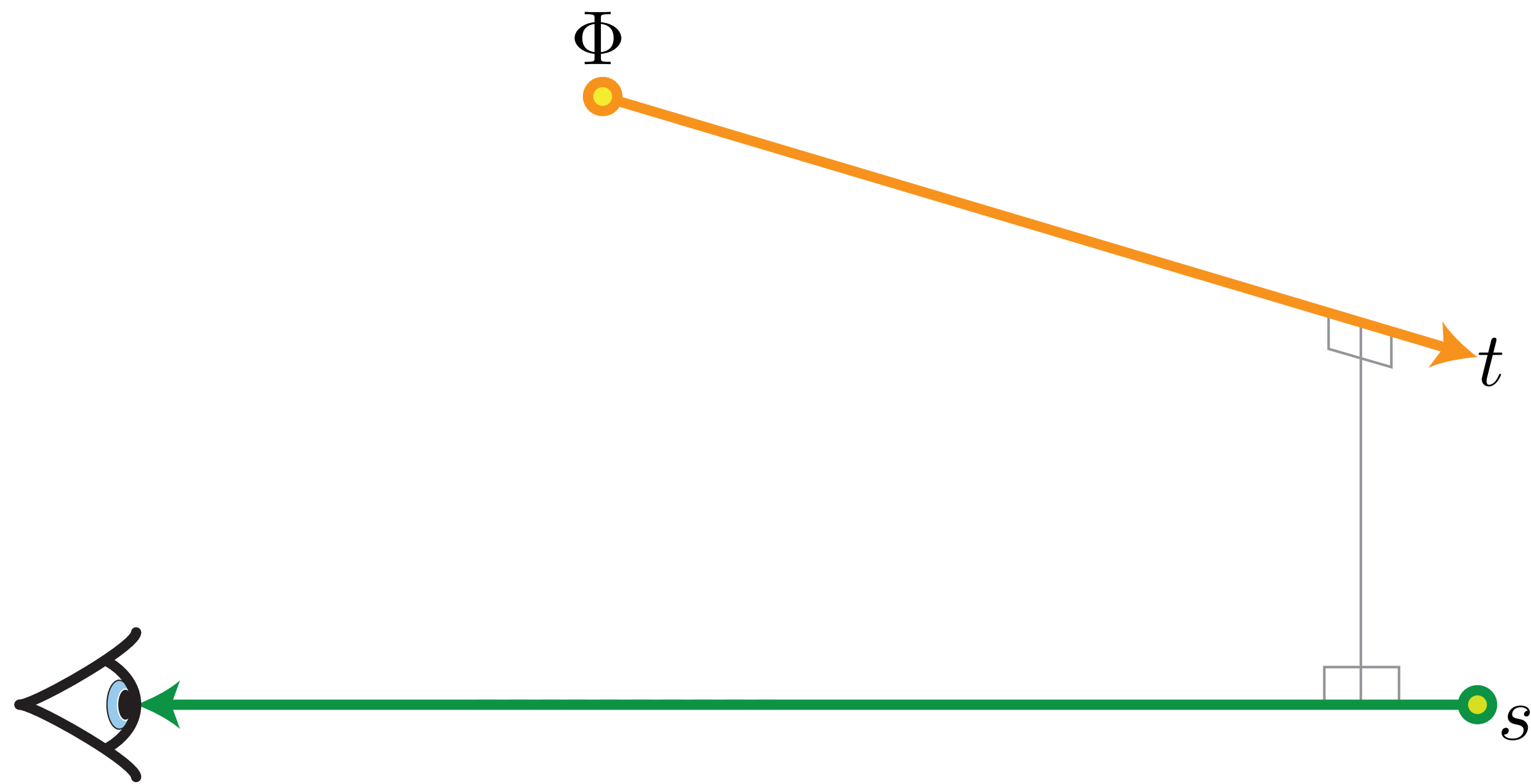
$$L = \Phi \int_0^s \int_0^t \text{---} dv du$$



Ray-to-Ray transport

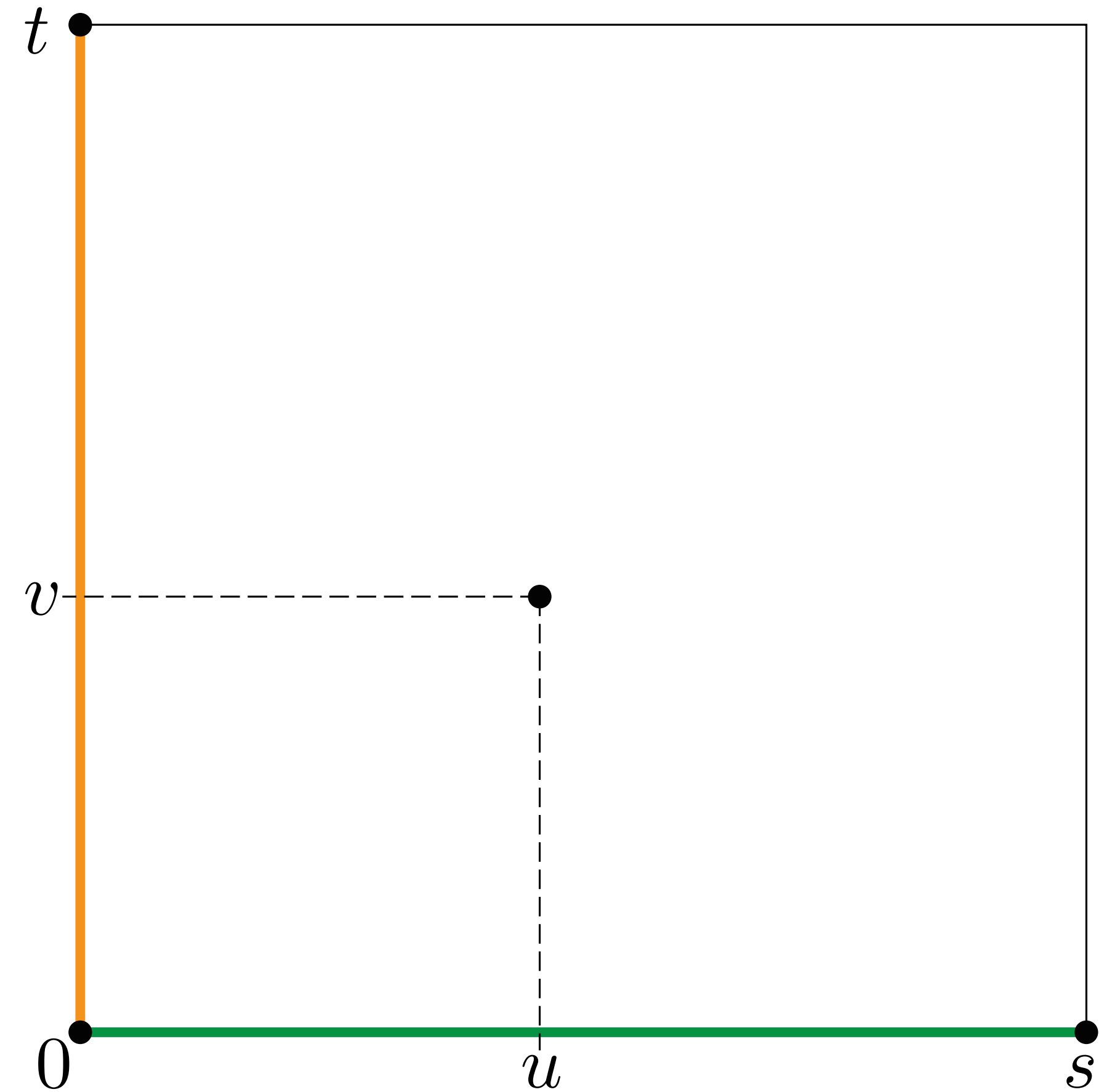
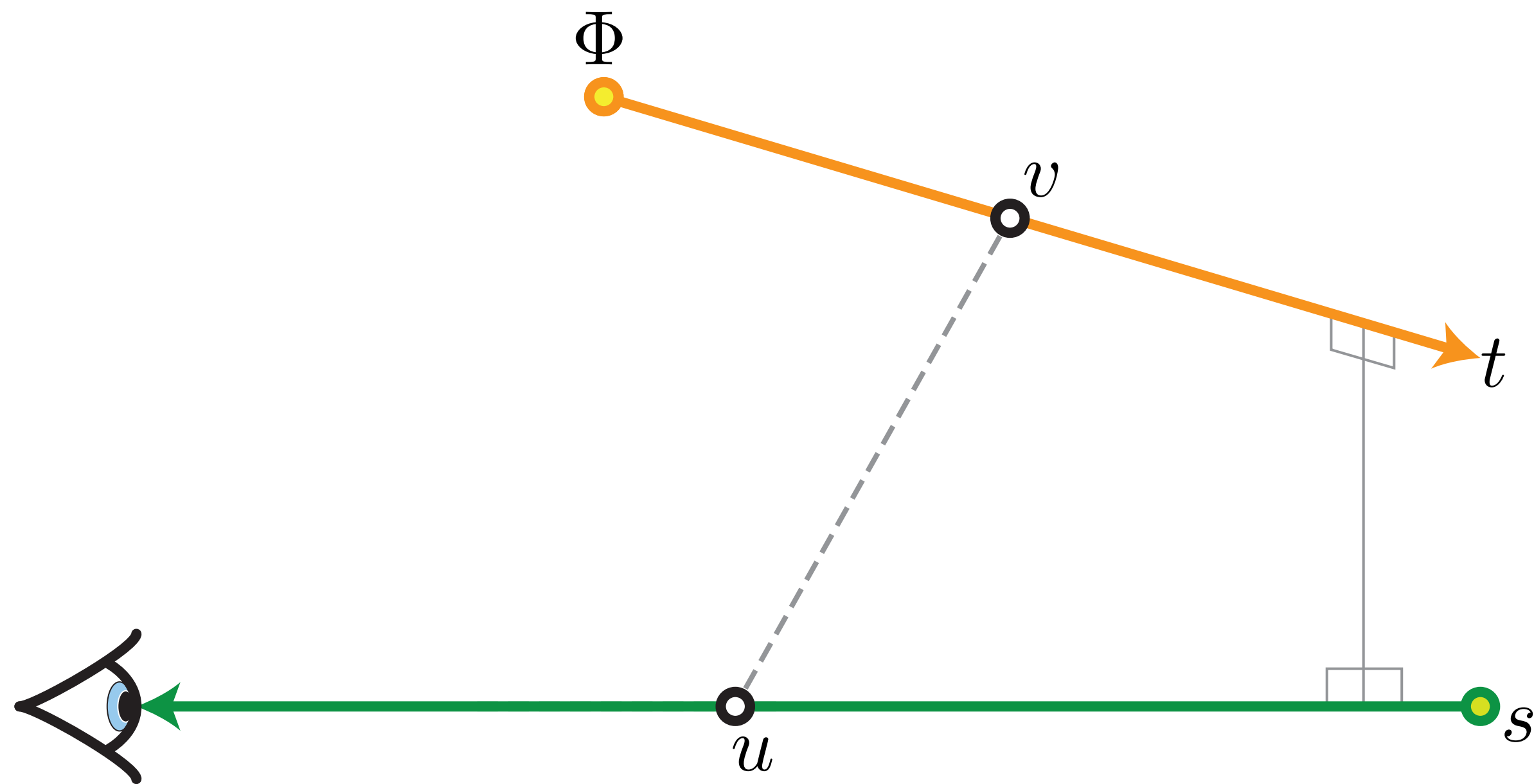
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_____ $dv du$



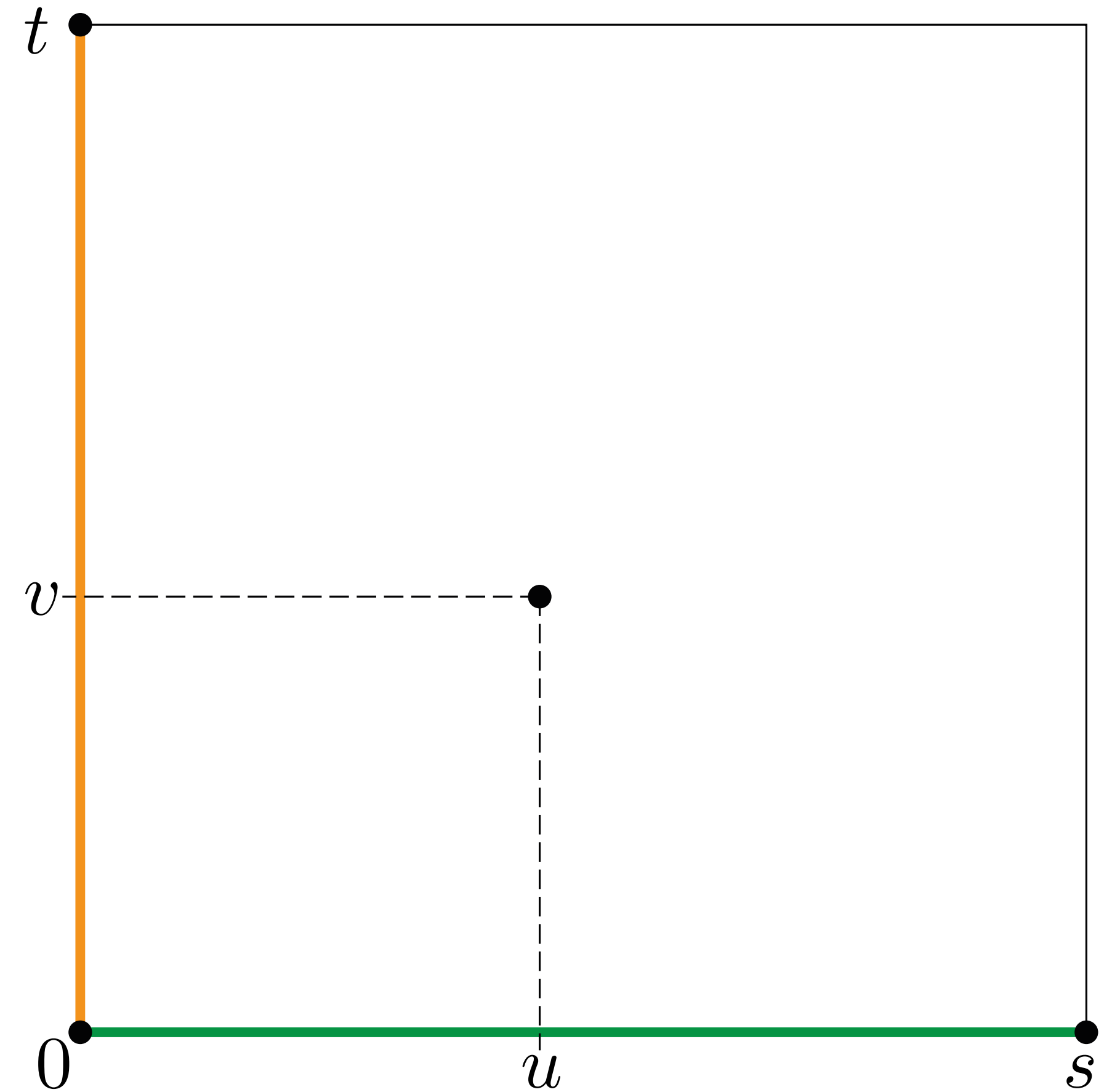
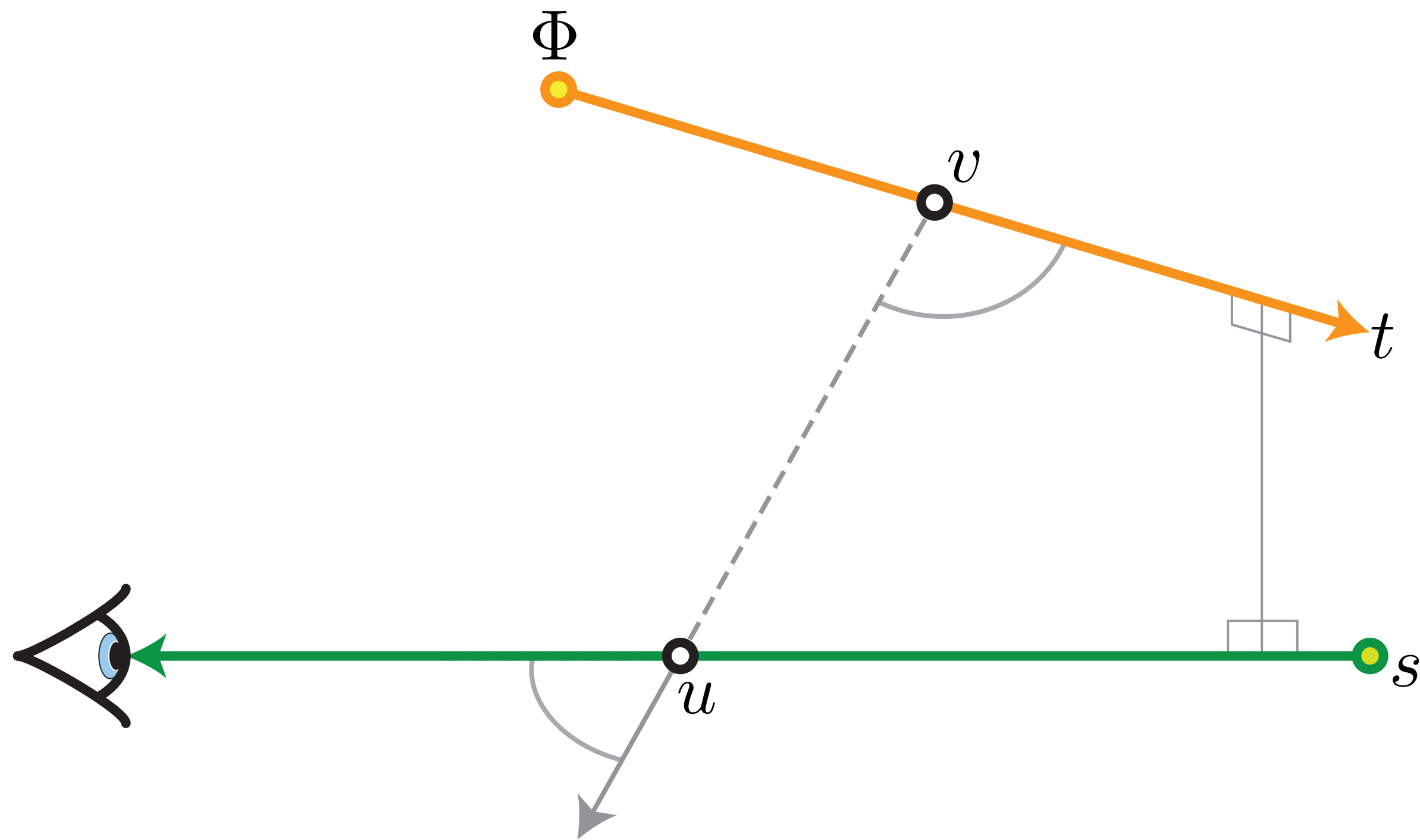
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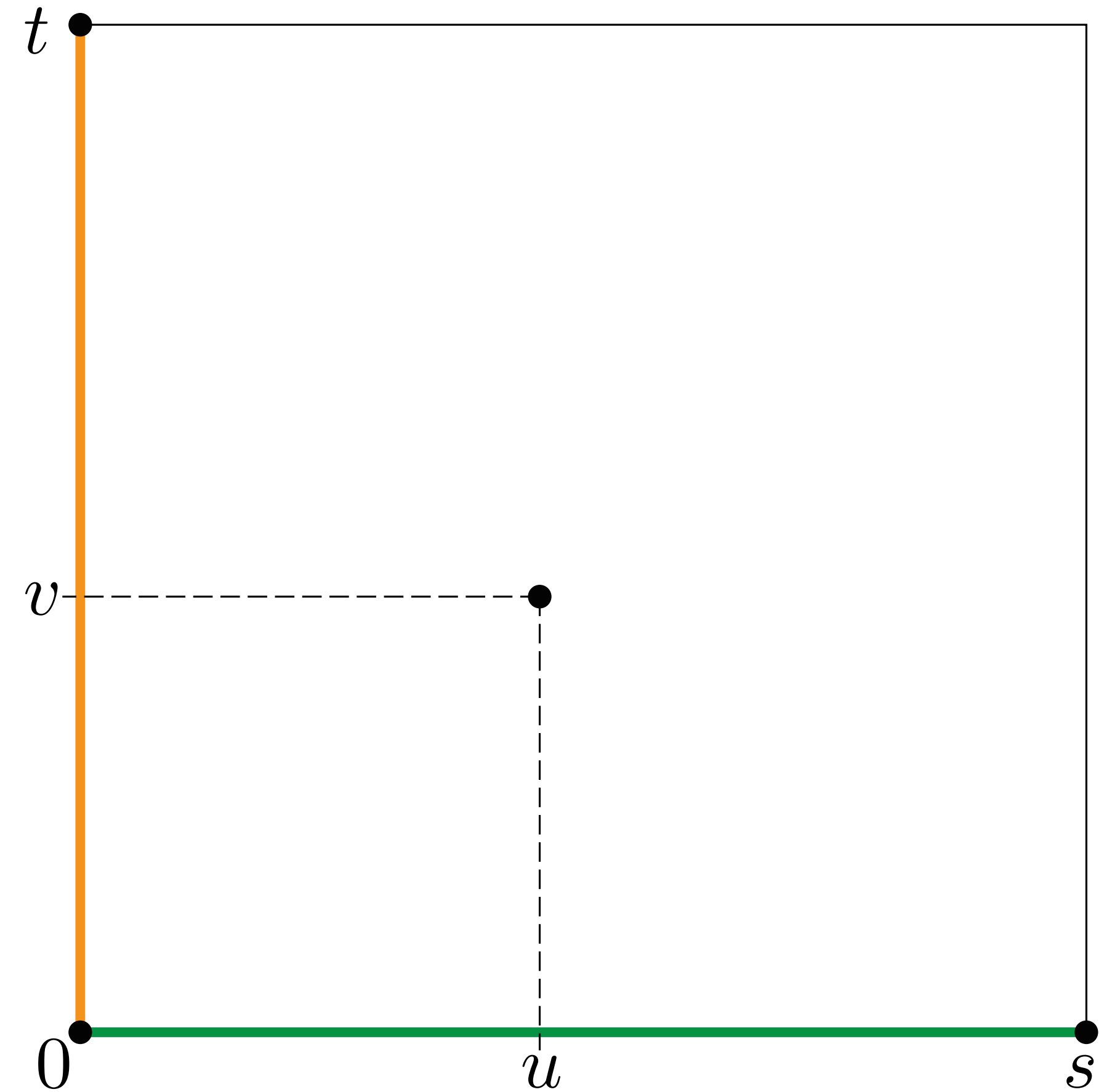
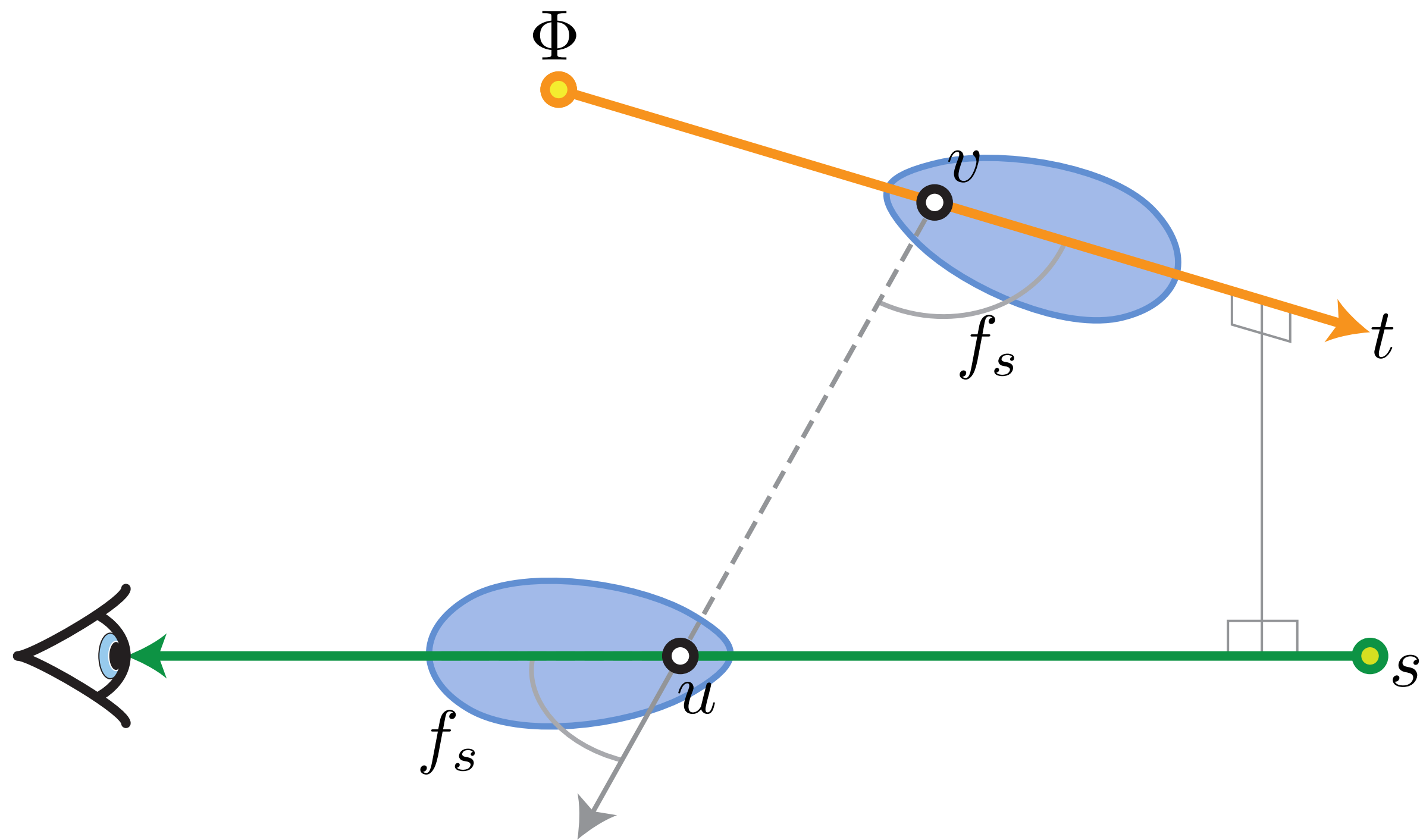
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v)}{\text{phase functions}} dv du$$



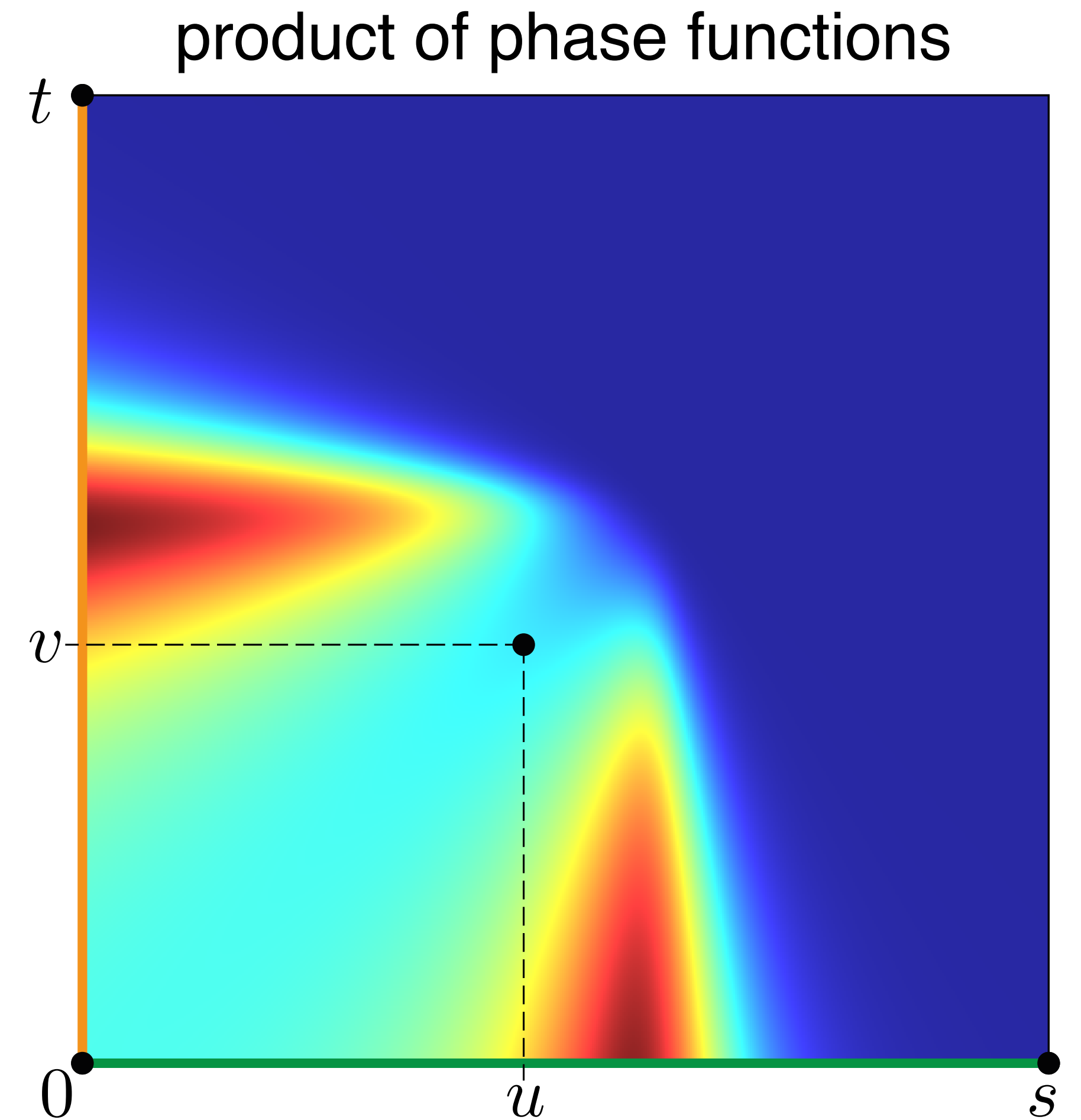
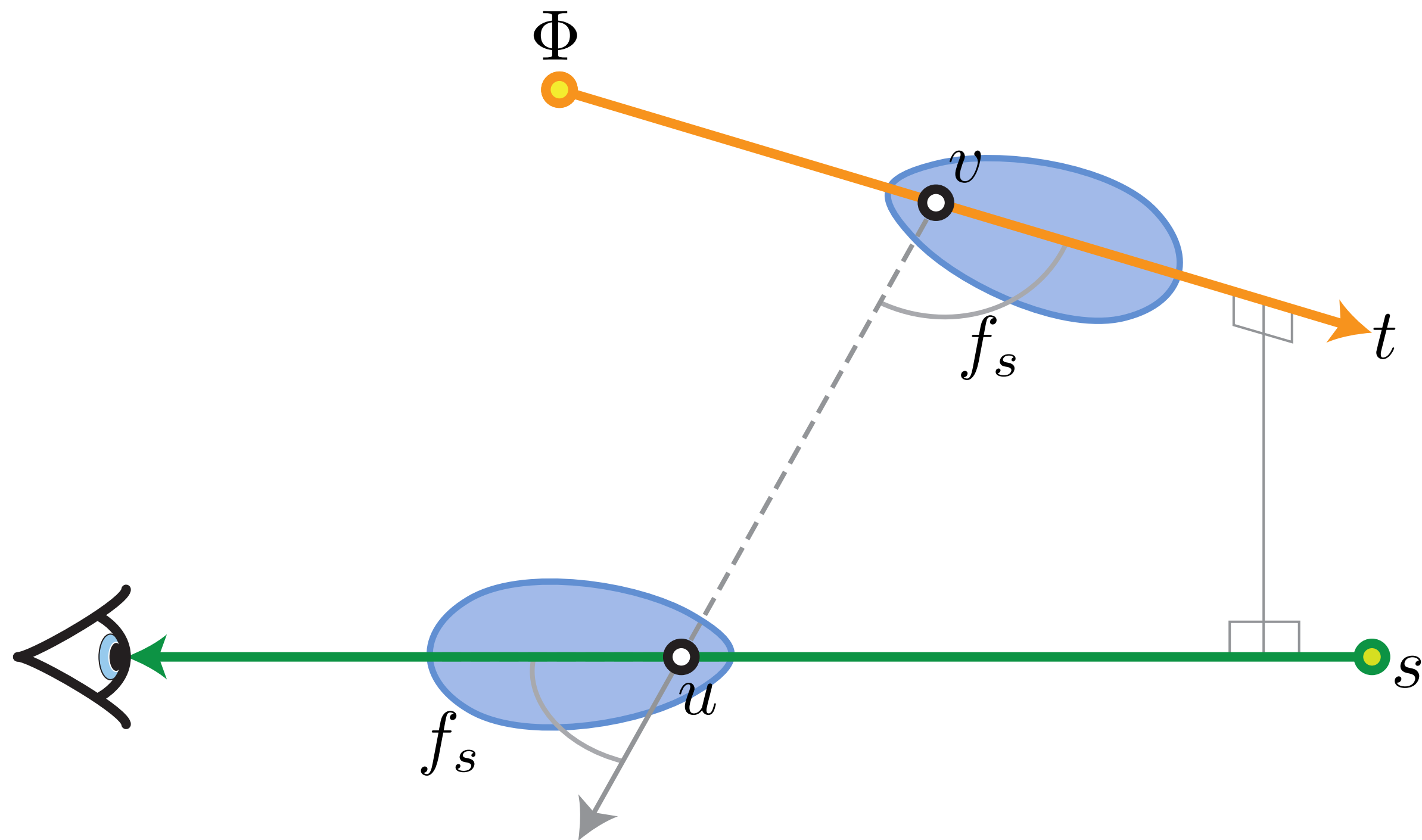
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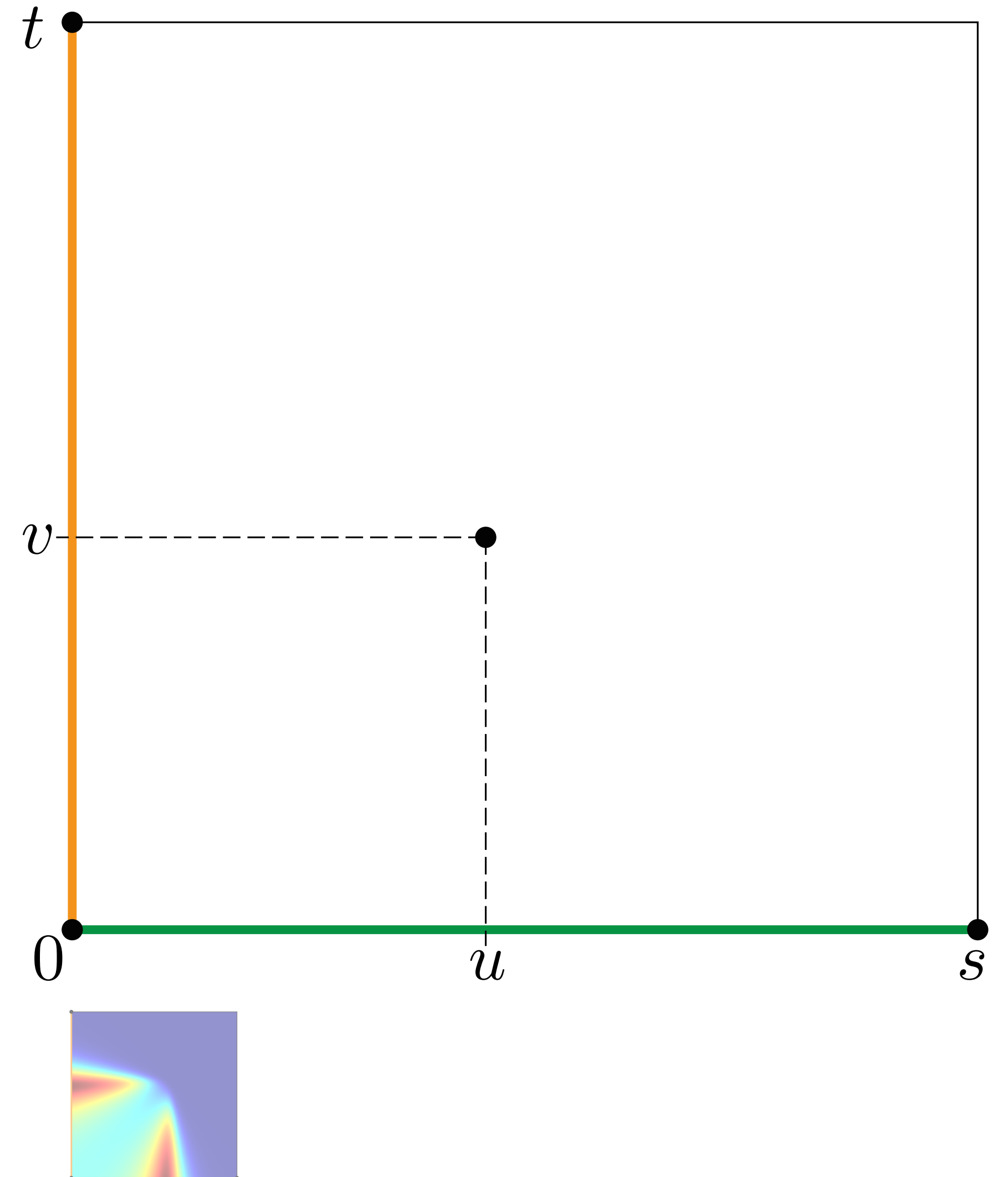
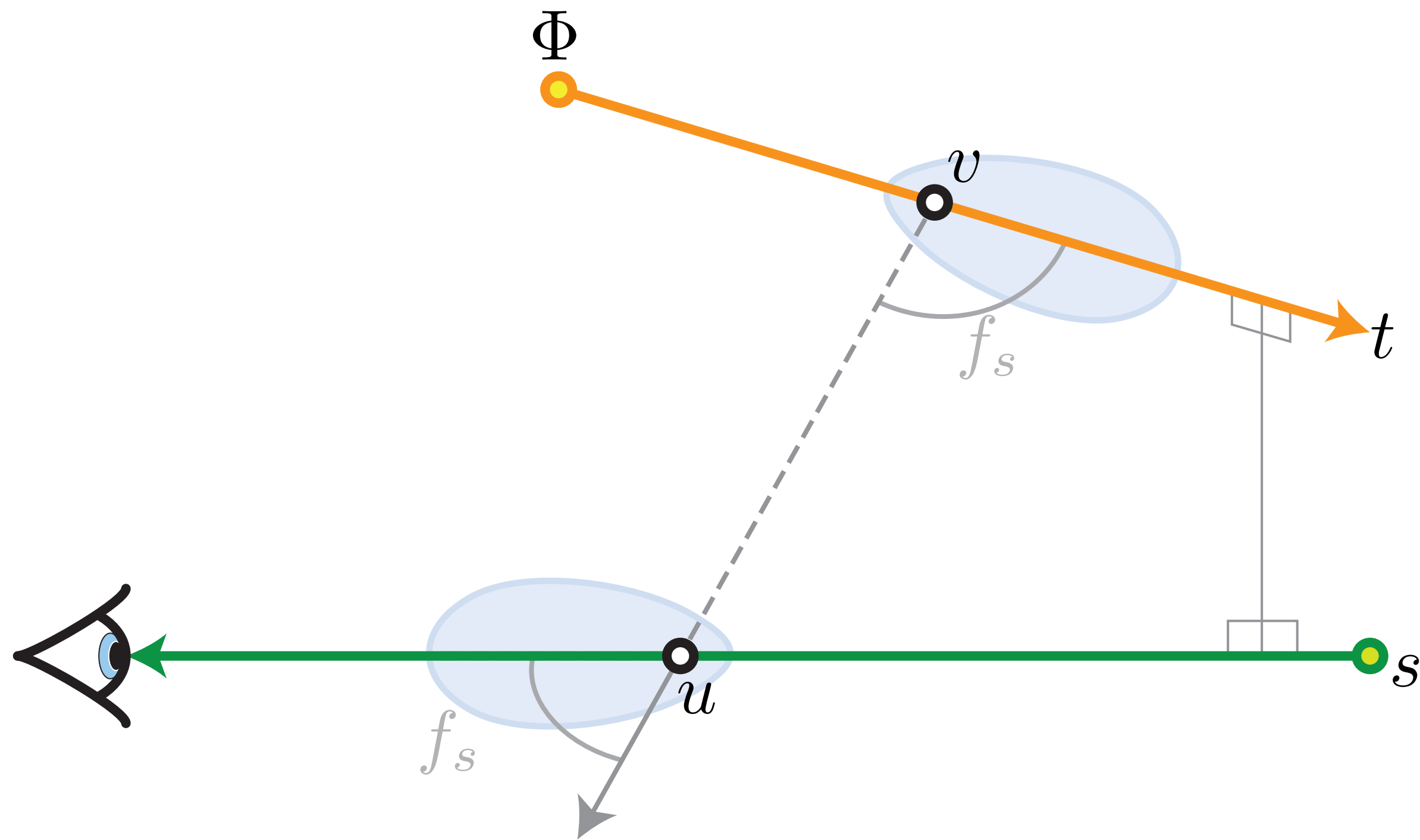
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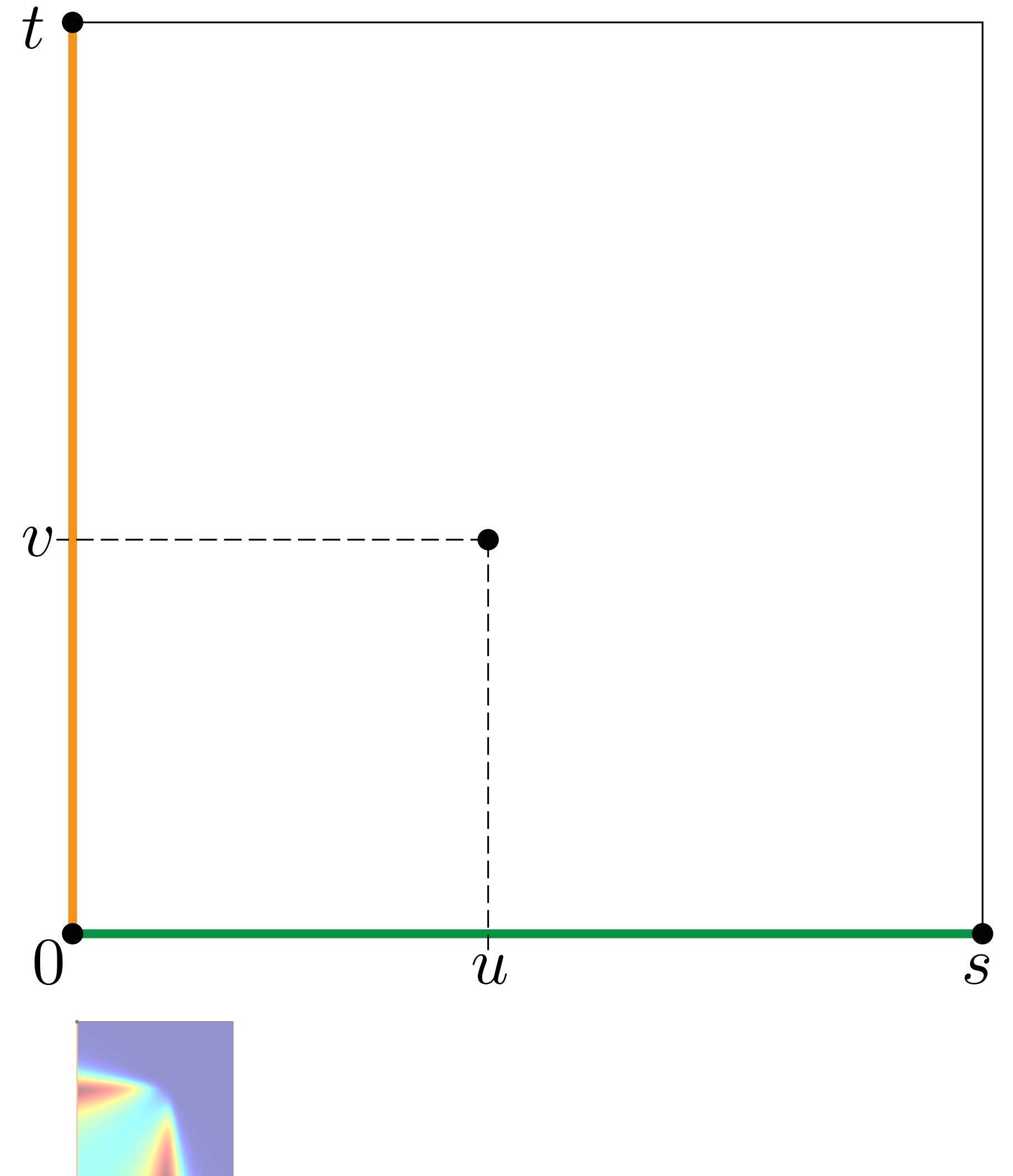
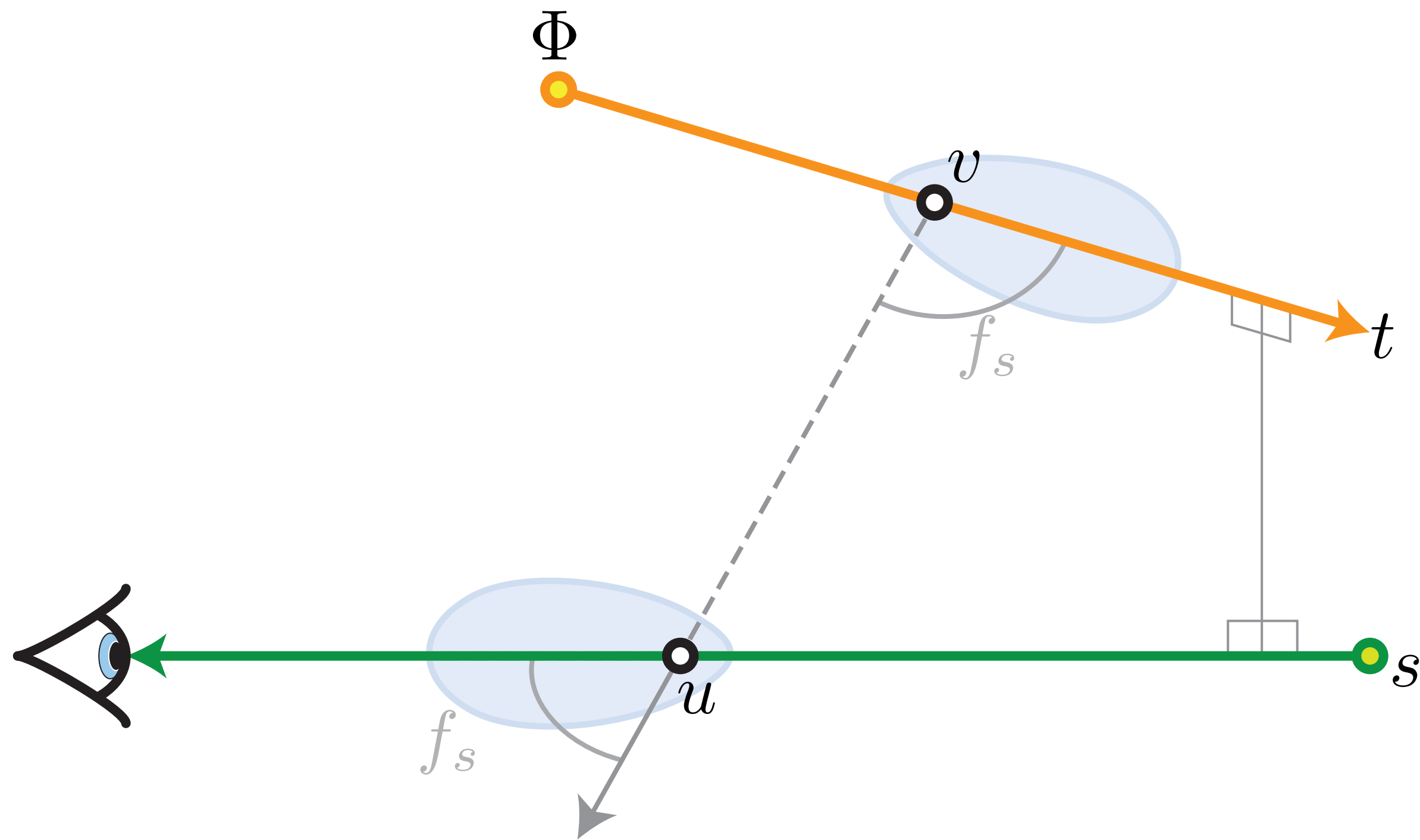
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$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v)}{dvdu}$$



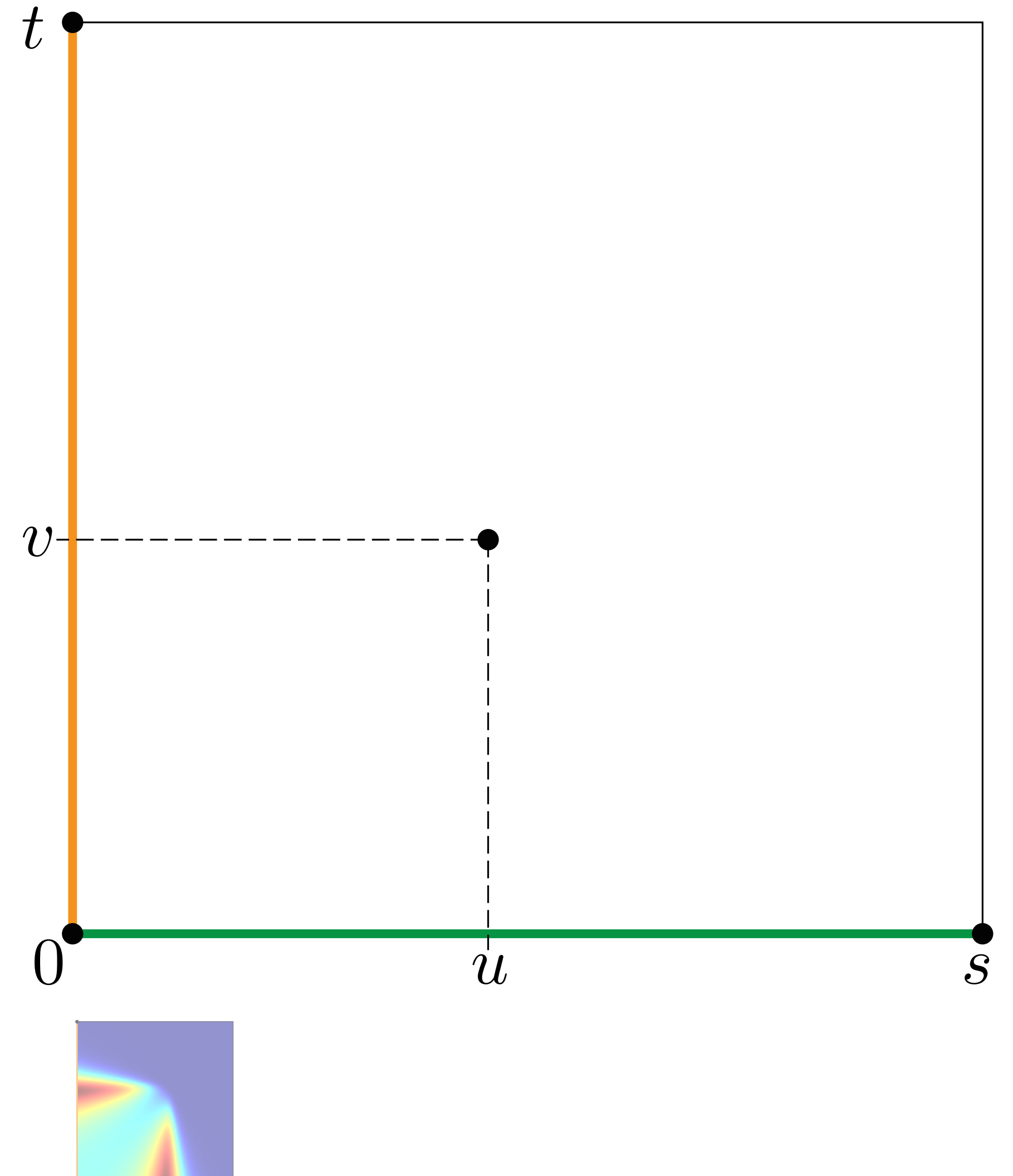
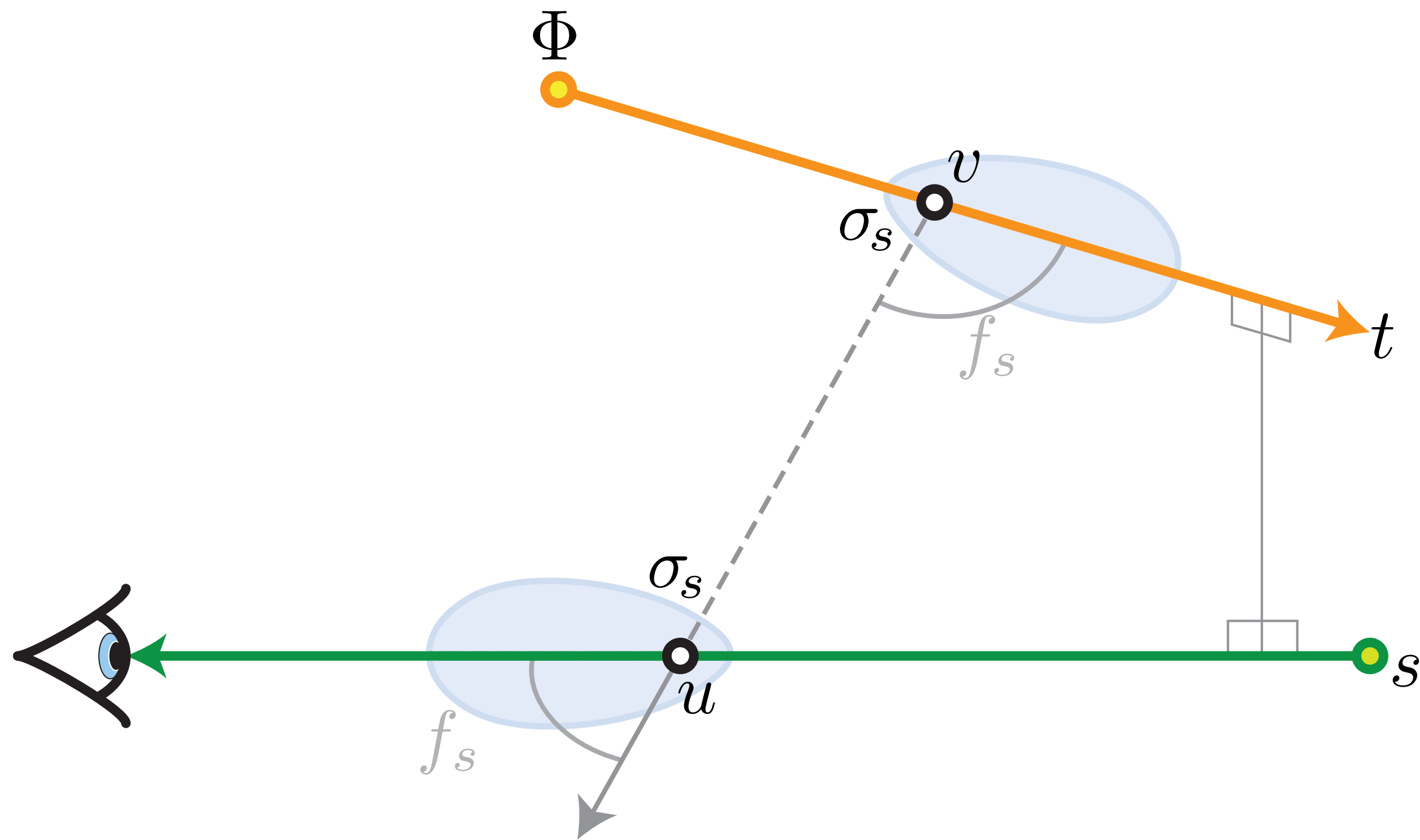
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v)}{\text{scattering}} dv du$$



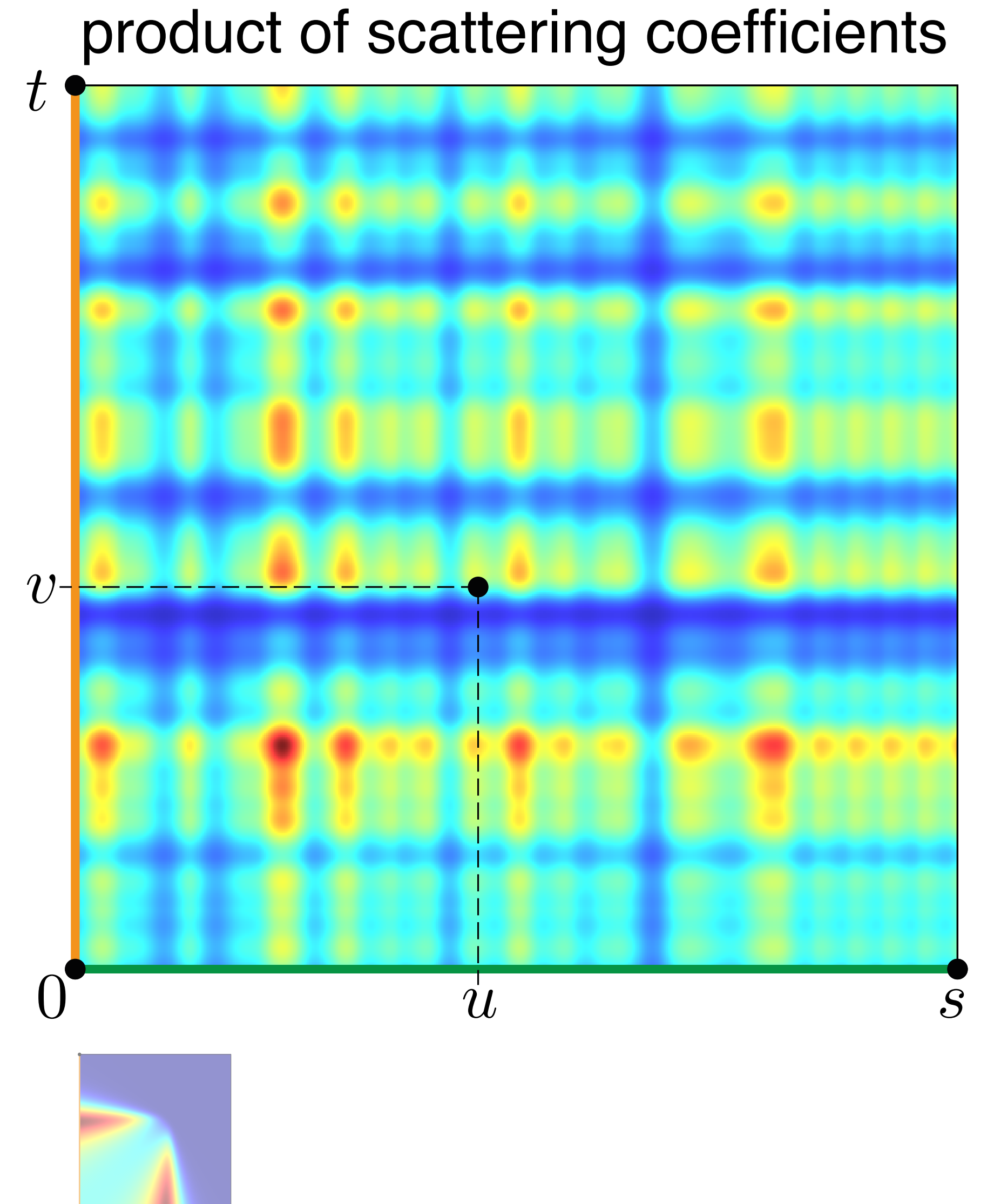
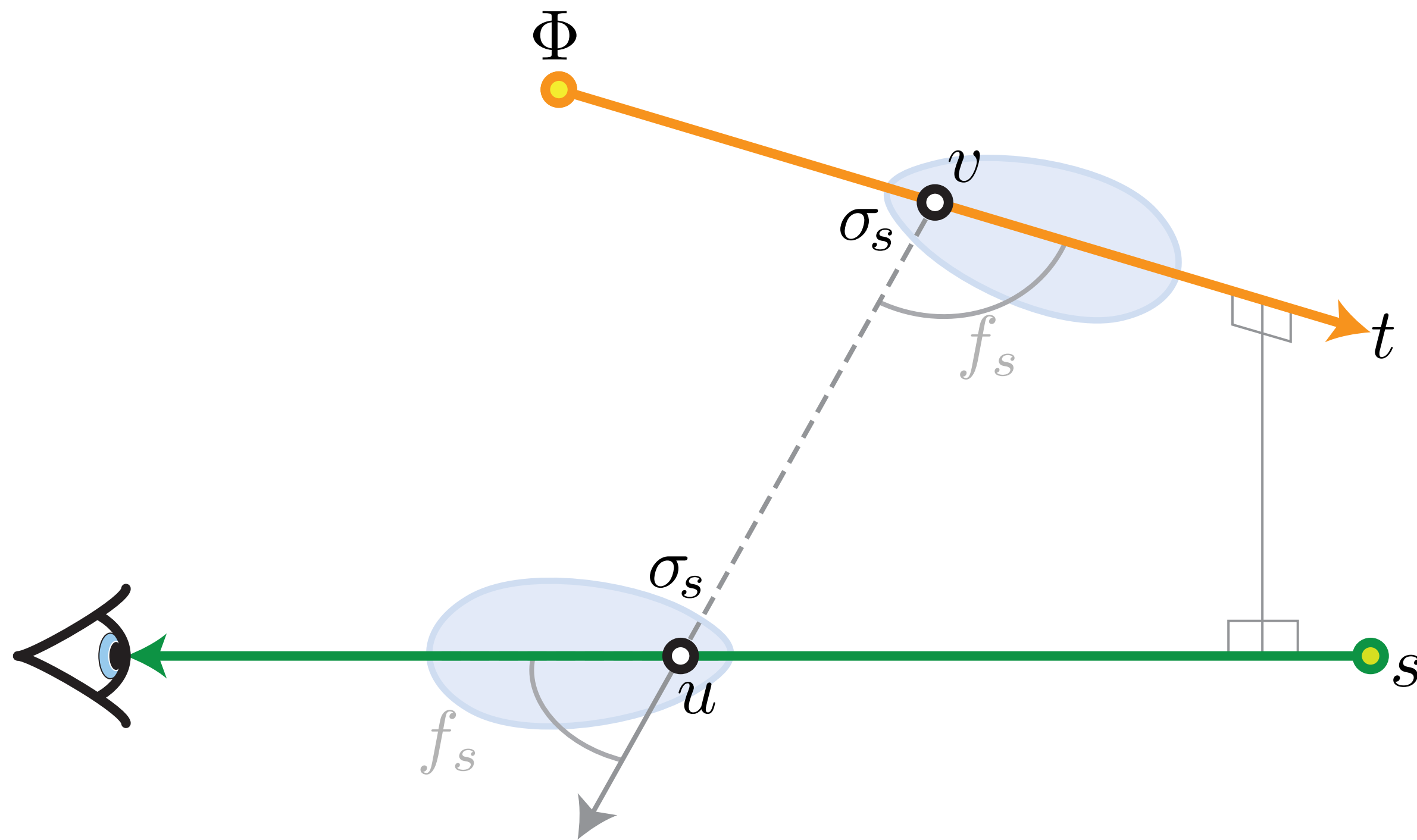
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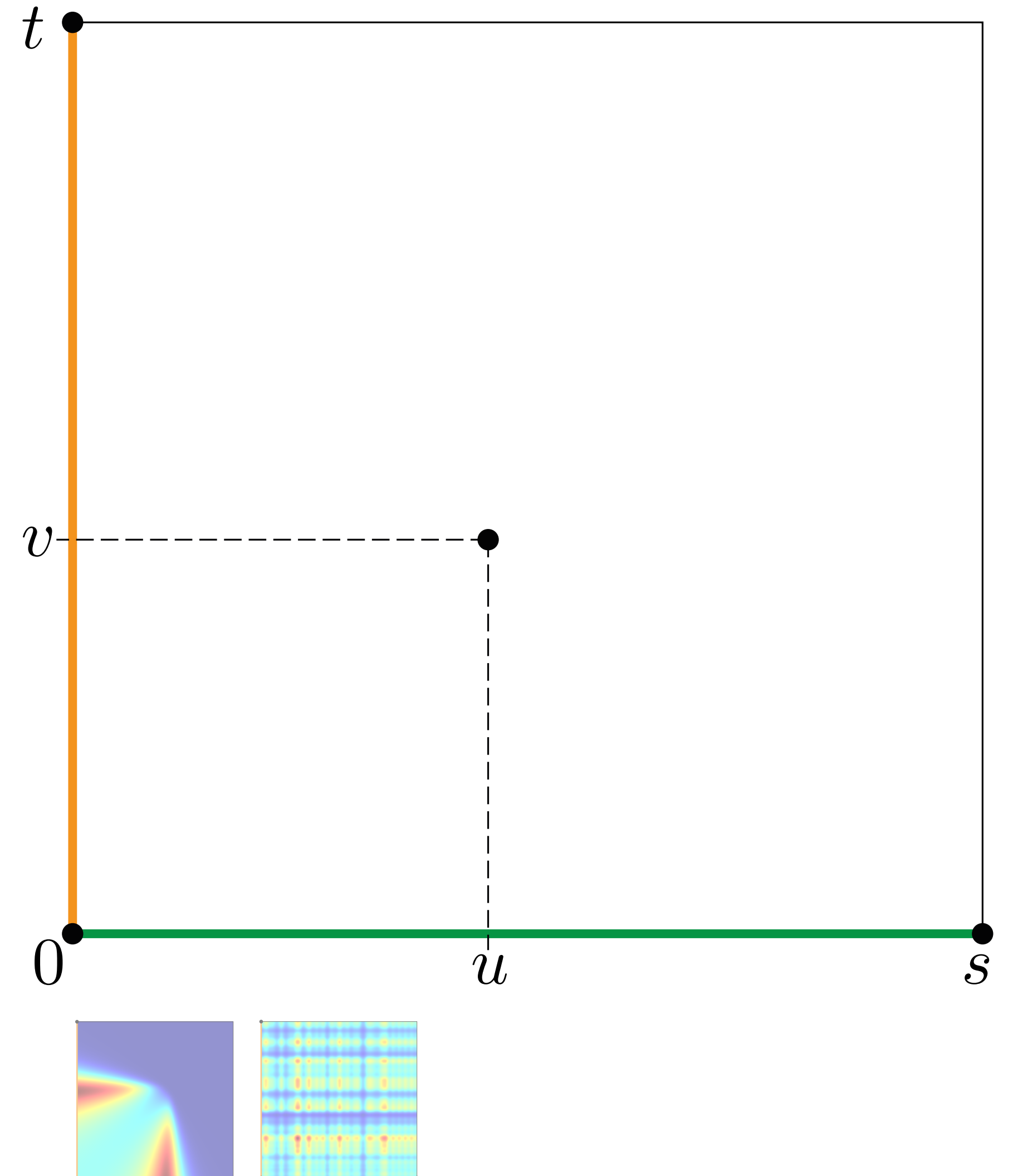
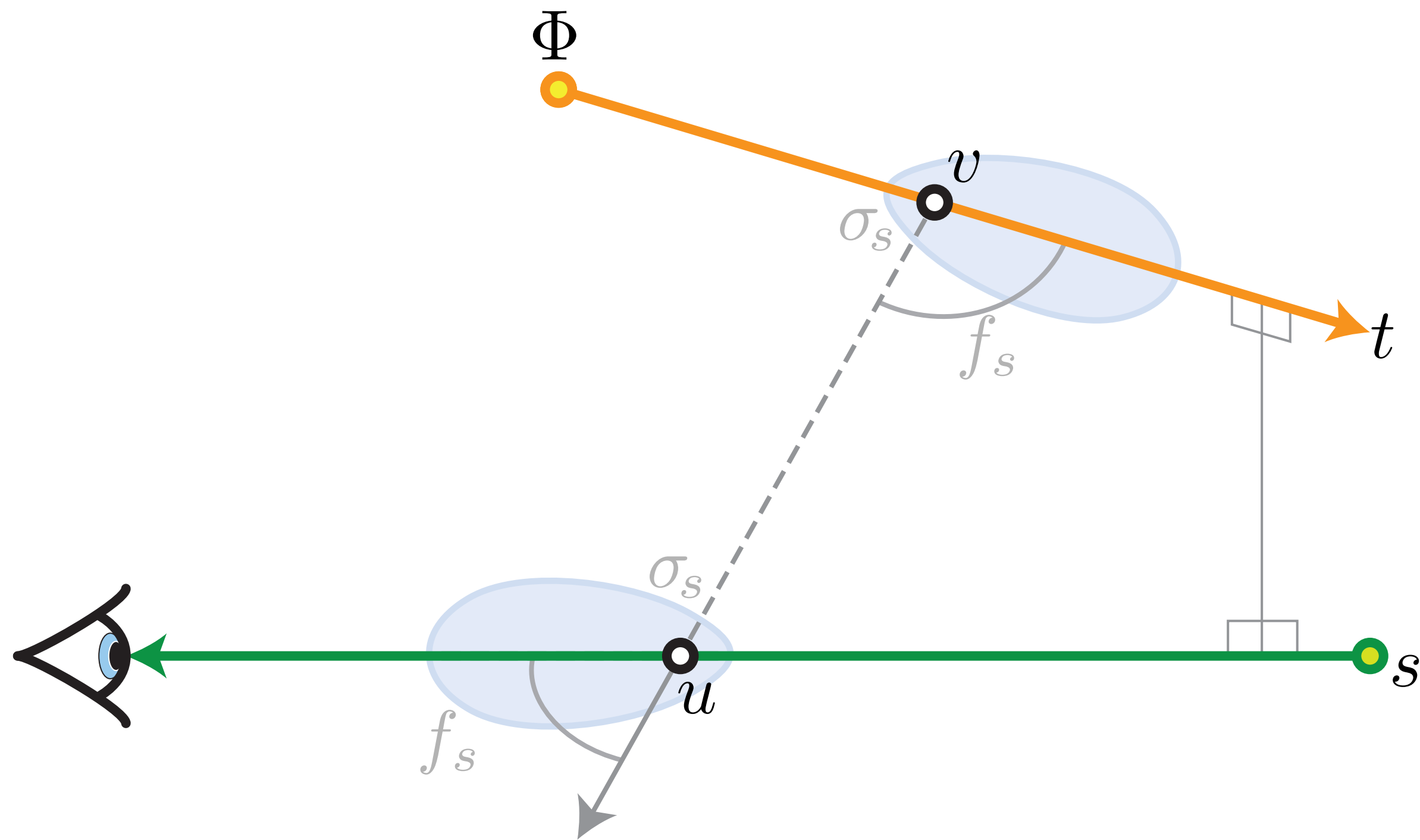
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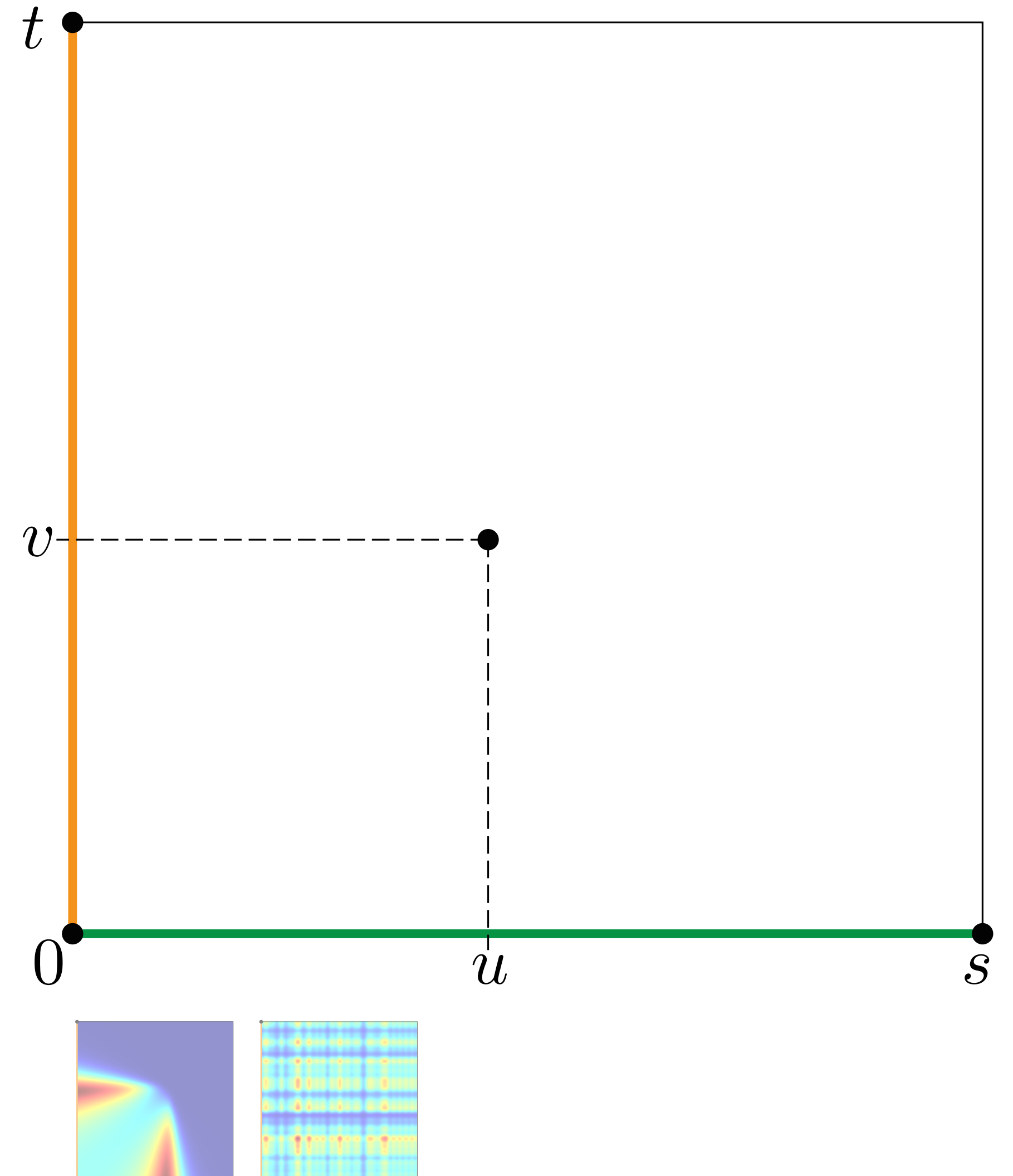
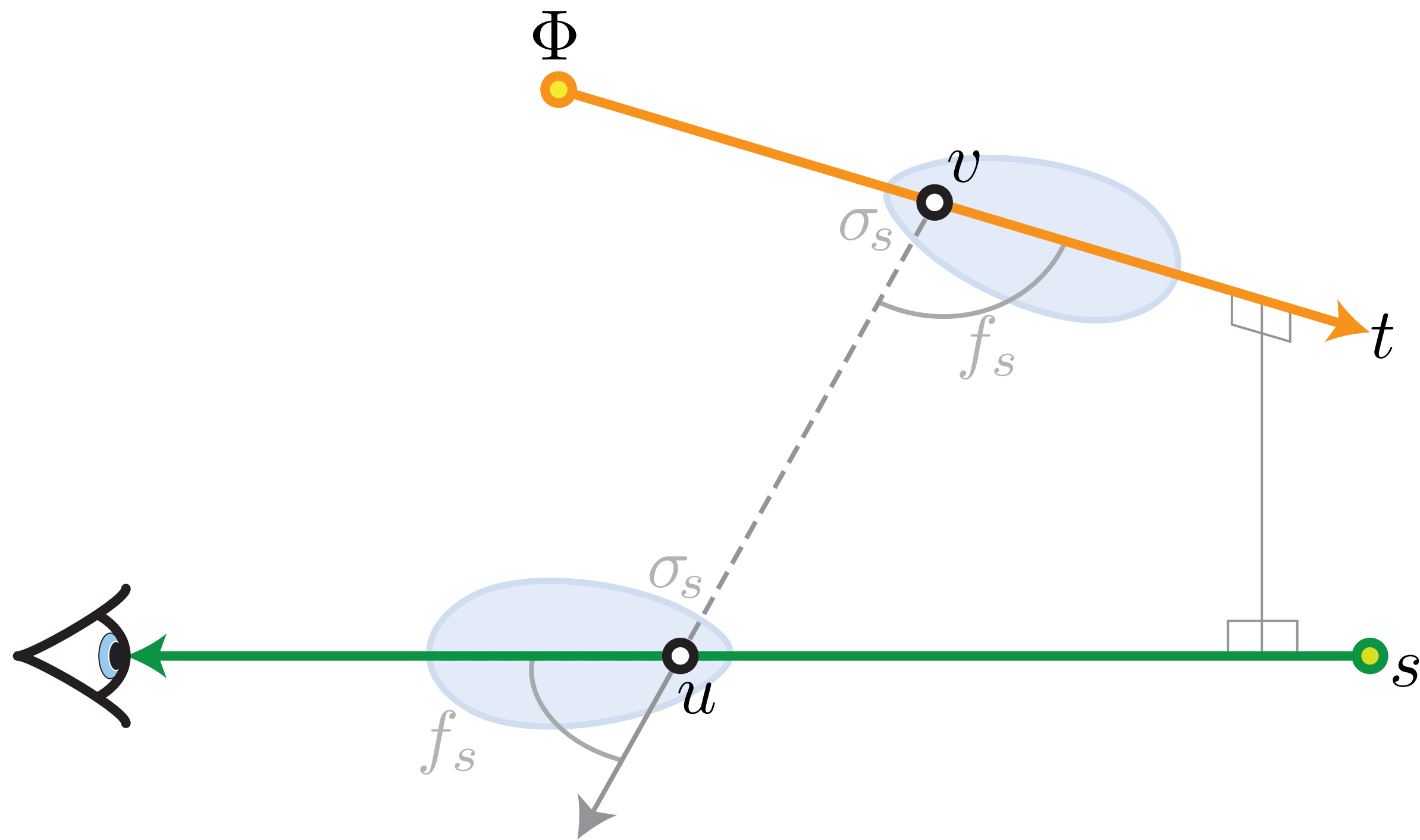
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$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v)}{dvdu}$$



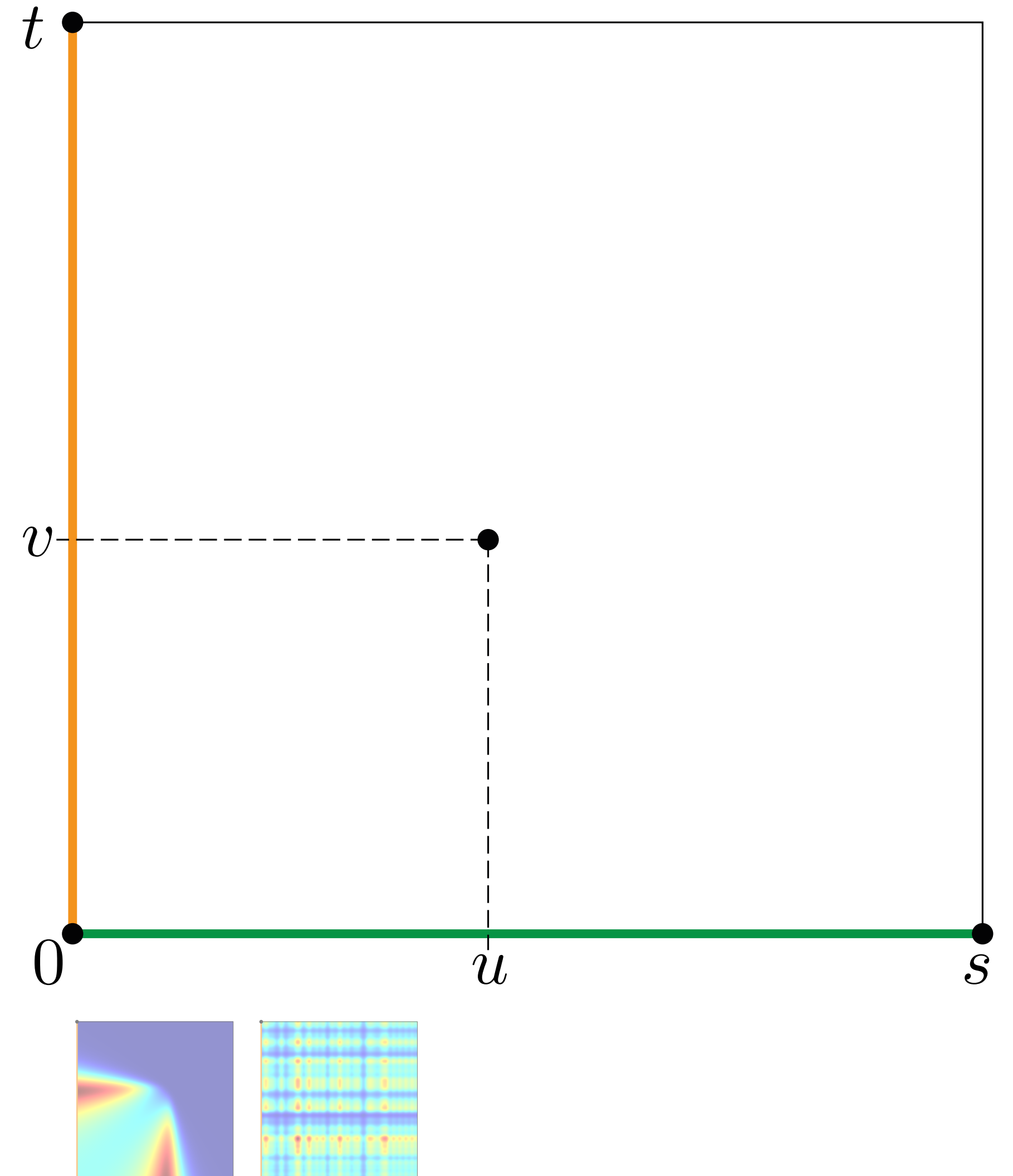
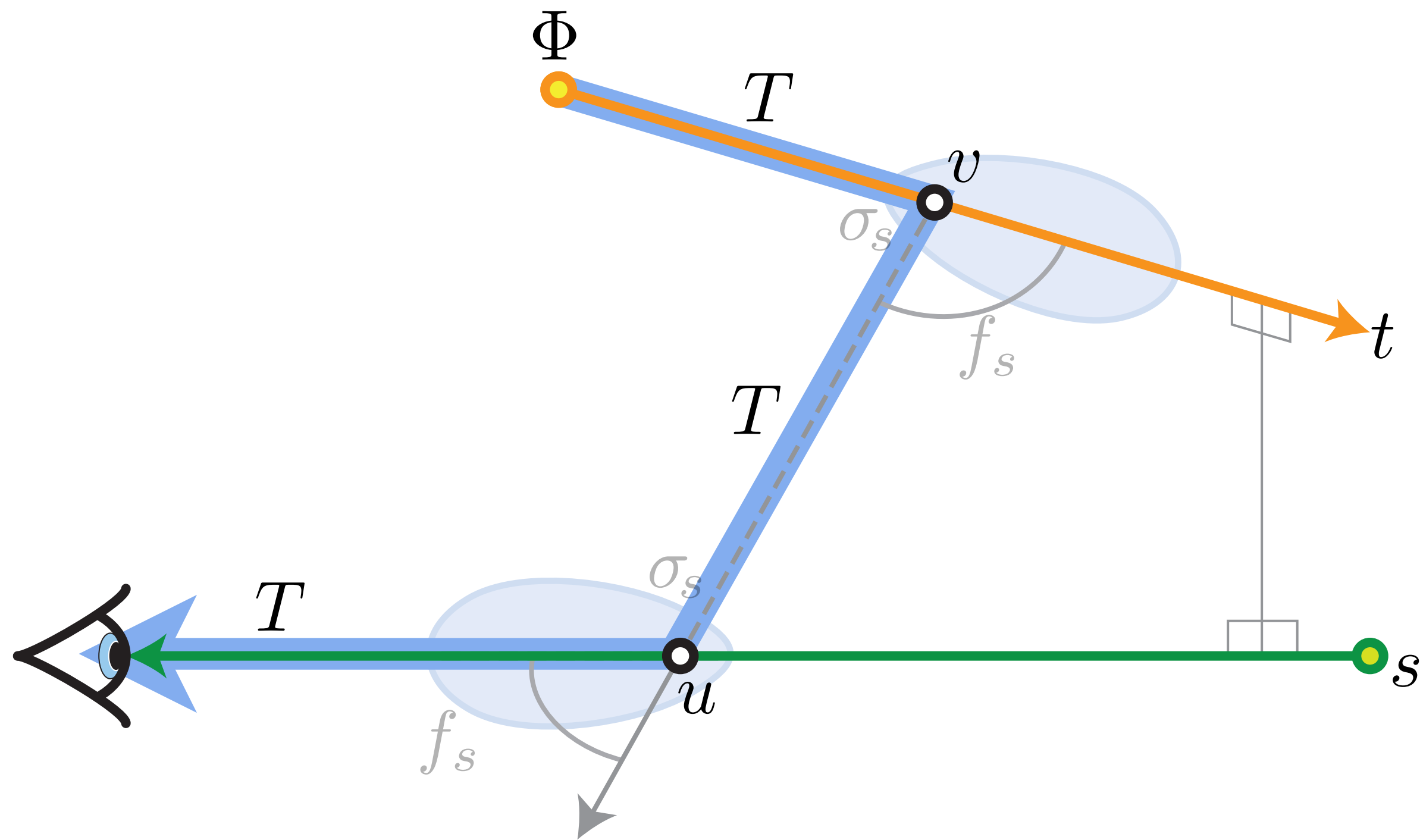
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w)}{\text{transmittance}} dv du$$



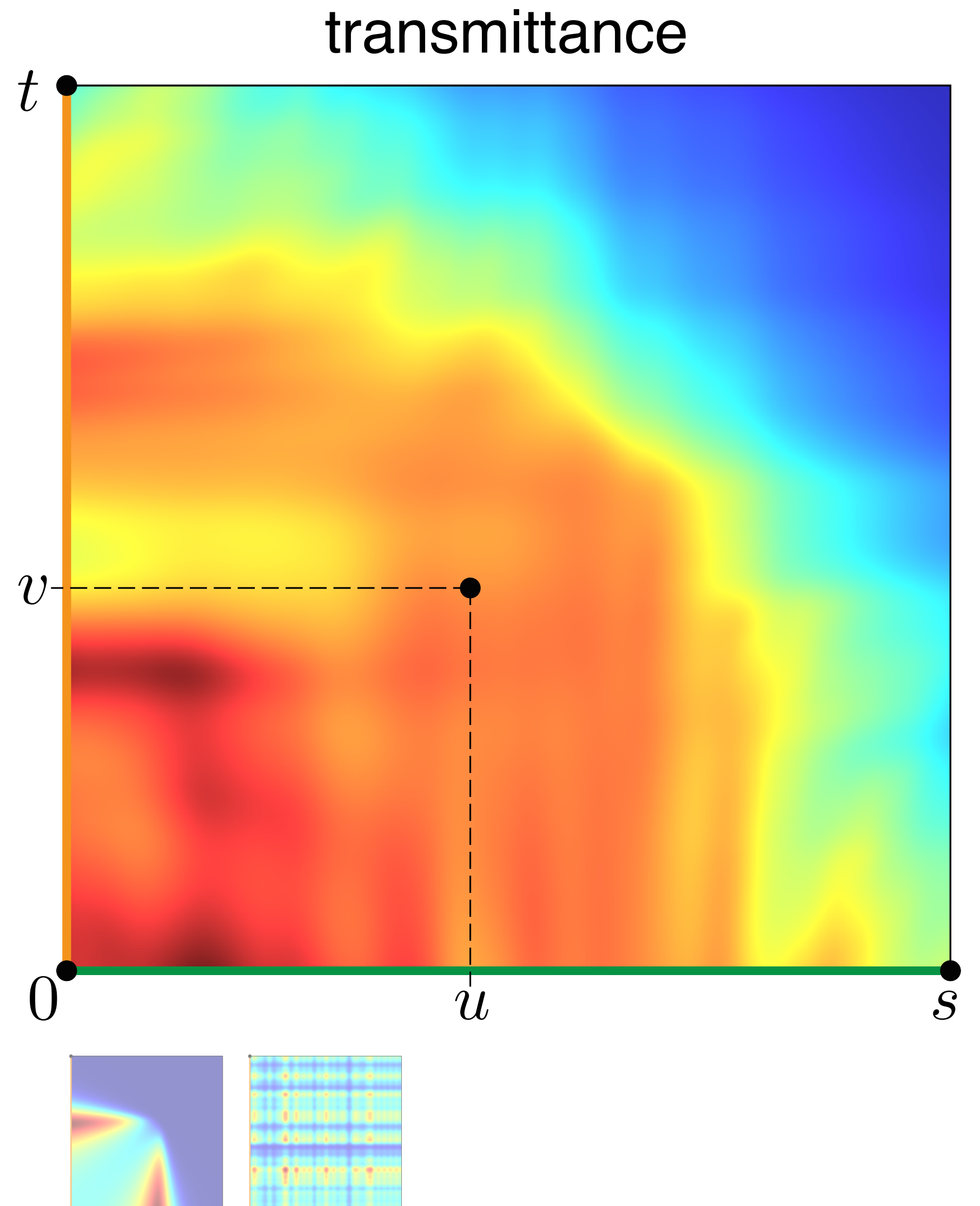
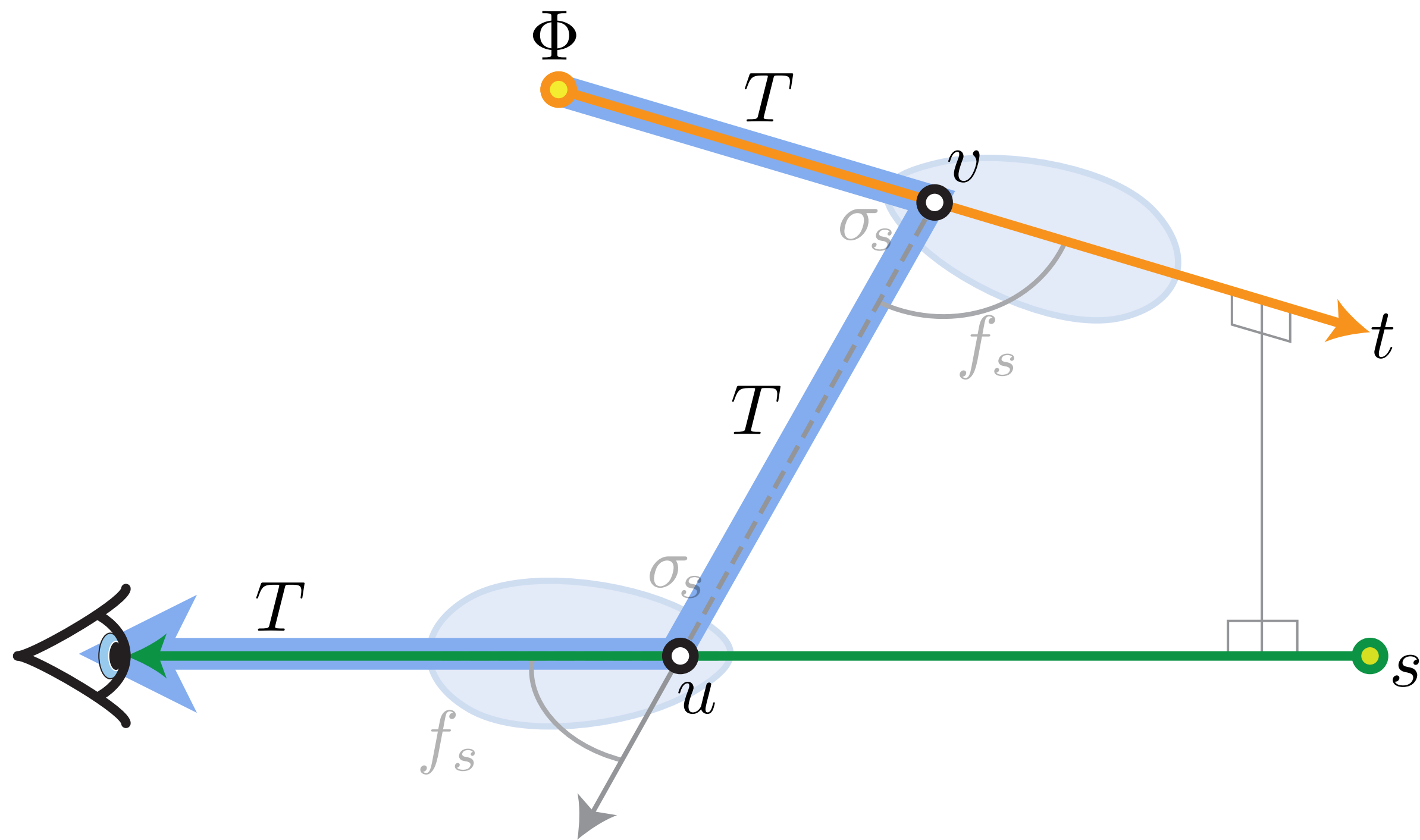
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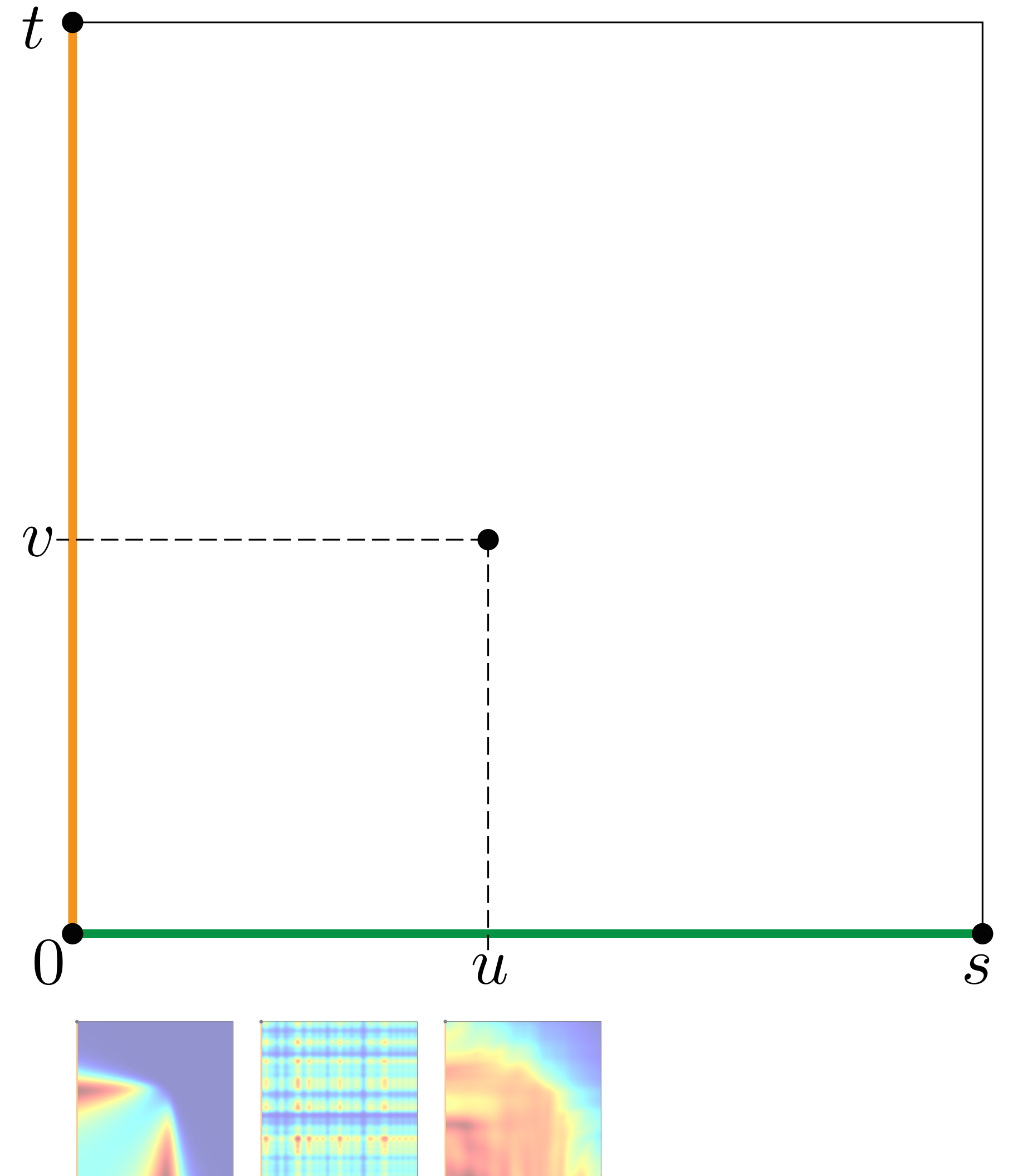
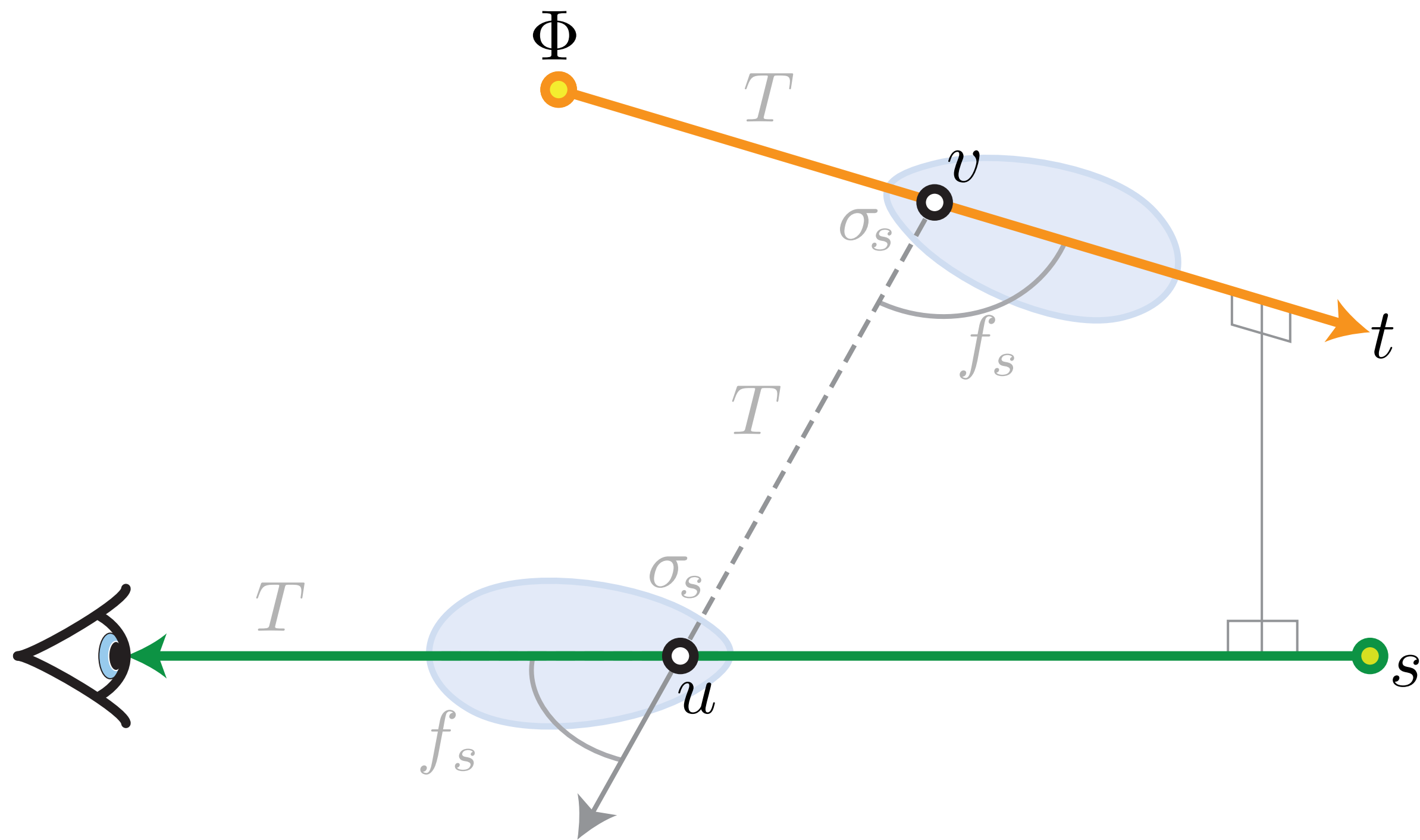
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w)}{dv du}$$



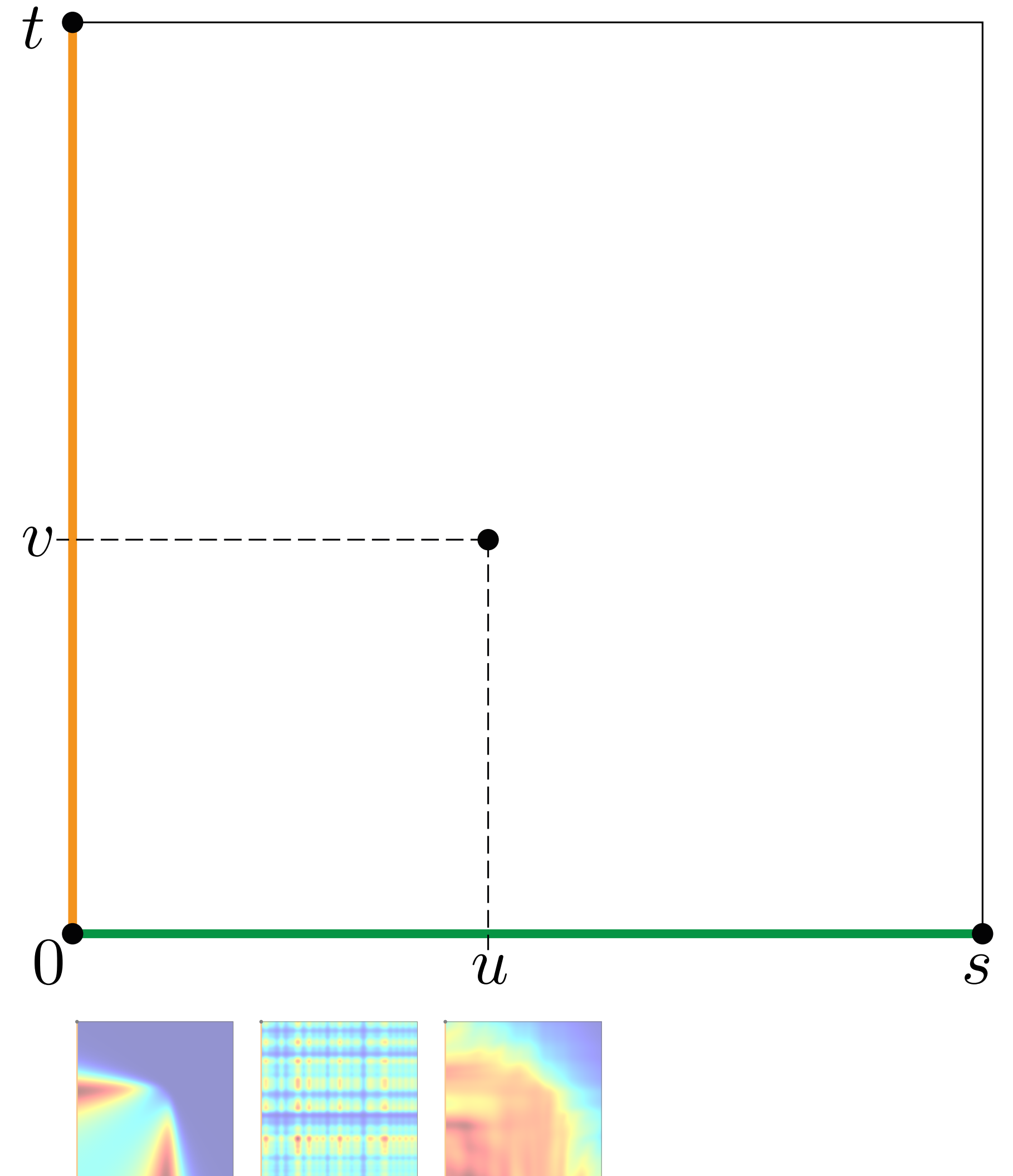
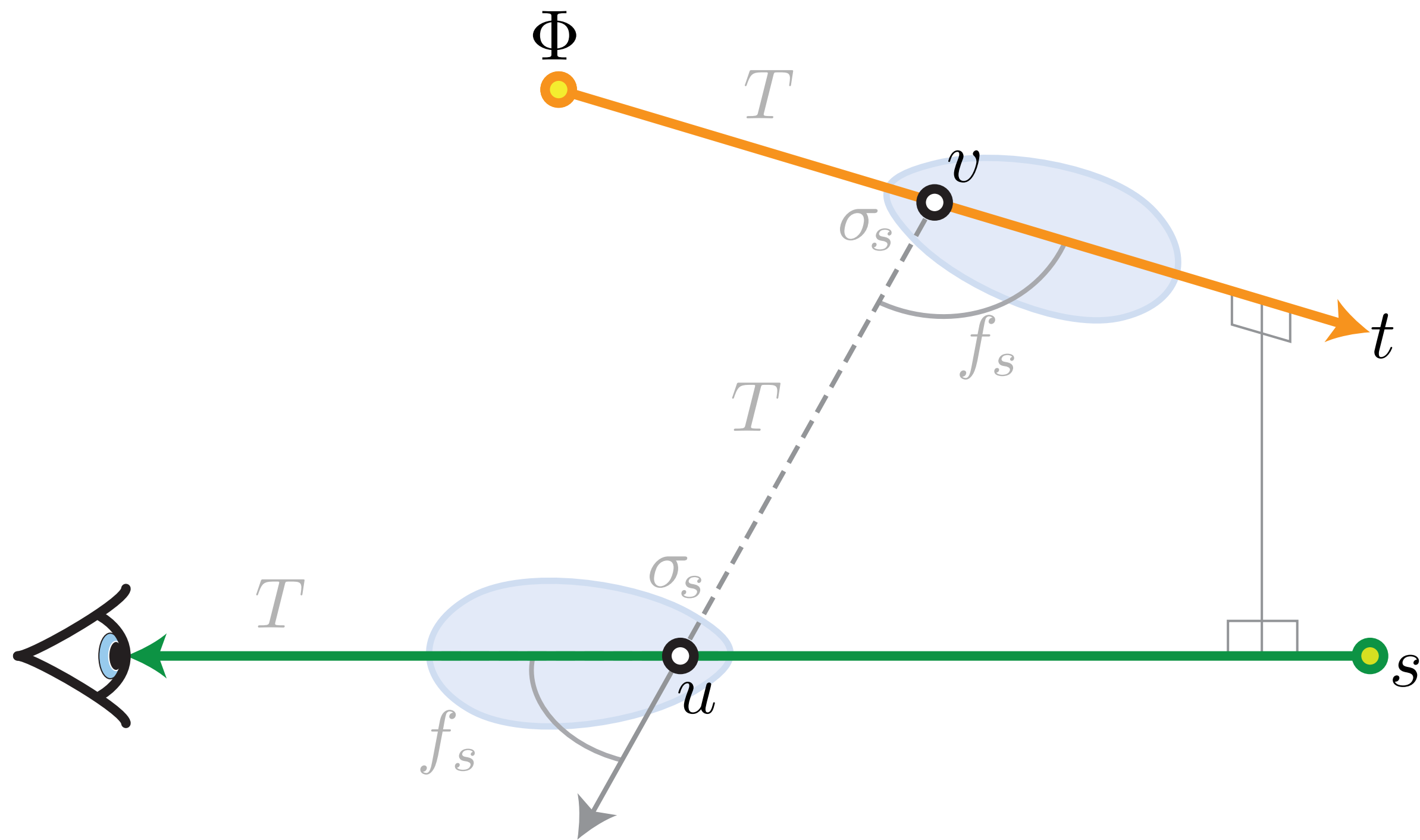
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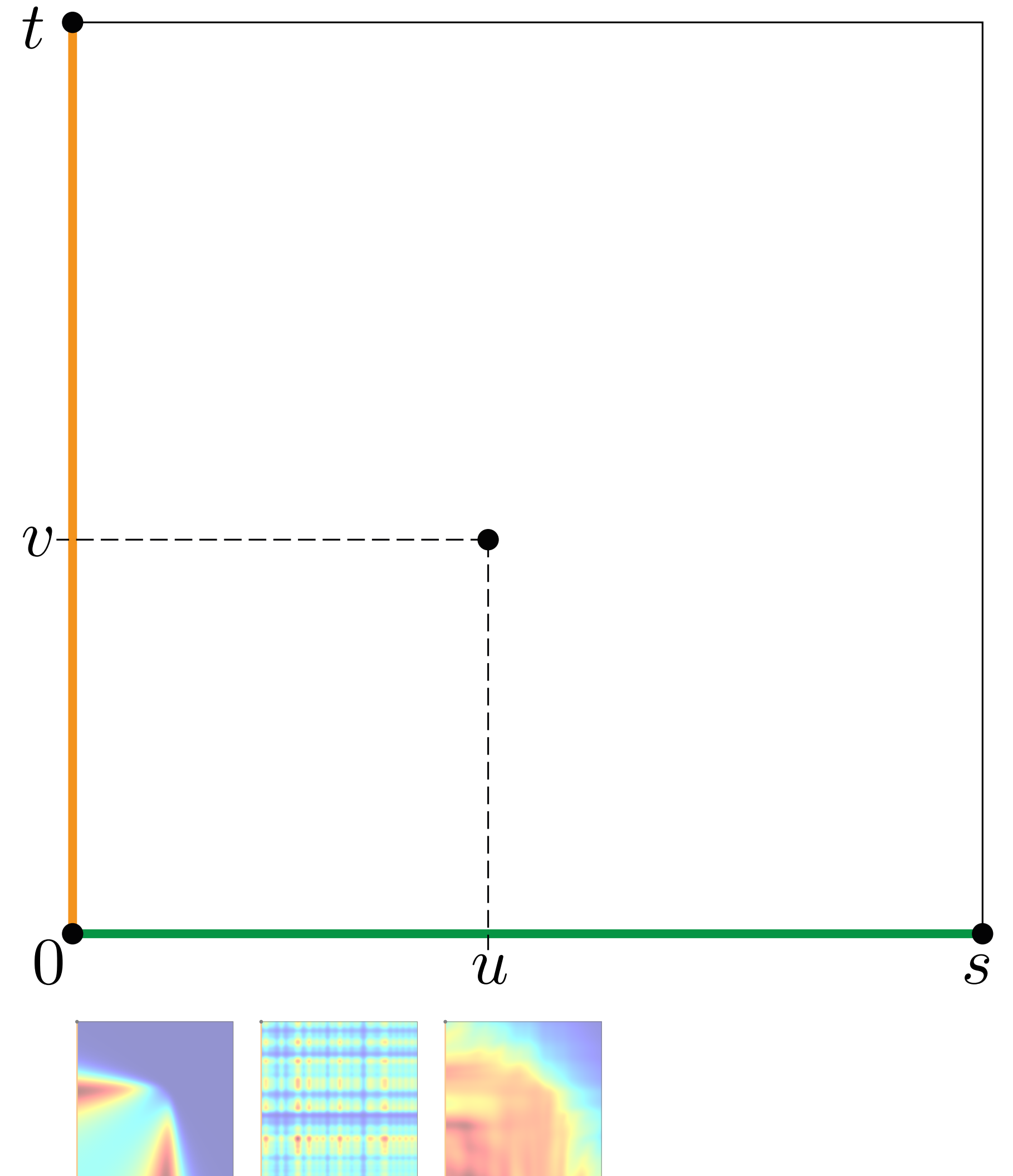
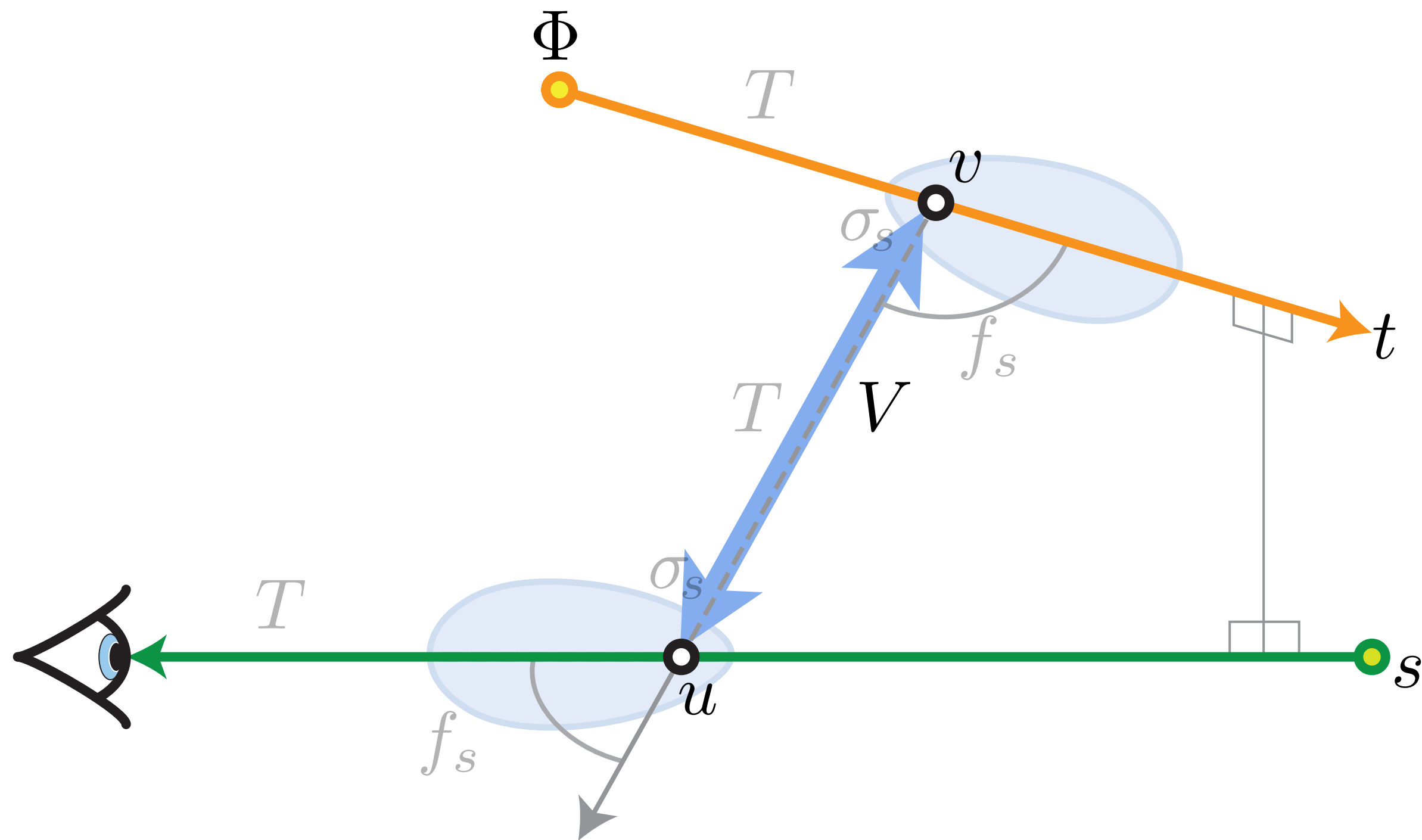
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{\text{visibility}} dv du$$



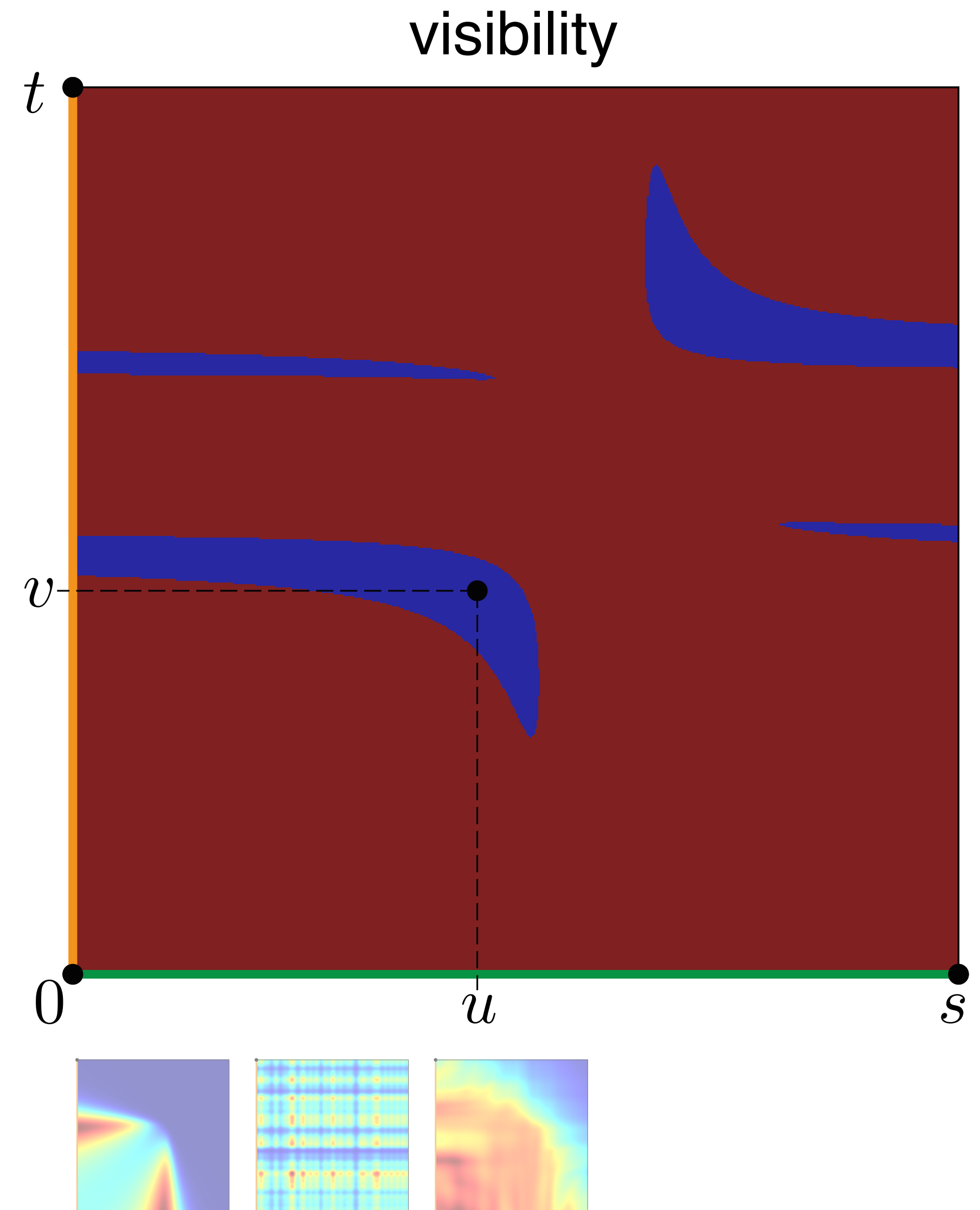
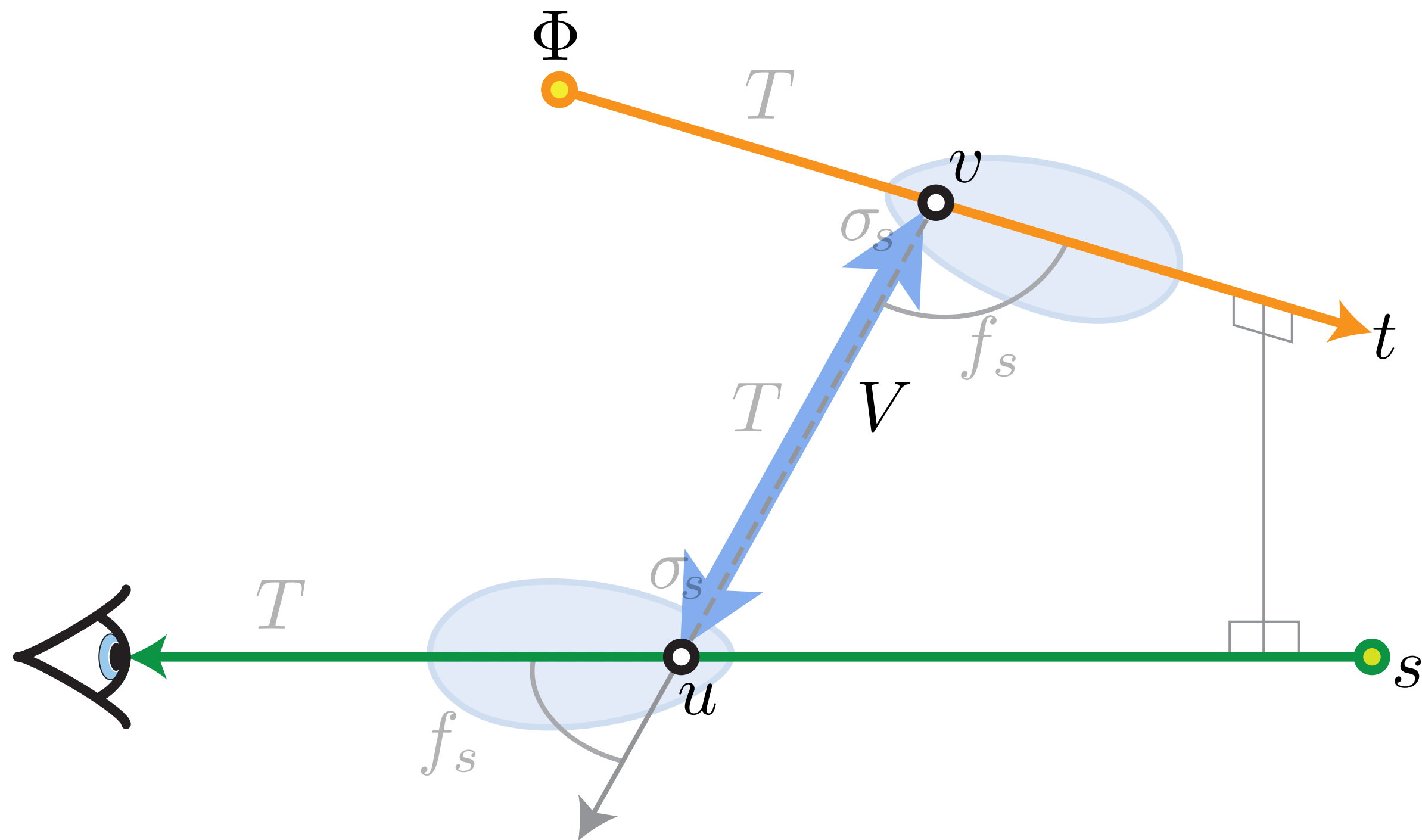
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{\text{visibility}} dv du$$



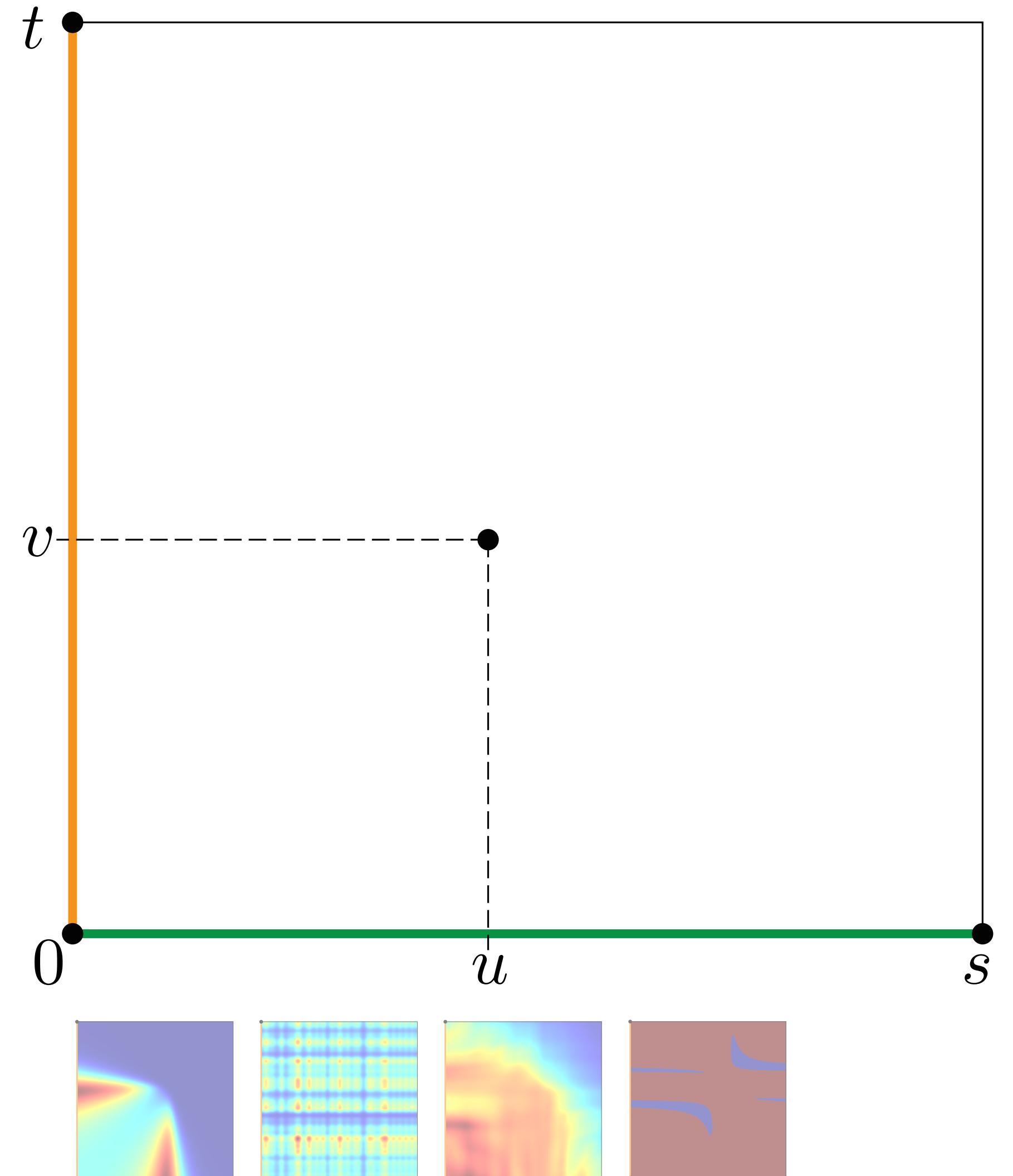
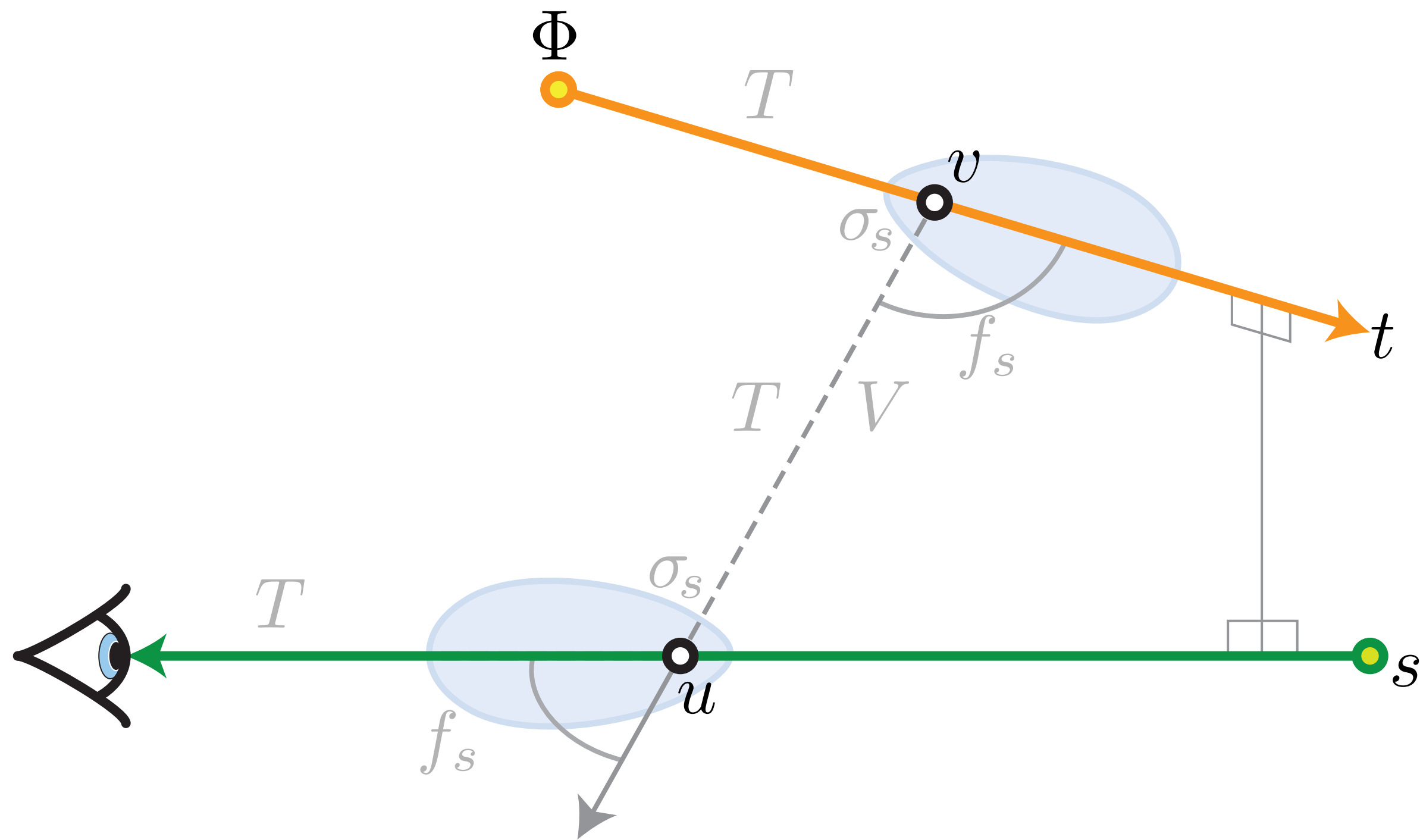
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{\text{visibility}} dv du$$



Ray-to-Ray transport

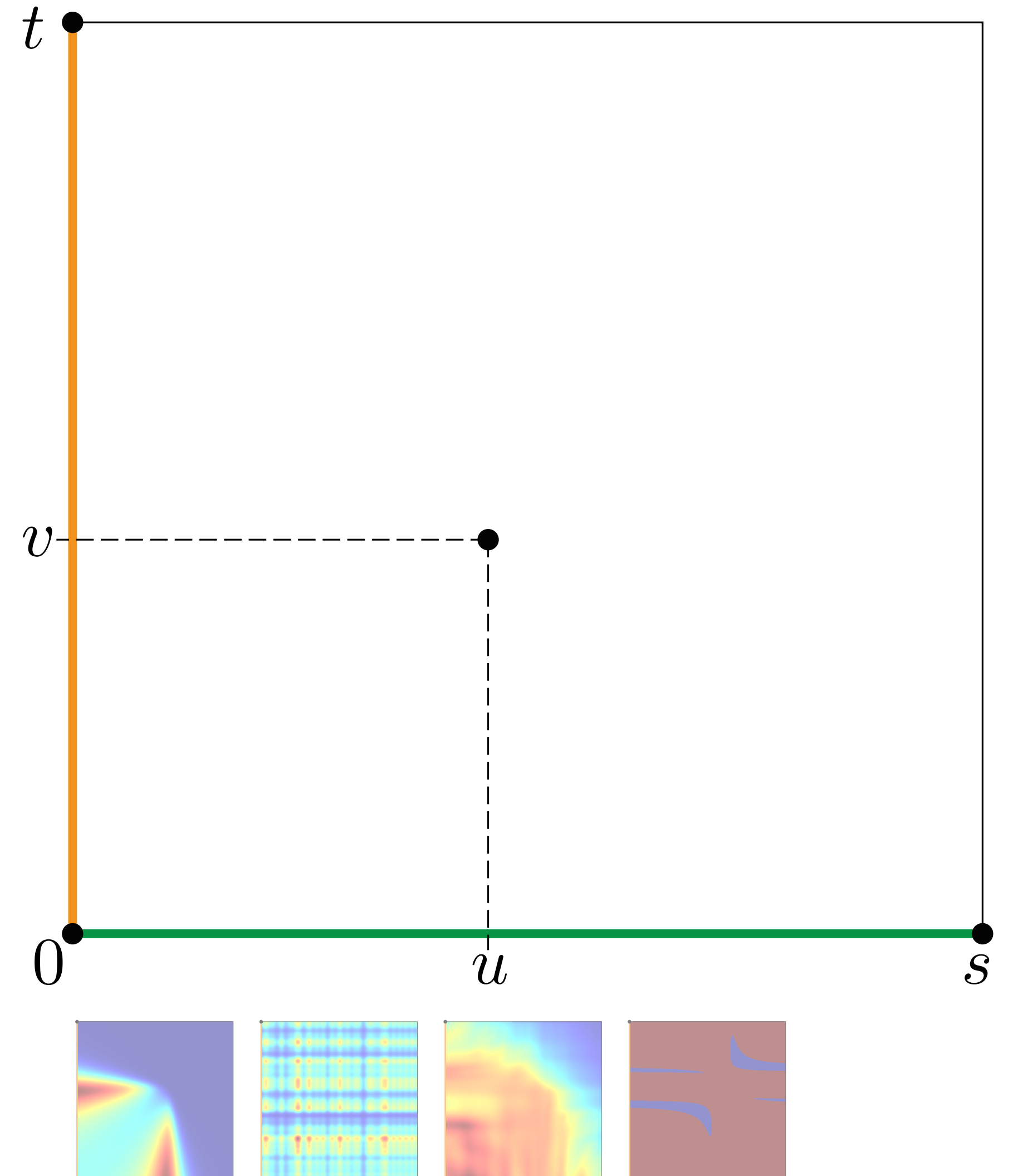
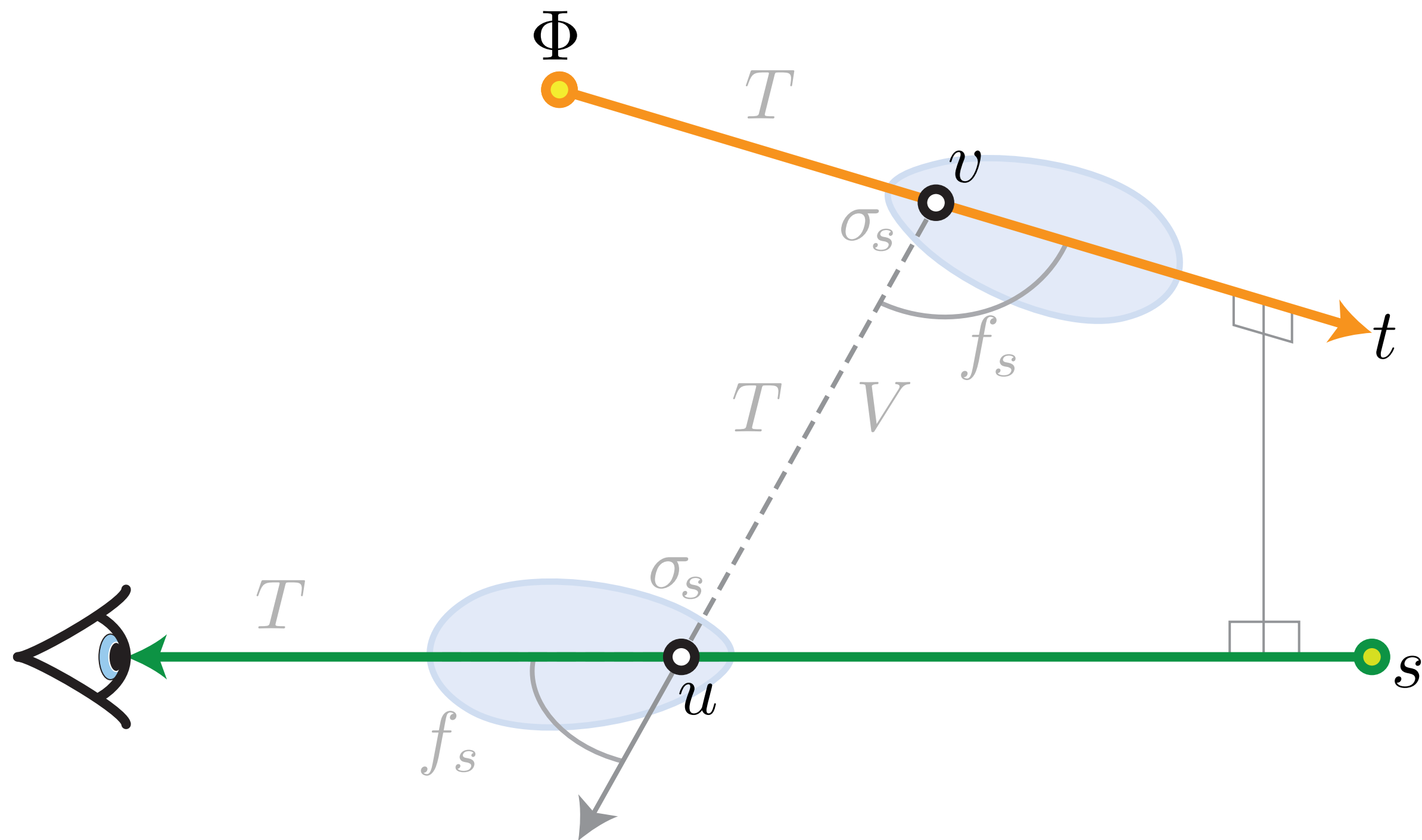
$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{\text{d}v \text{d}u}$$



Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{w(u, v)^2} dv du$$

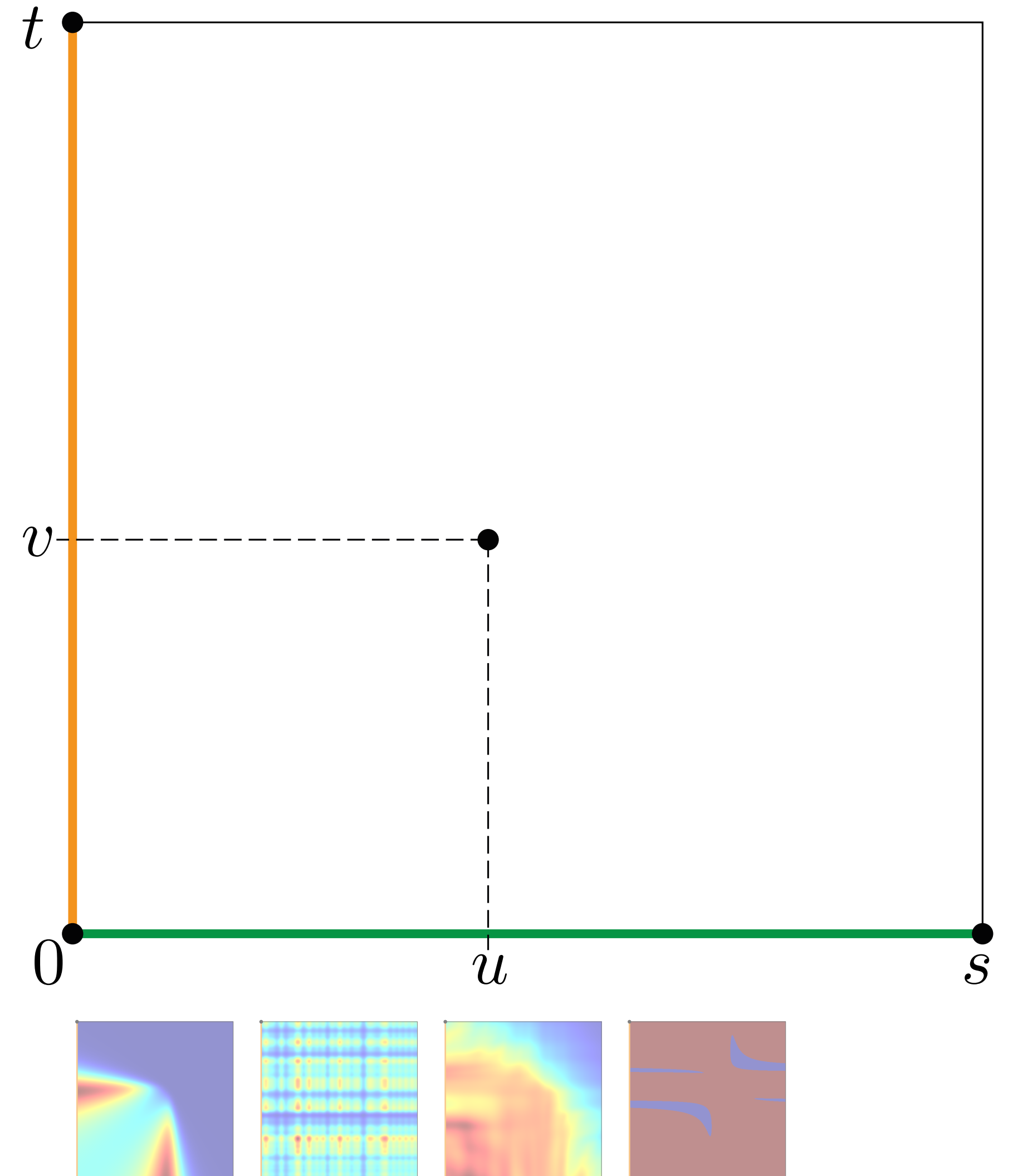
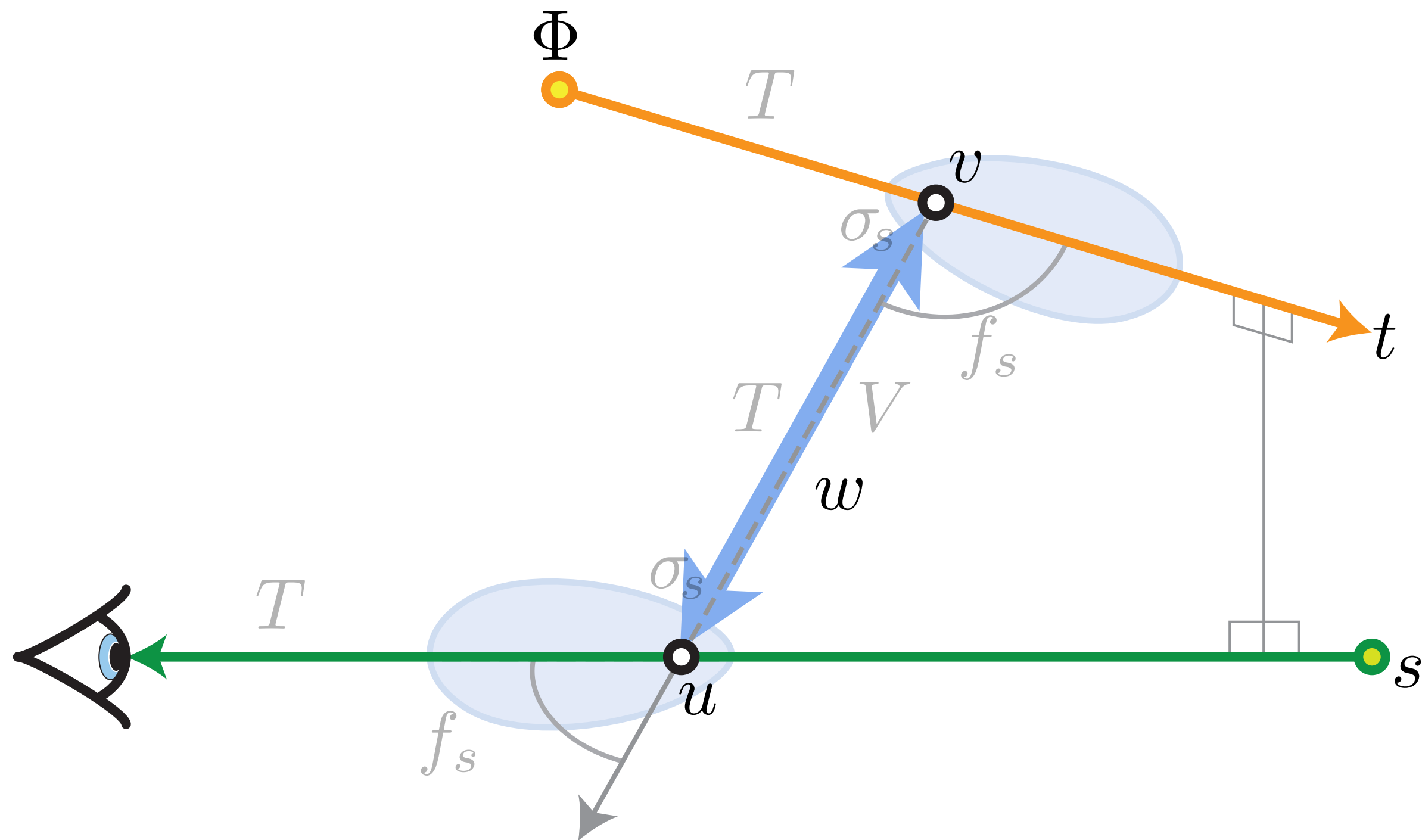
squared distance



Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{w(u, v)^2} dv du$$

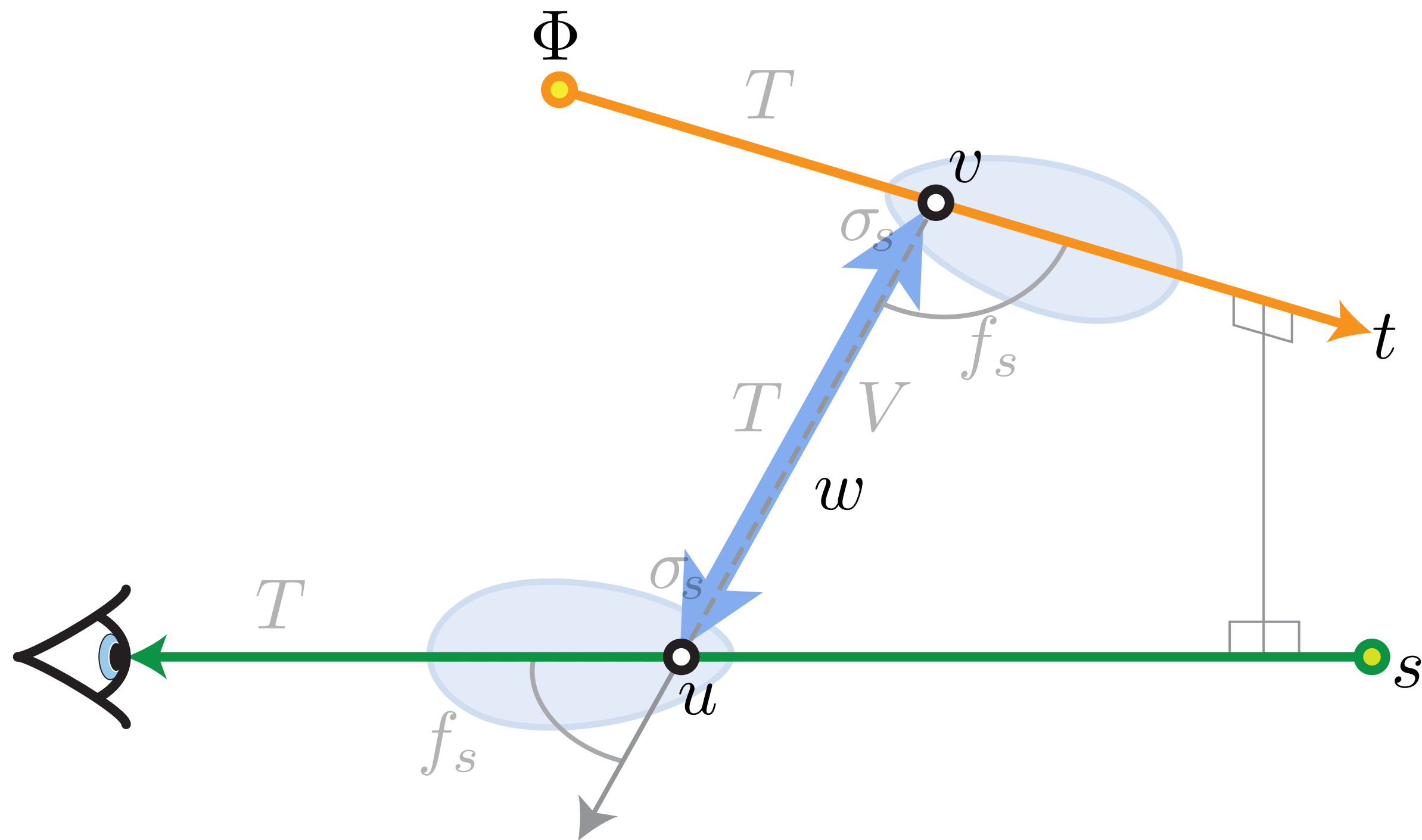
squared distance



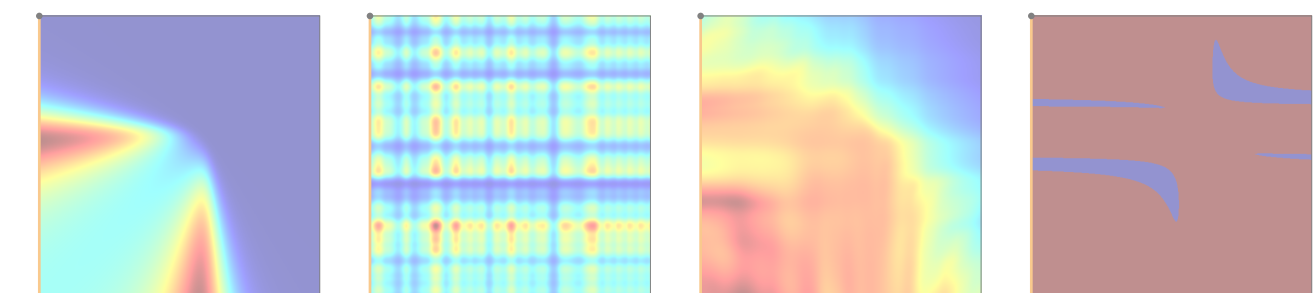
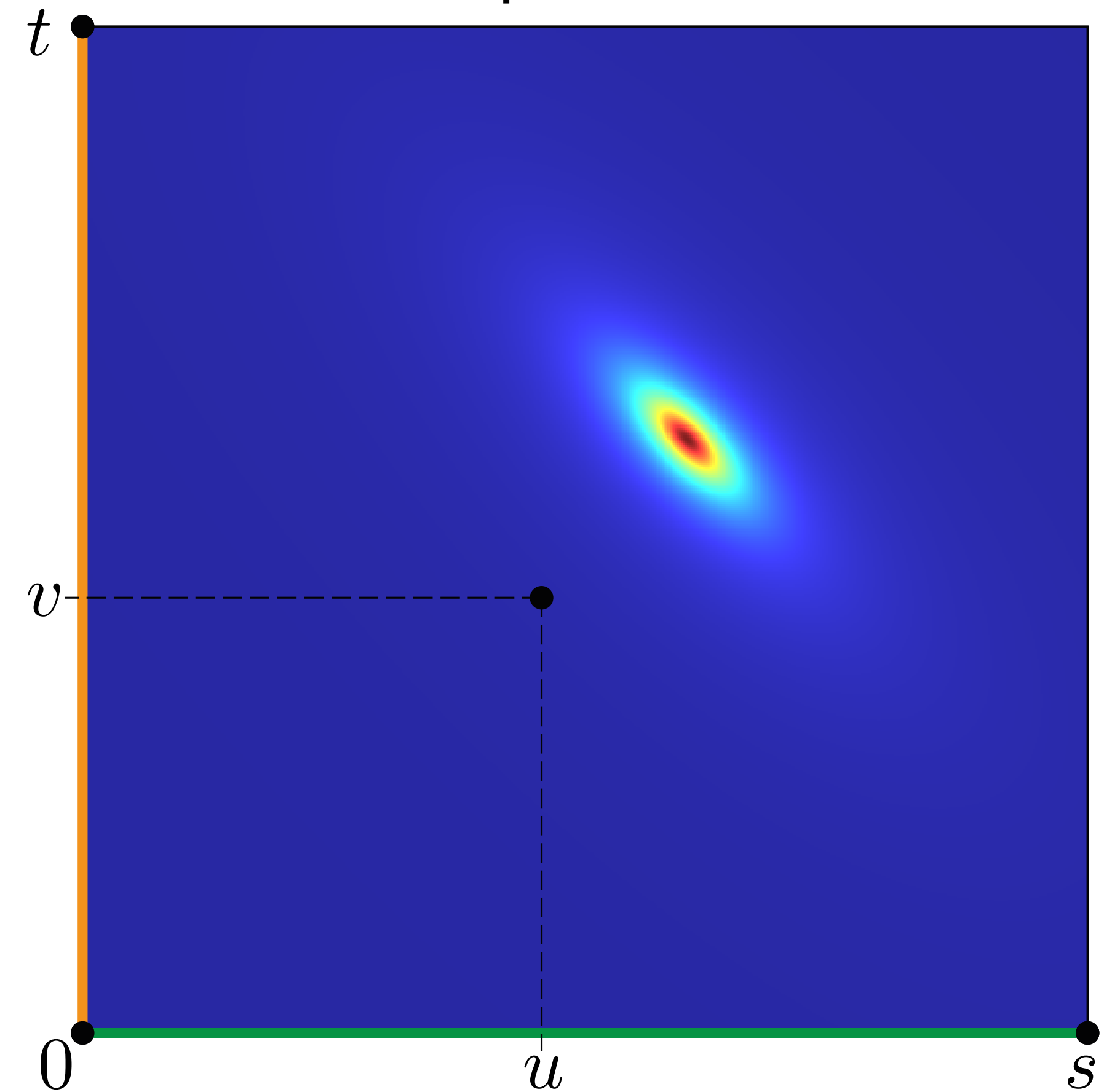
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{w(u, v)^2} dv du$$

squared distance

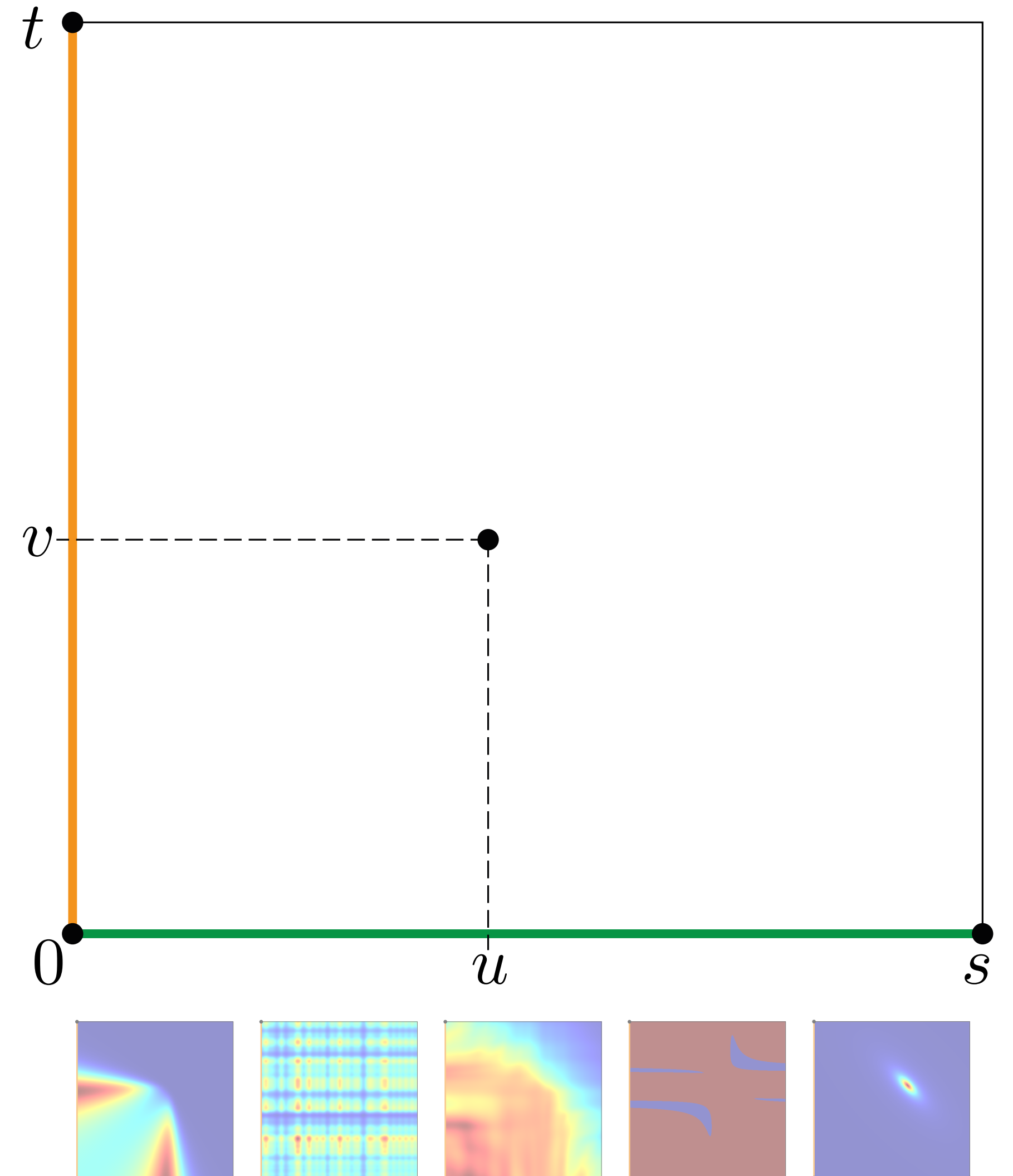
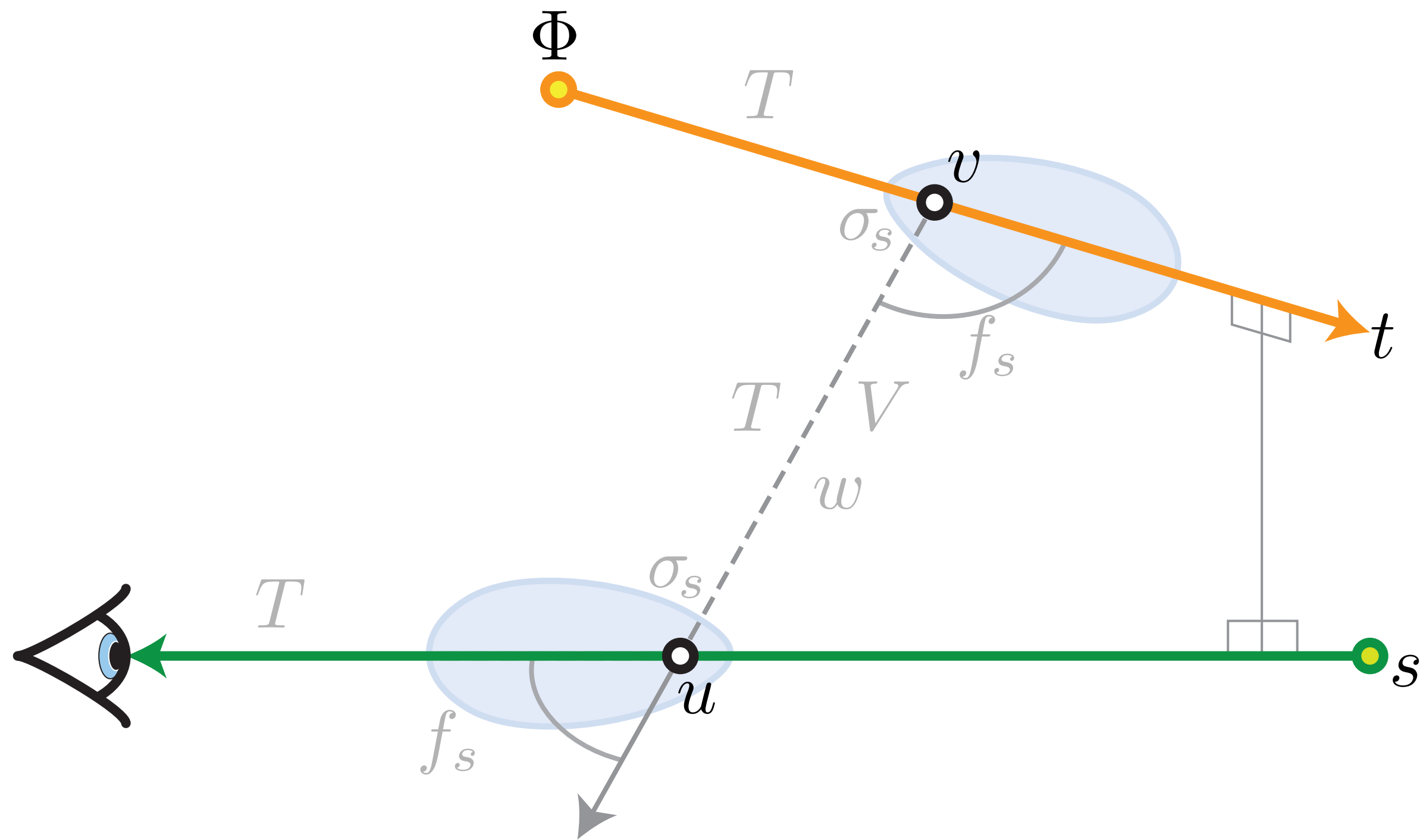


inverse squared distance



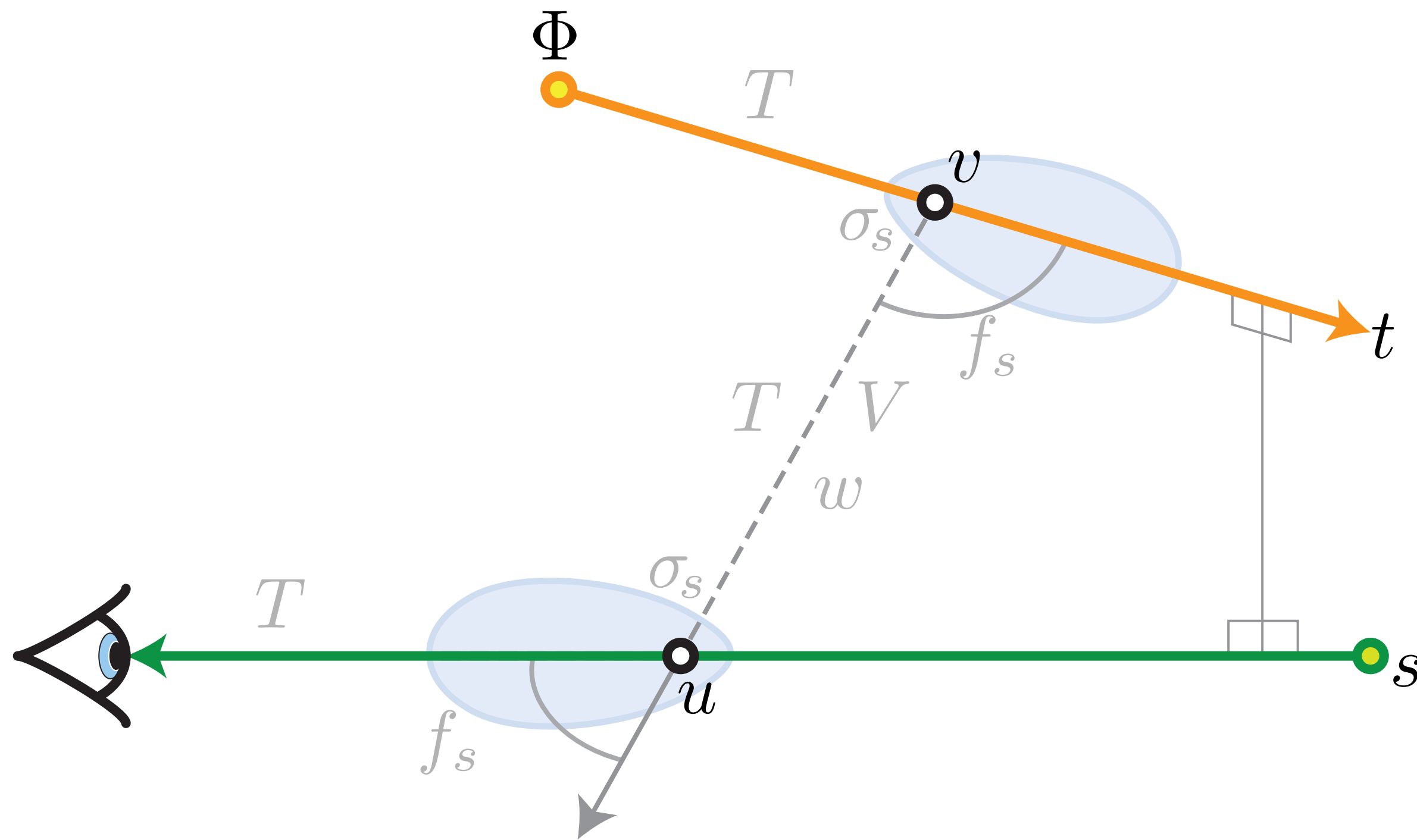
Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{w(u, v)^2} dv du$$

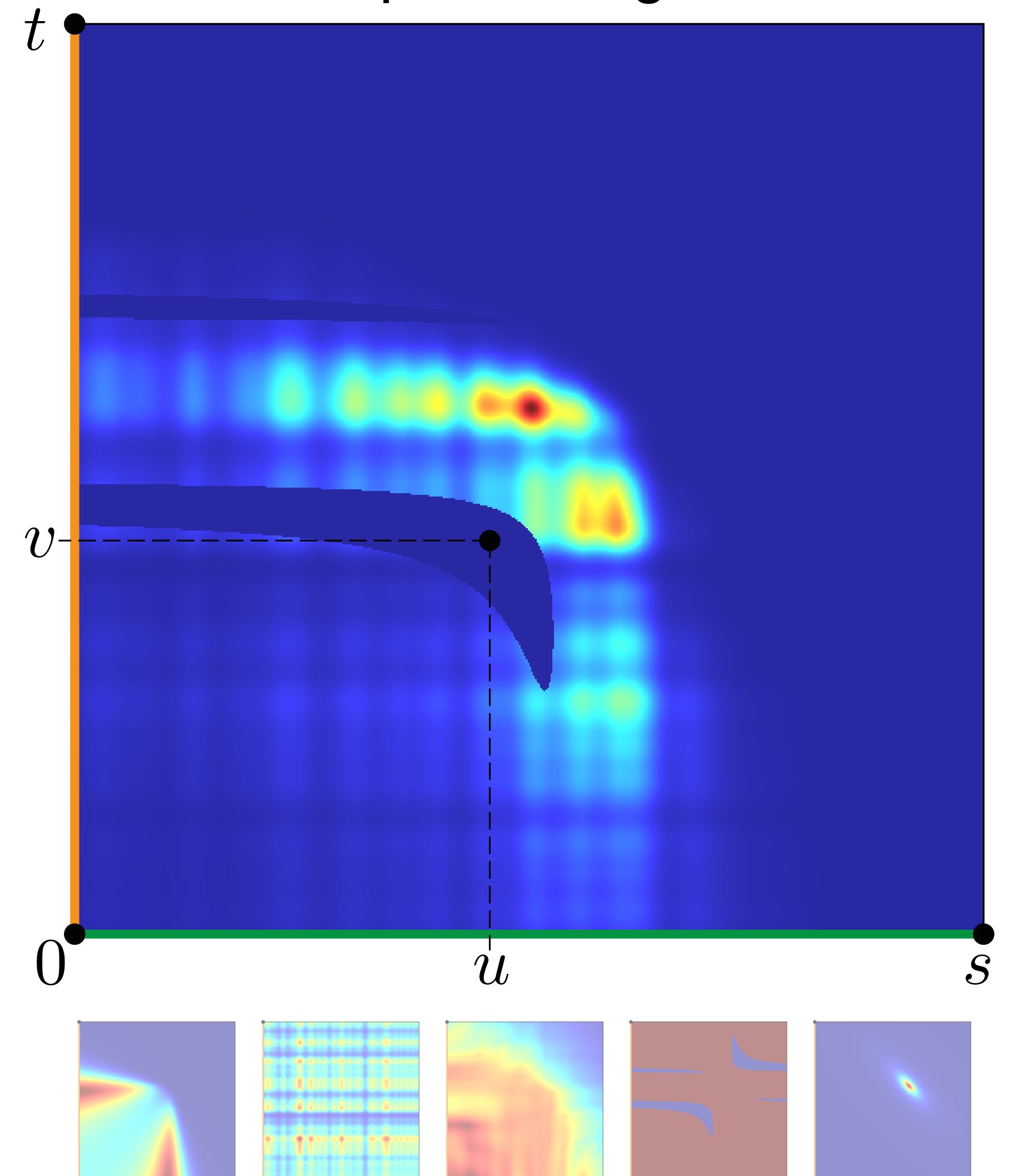


Ray-to-Ray transport

$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{w(u, v)^2} dv du$$

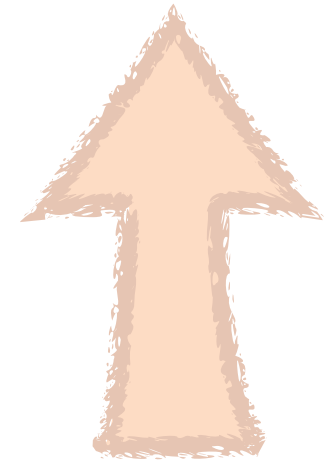


complete integrand

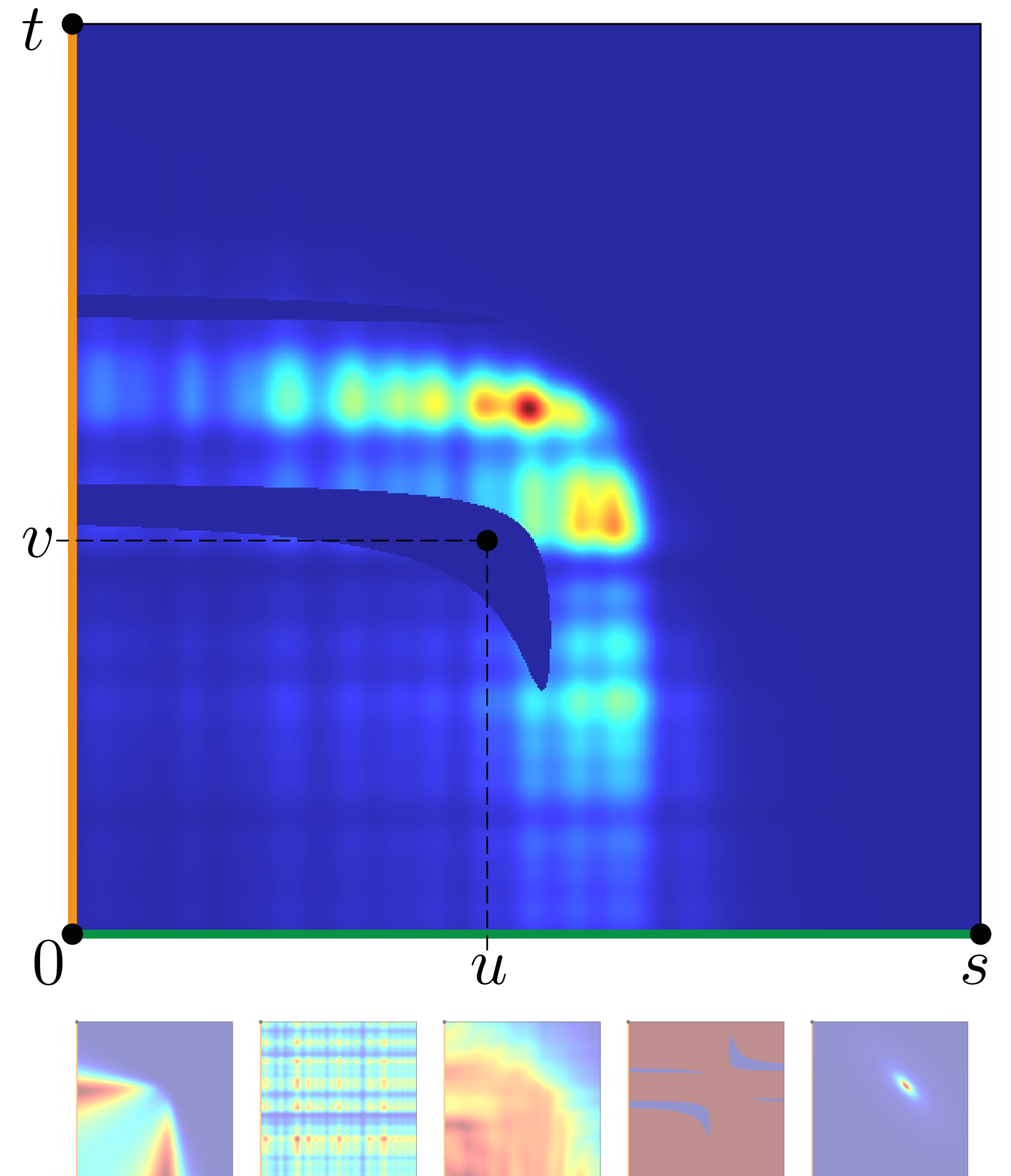


Ray-to-Ray transport

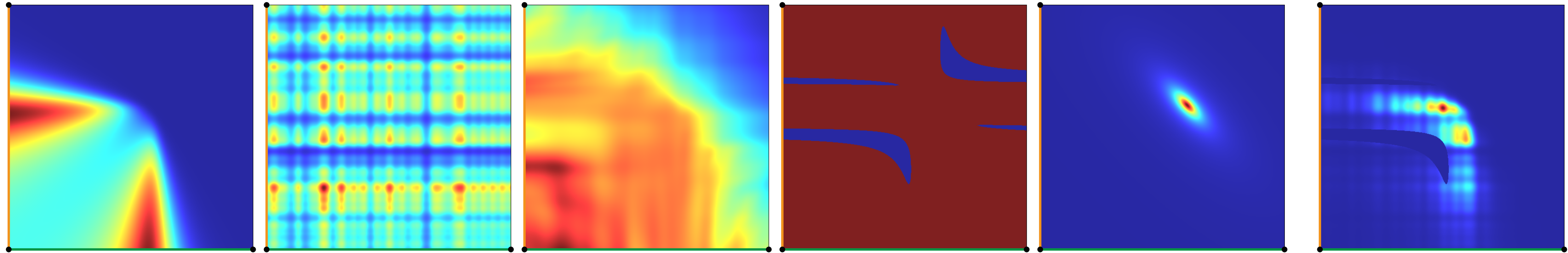
$$L = \Phi \int_0^s \int_0^t \frac{f_s(\theta_u) f_s(\theta_v) \sigma_s(u) \sigma_s(v) T(u) T(v) T(w) V}{w(u, v)^2} dv du$$



**approximate using Monte Carlo
with importance sampling**

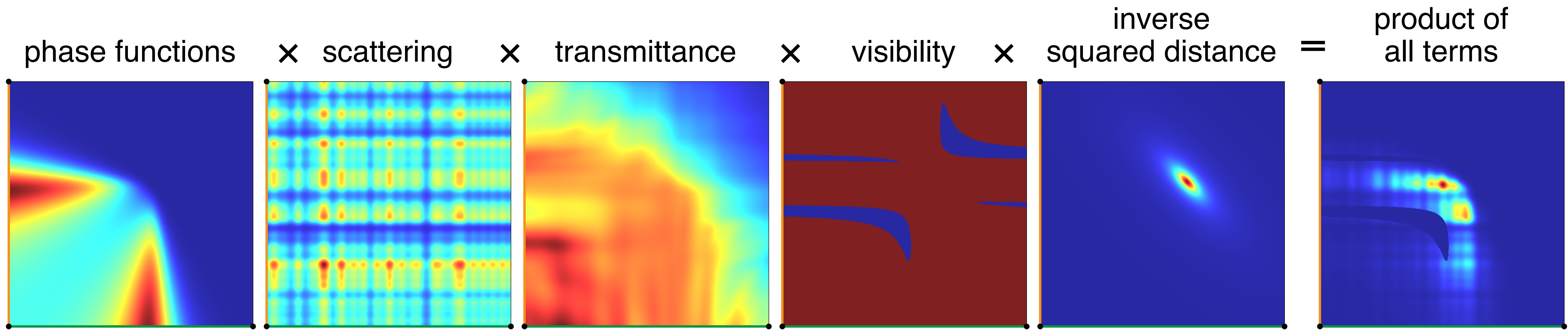


Importance sampling



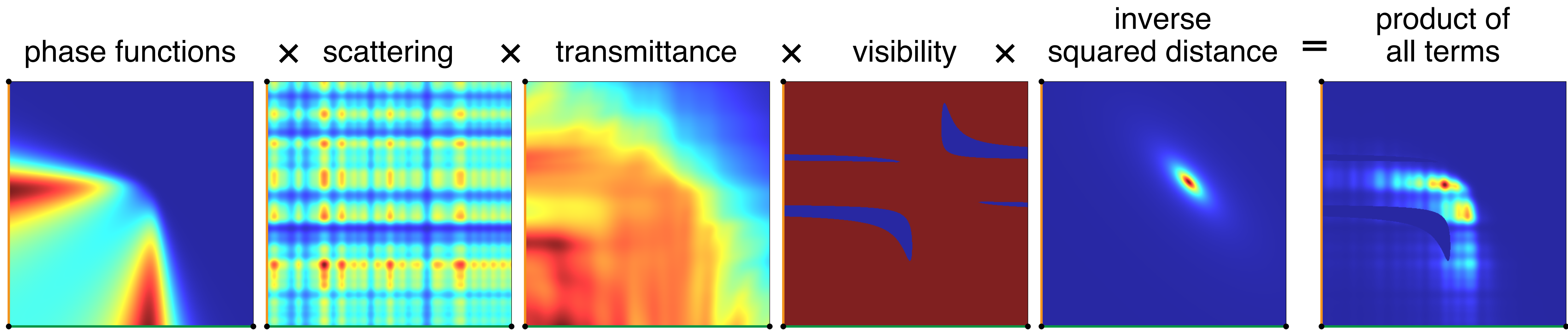
Importance sampling

How to (importance) sample?



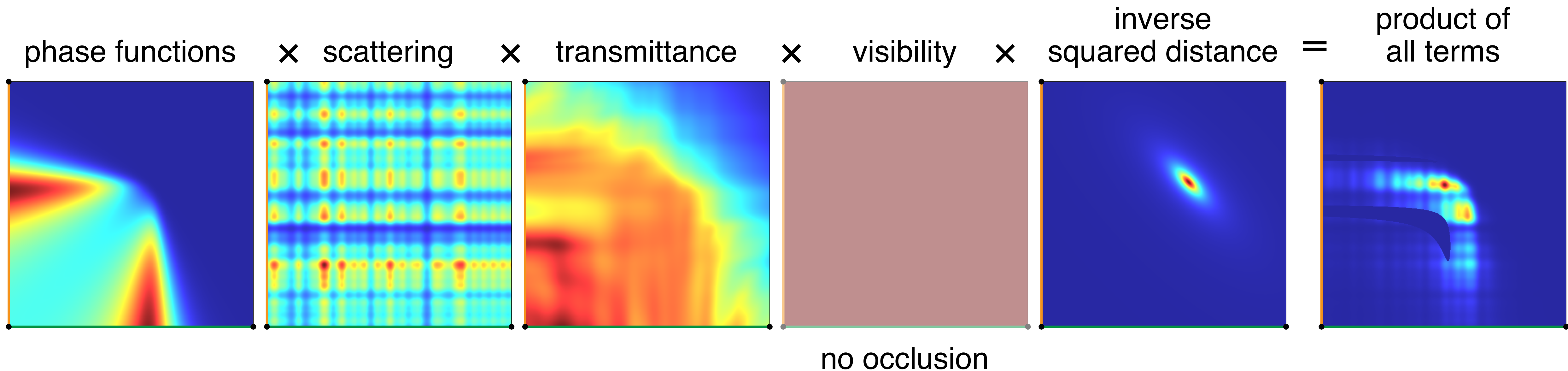
Importance sampling

How to (importance) sample?
Simple cases first!



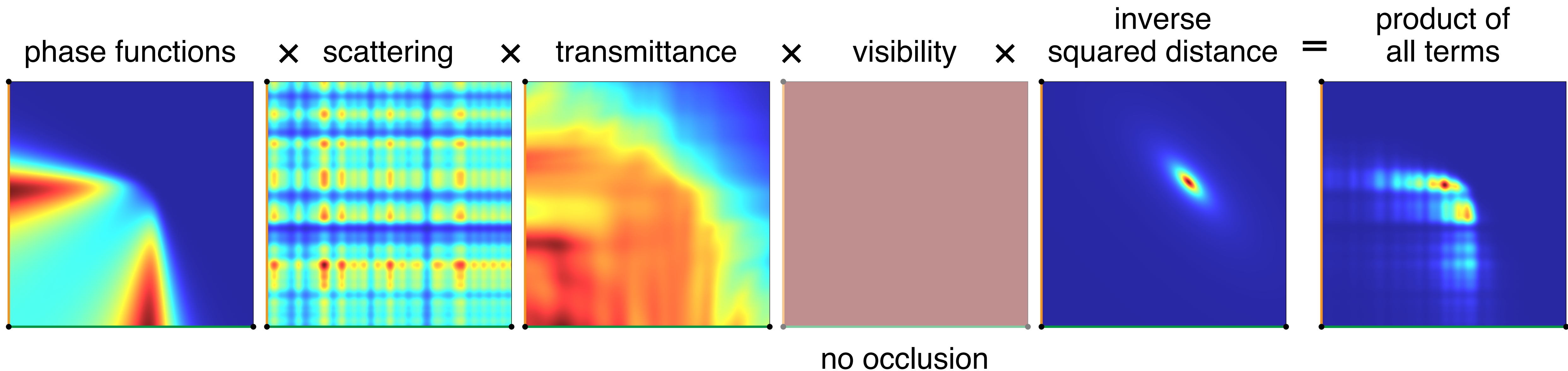
Importance sampling

How to (importance) sample?
Simple cases first!



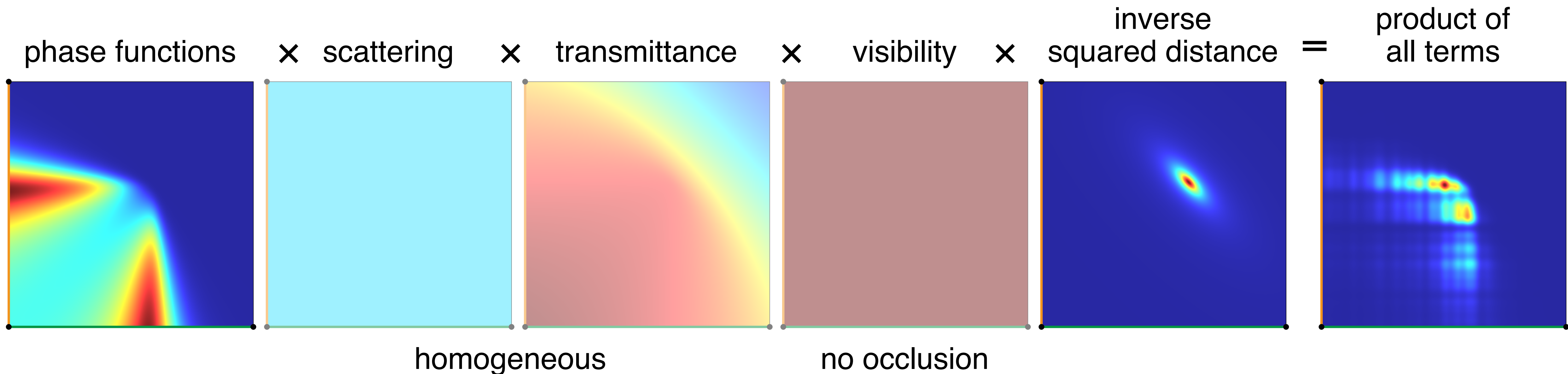
Importance sampling

How to (importance) sample?
Simple cases first!



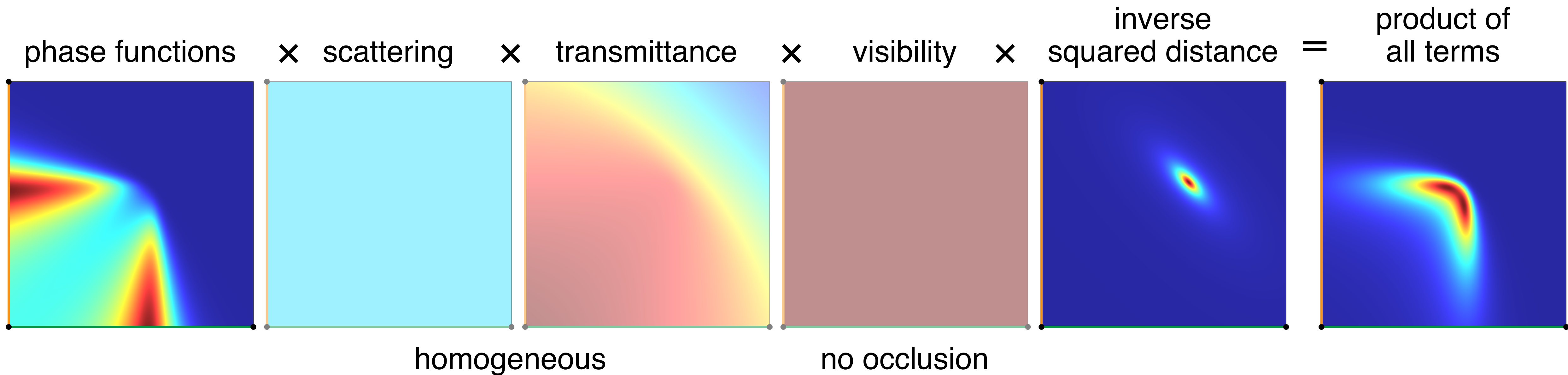
Importance sampling

How to (importance) sample?
Simple cases first!



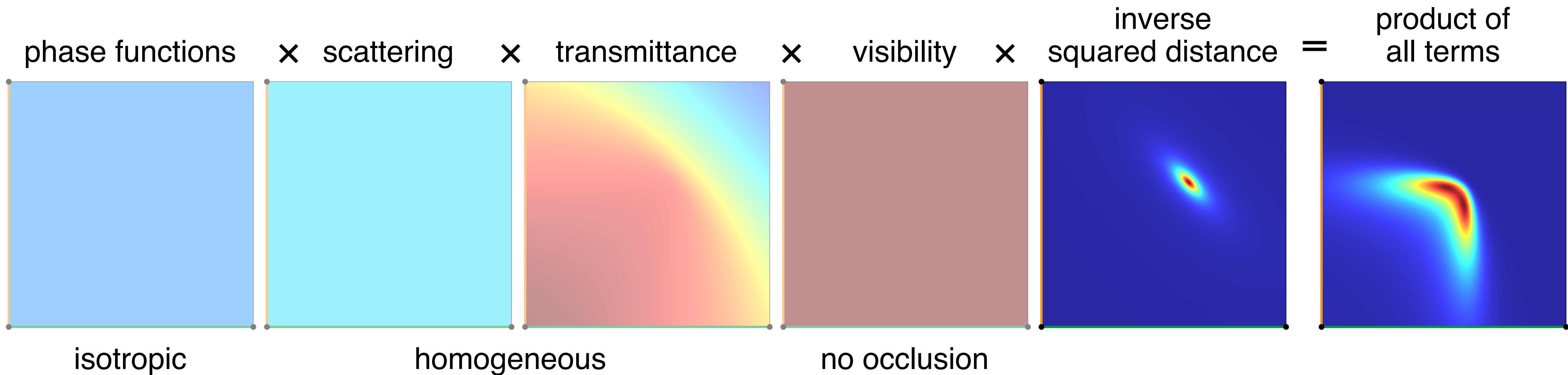
Importance sampling

How to (importance) sample?
Simple cases first!



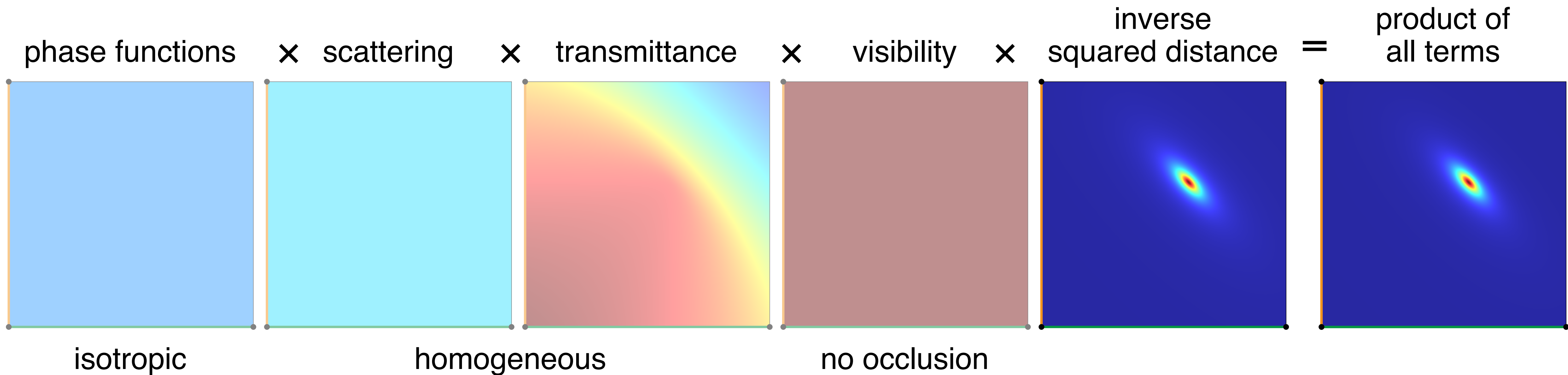
Importance sampling

How to (importance) sample?
Simple cases first!



Importance sampling

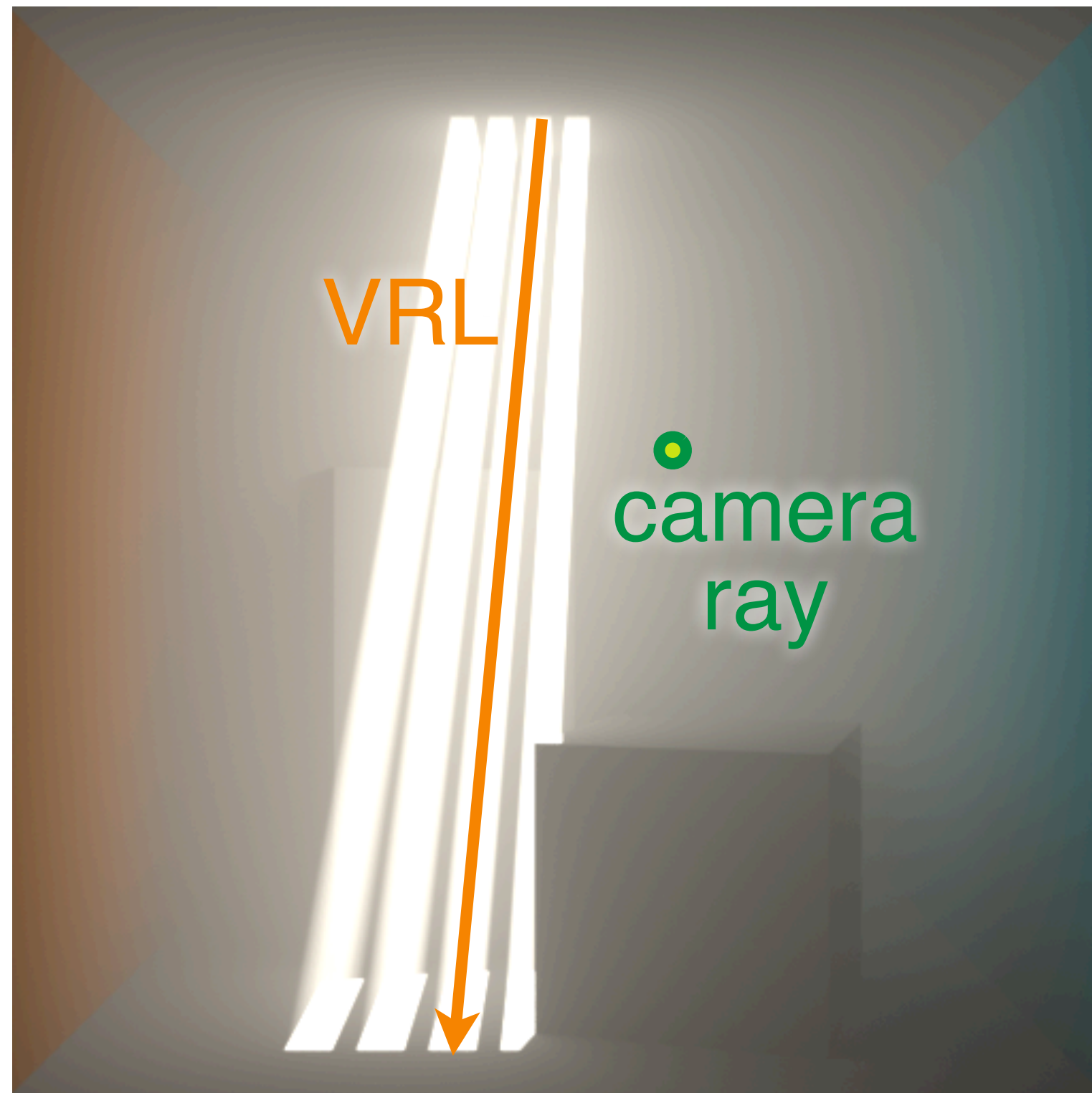
How to (importance) sample?
Simple cases first!



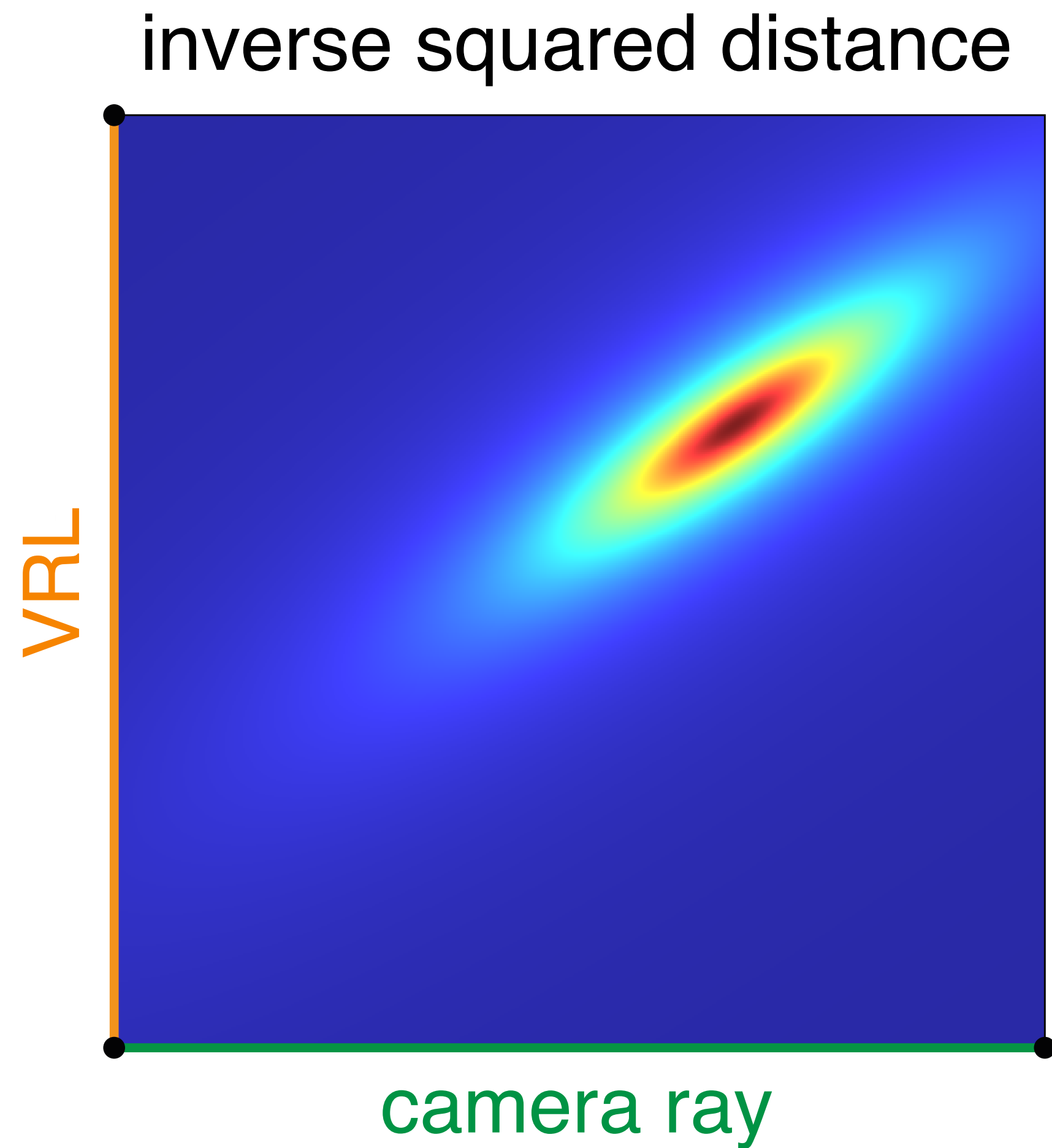
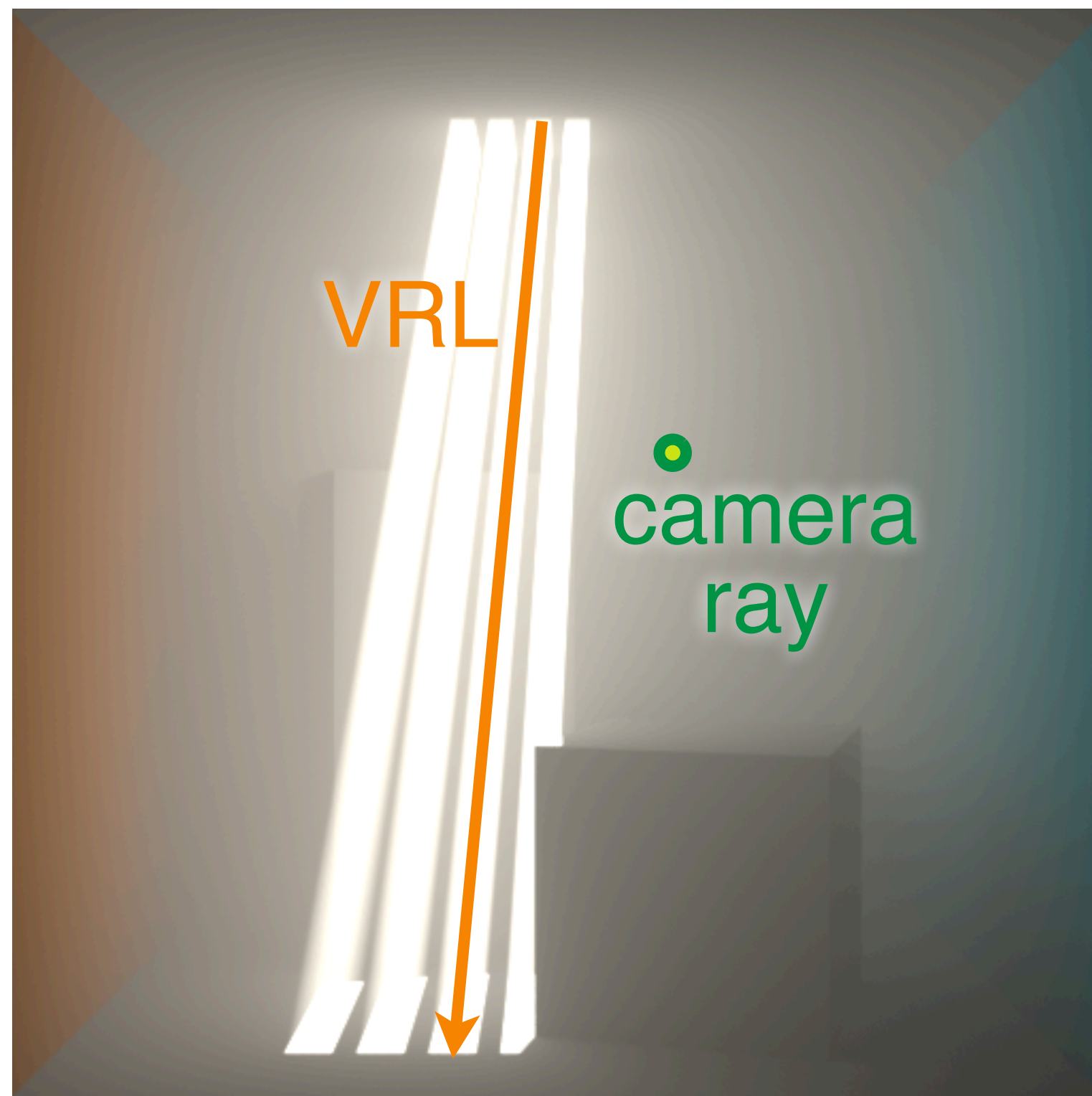
Isotropic media



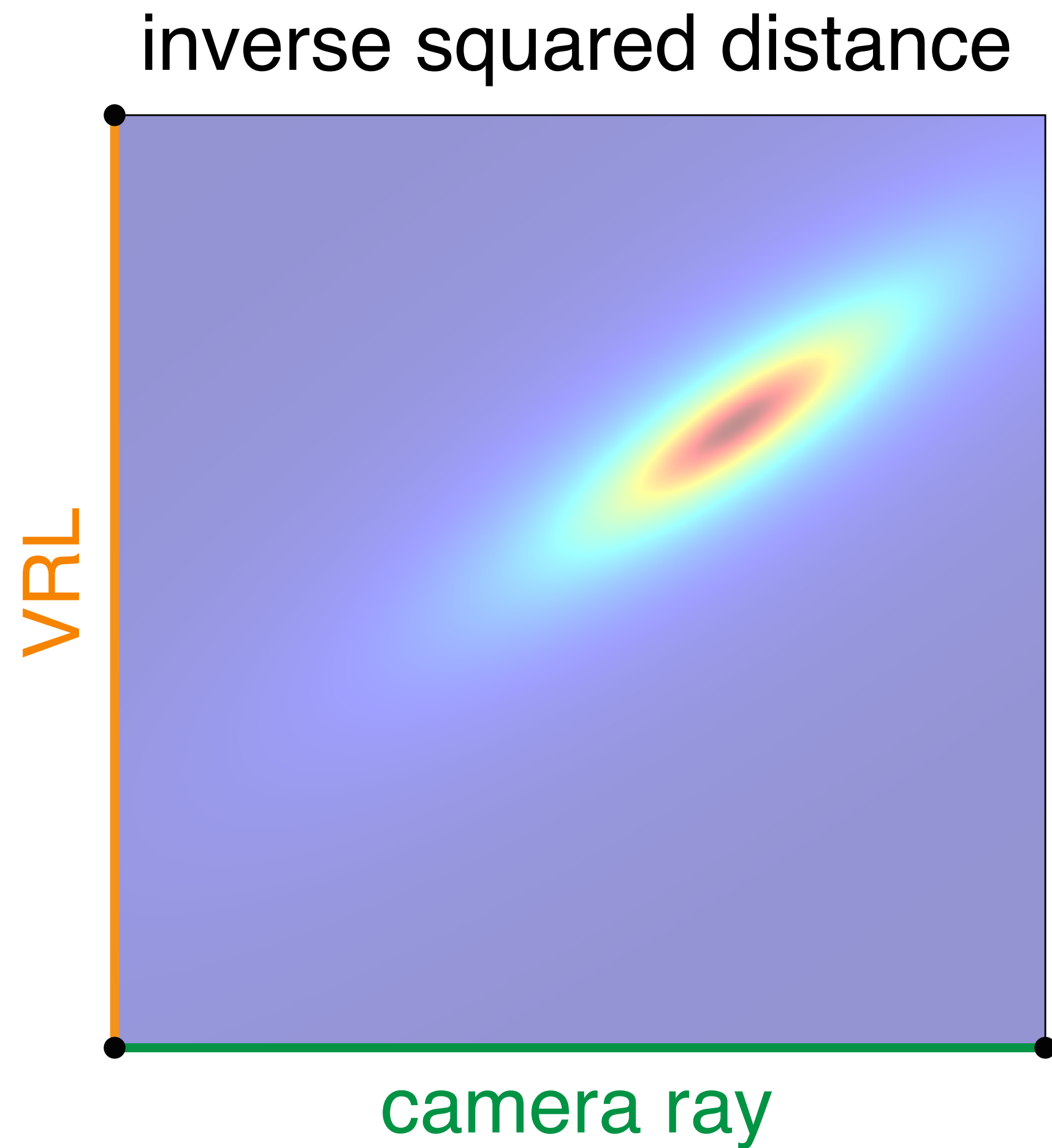
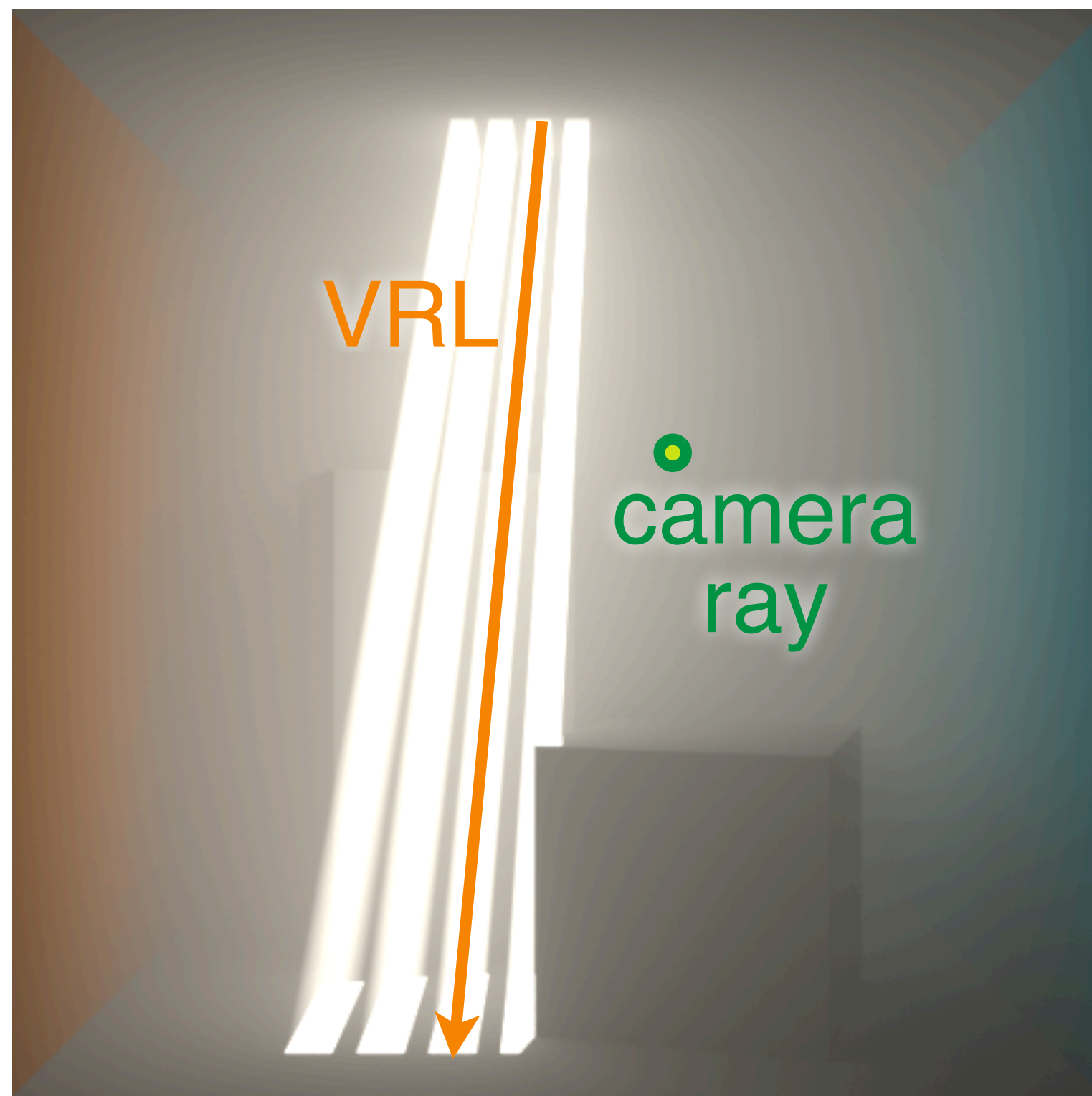
Isotropic media



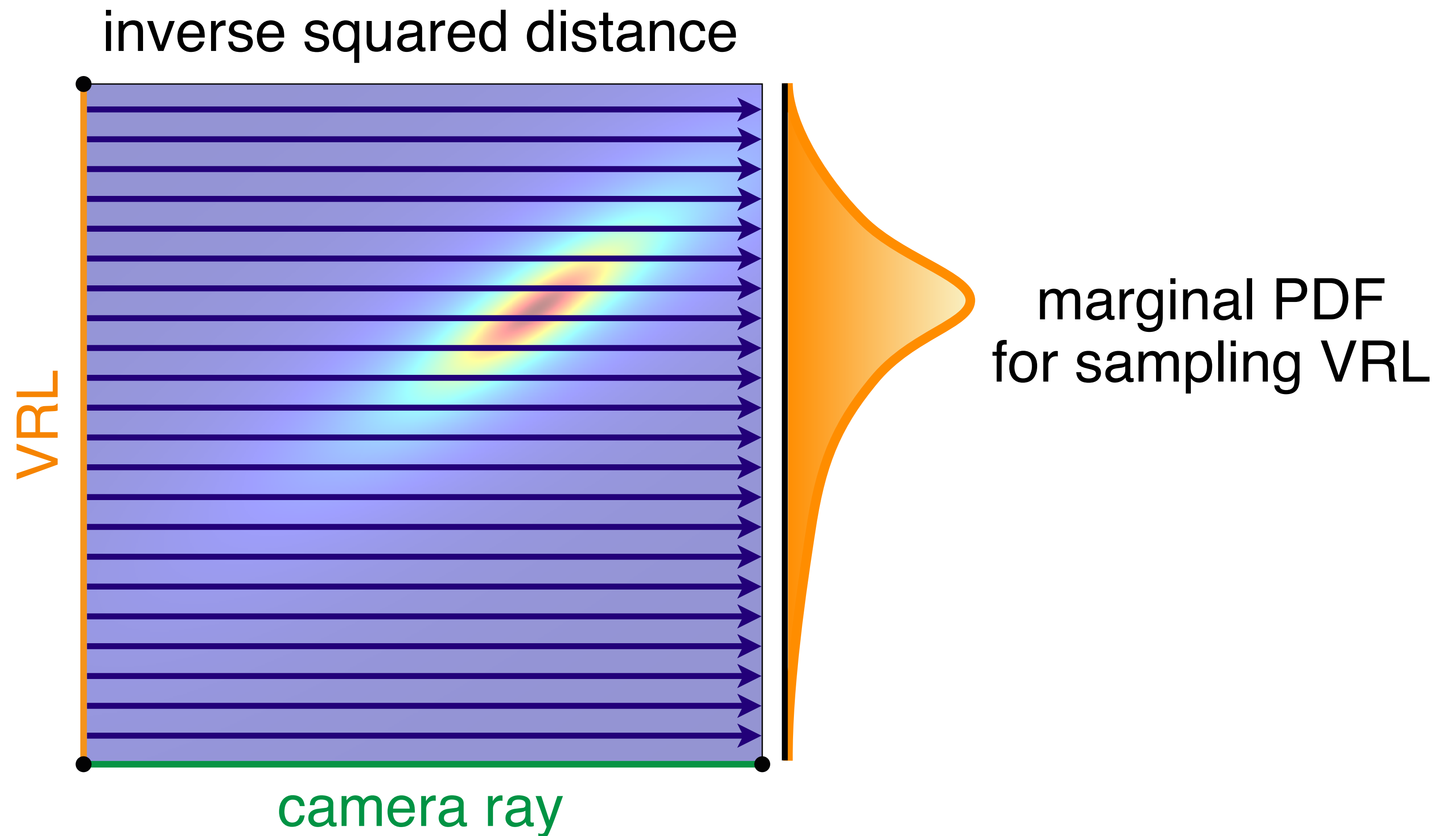
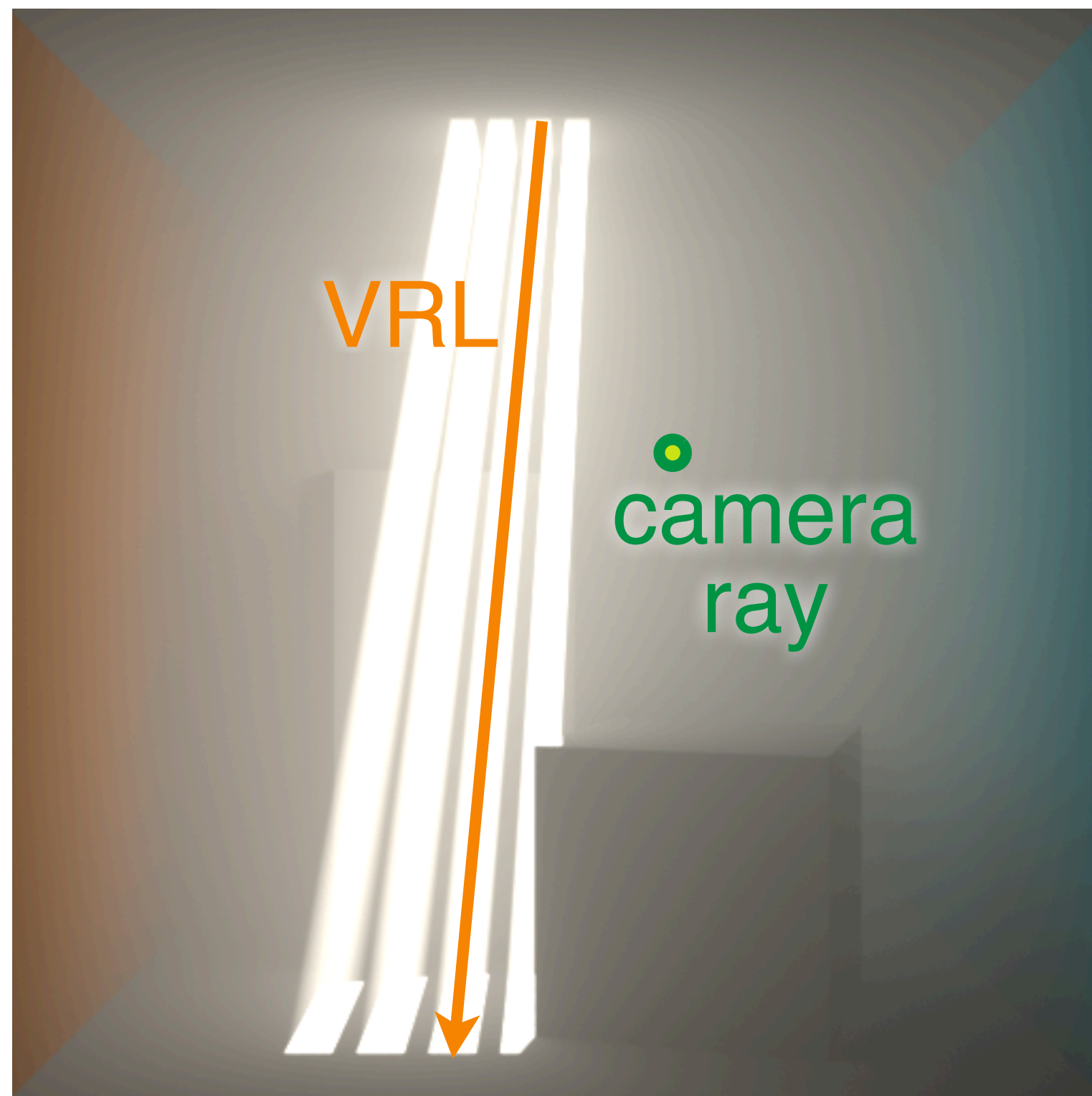
Isotropic media



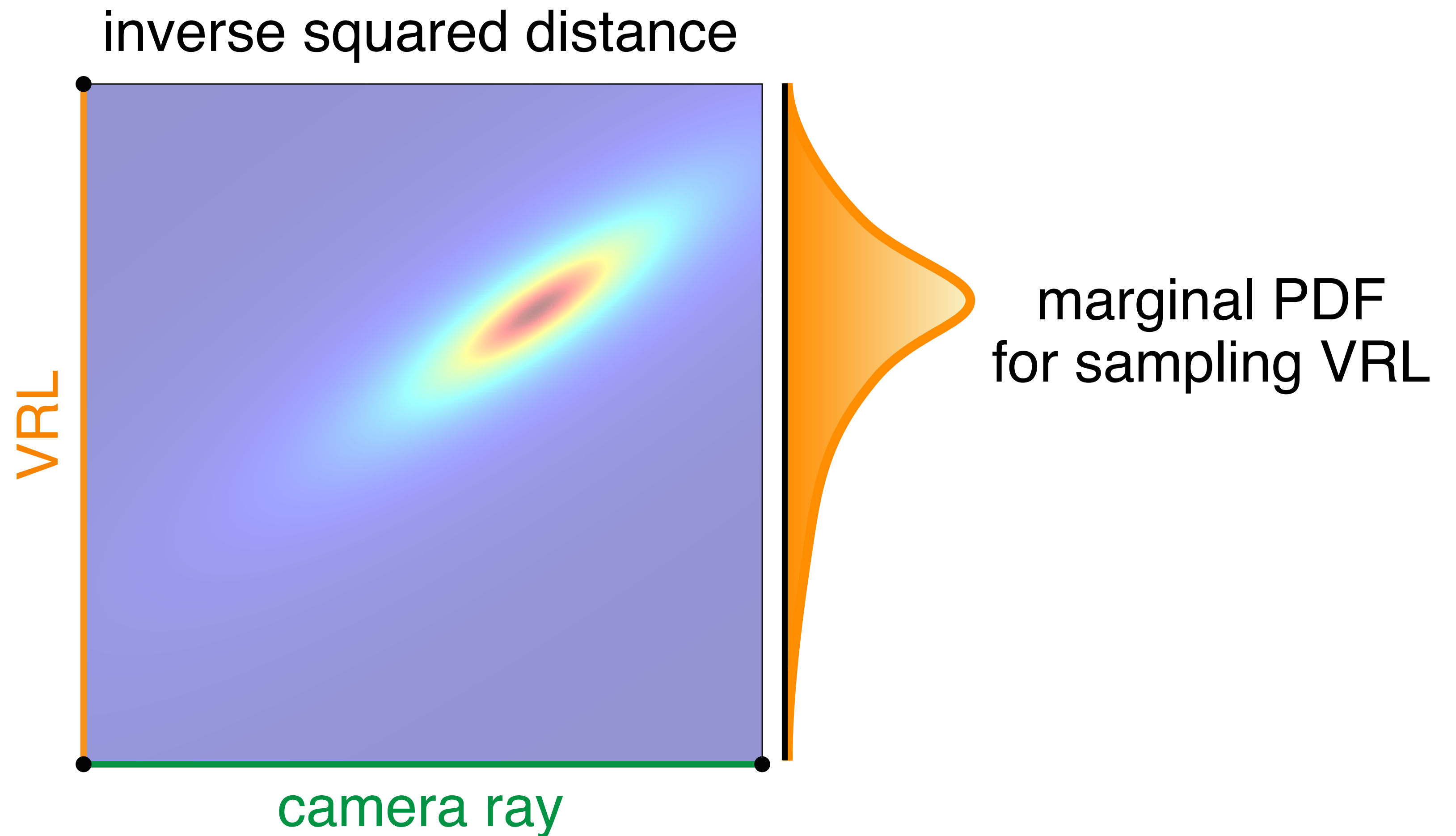
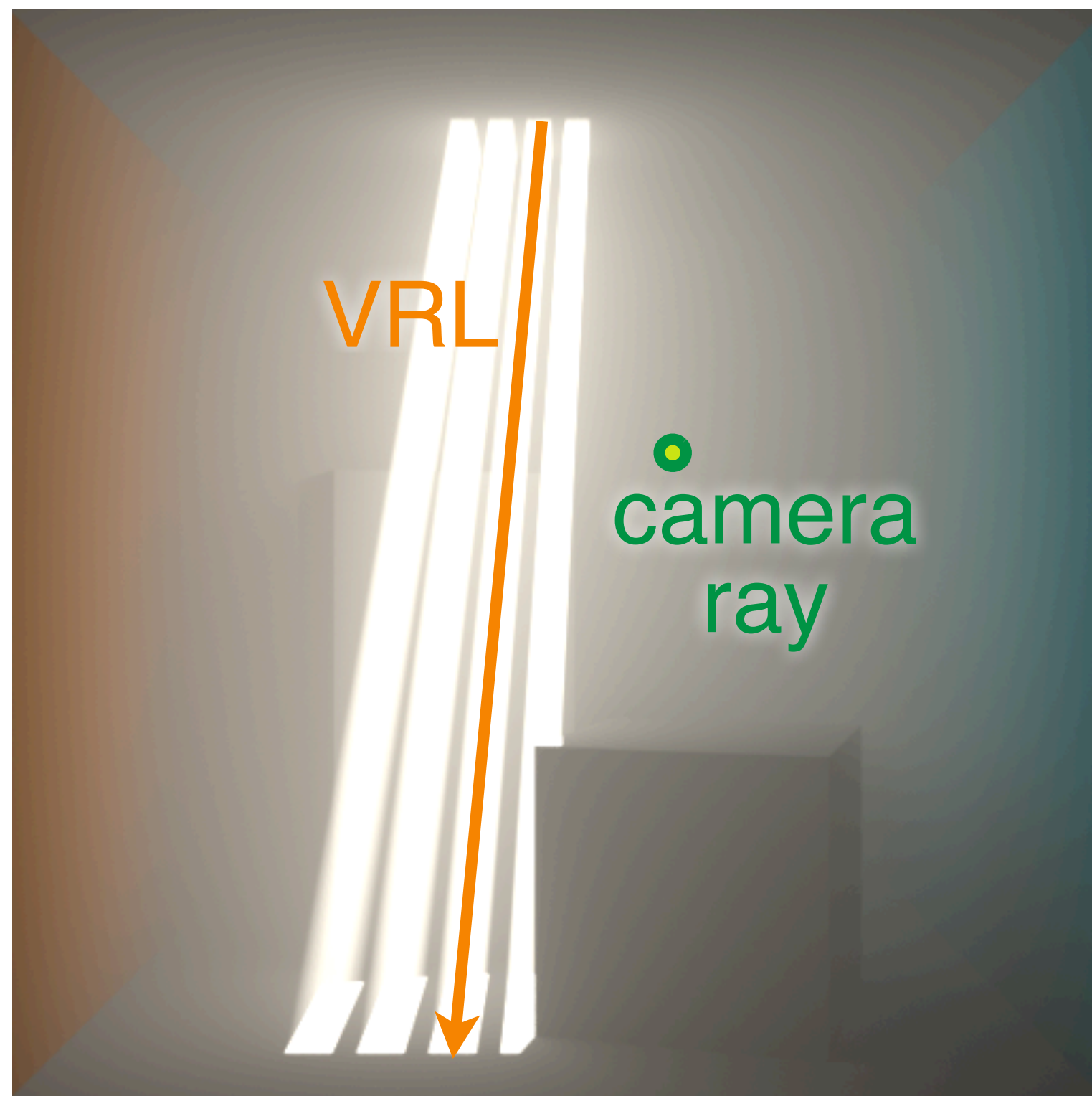
Isotropic media



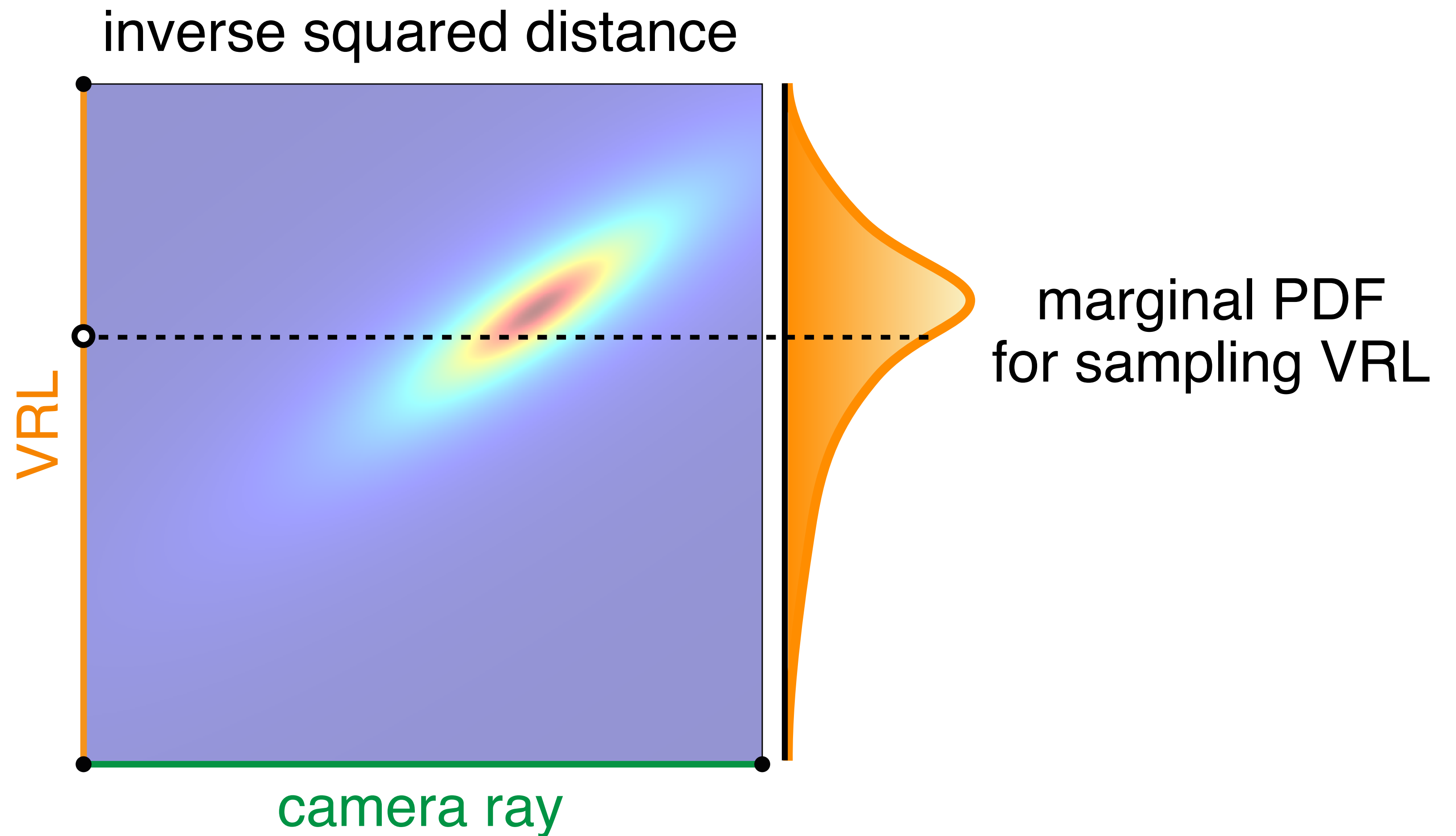
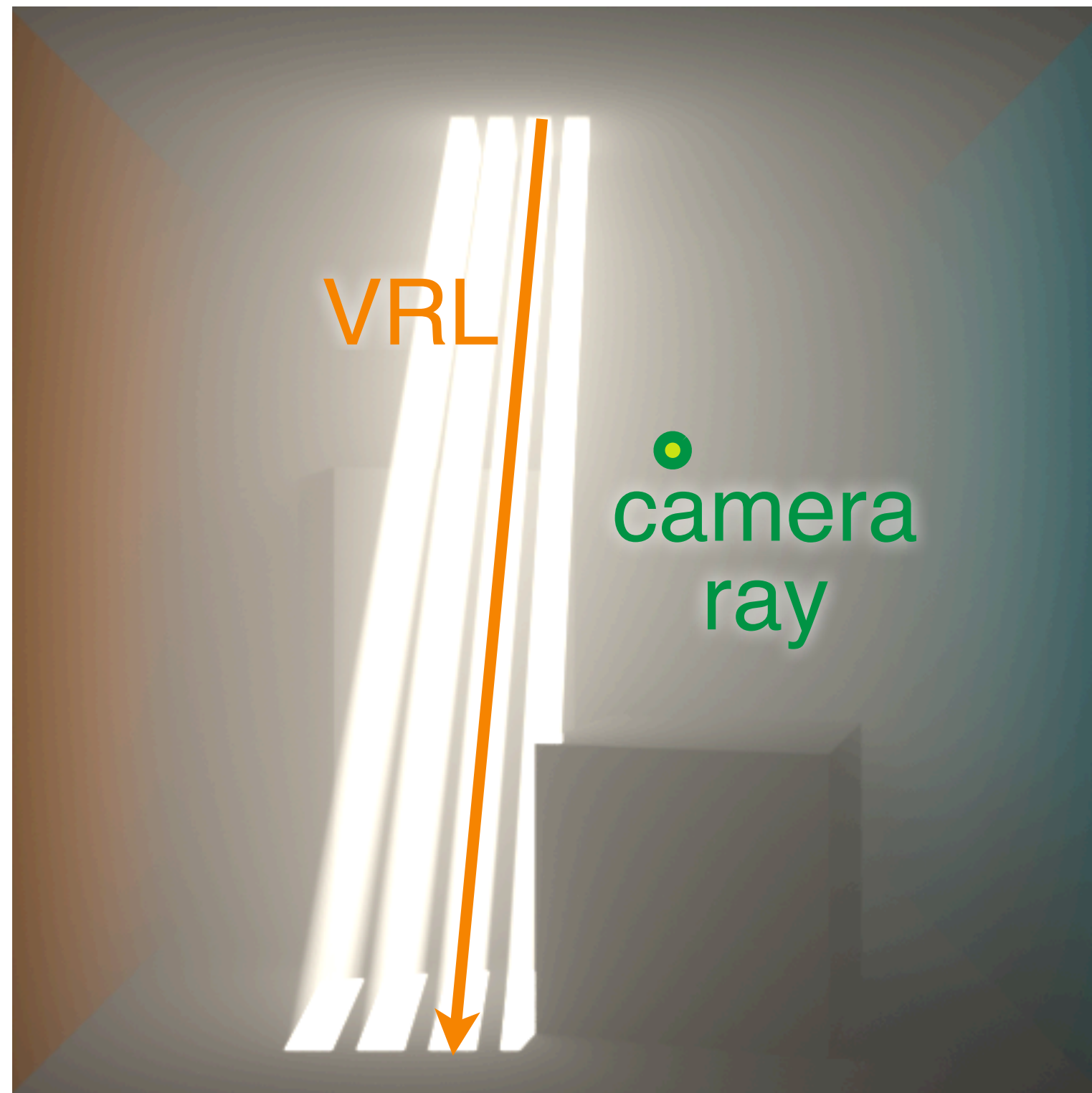
Isotropic media



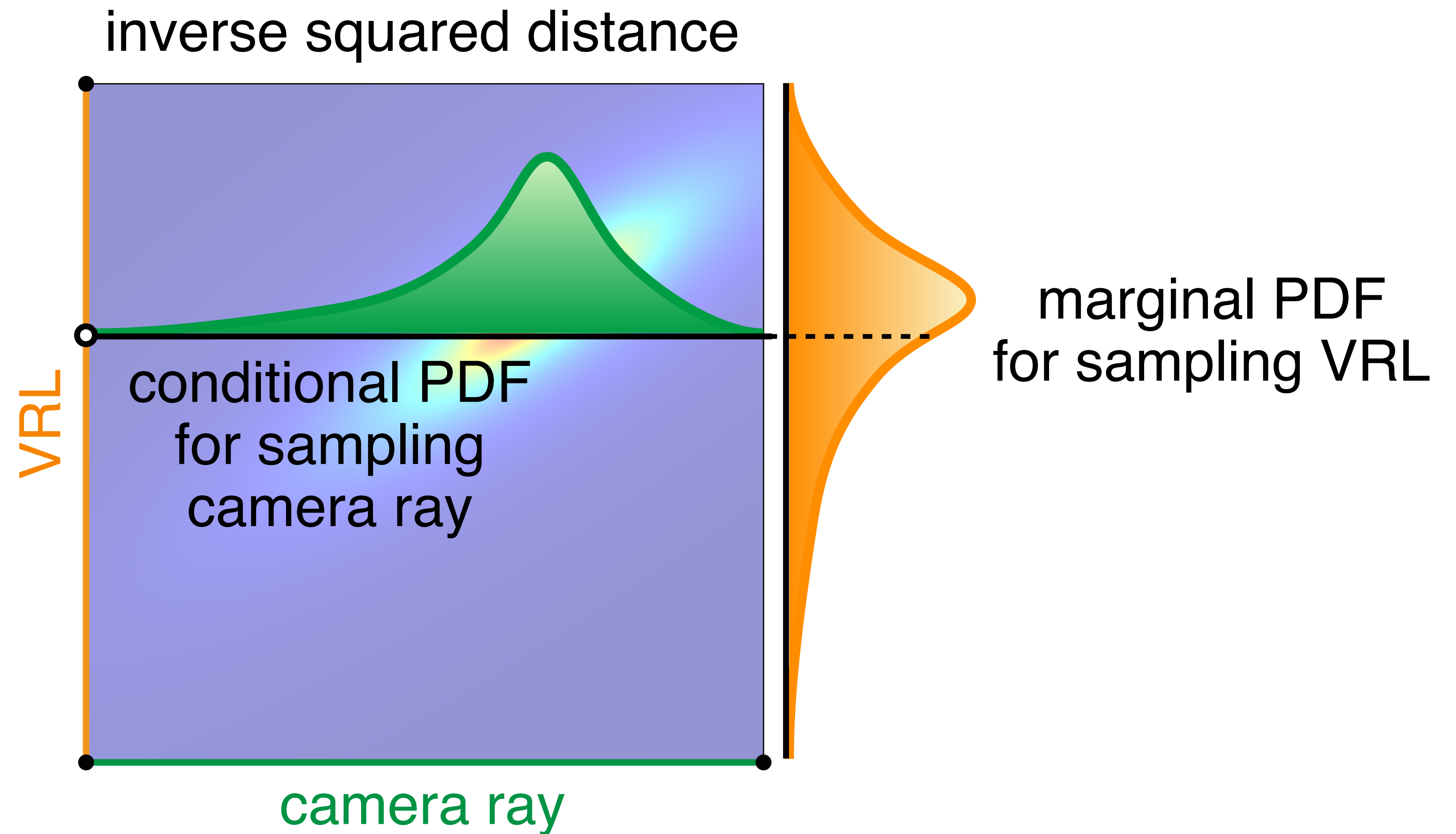
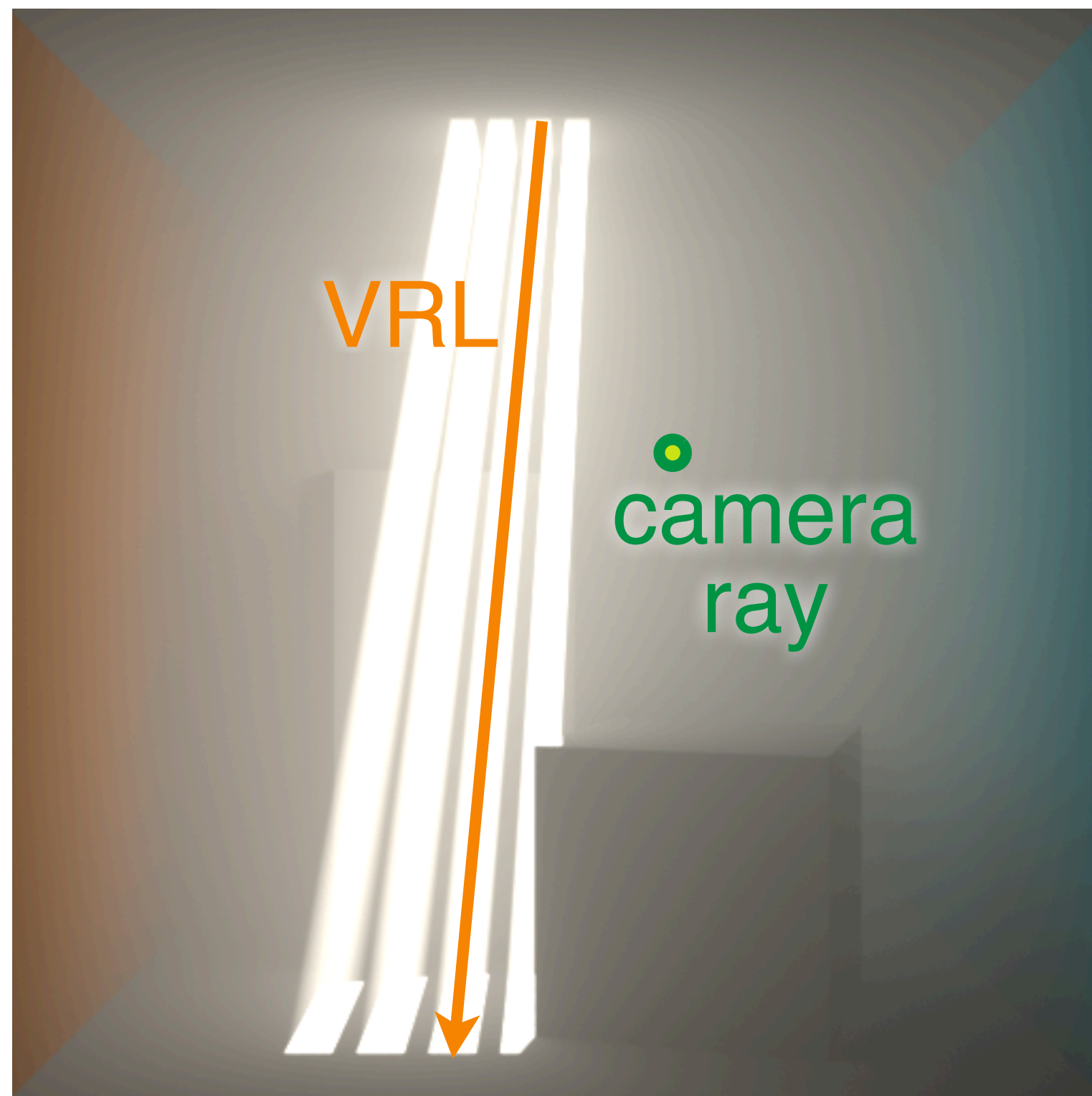
Isotropic media



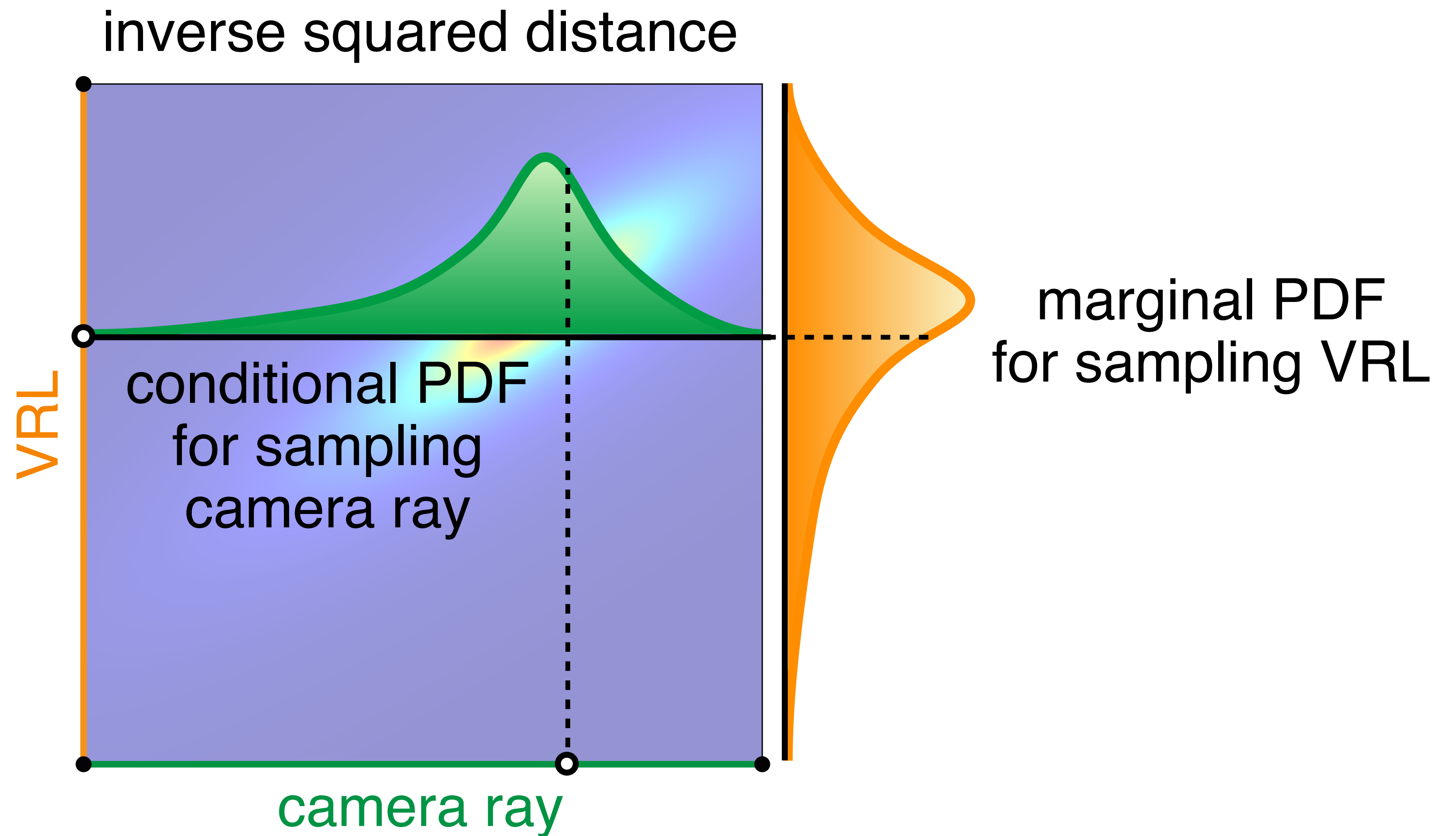
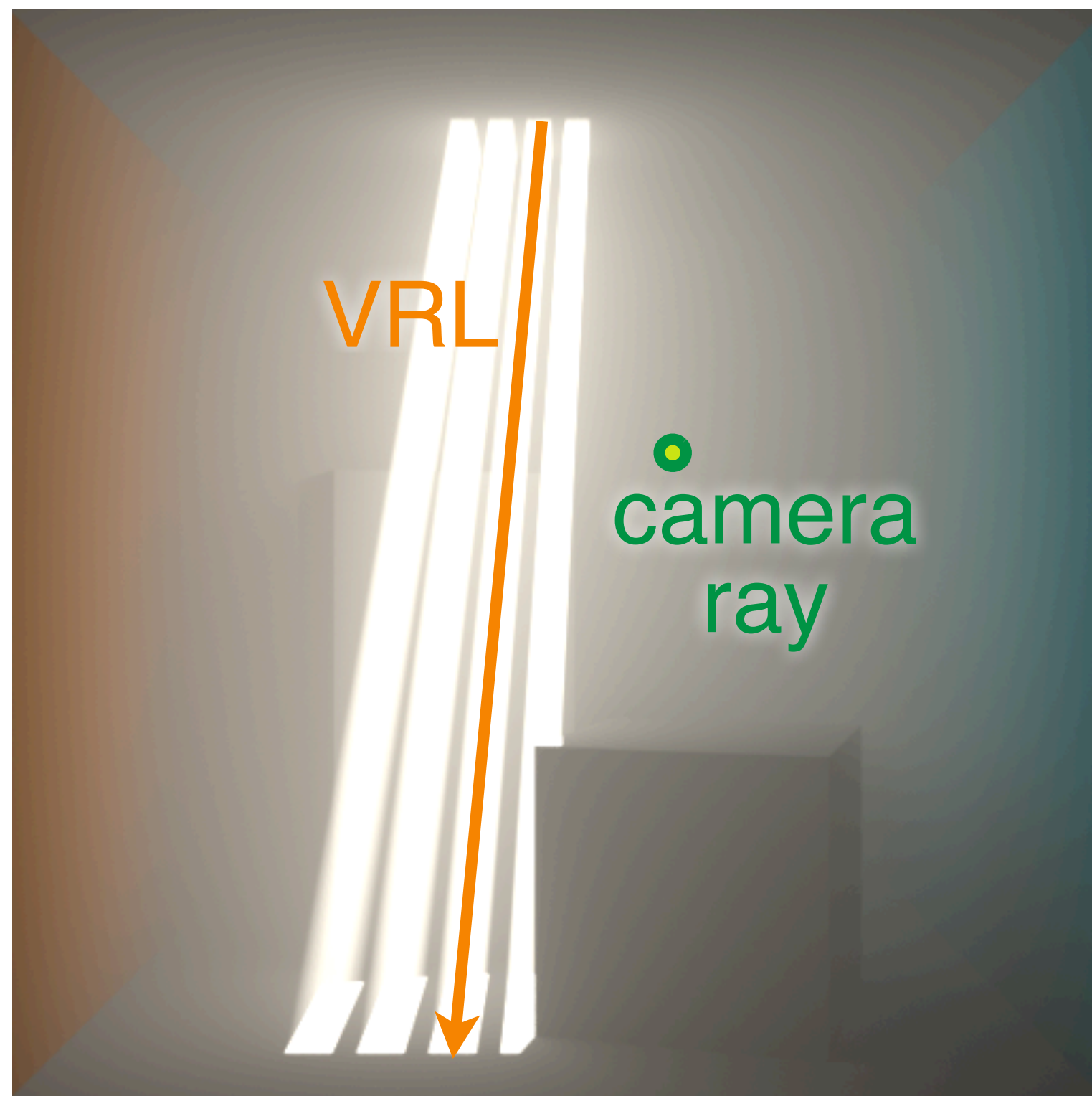
Isotropic media



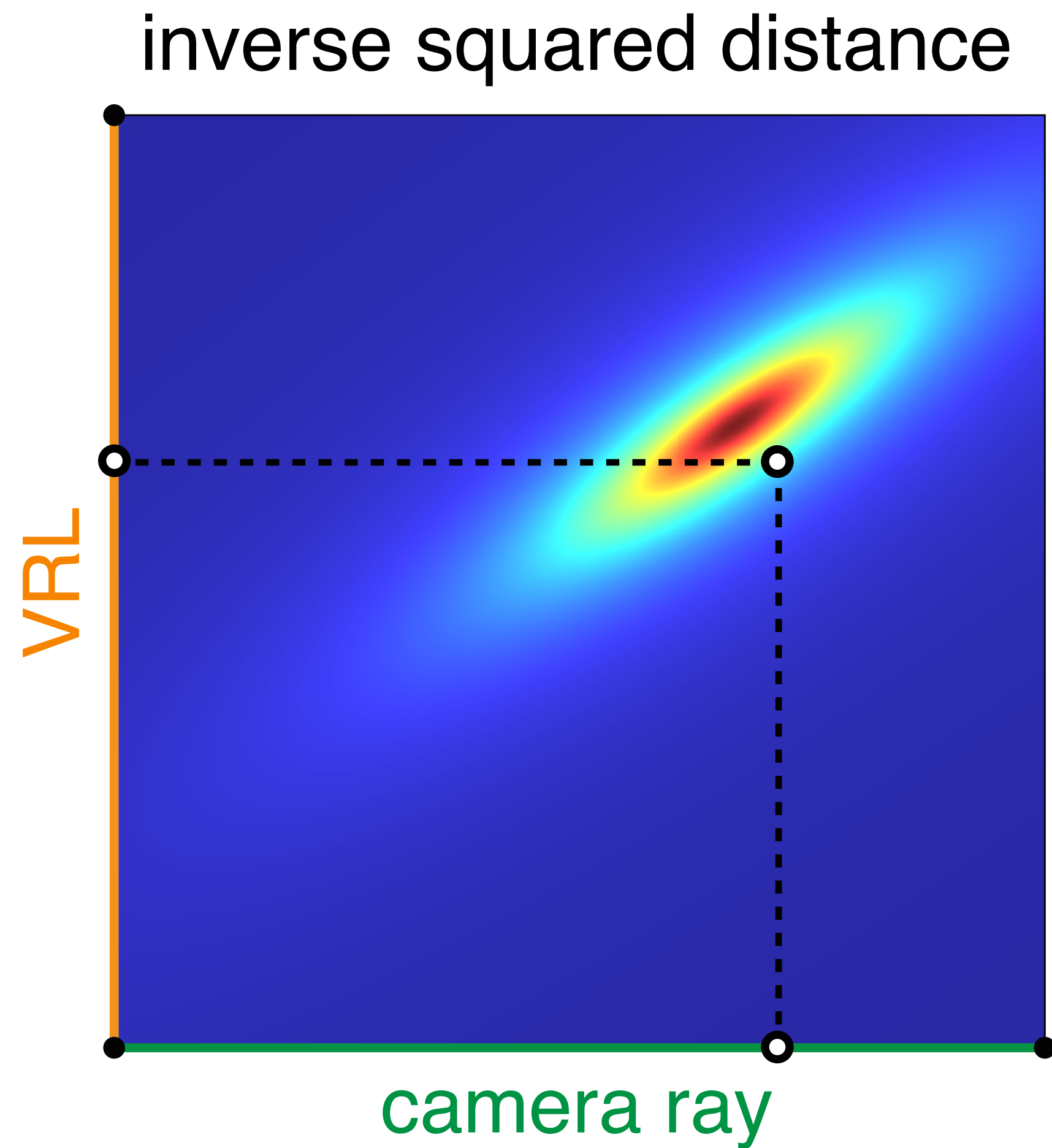
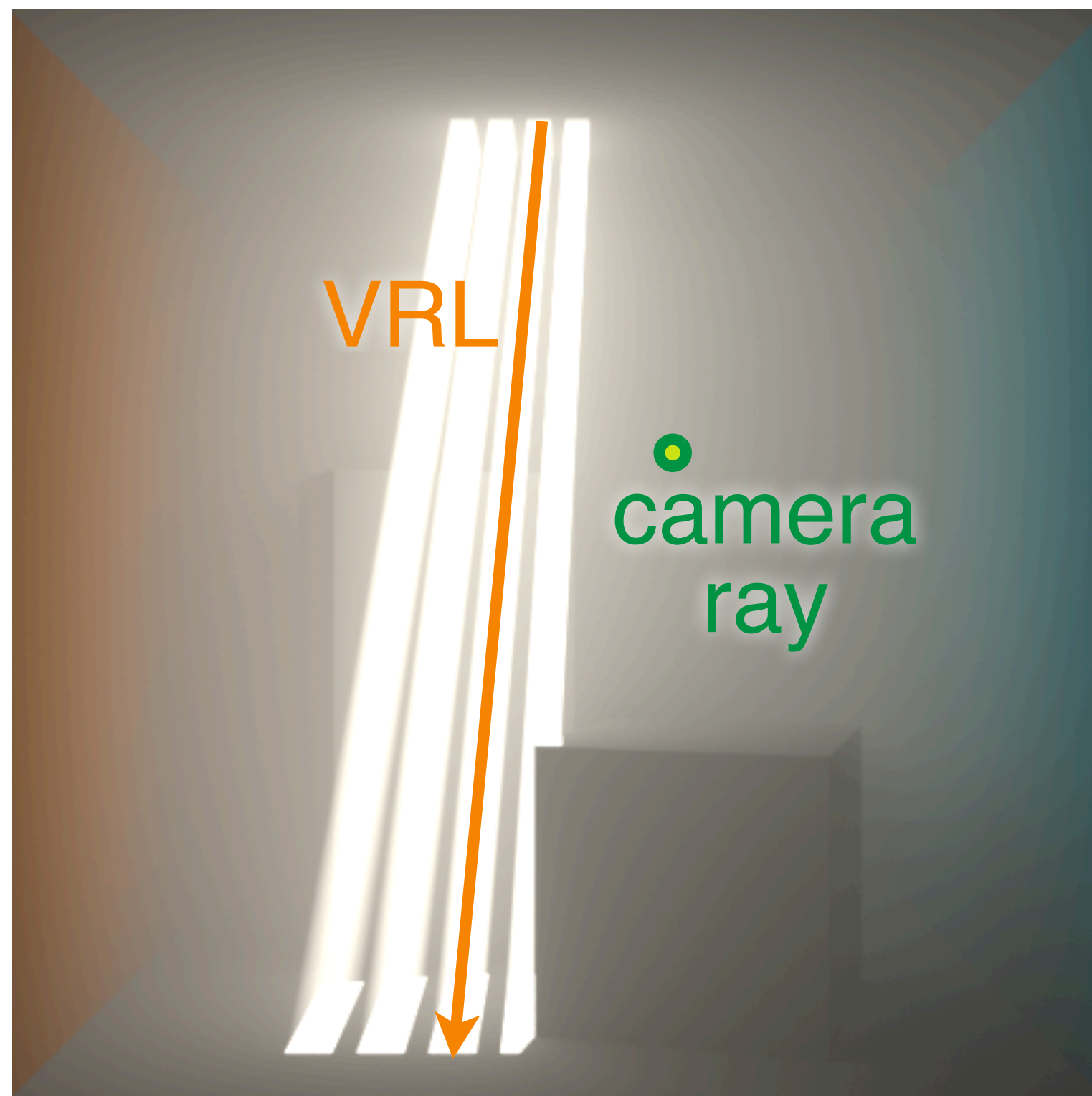
Isotropic media



Isotropic media



Isotropic media



Isotropic media

- **Marginal PDF** 

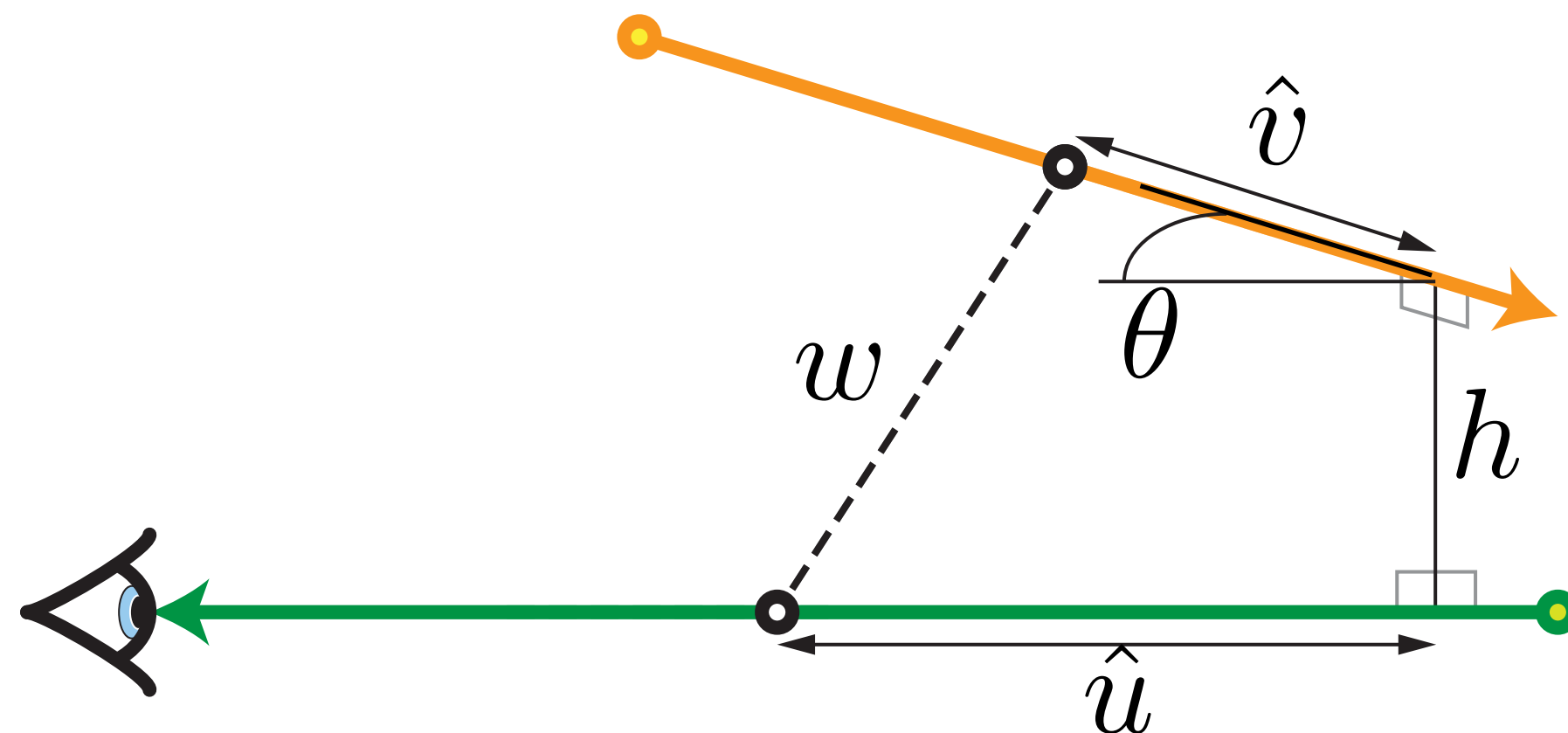
$$\text{pdf}(v) = \frac{\int_0^s w^{-2} \, du}{\int_0^t \int_0^s w^{-2} \, du \, dv}$$

Isotropic media

- **Marginal PDF** 

$$\text{pdf}(v) = \frac{\int_0^s w^{-2} \, du}{\int_0^t \int_0^s w^{-2} \, du \, dv}$$

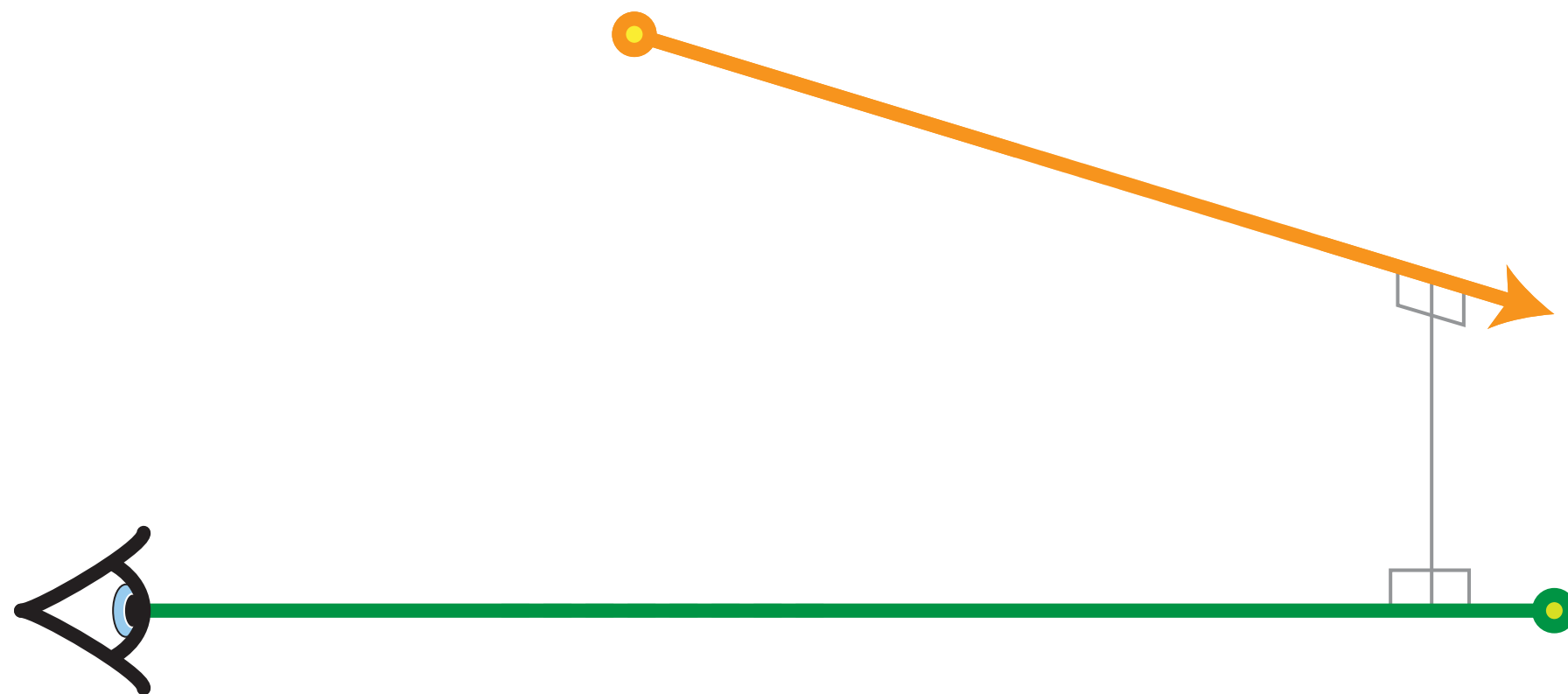
$$w = \sqrt{h^2 + \hat{u}^2 + \hat{v}^2 - 2\hat{u}\hat{v} \cos \theta}$$



Isotropic media

- **Marginal PDF** 

$$\text{pdf}(v) = \frac{\int_0^s w^{-2} \, du}{\int_0^t \int_0^s w^{-2} \, du \, dv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} \, du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} \, du \, dv}$$

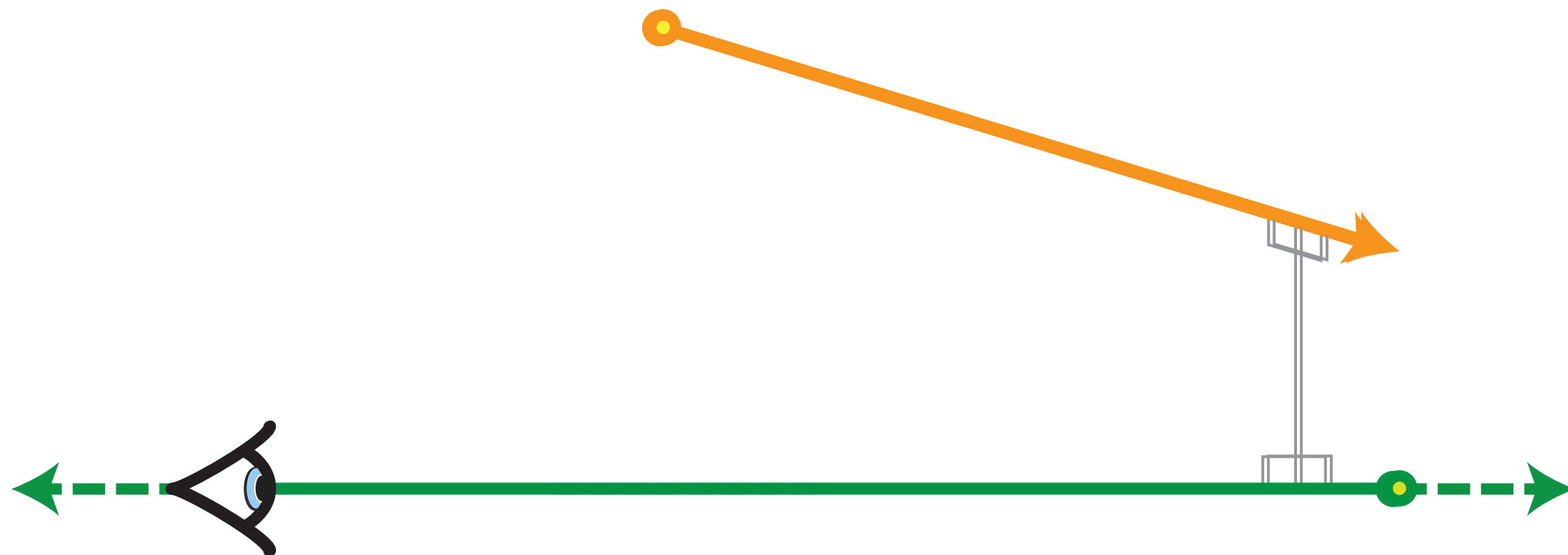


Isotropic media

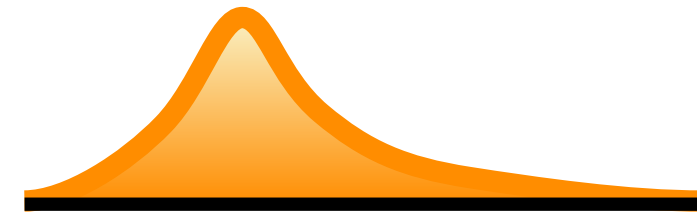
- **Marginal PDF** 

$$\text{pdf}(v) = \frac{\int_0^s w^{-2} \, du}{\int_0^t \int_0^s w^{-2} \, du \, dv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} \, du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} \, du \, dv}$$

assume infinite
camera ray

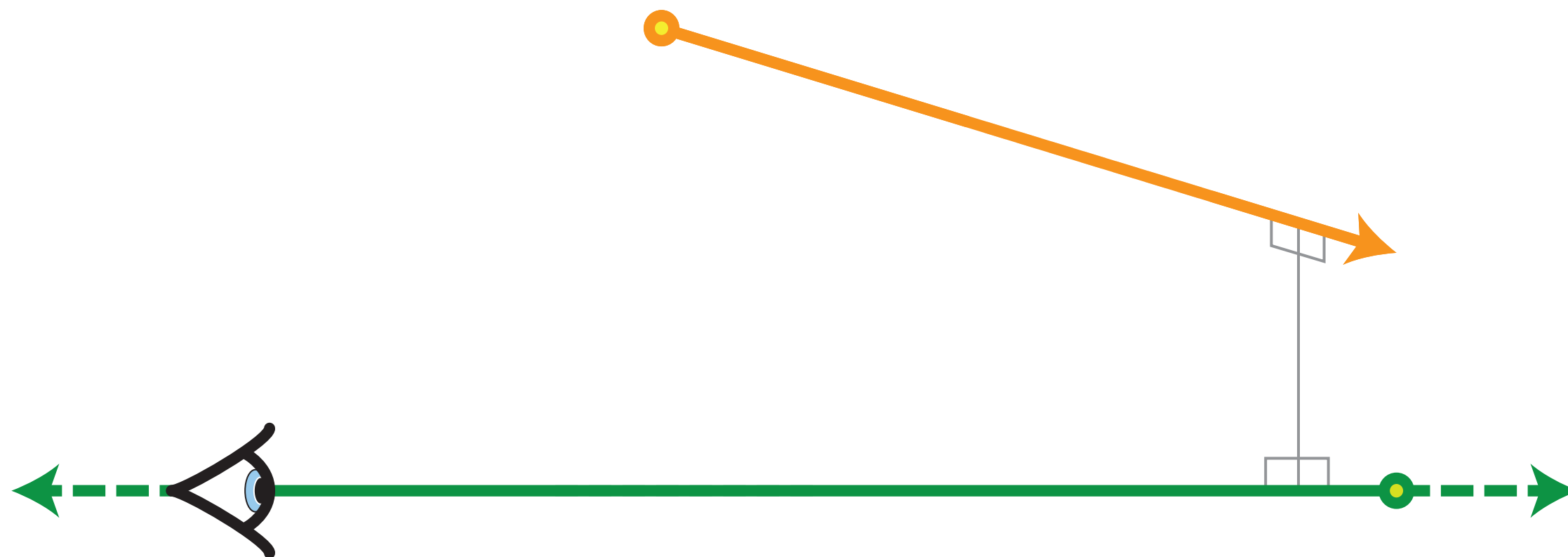


Isotropic media

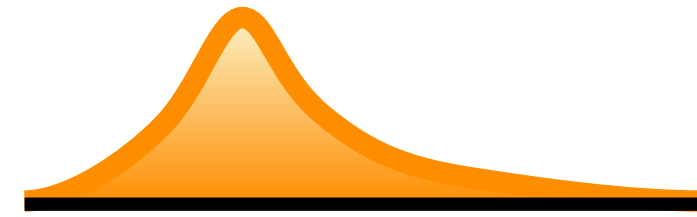


$$\text{pdf}(v) = \frac{\int_0^s w^{-2} \, du}{\int_0^t \int_0^s w^{-2} \, du \, dv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} \, du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} \, du \, dv} = \frac{\sin \theta}{(A(\hat{v}_1) - A(\hat{v}_0)) \sqrt{h^2 + v^2 \sin^2 \theta}}$$

assume infinite
camera ray



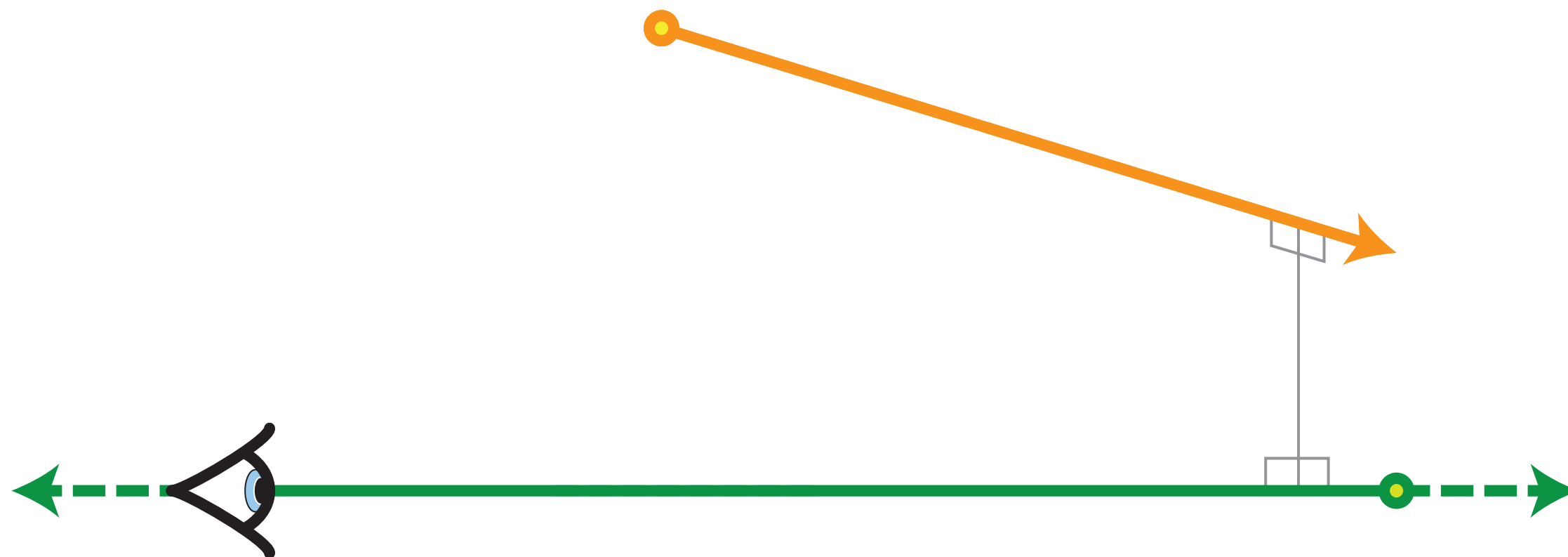
Isotropic media



$$\text{pdf}(v) = \frac{\int_0^s w^{-2} \, du}{\int_0^t \int_0^s w^{-2} \, du \, dv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} \, du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} \, du \, dv} = \frac{\sin \theta}{(A(\hat{v}_1) - A(\hat{v}_0)) \sqrt{h^2 + v^2 \sin^2 \theta}}$$

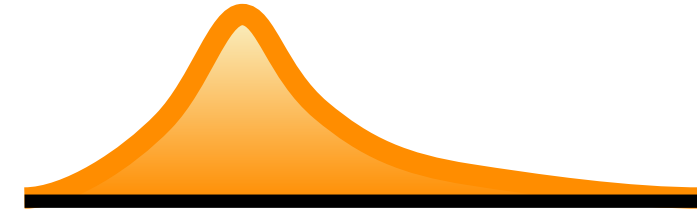
assume infinite
camera ray

$$A(x) = \sinh^{-1} \left(\frac{x}{h} \sin \theta \right)$$



Isotropic media

- **Marginal PDF**

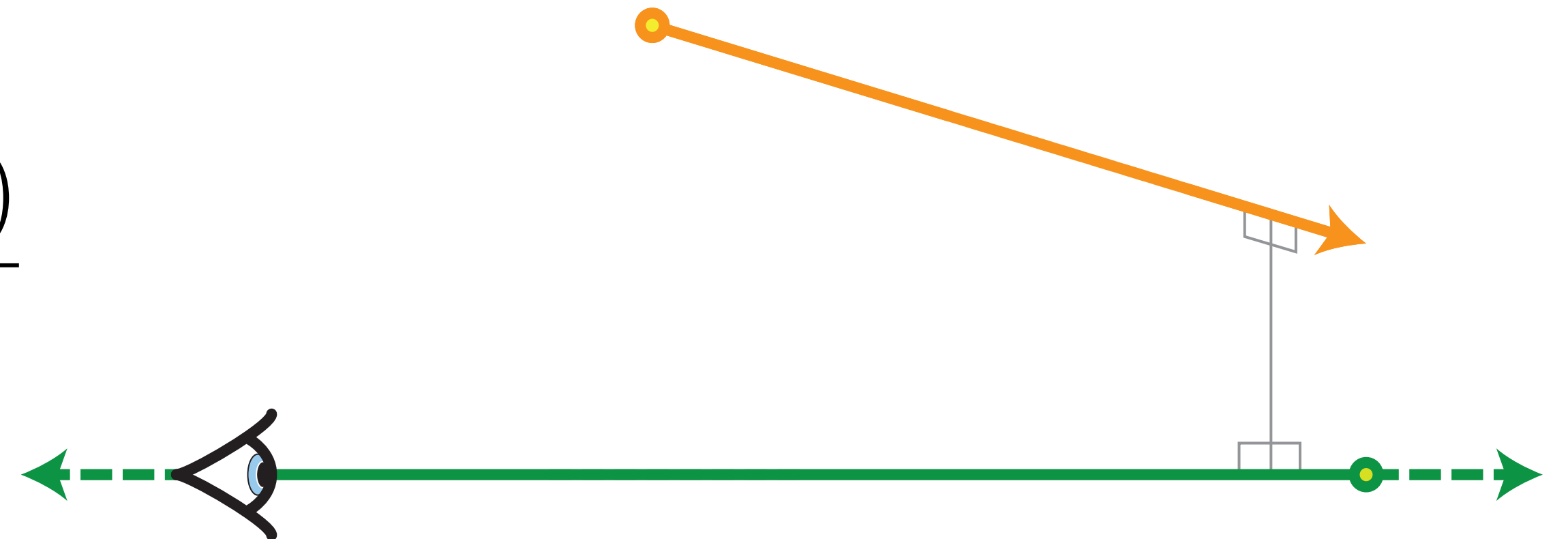


$$\text{pdf}(v) = \frac{\int_0^s w^{-2} \, du}{\int_0^t \int_0^s w^{-2} \, du \, dv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} \, du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} \, du \, dv} = \frac{\sin \theta}{(A(\hat{v}_1) - A(\hat{v}_0)) \sqrt{h^2 + v^2 \sin^2 \theta}}$$

assume infinite
camera ray

$$A(x) = \sinh^{-1} \left(\frac{x}{h} \sin \theta \right)$$

$$\text{cdf}^{-1}(\xi) = \frac{h \sinh(\text{lerp}(A(\hat{v}_0), A(\hat{v}_1), \xi))}{\sin \theta}$$



Isotropic media

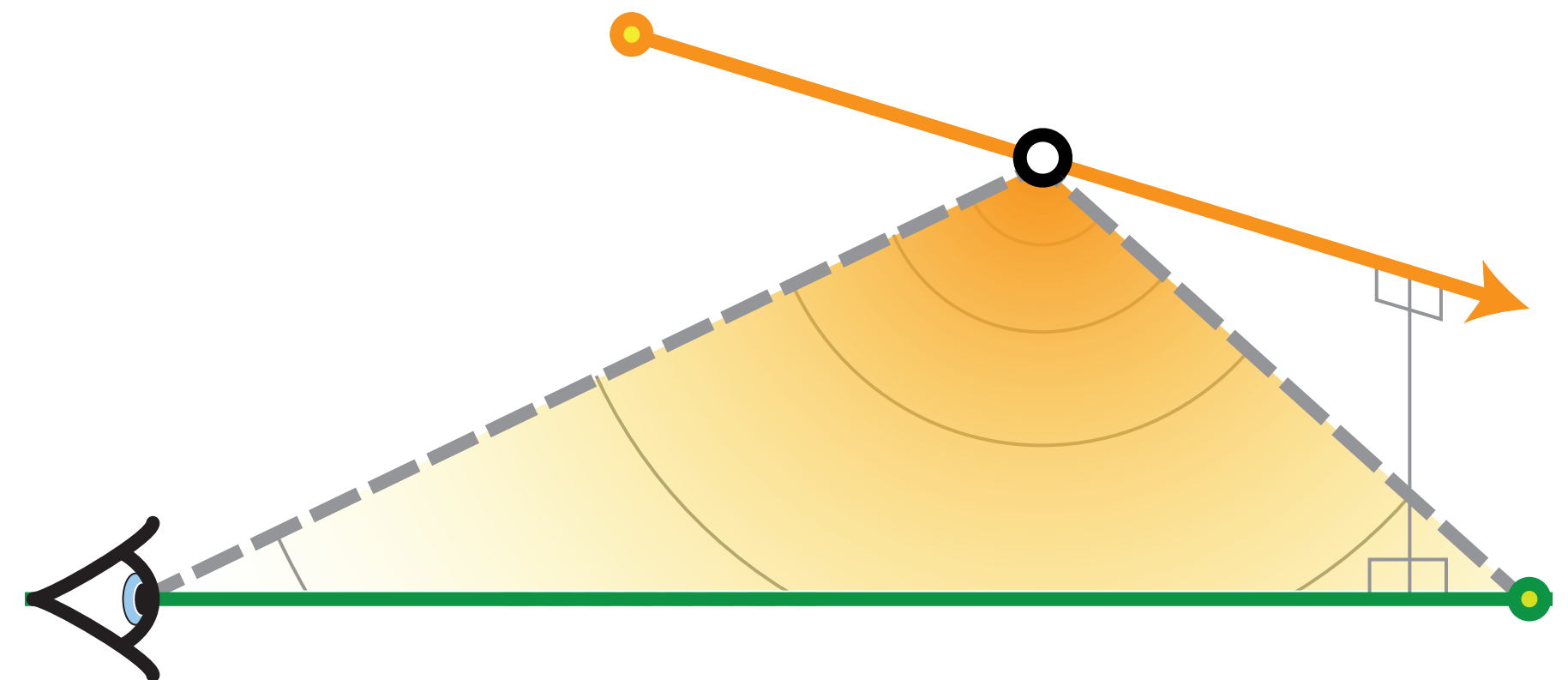
• Marginal PDF

$$\text{pdf}(v) = \frac{\int_0^s w^{-2} du}{\int_0^t \int_0^s w^{-2} dudv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} dudv} = \frac{\sin \theta}{(A(\hat{v}_1) - A(\hat{v}_0)) \sqrt{h^2 + v^2 \sin^2 \theta}}$$

assume infinite
camera ray

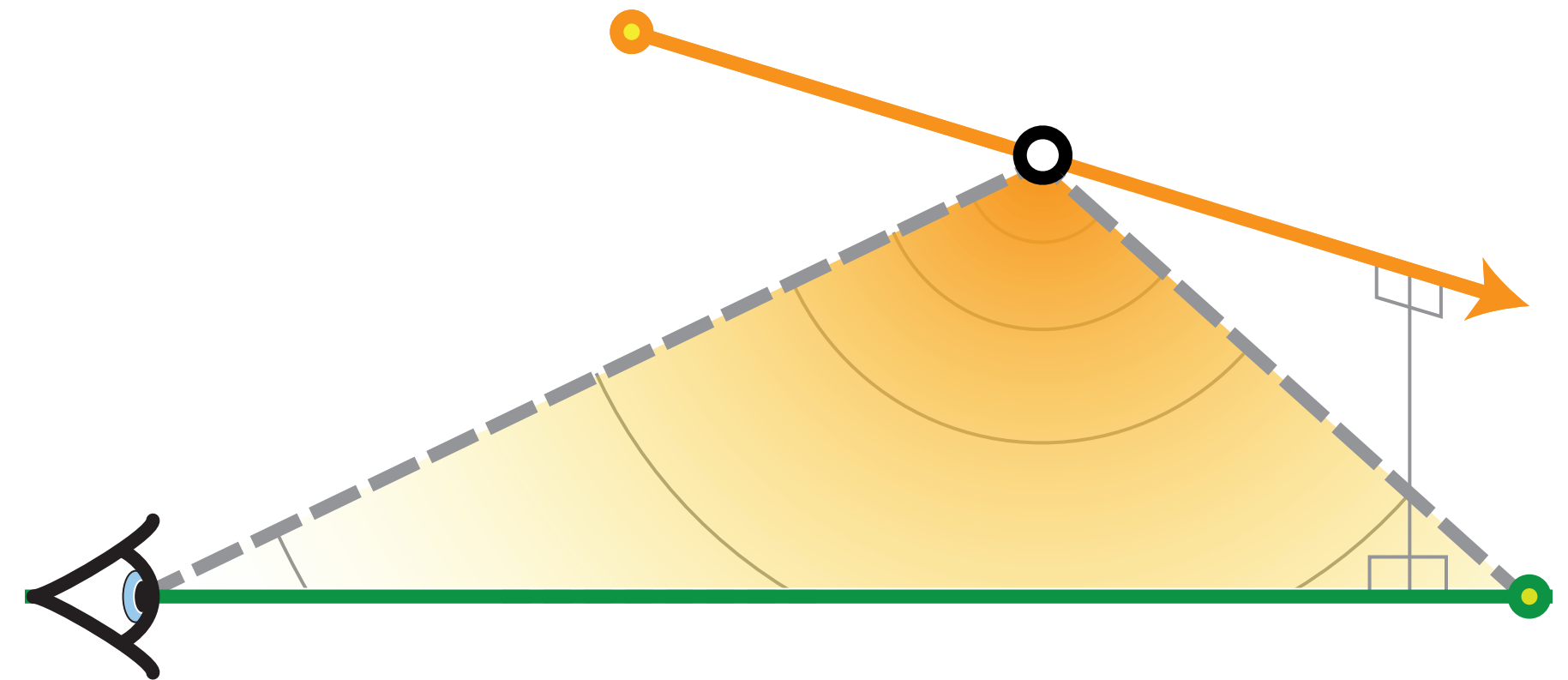
$$A(x) = \sinh^{-1} \left(\frac{x}{h} \sin \theta \right)$$

$$\text{cdf}^{-1}(\xi) = \frac{h \sinh(\text{lerp}(A(\hat{v}_0), A(\hat{v}_1), \xi))}{\sin \theta}$$



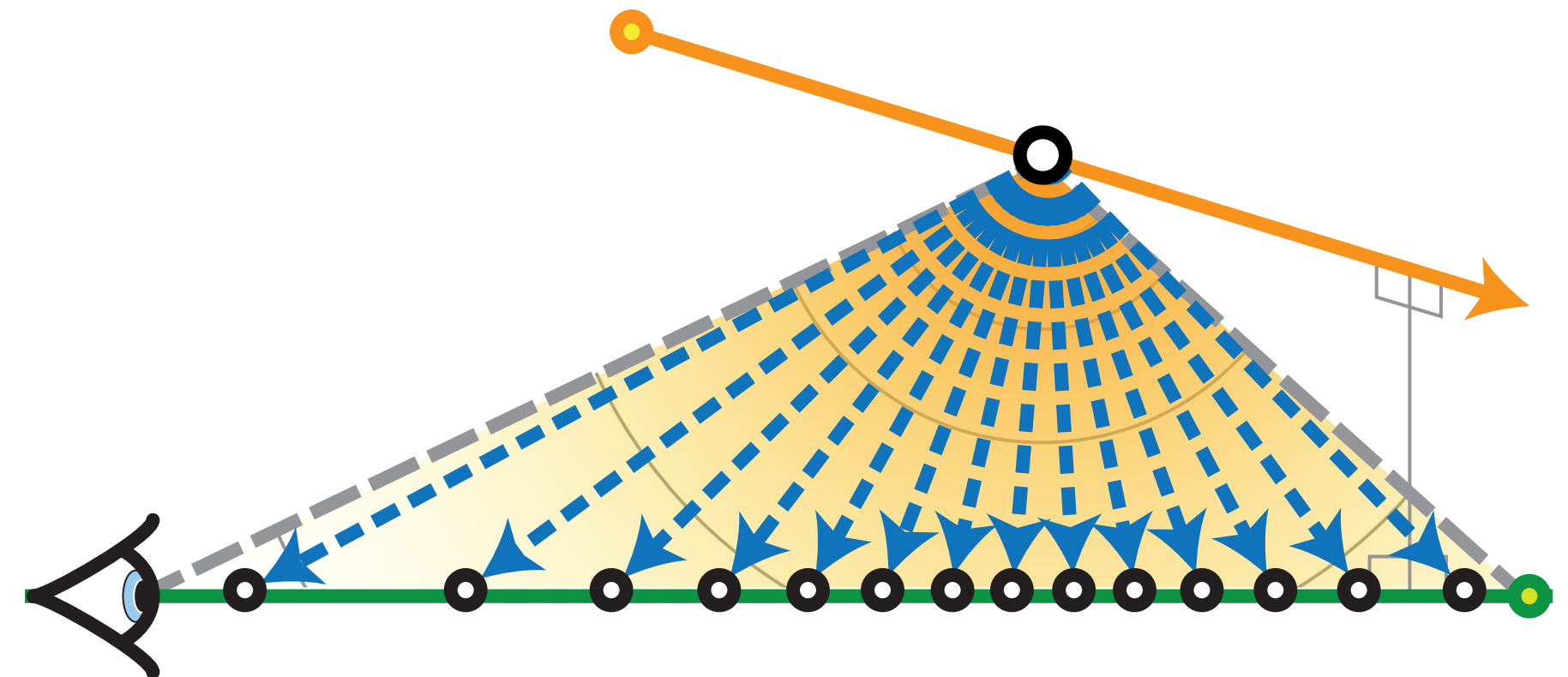
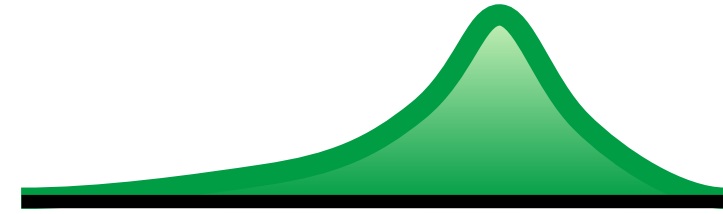
Isotropic media

- **Conditional PDF** 



Isotropic media

- **Conditional PDF**

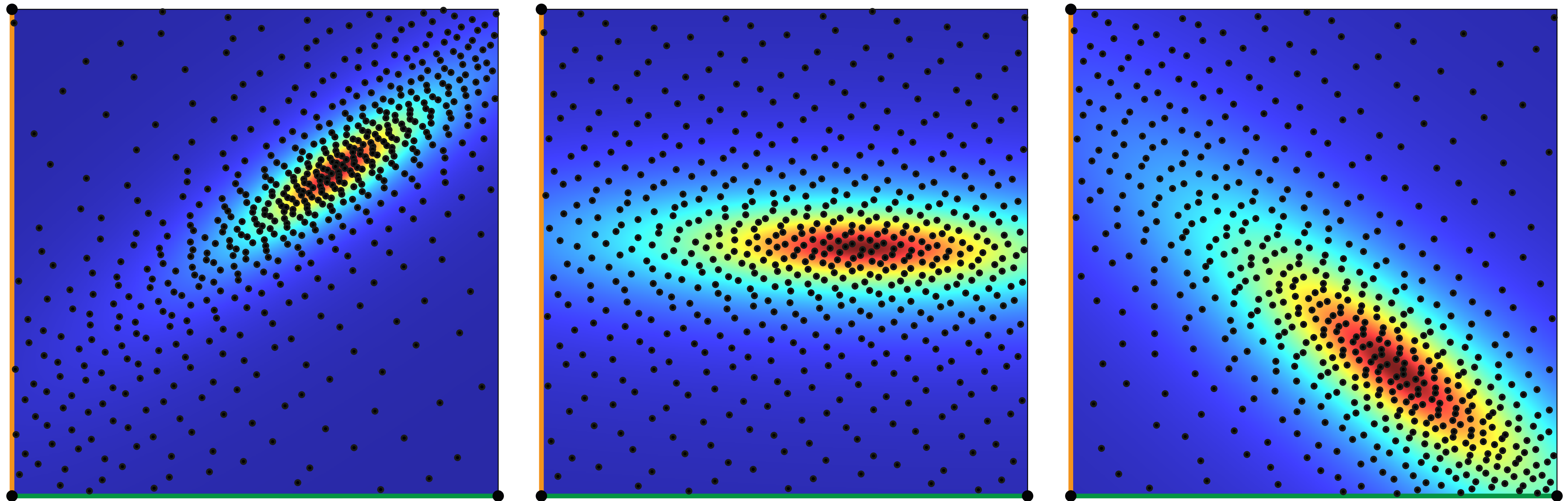


Isotropic media

Summary of isotropic media:

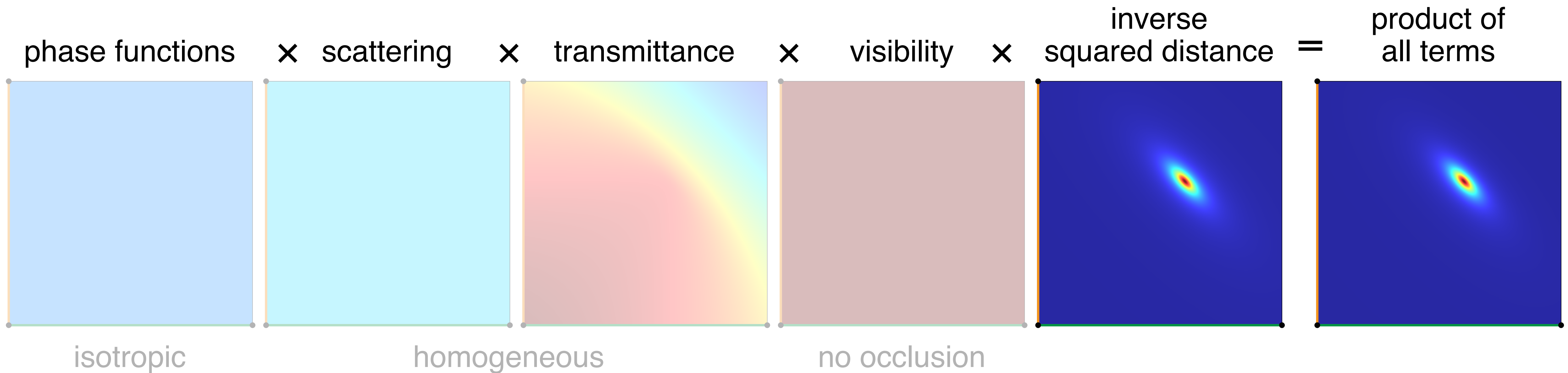
Isotropic media

Summary of isotropic media:



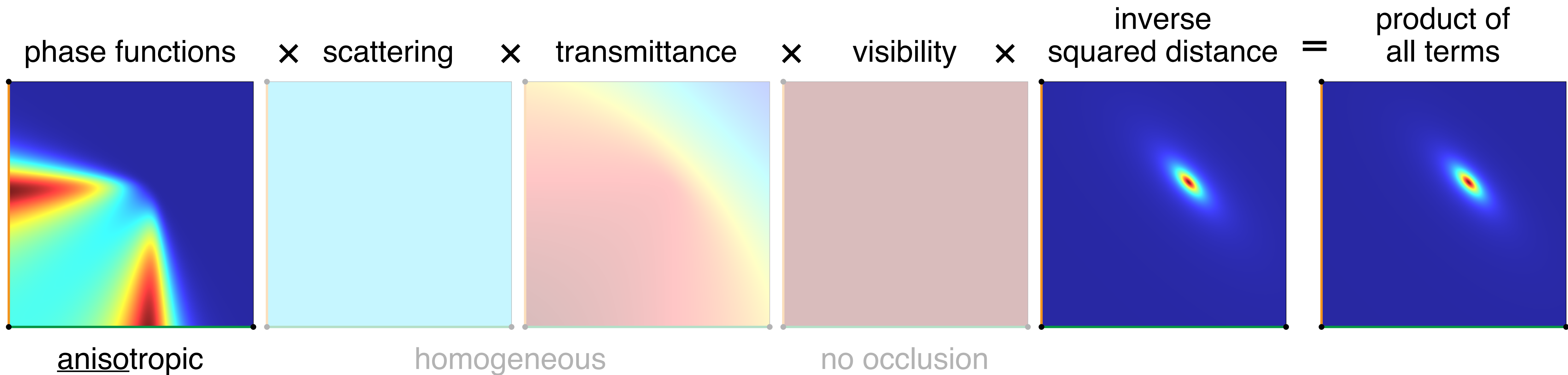
Importance sampling

How to (importance) sample?



Importance sampling

How to (importance) sample?



Importance sampling

How to (importance) sample?



phase functions

×

scattering

×

transmittance

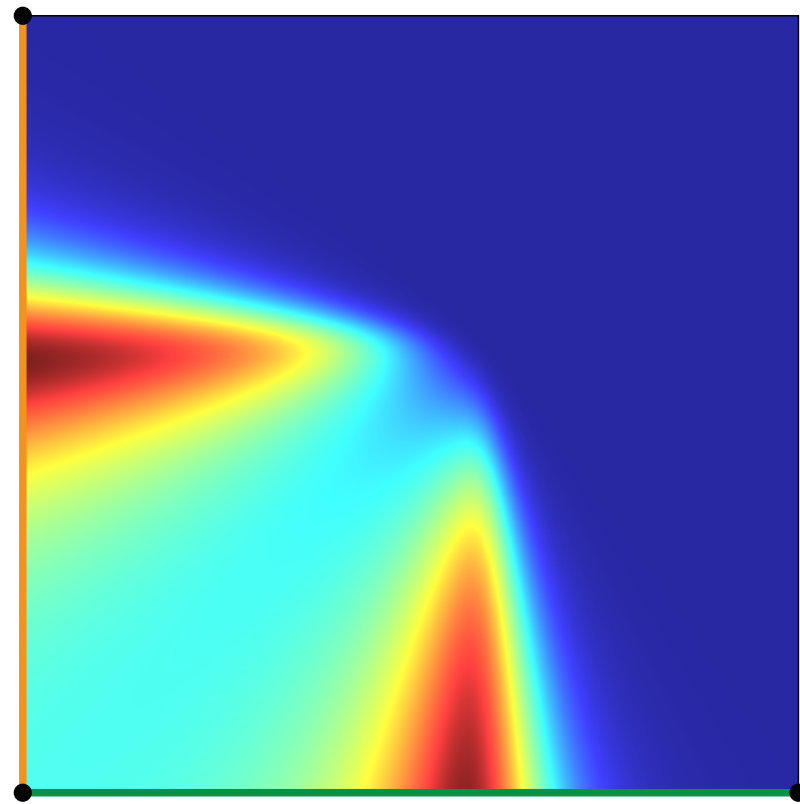
×

visibility

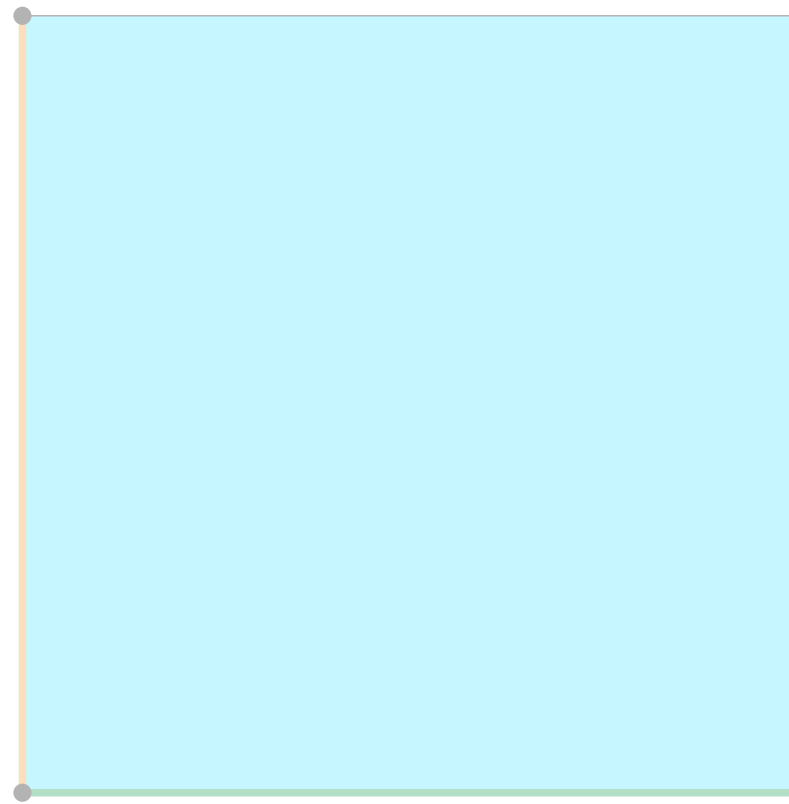
×

inverse squared distance =

product of all terms



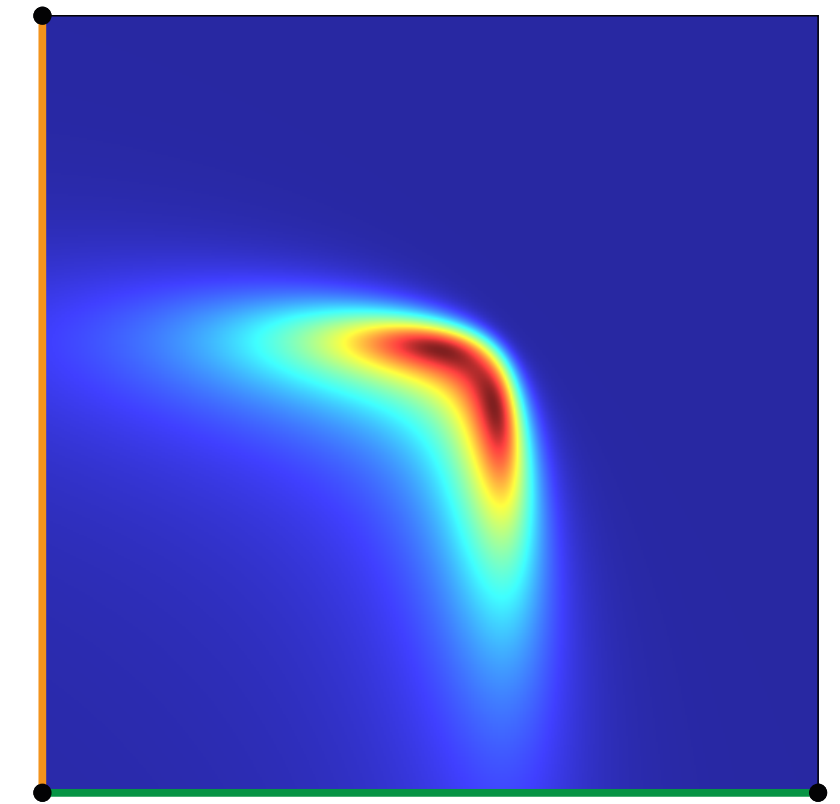
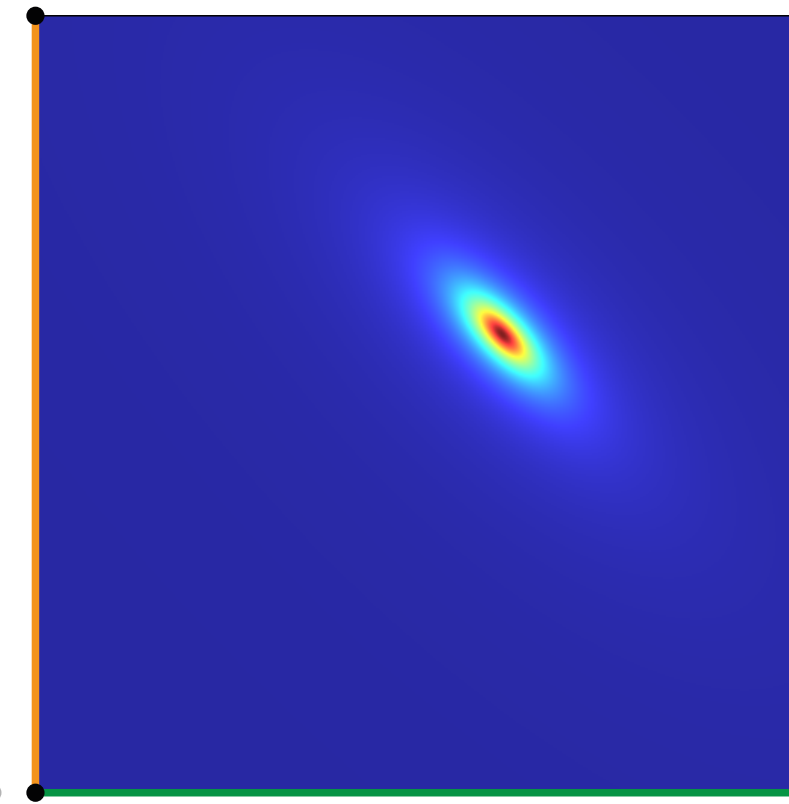
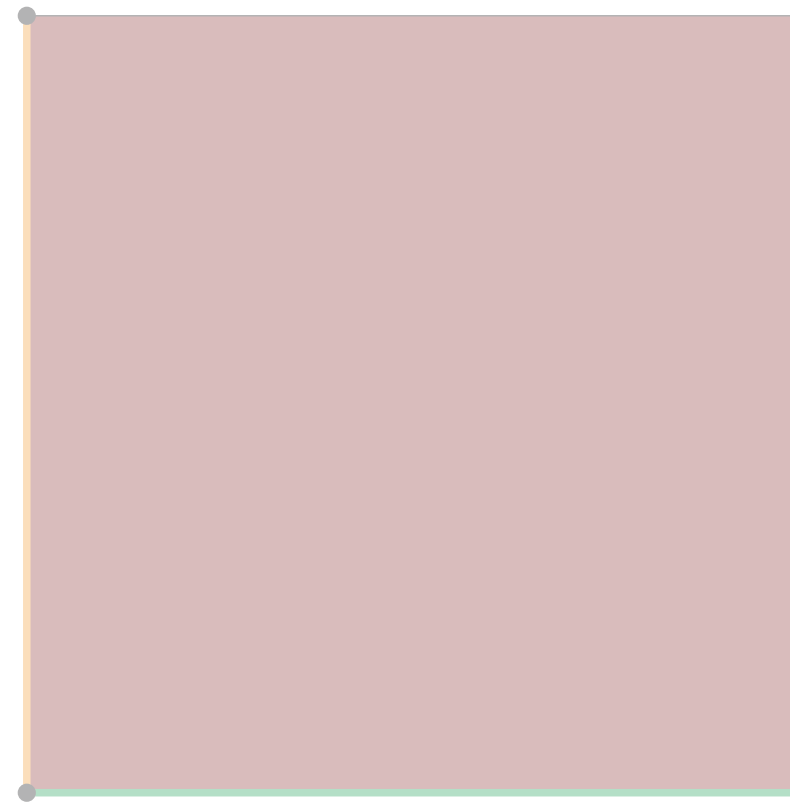
anisotropic



homogeneous

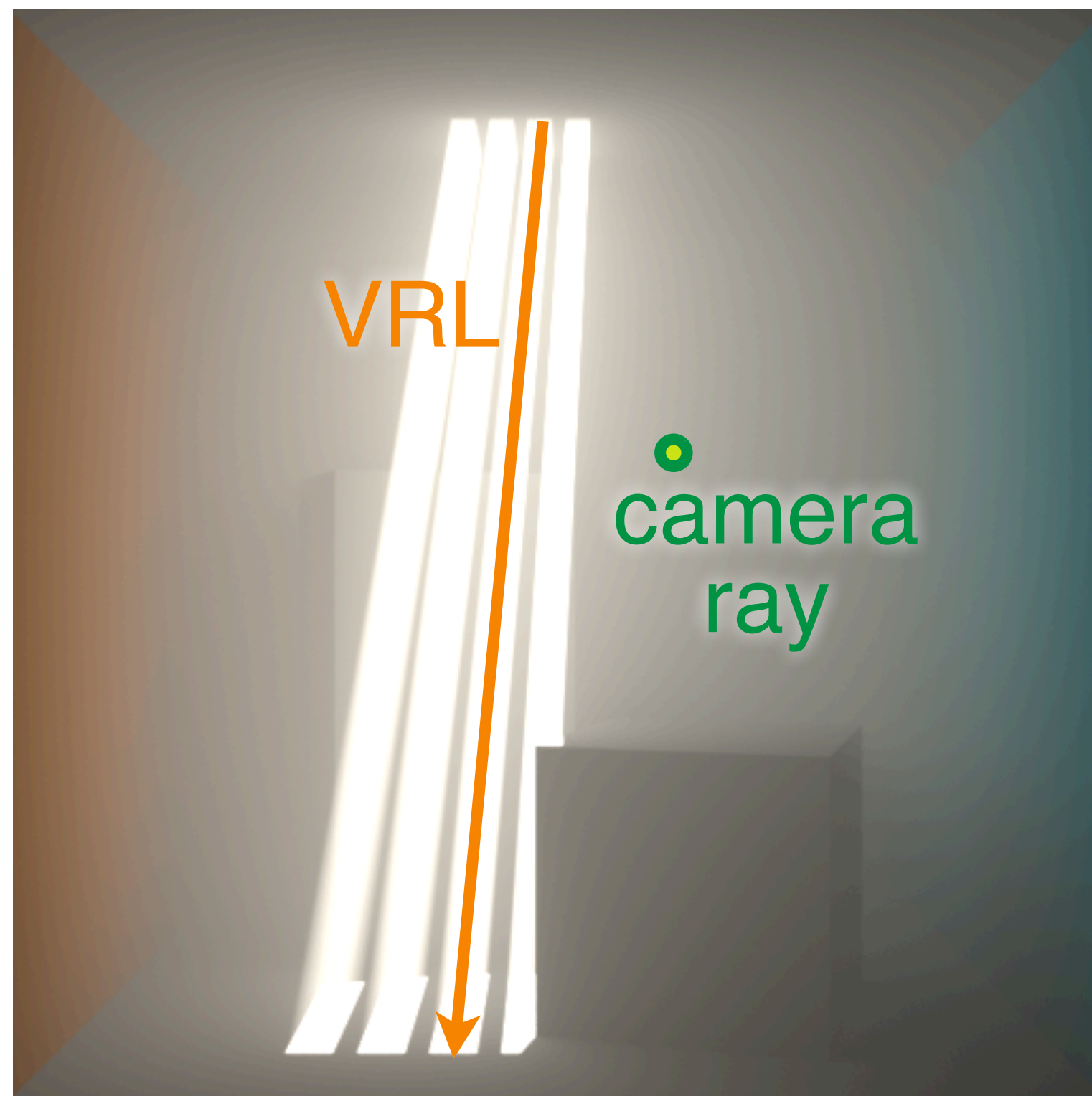


no occlusion

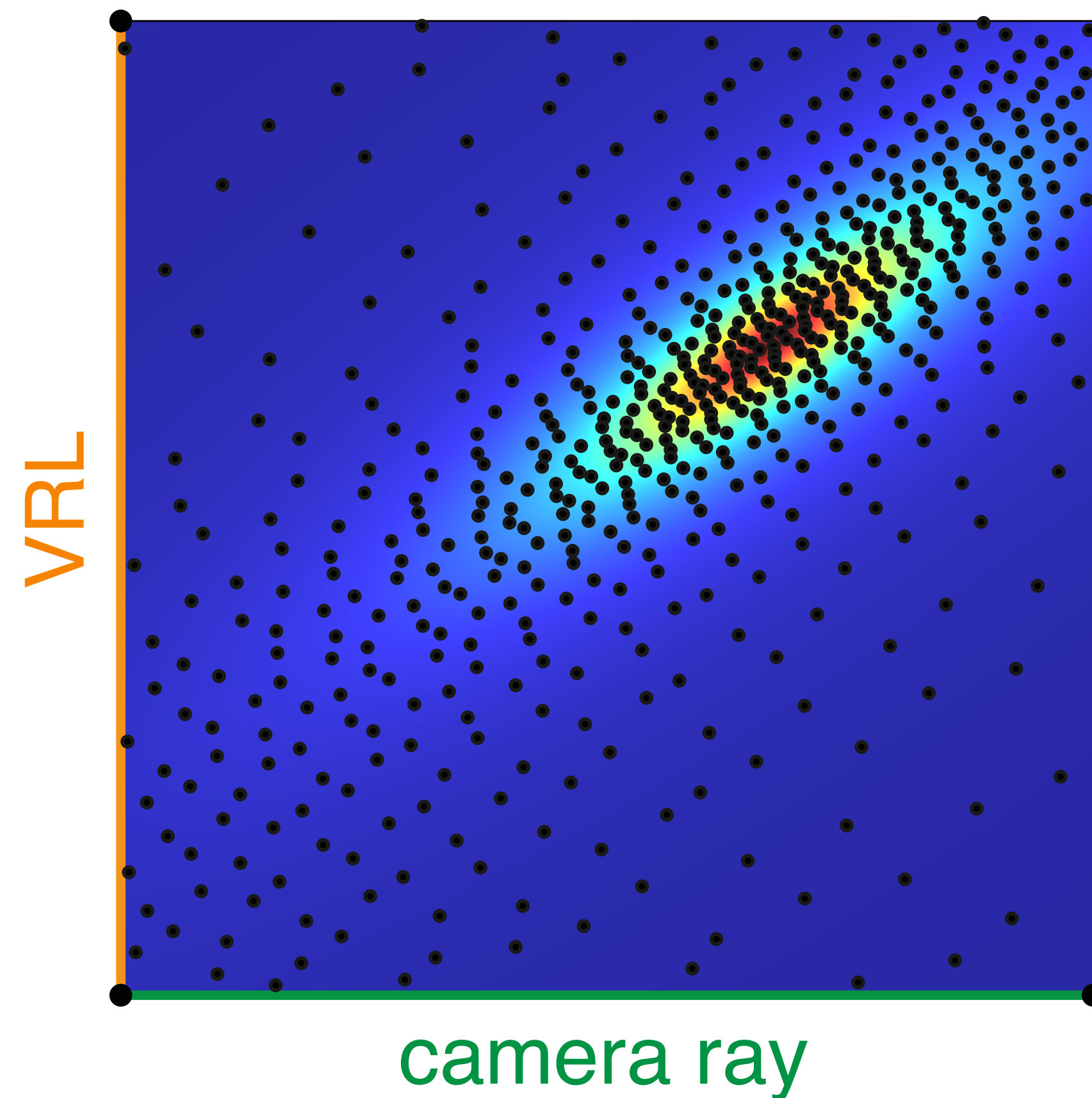


Anisotropic media

isotropic

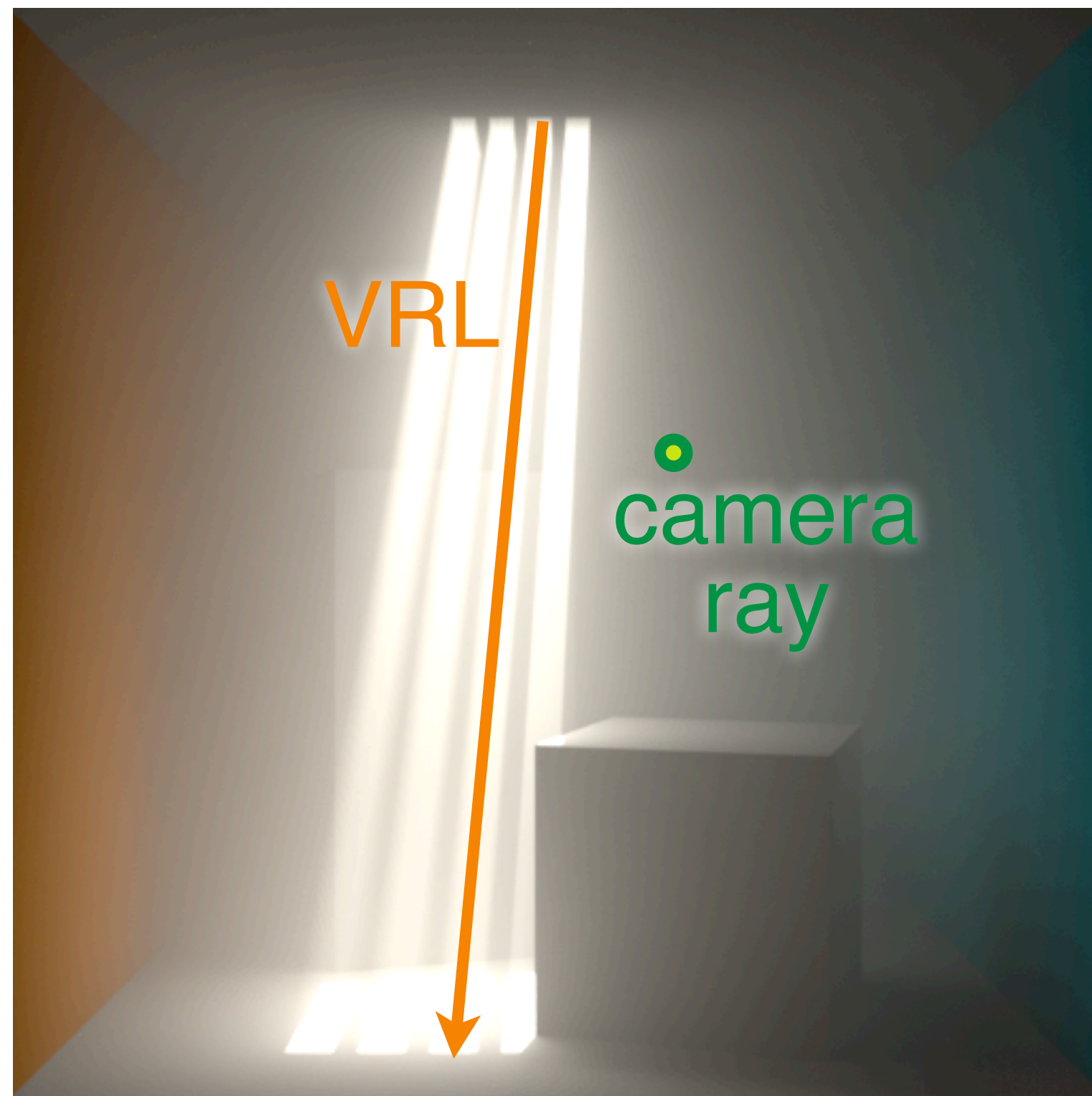


inverse squared distance

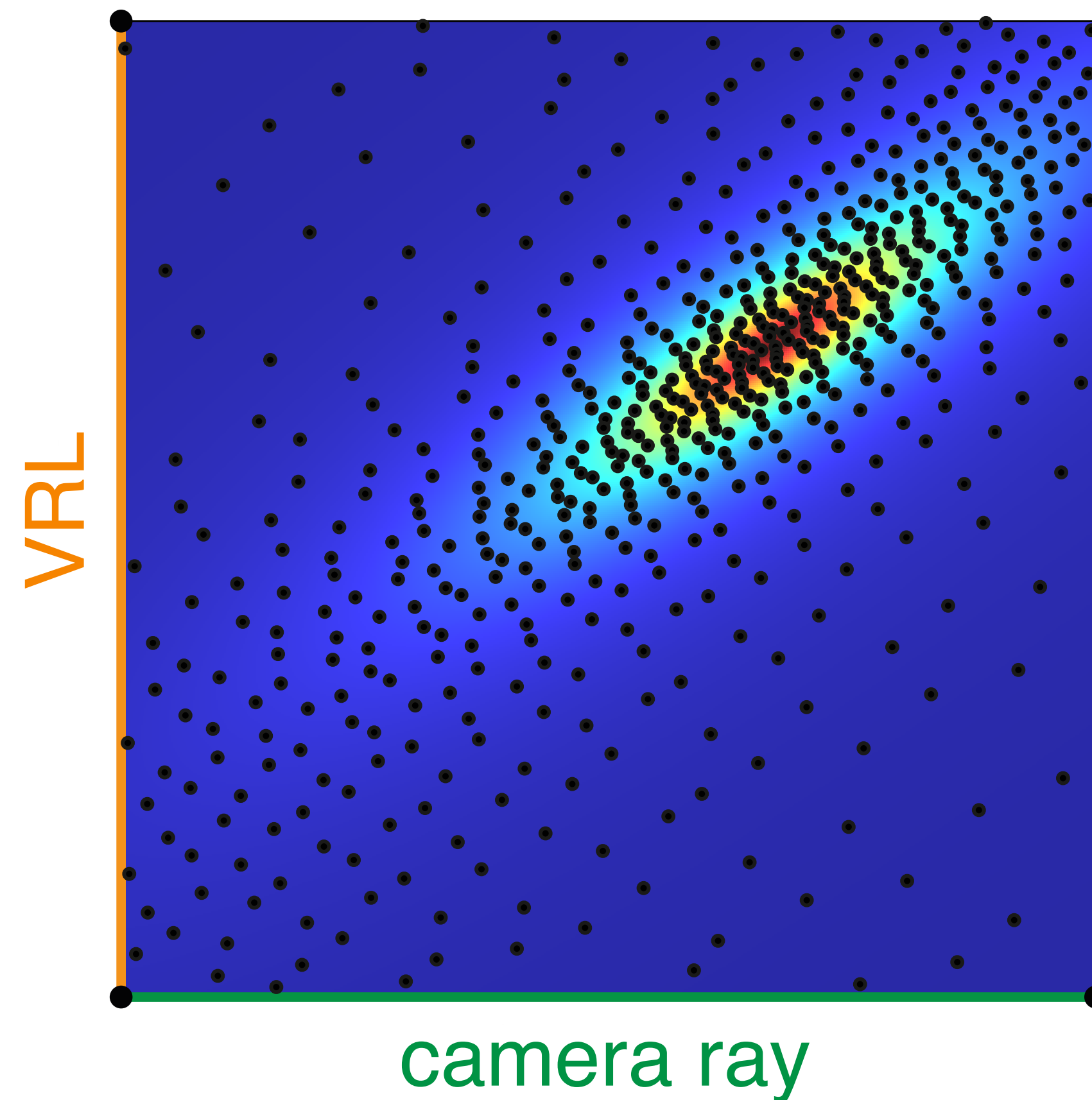


Anisotropic media

anisotropic

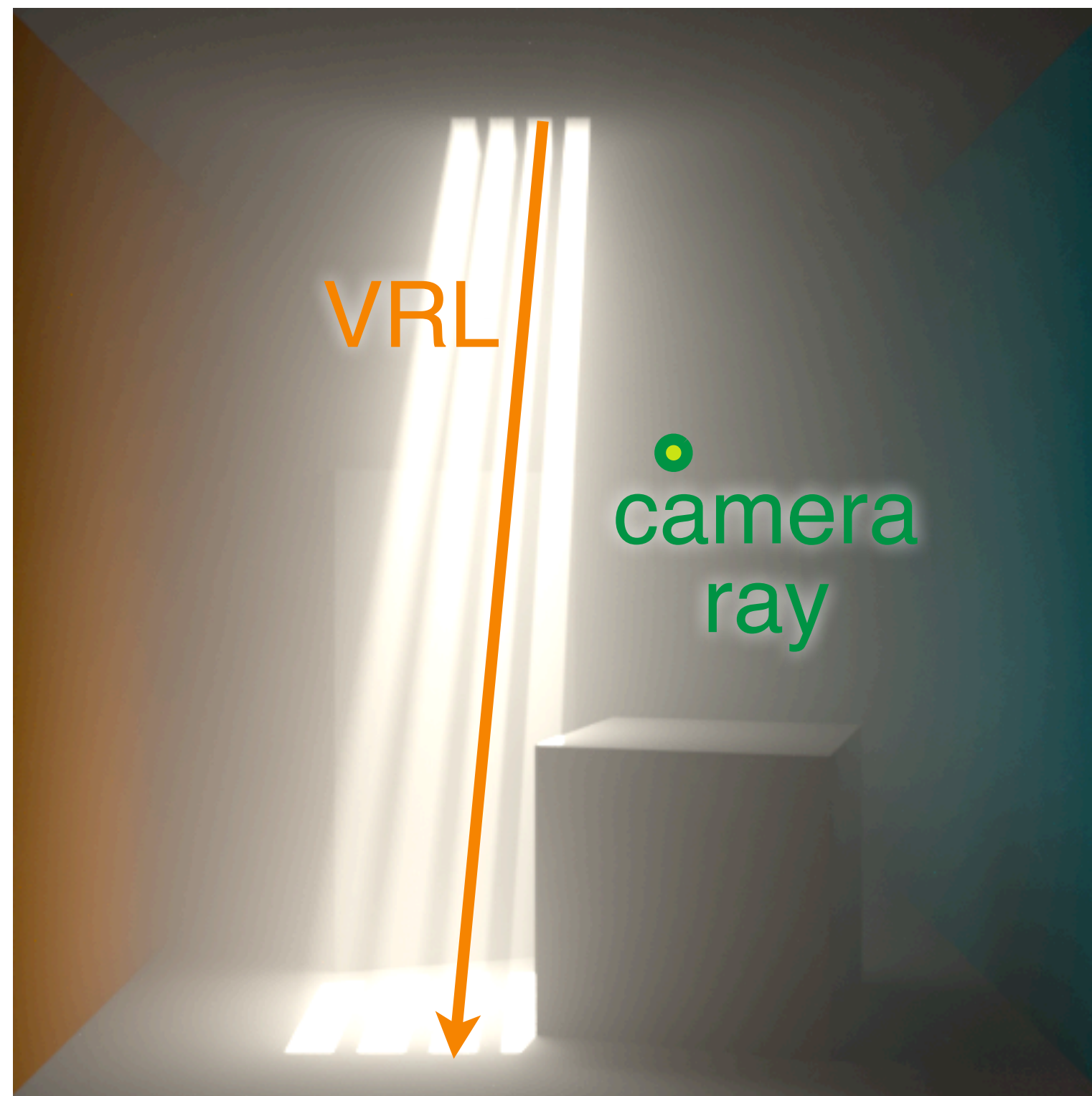


inverse squared distance

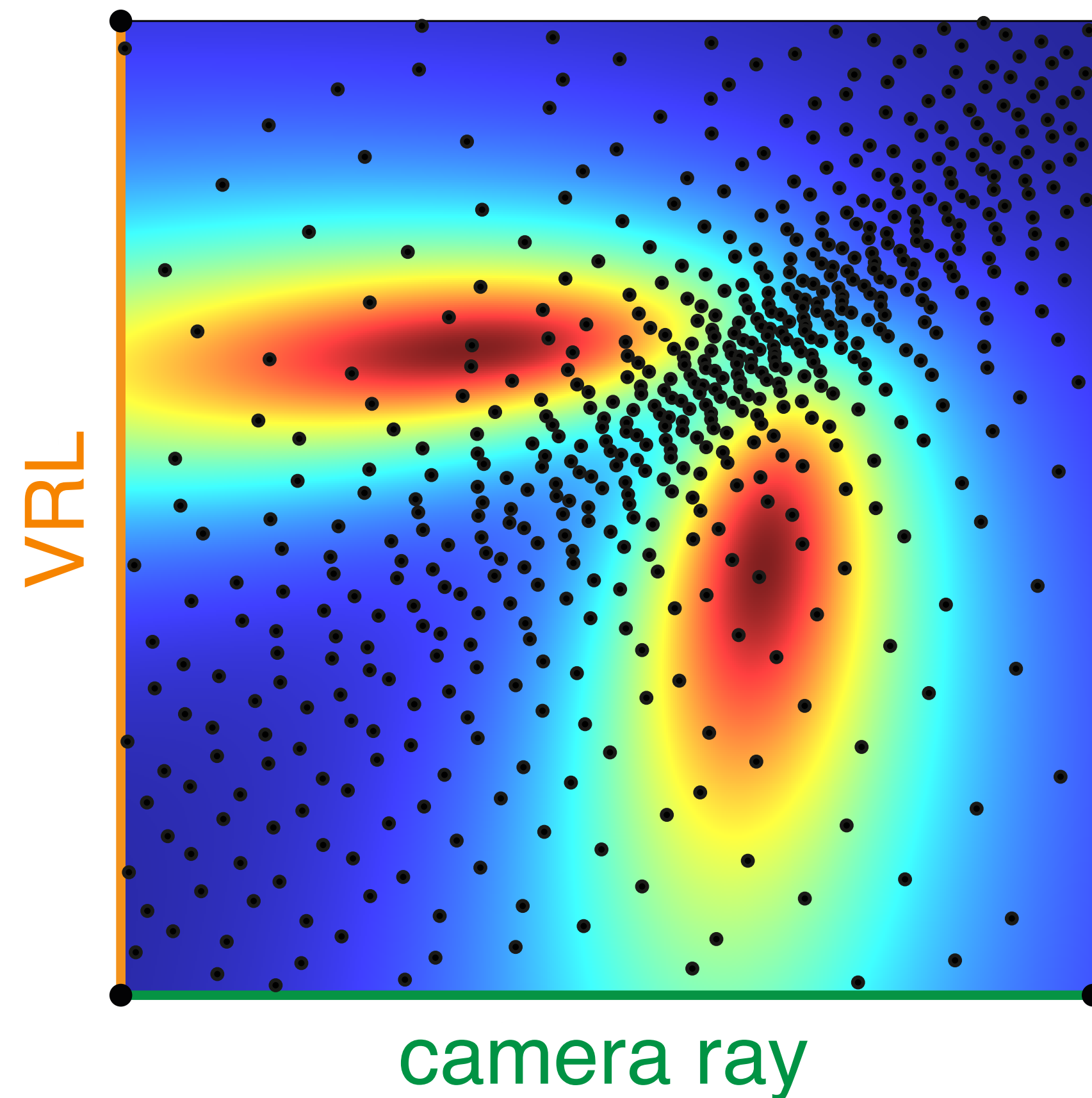


Anisotropic media

anisotropic

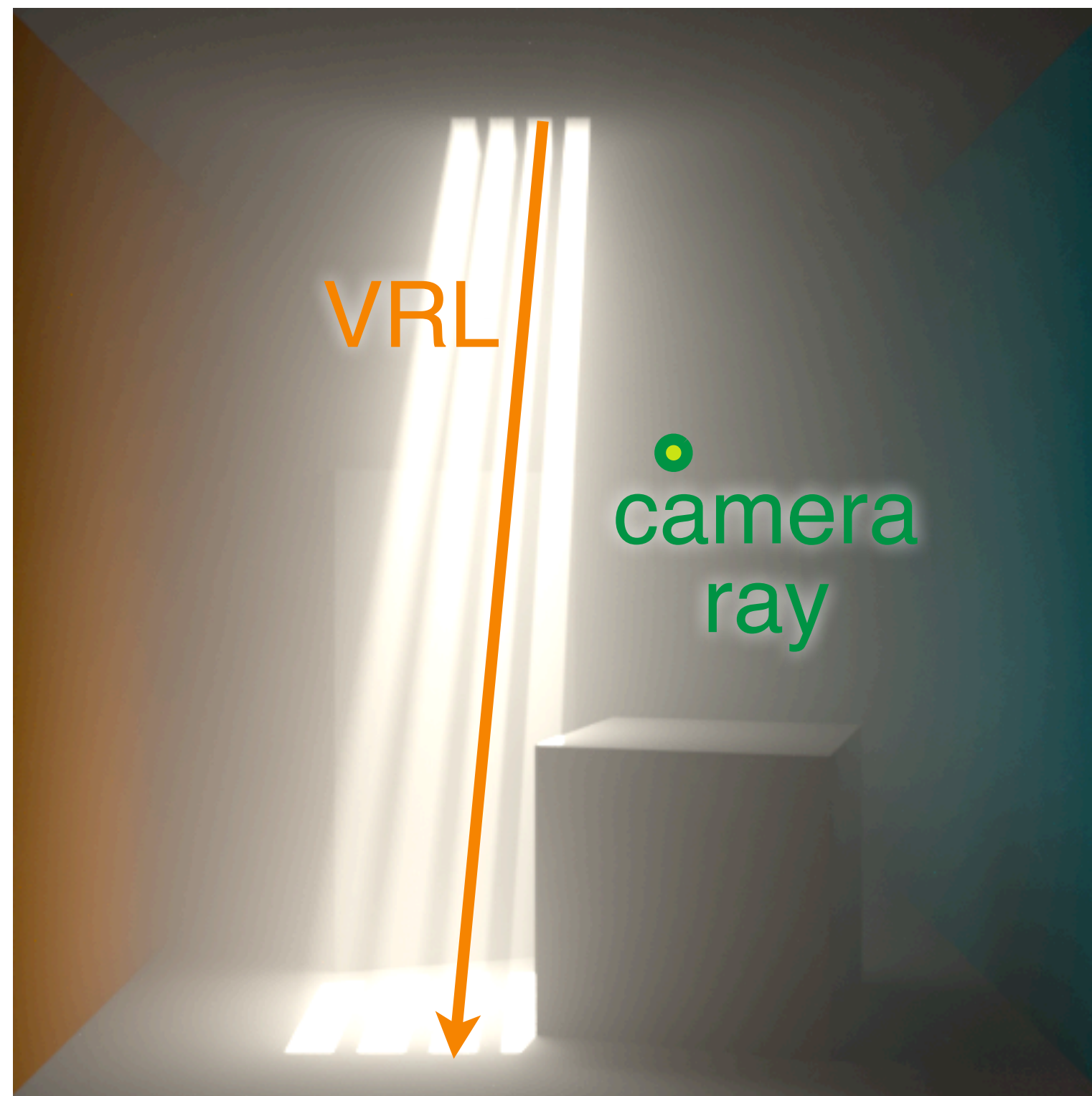


PF product / squared distance

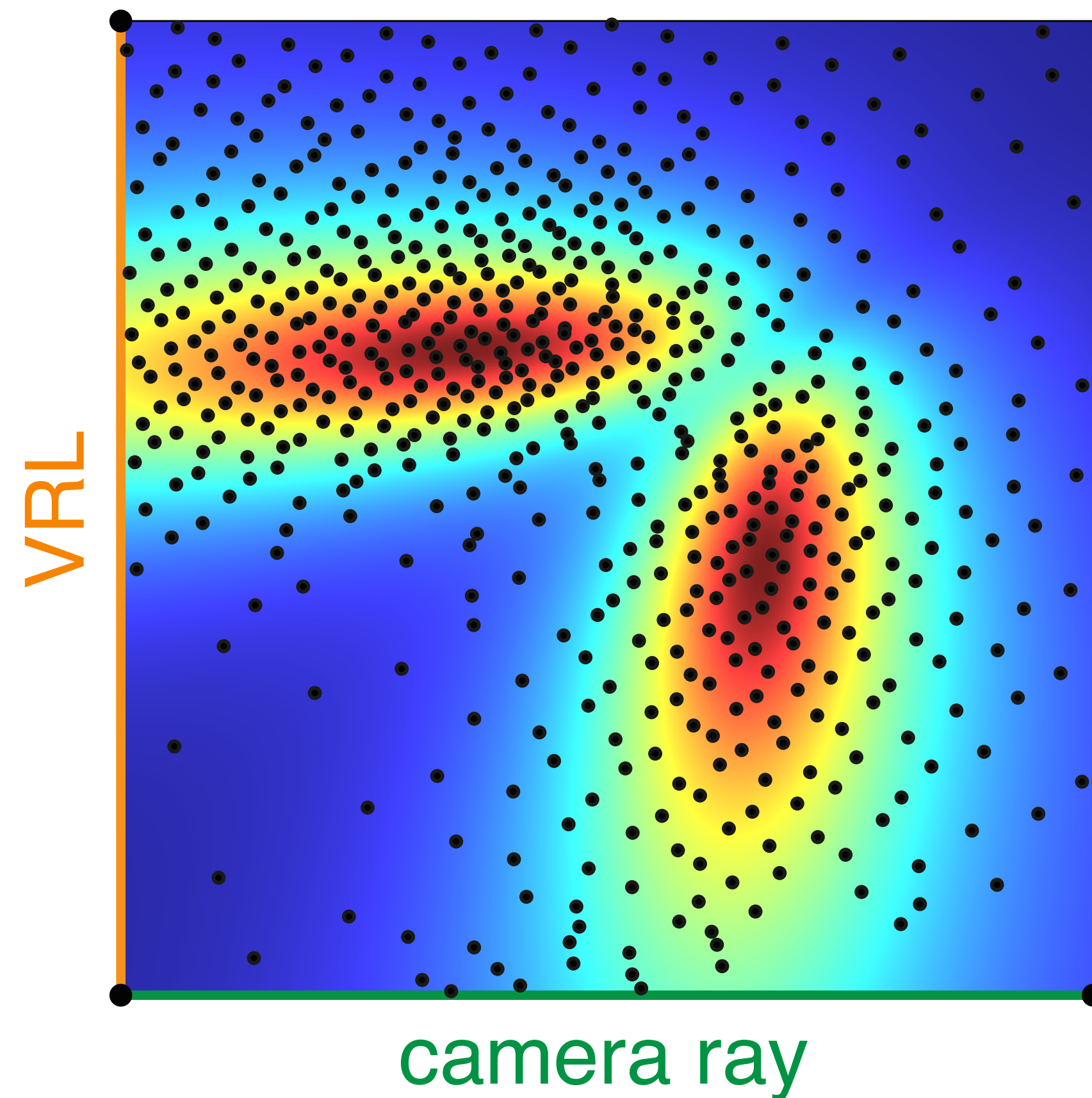


Anisotropic media

anisotropic



PF product / squared distance



Anisotropic media

- **Marginal PDF** 

$$\text{pdf}(v) = \frac{\int_0^s f_s(u) f_s(v) w^{-2} du}{\int_0^t \int_0^s f_s(u) f_s(v) w^{-2} du dv}$$

Anisotropic media

- **Marginal PDF** 

$$\text{pdf}(v) = \frac{\int_0^s \boxed{f_s(u) f_s(v)} w^{-2} \, du}{\int_0^t \int_0^s \boxed{f_s(u) f_s(v)} w^{-2} \, du \, dv}$$

Anisotropic media

- **Marginal PDF** 

$$\text{pdf}(v) = \frac{\int_0^s f_s(u) f_s(v) w^{-2} du}{\int_0^t \int_0^s f_s(u) f_s(v) w^{-2} du dv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} du dv}$$

Anisotropic media

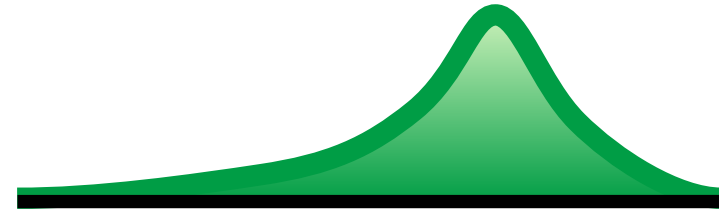
- **Marginal PDF** 

$$\text{pdf}(v) = \frac{\int_0^s f_s(u) f_s(v) w^{-2} du}{\int_0^t \int_0^s f_s(u) f_s(v) w^{-2} du dv} \approx \frac{\int_{-\infty}^{\infty} w^{-2} du}{\int_0^t \int_{-\infty}^{\infty} w^{-2} du dv}$$

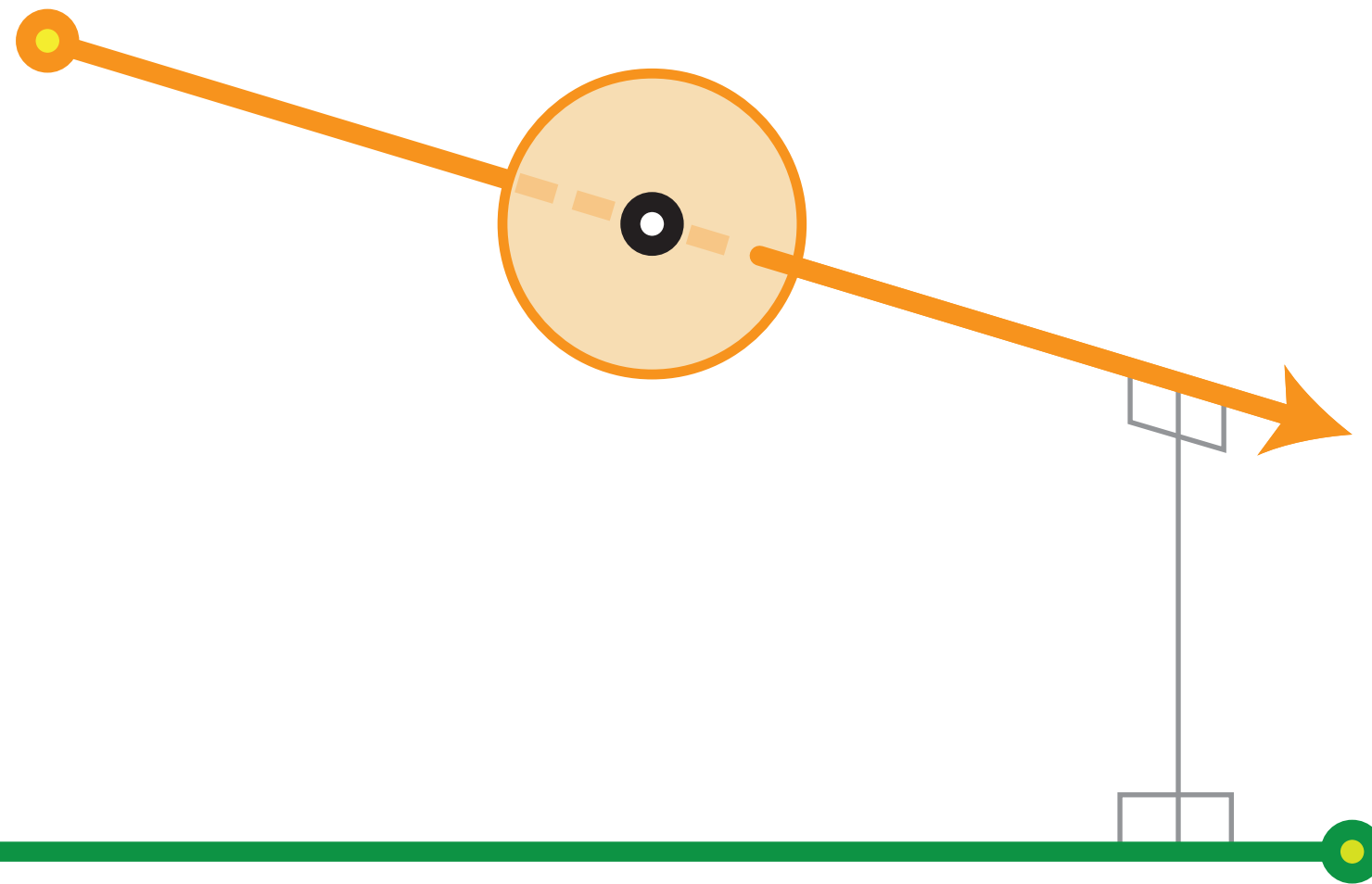
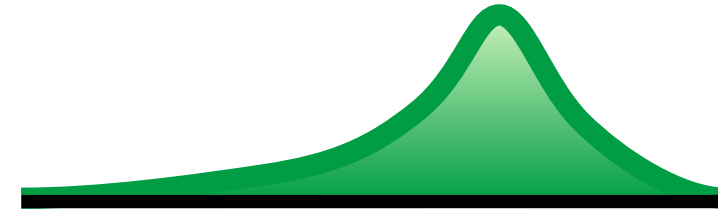
identical to isotropic medium

Anisotropic media

Anisotropic media

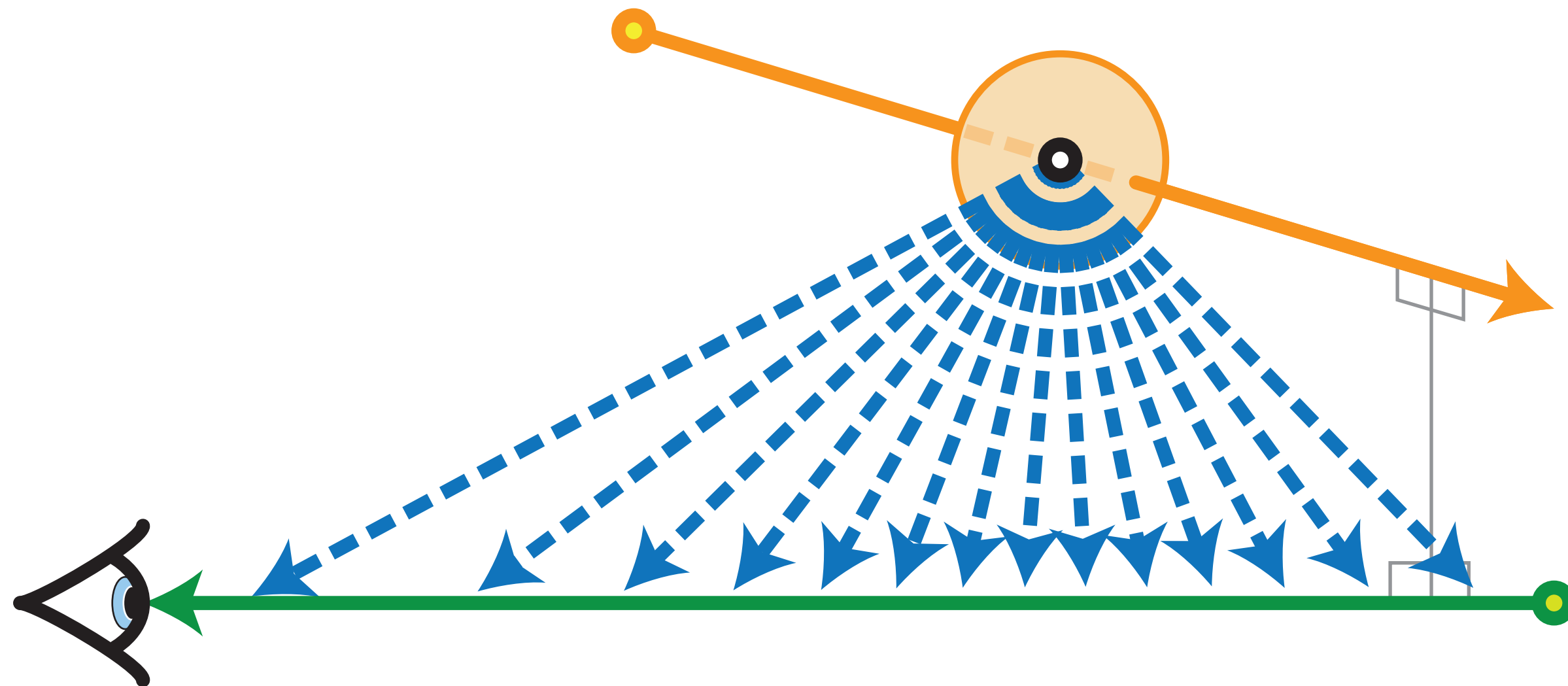
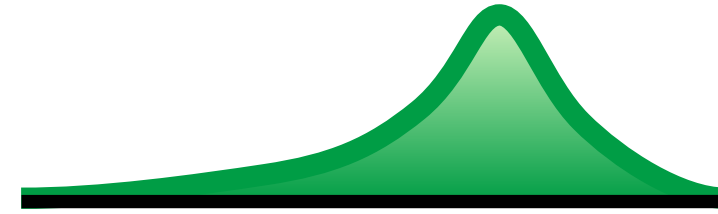


Anisotropic media



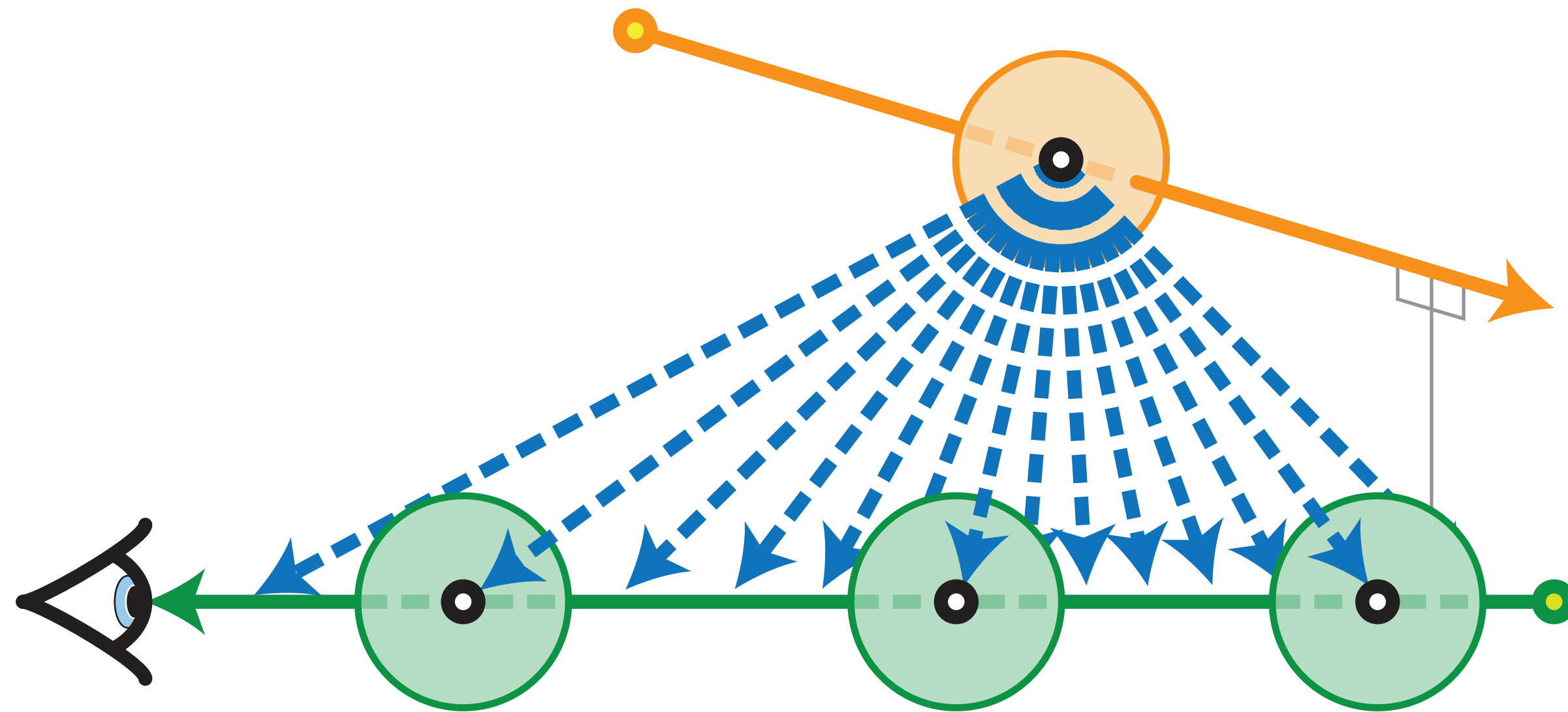
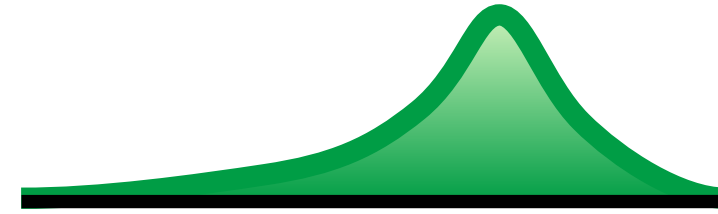
isotropic \sim equi-angular

Anisotropic media



isotropic \sim equi-angular

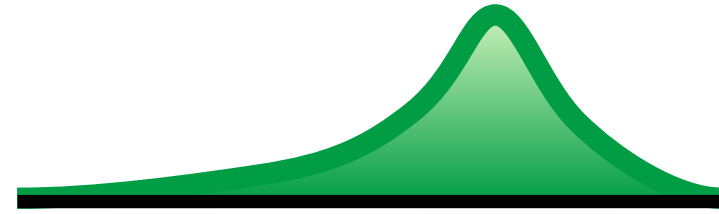
Anisotropic media



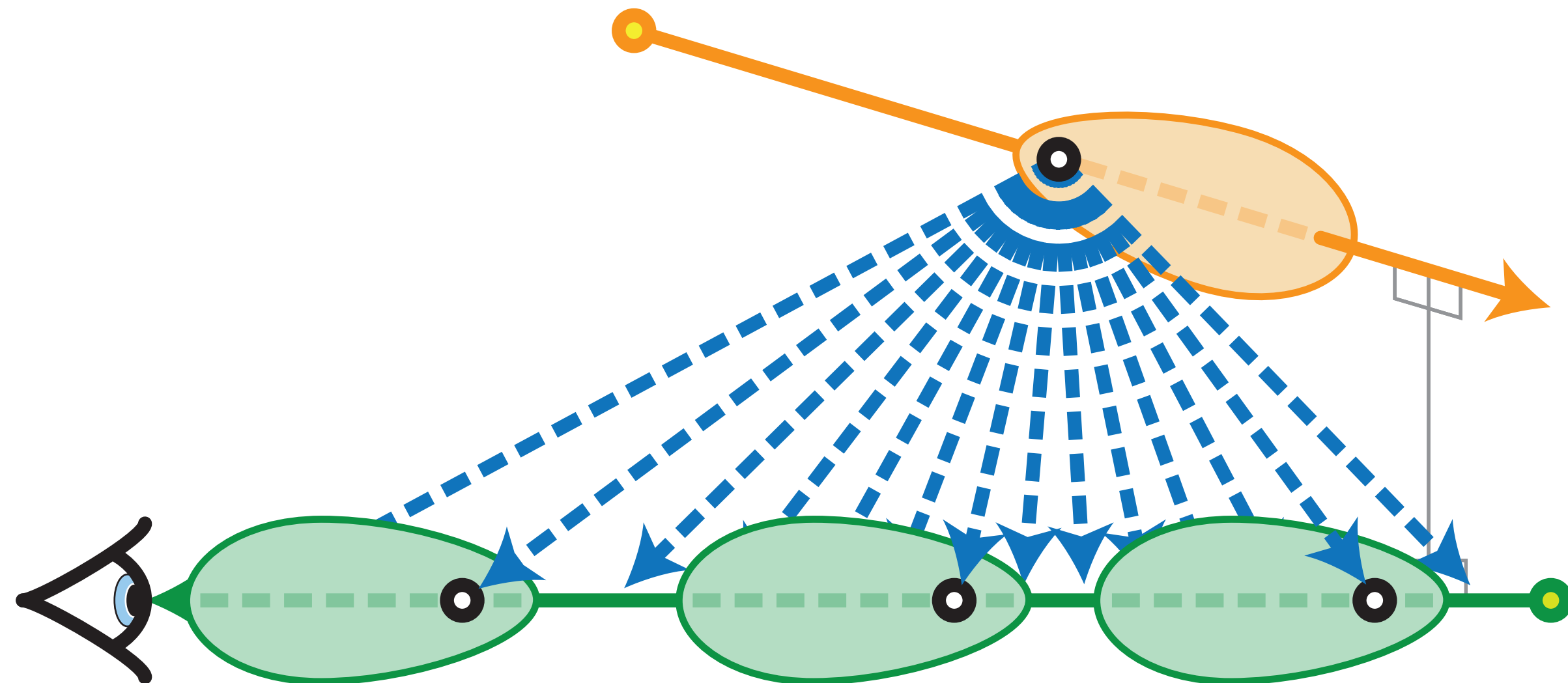
isotropic \sim equi-angular

Anisotropic media

- **Conditional PDF**



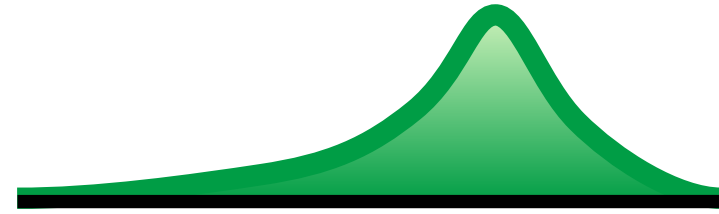
- ▶ replace equi-angular sampling by **importance sampling the PF product**



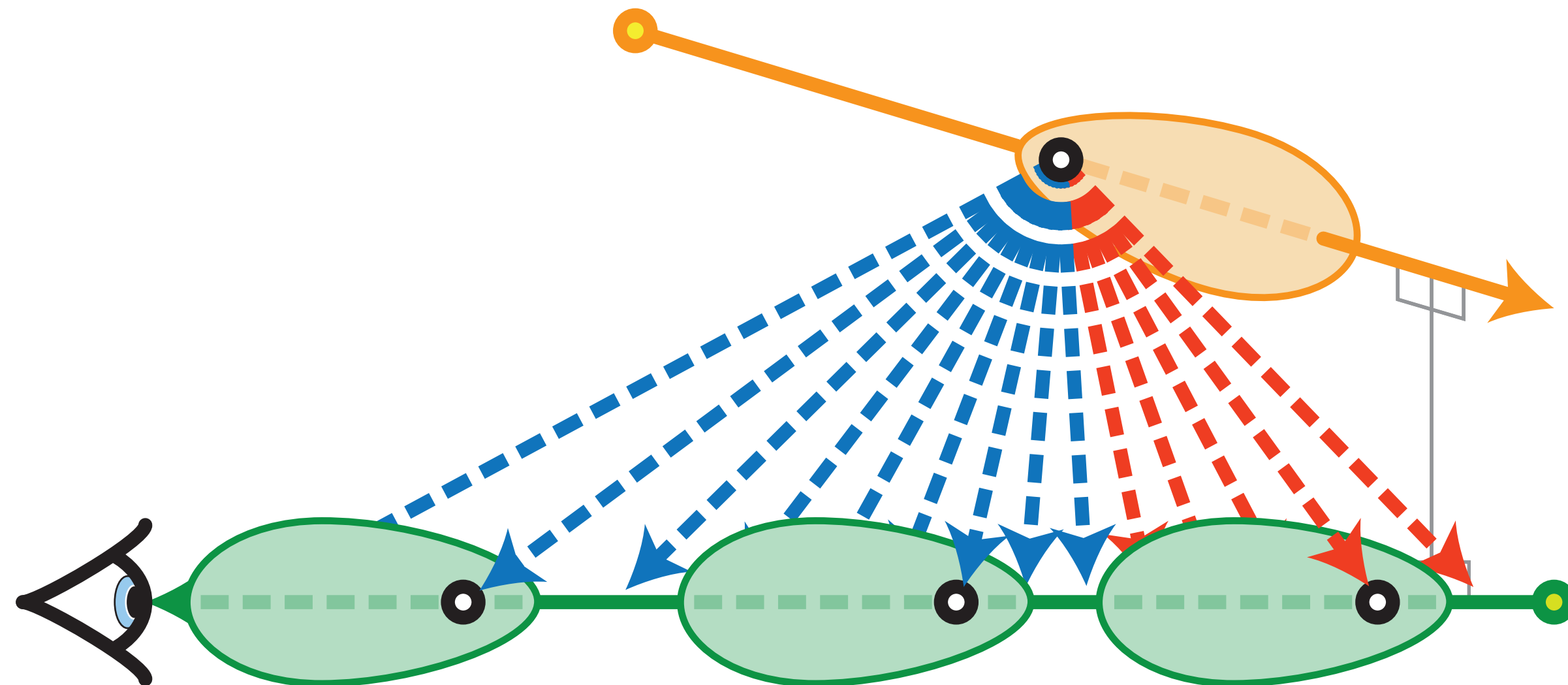
anisotropic

Anisotropic media

- **Conditional PDF**



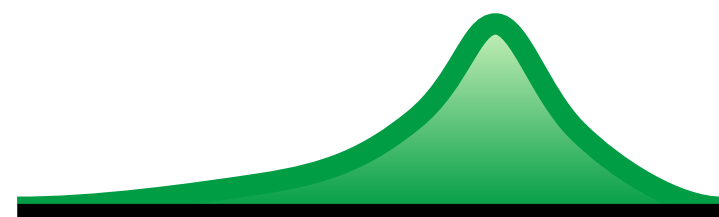
- ▶ replace equi-angular sampling by **importance sampling the PF product**



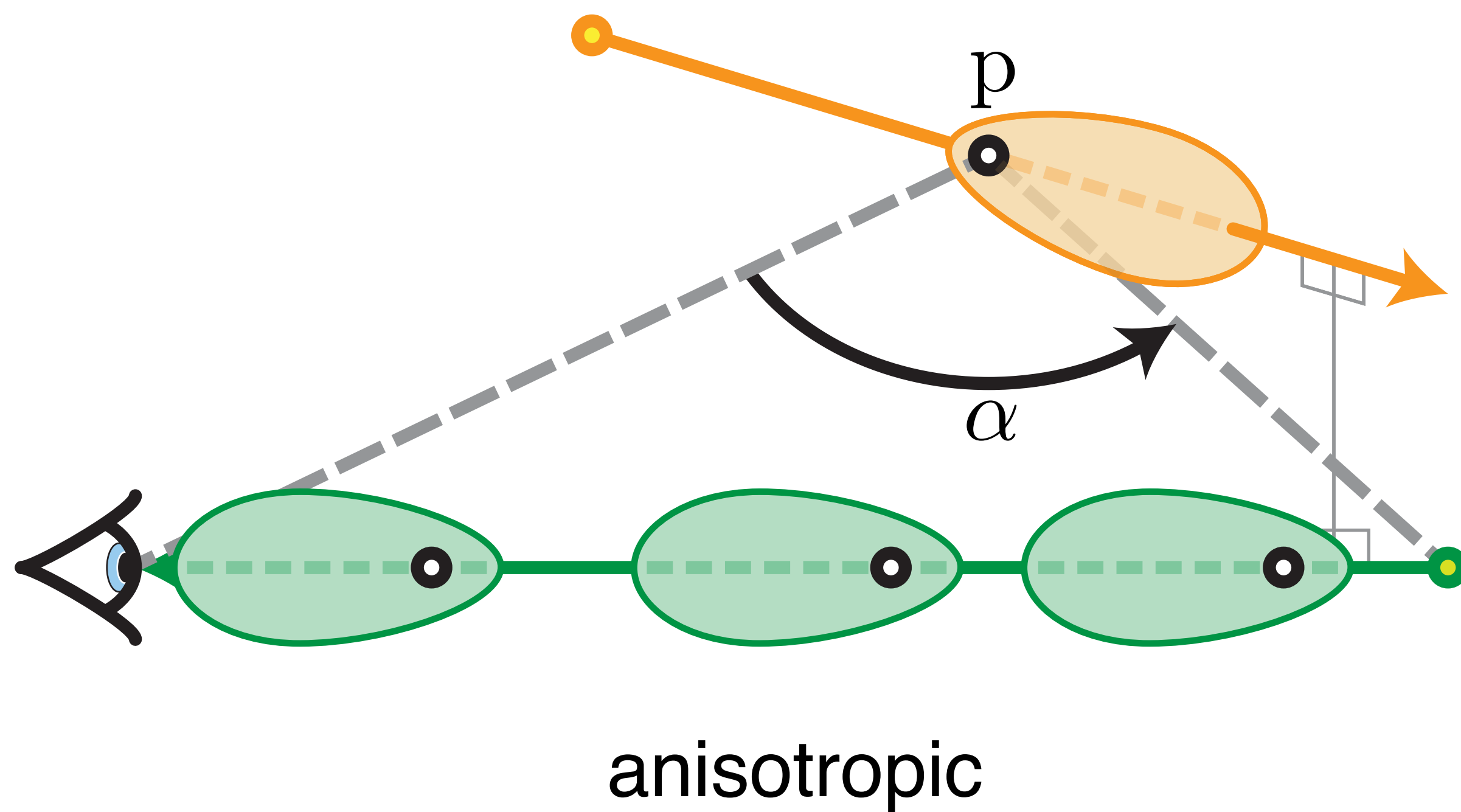
anisotropic

Anisotropic media

- **Conditional PDF**

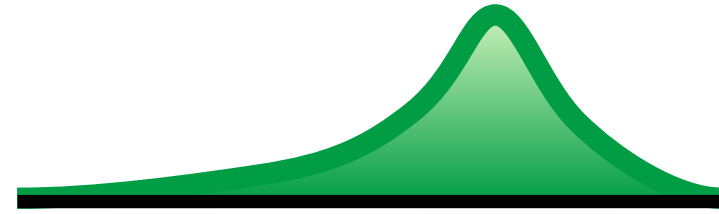


- ▶ replace equi-angular sampling by **importance sampling the PF product**

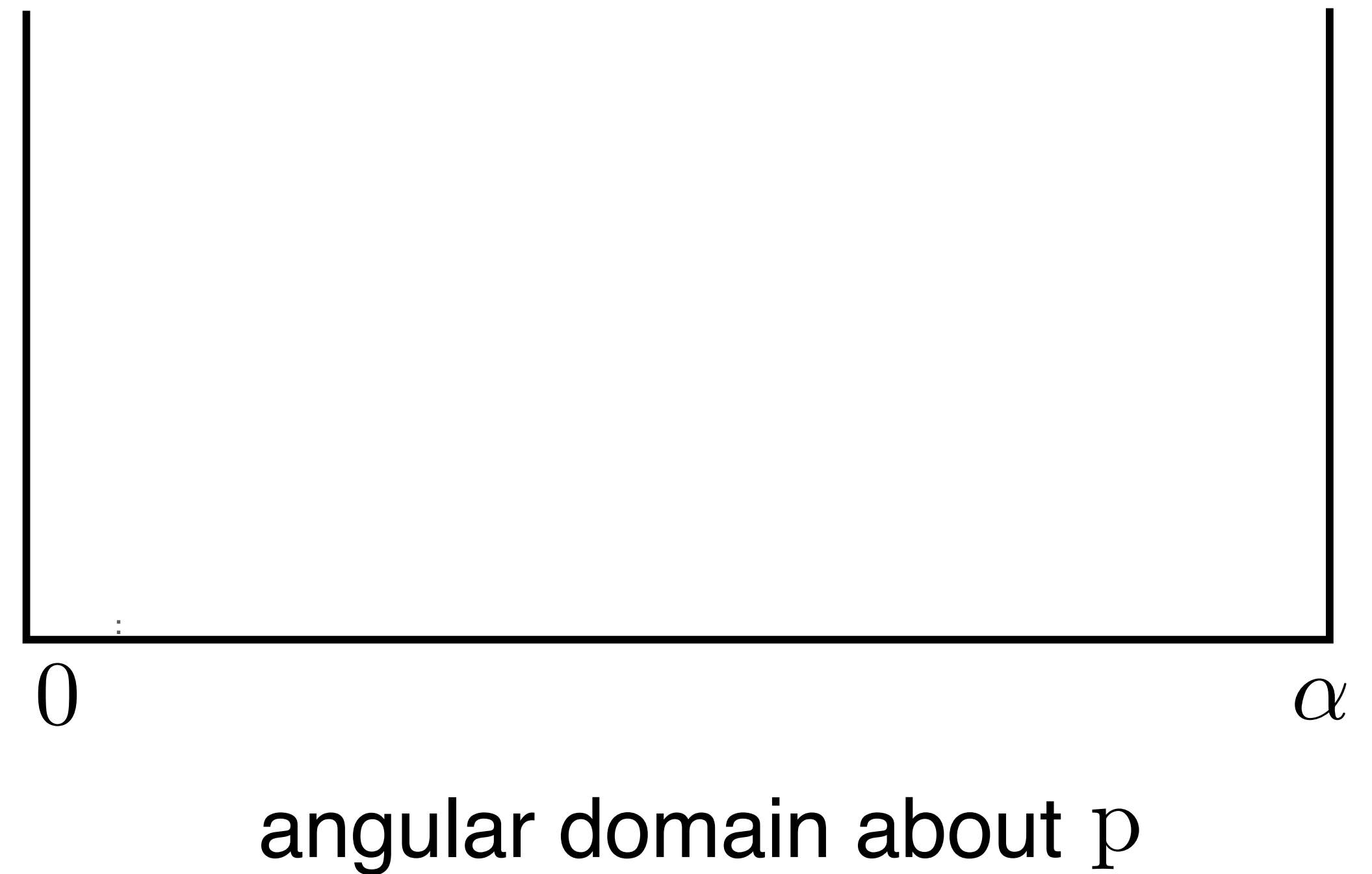
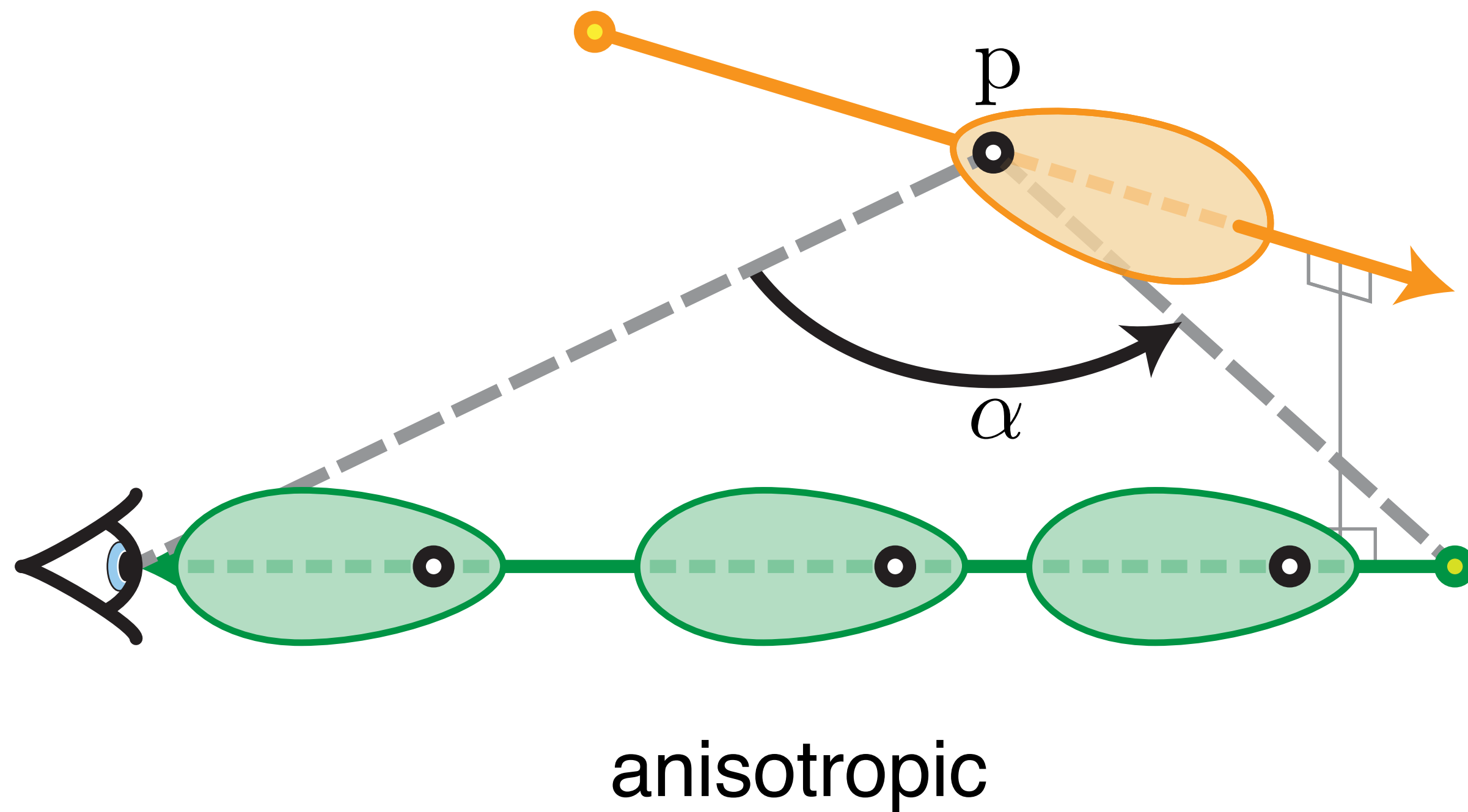


Anisotropic media

- **Conditional PDF**

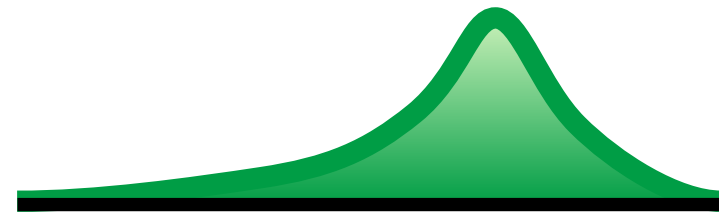


- ▶ replace equi-angular sampling by **importance sampling the PF product**

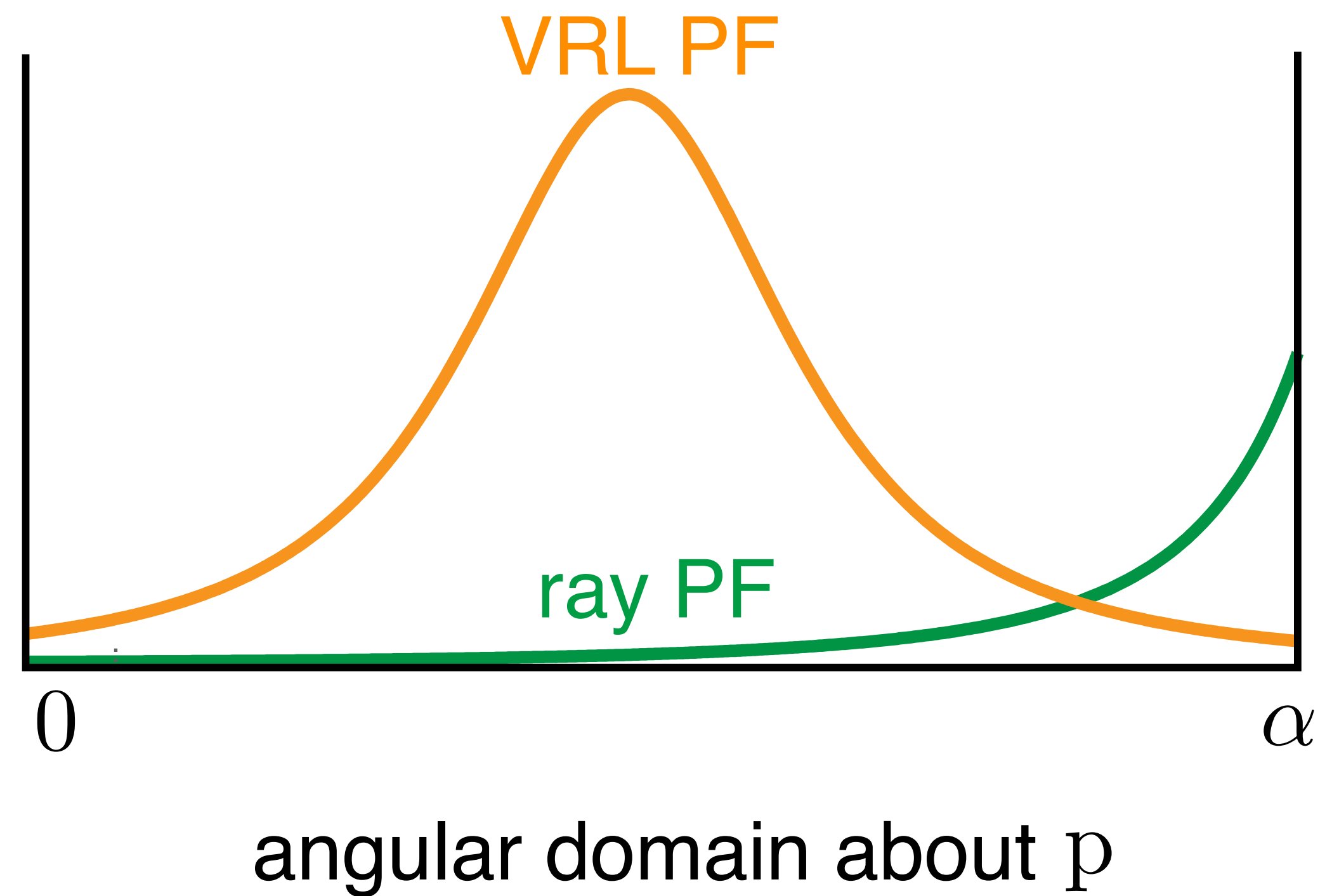
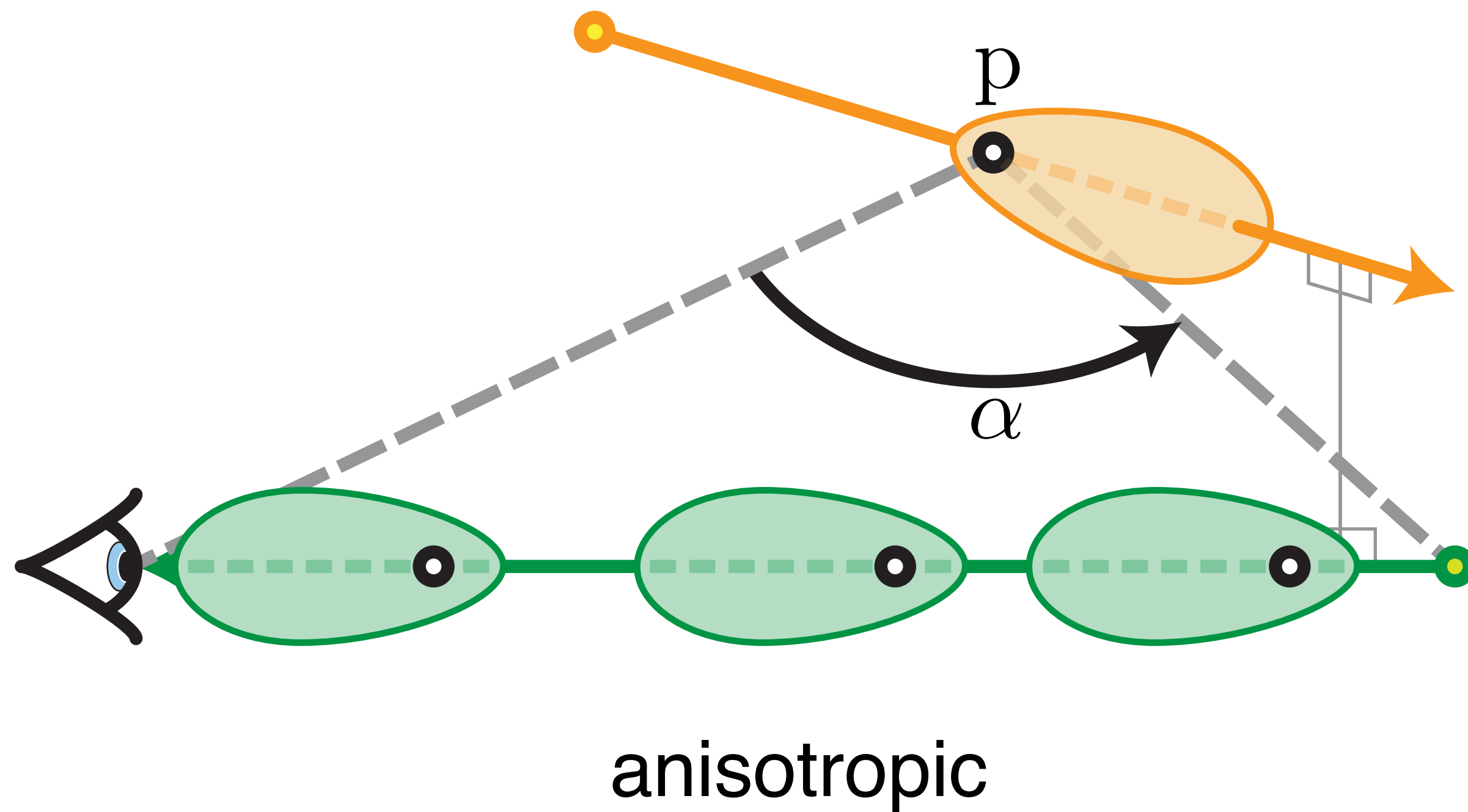


Anisotropic media

- **Conditional PDF**

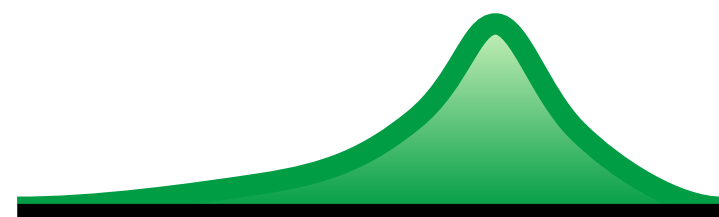


- ▶ replace equi-angular sampling by **importance sampling the PF product**

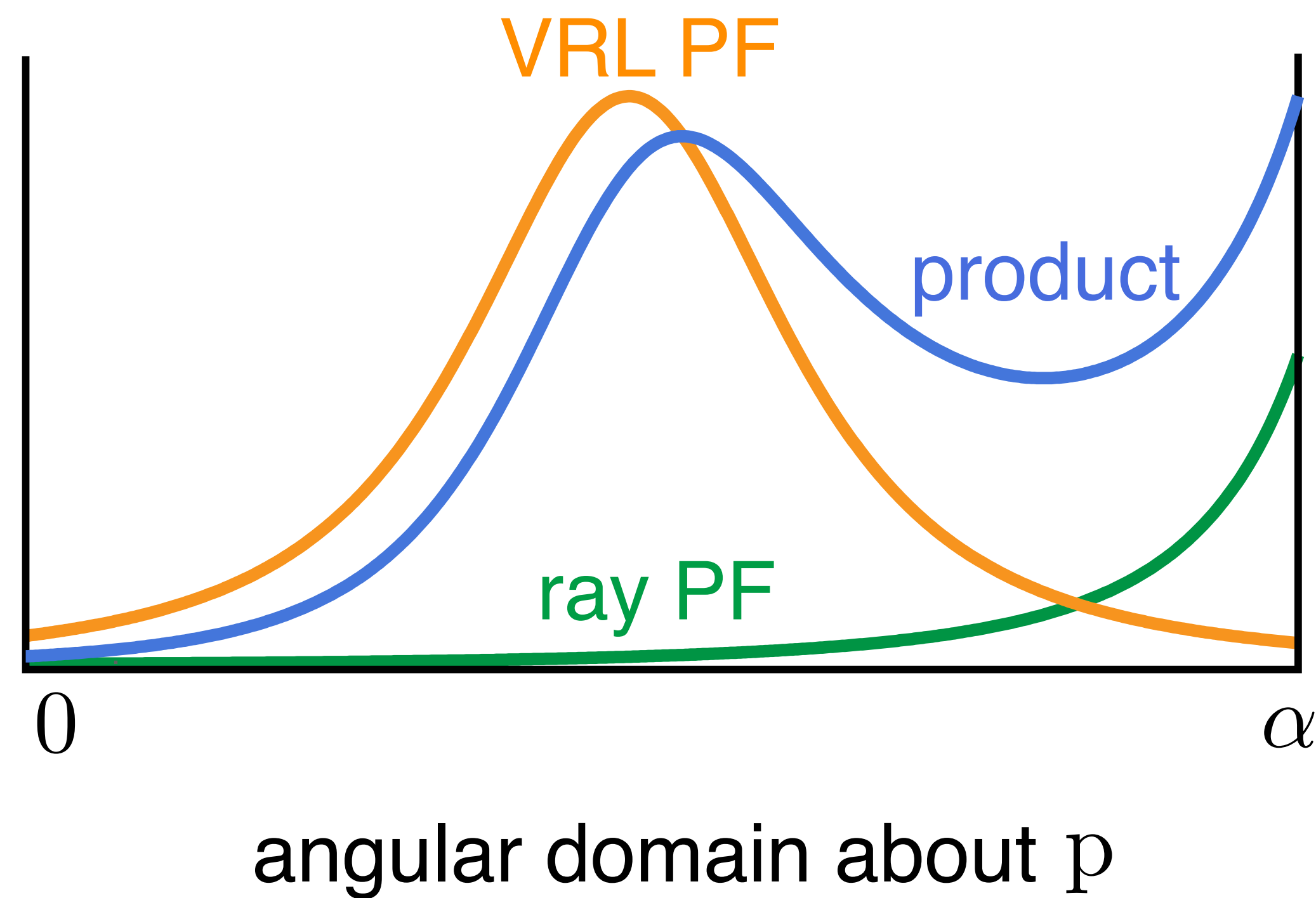
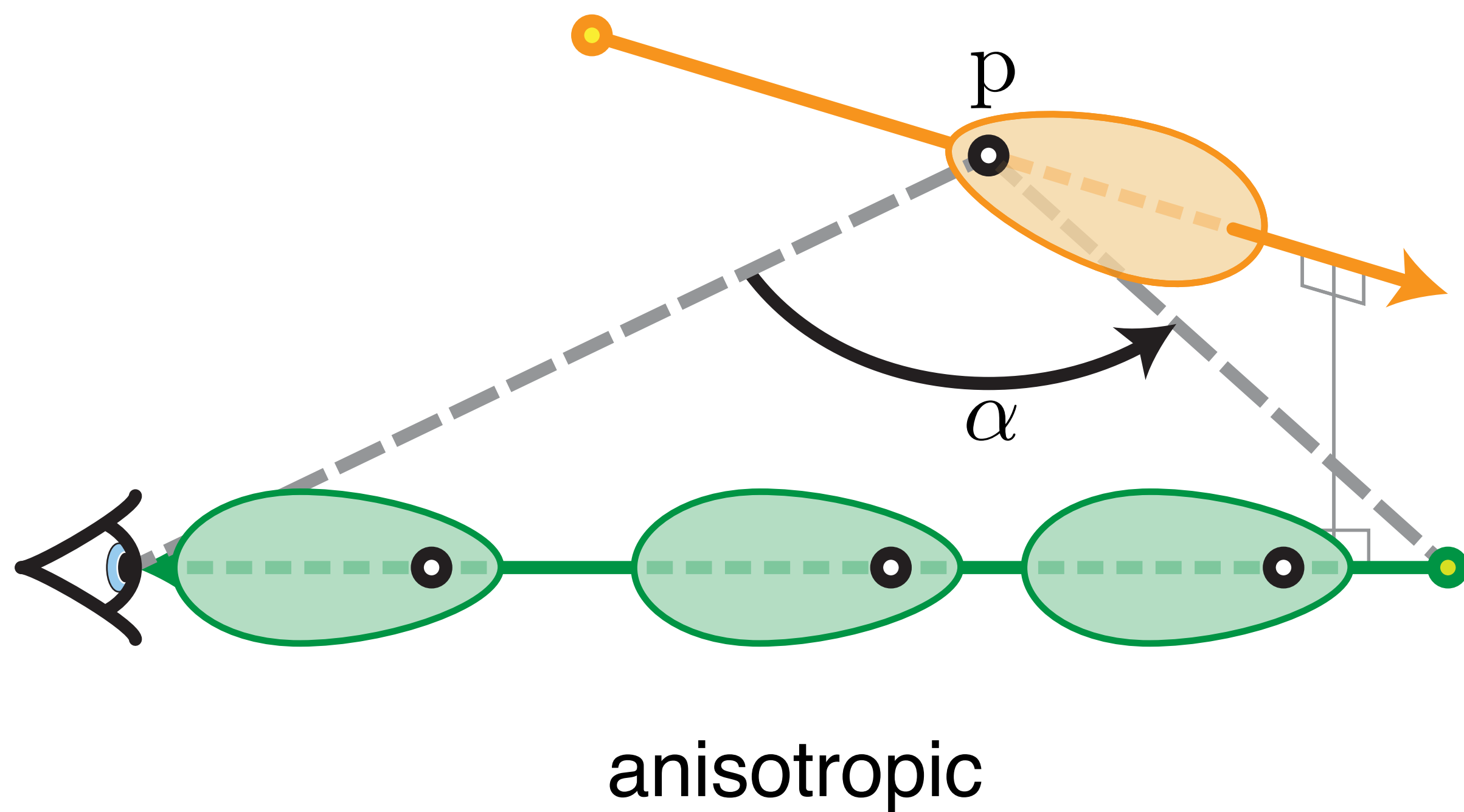


Anisotropic media

- **Conditional PDF**

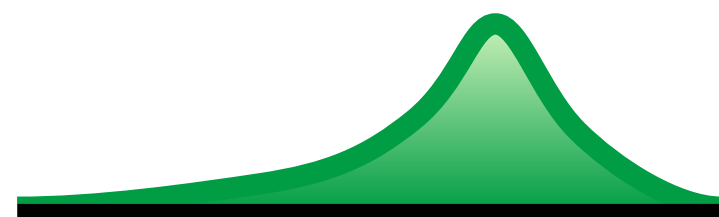


- ▶ replace equi-angular sampling by **importance sampling the PF product**

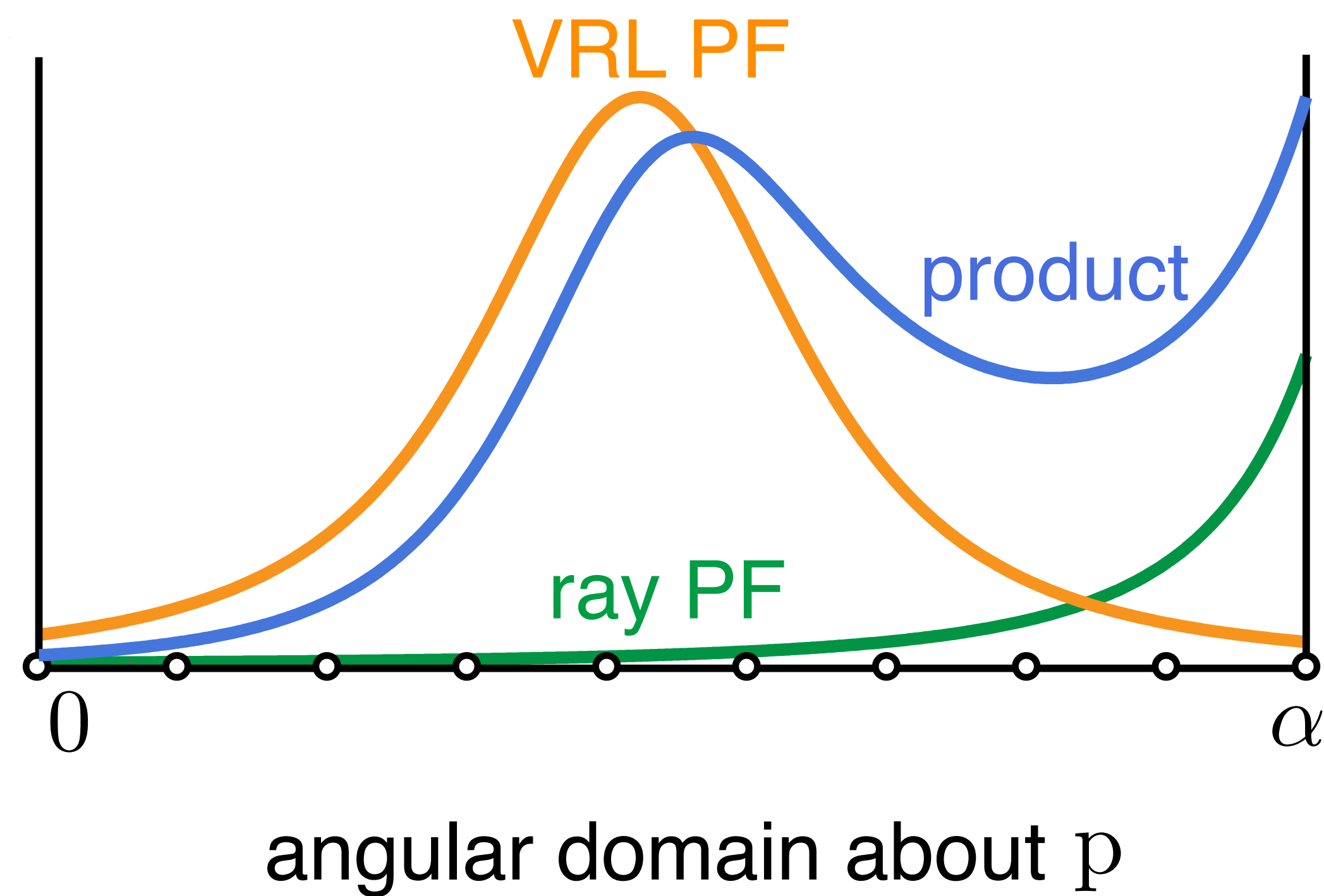
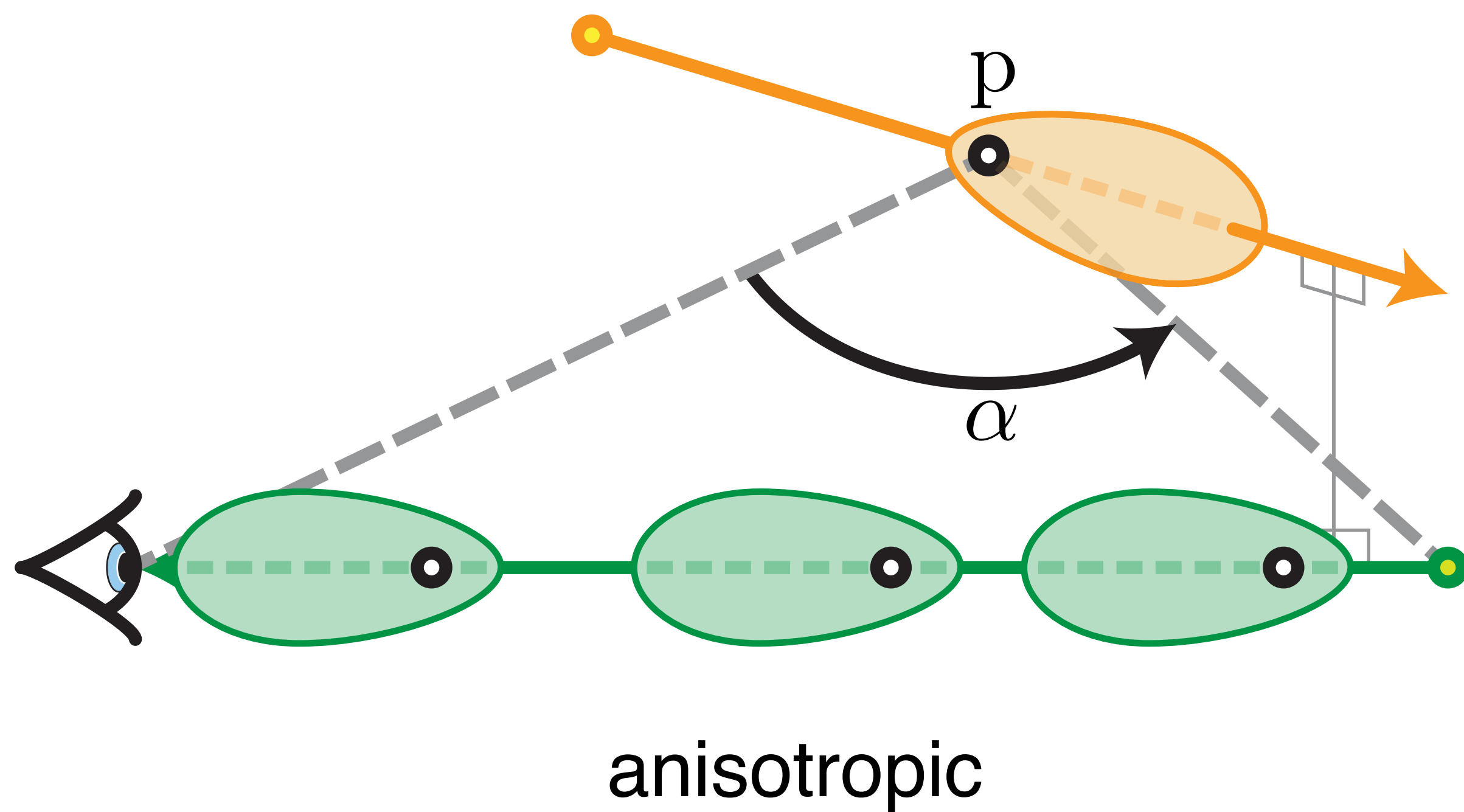


Anisotropic media

- **Conditional PDF**

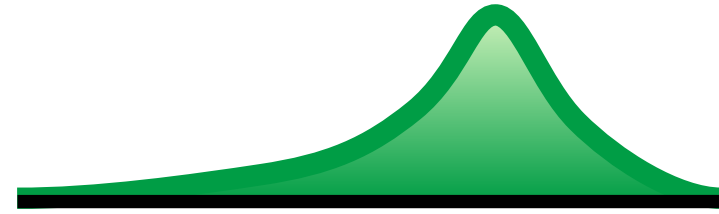


- ▶ replace equi-angular sampling by **importance sampling the PF product**

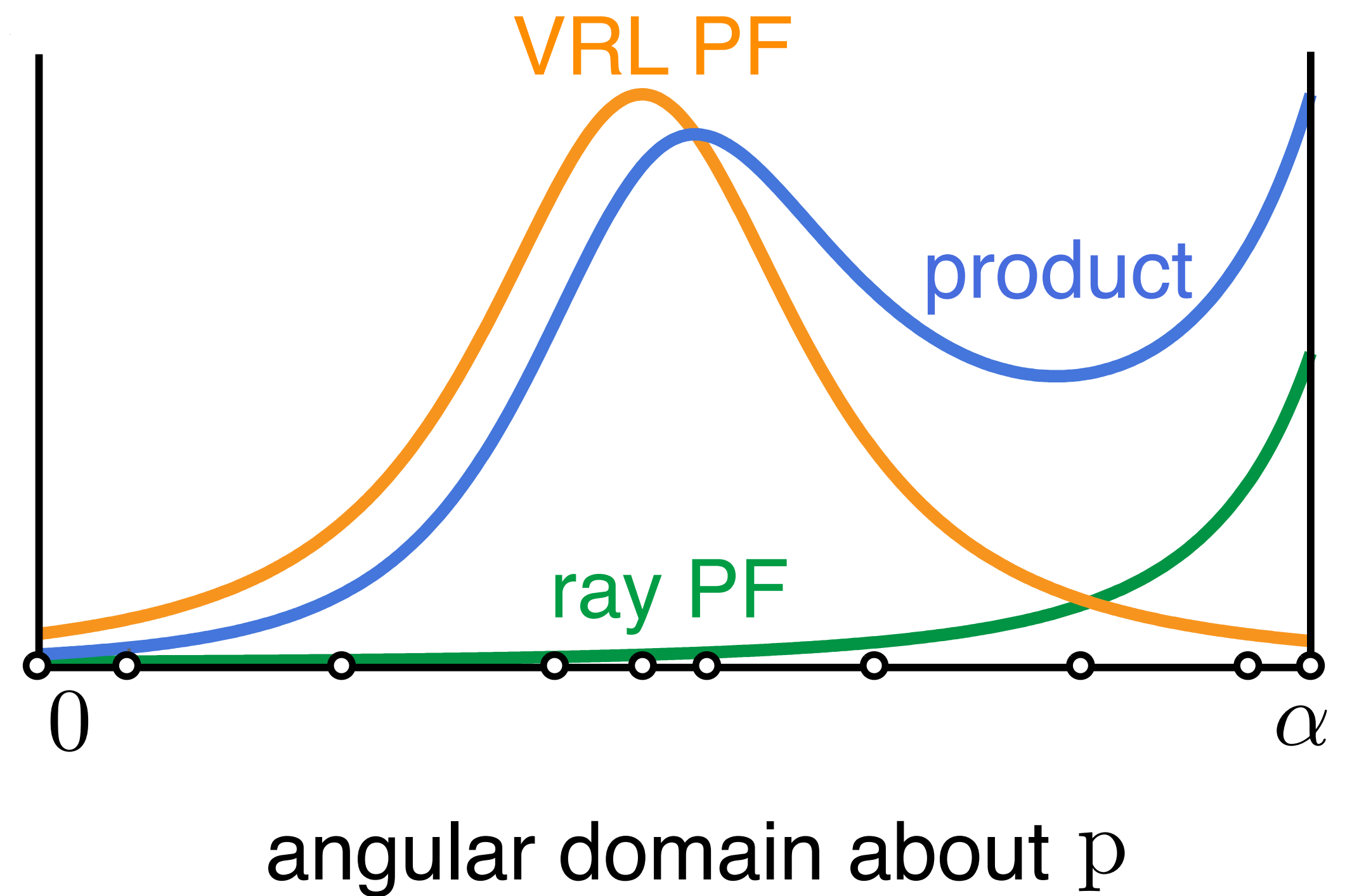
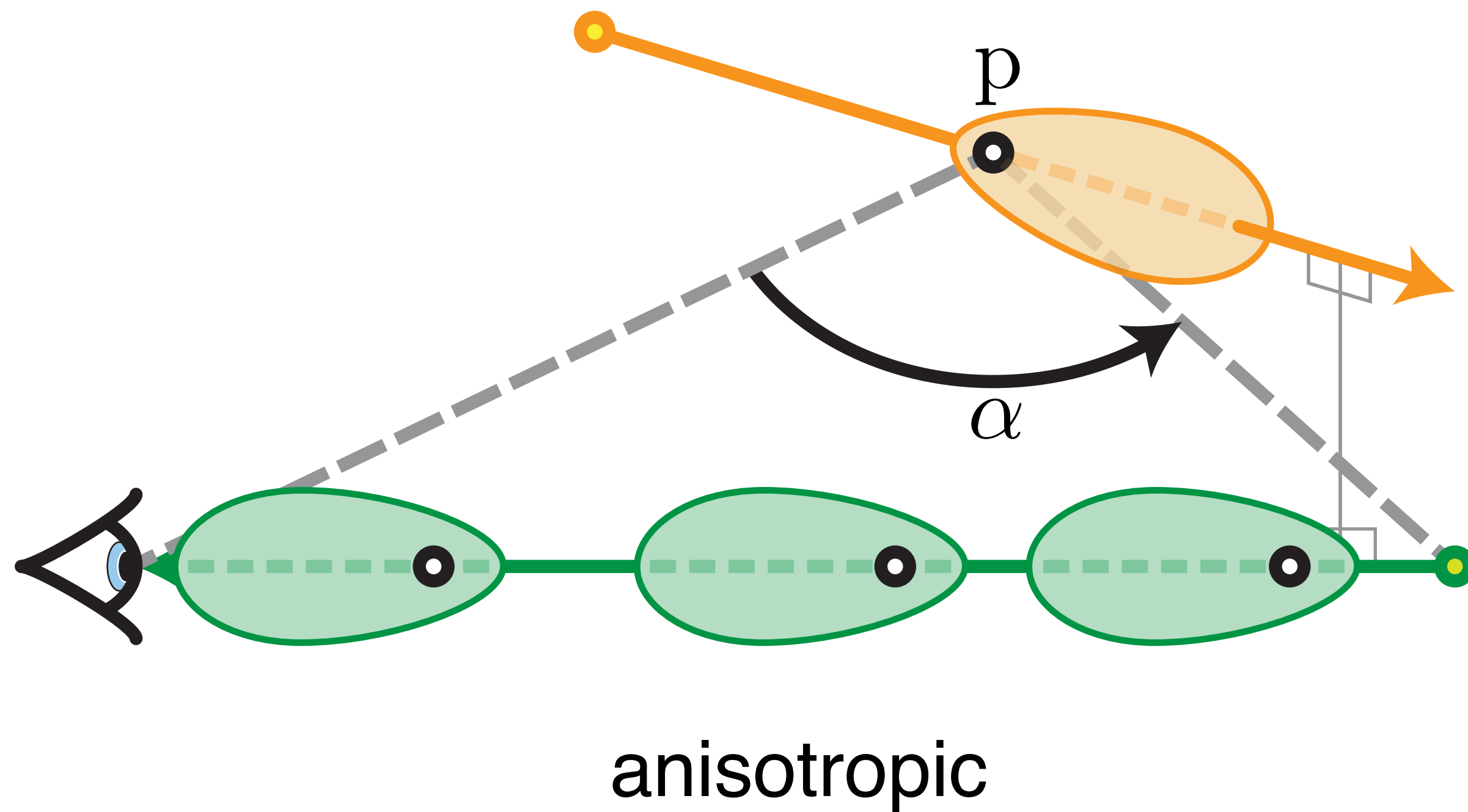


Anisotropic media

- **Conditional PDF**

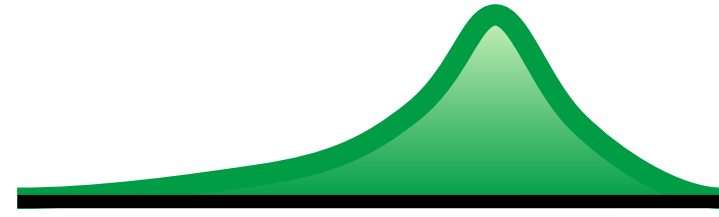


- ▶ replace equi-angular sampling by **importance sampling the PF product**

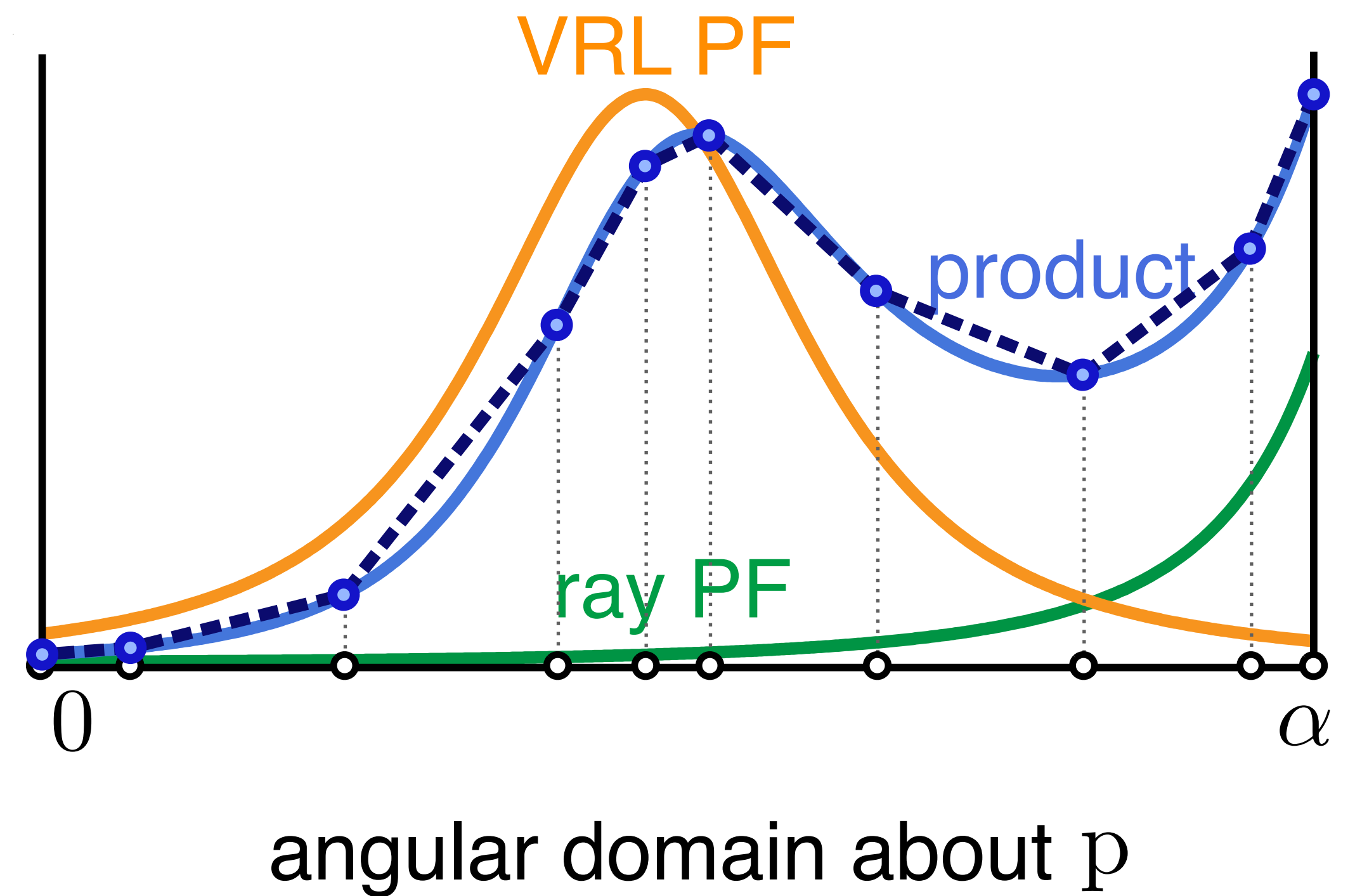
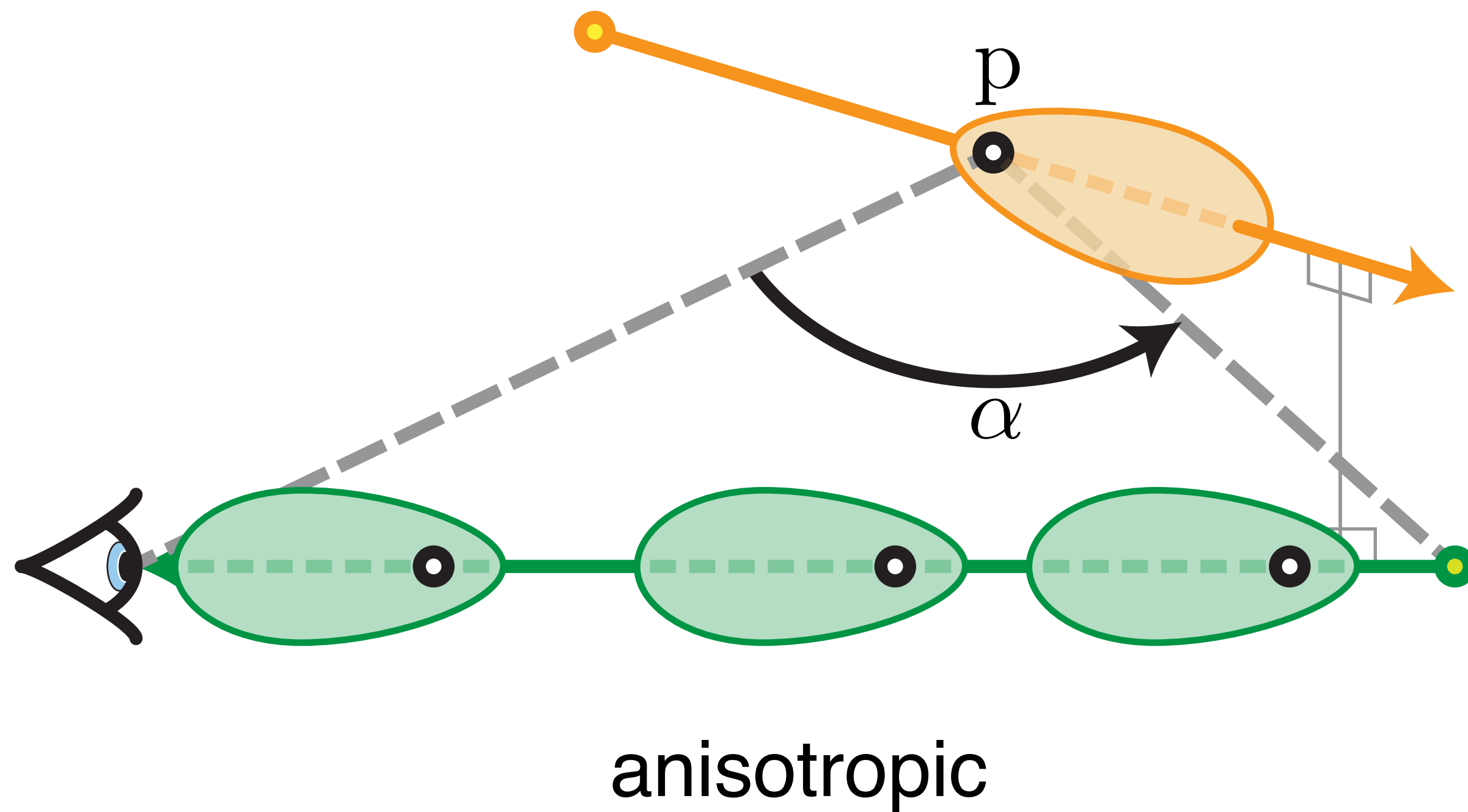


Anisotropic media

- **Conditional PDF**

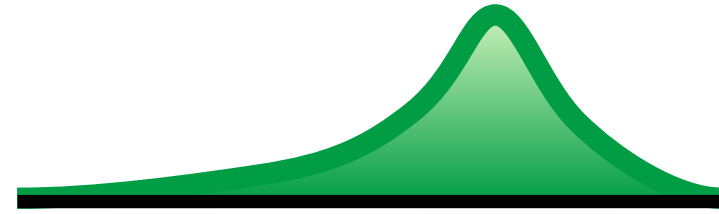


- ▶ replace equi-angular sampling by **importance sampling the PF product**



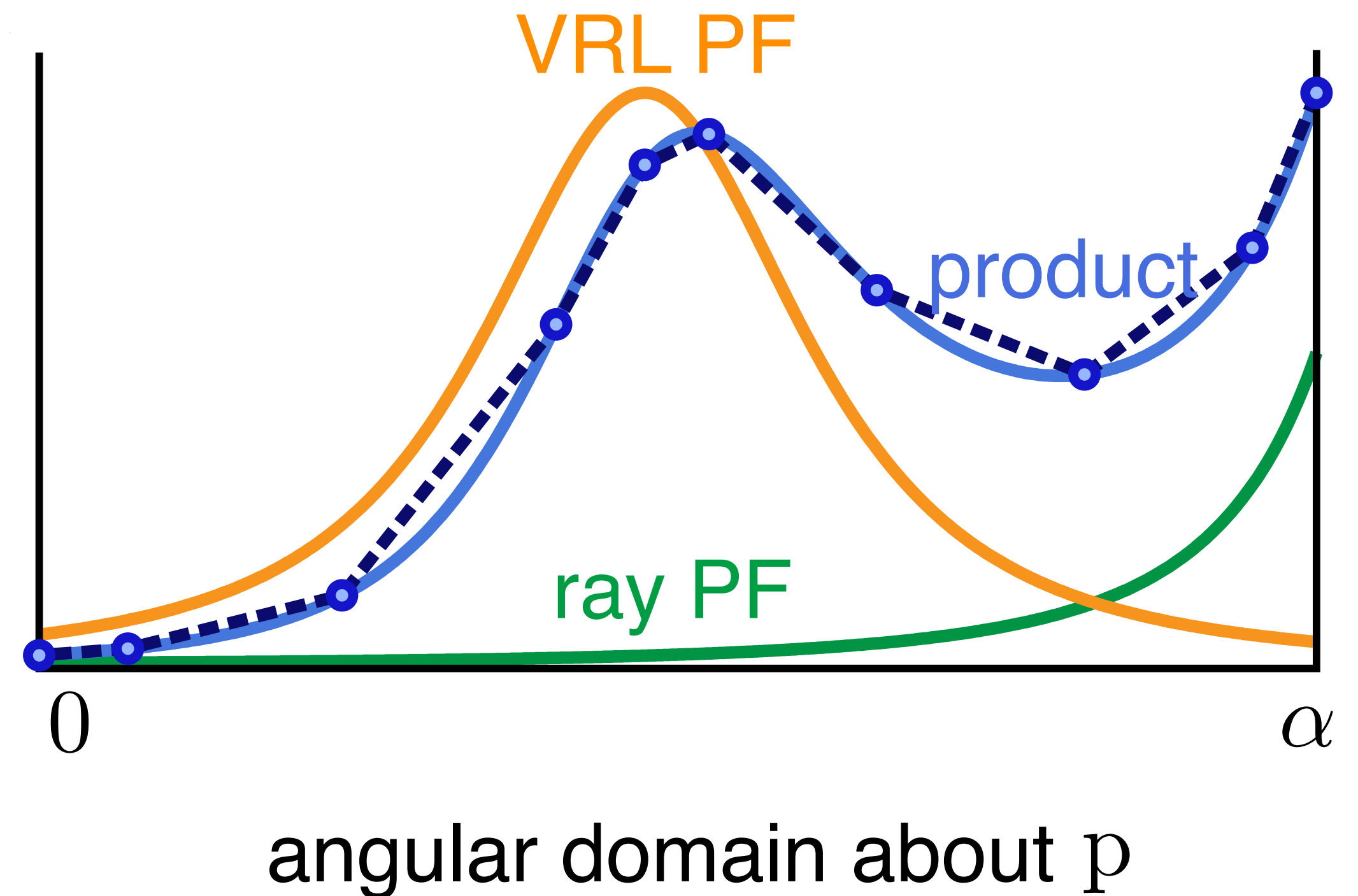
Anisotropic media

- **Conditional PDF**



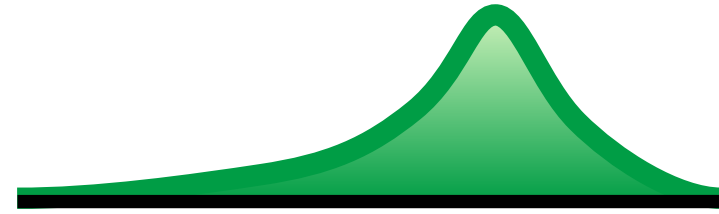
- ▶ replace equi-angular sampling by **importance sampling the PF product**

- ▶ piece-wise **linear PDF**



Anisotropic media

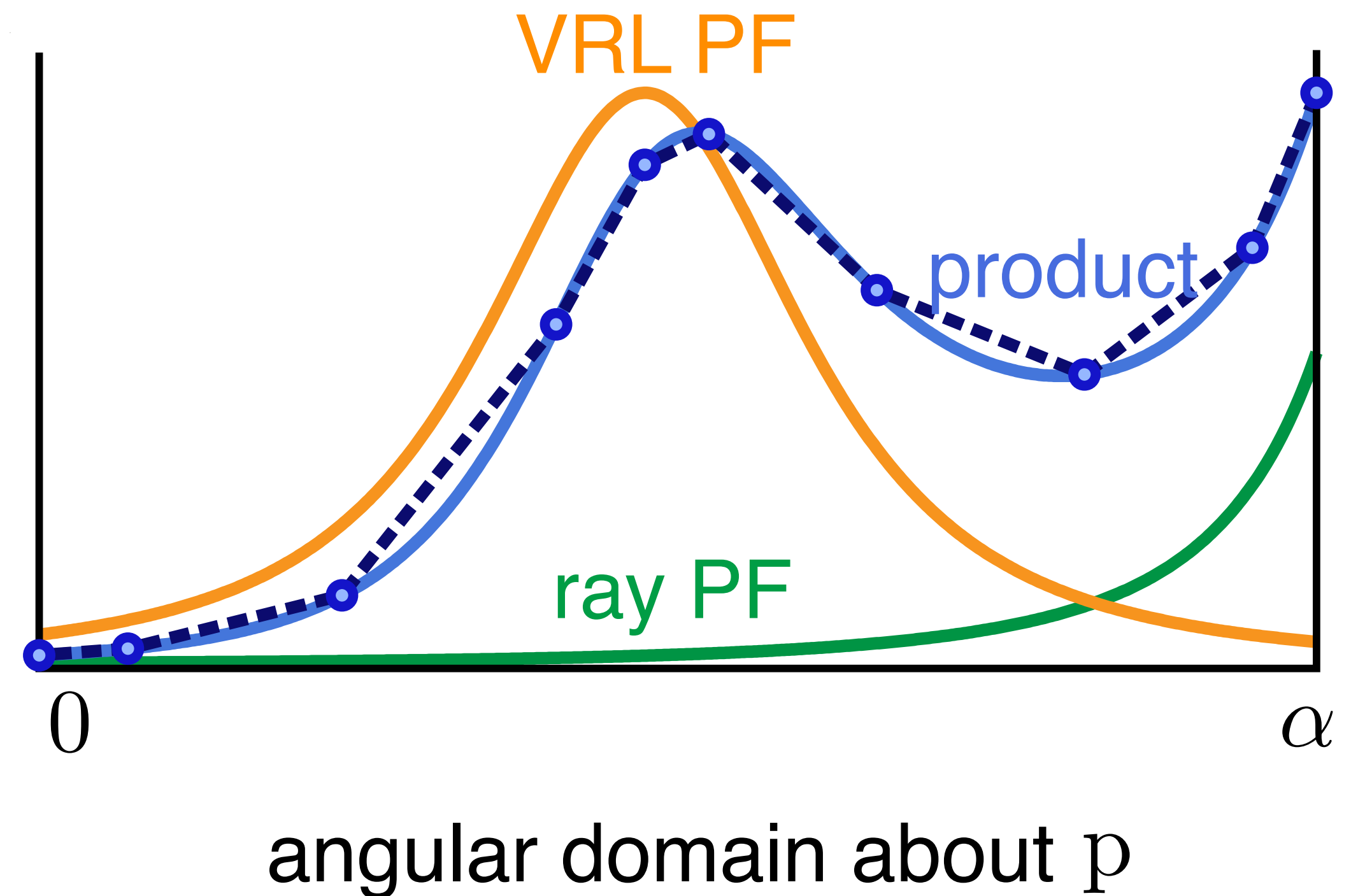
- **Conditional PDF**



- ▶ replace equi-angular sampling by **importance sampling the PF product**

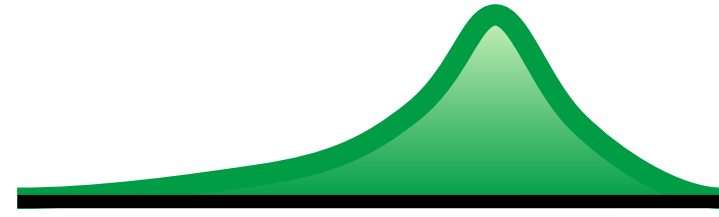
- ▶ piece-wise **linear PDF**

- ▶ piece-wise **quadratic CDF**



Anisotropic media

- **Conditional PDF**

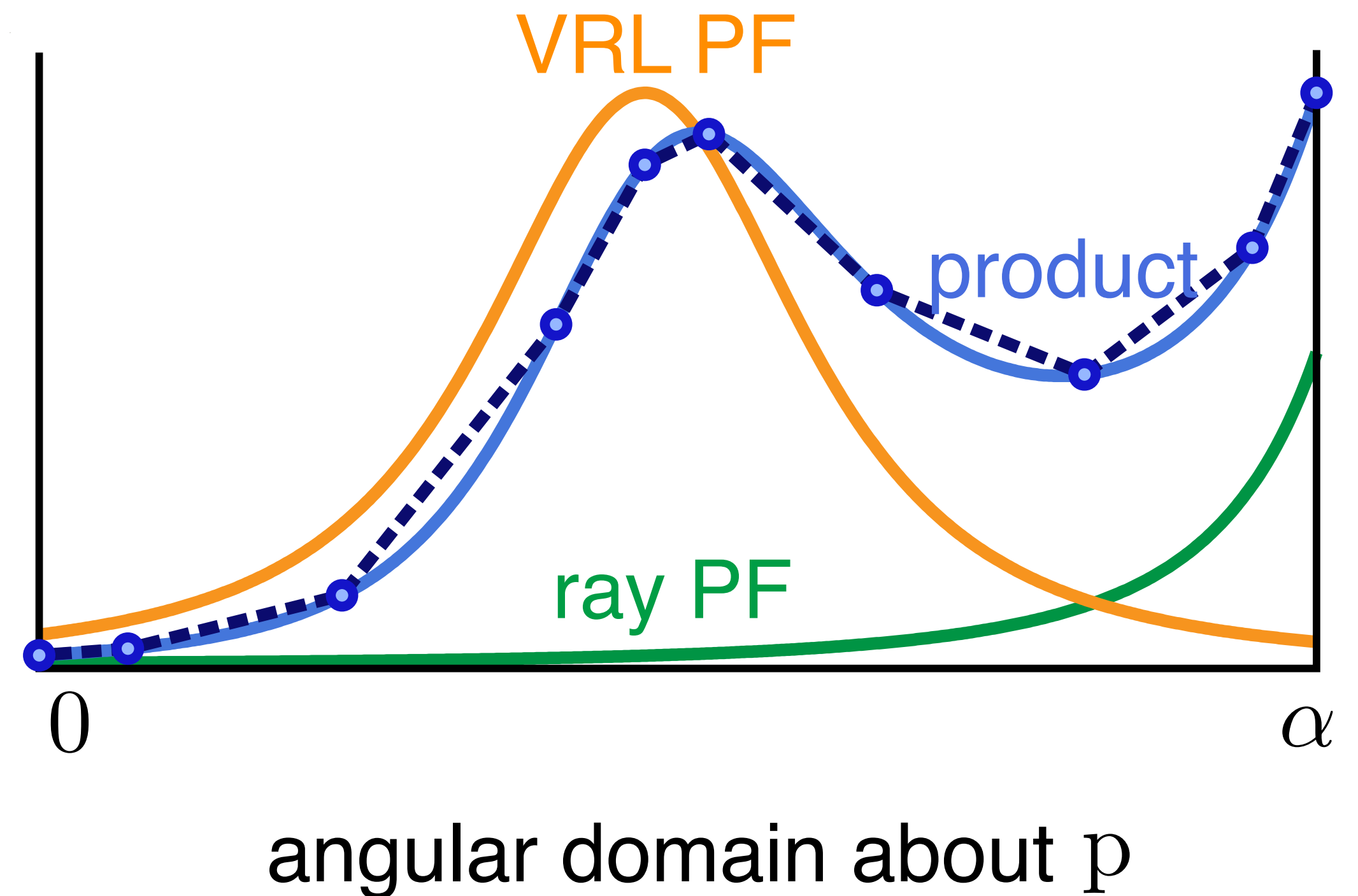


- ▶ replace equi-angular sampling by **importance sampling the PF product**

- ▶ piece-wise **linear PDF**

- ▶ piece-wise **quadratic CDF**

- ▶ 10 adaptively distributed vertices
balance between speed and quality

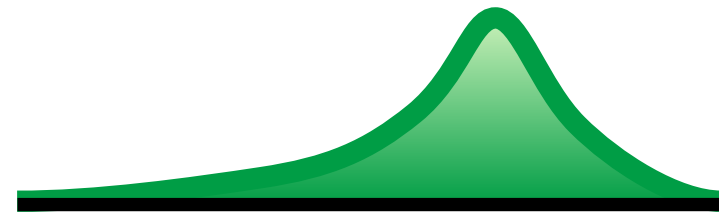


Anisotropic media

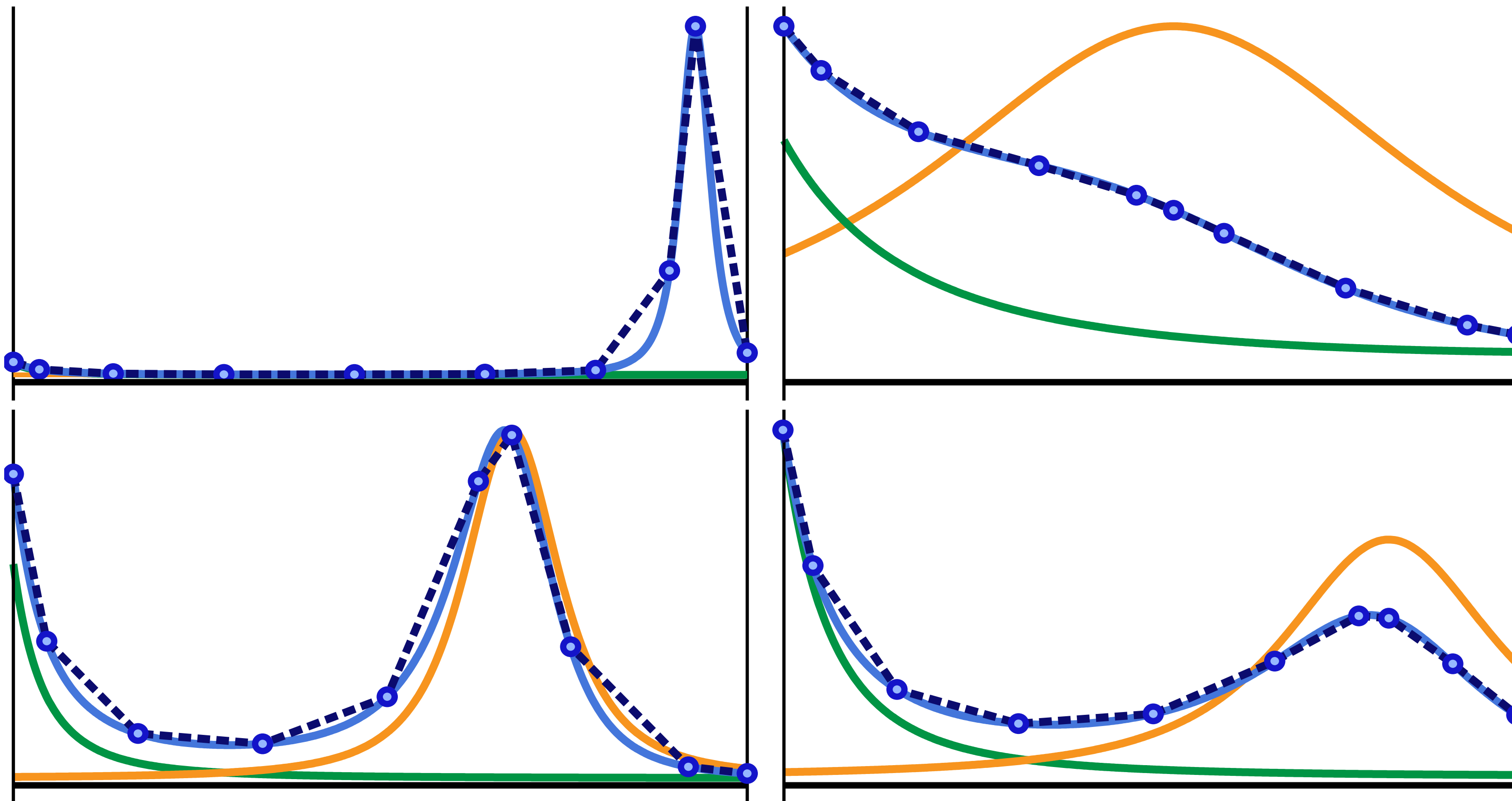
- **Conditional PDF** 
 - ▶ examples for Henyey-Greenstein PF with $g = 0.95$

Anisotropic media

- **Conditional PDF**

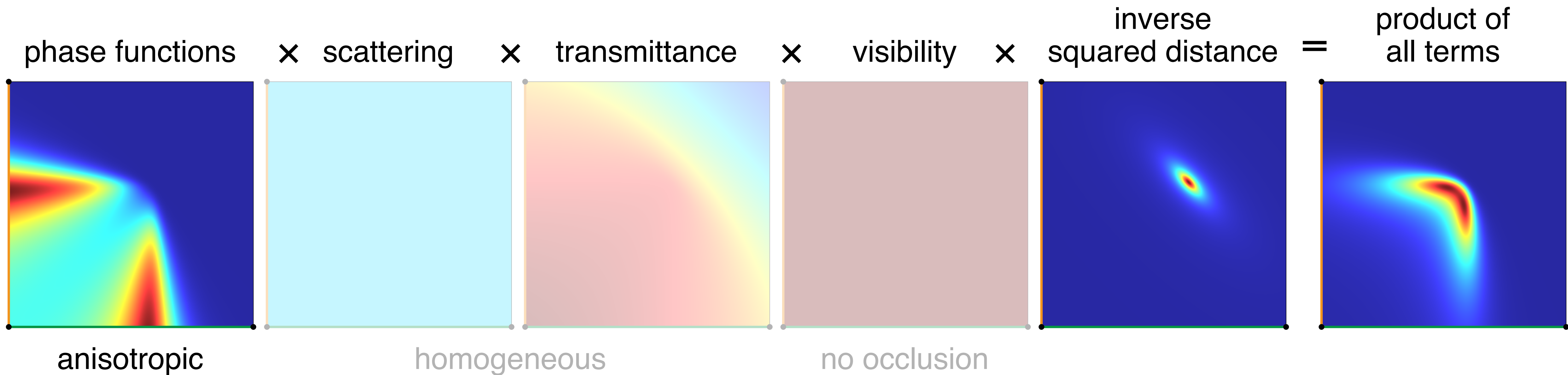


- ▶ examples for Henyey-Greenstein PF with $g = 0.95$



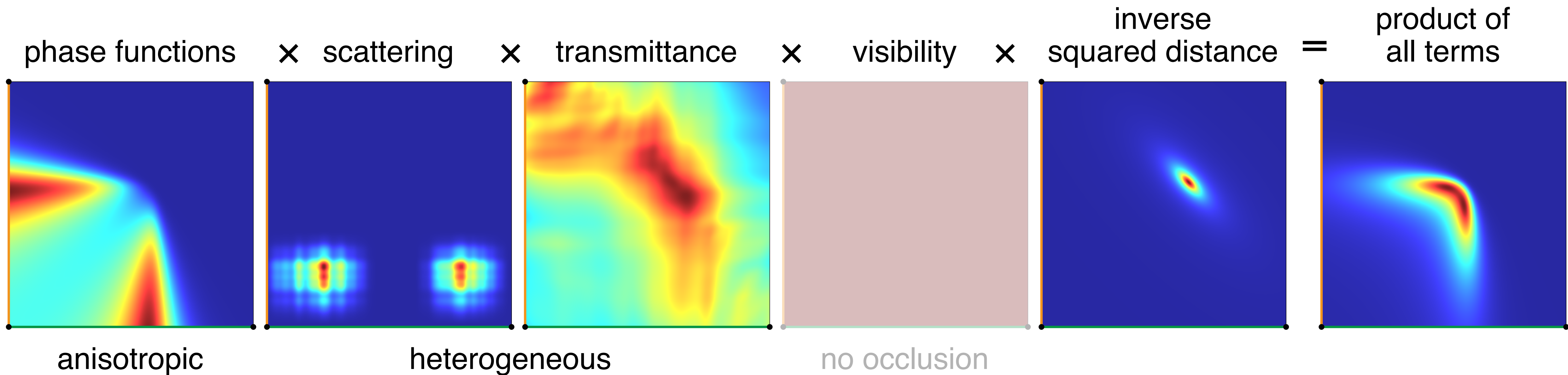
Importance sampling

How to (importance) sample?



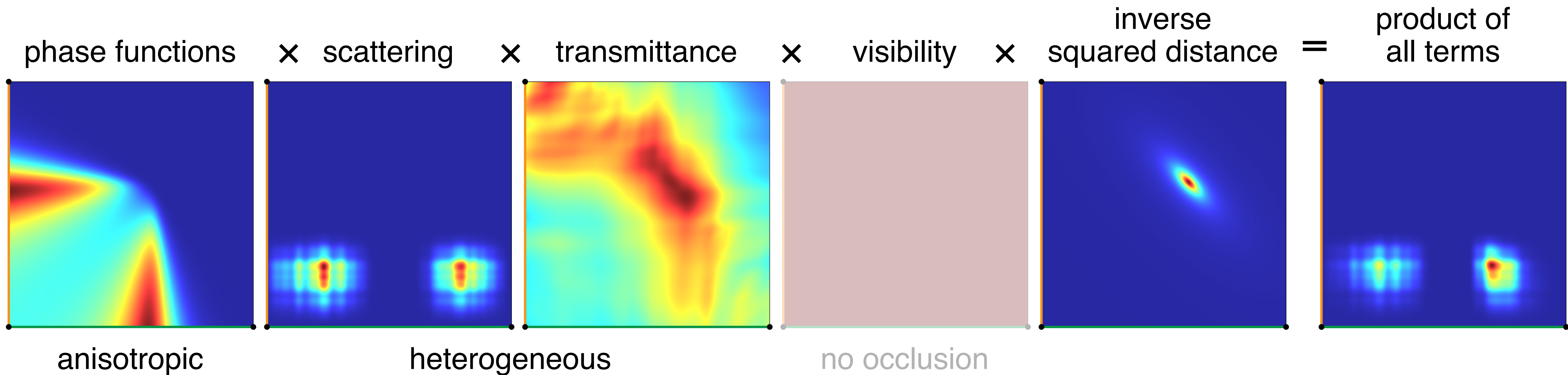
Importance sampling

How to (importance) sample?



Importance sampling

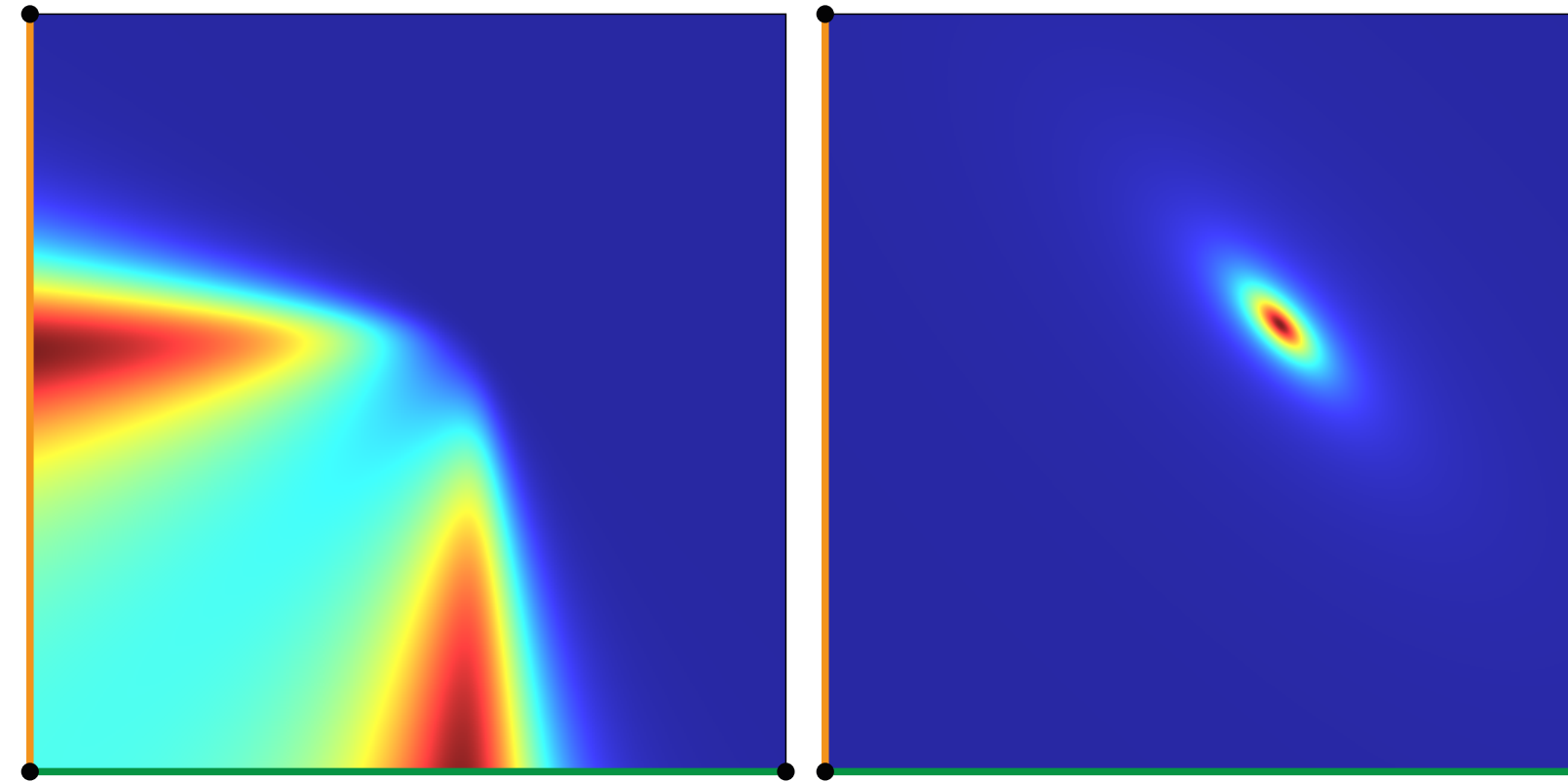
How to (importance) sample?



Importance sampling

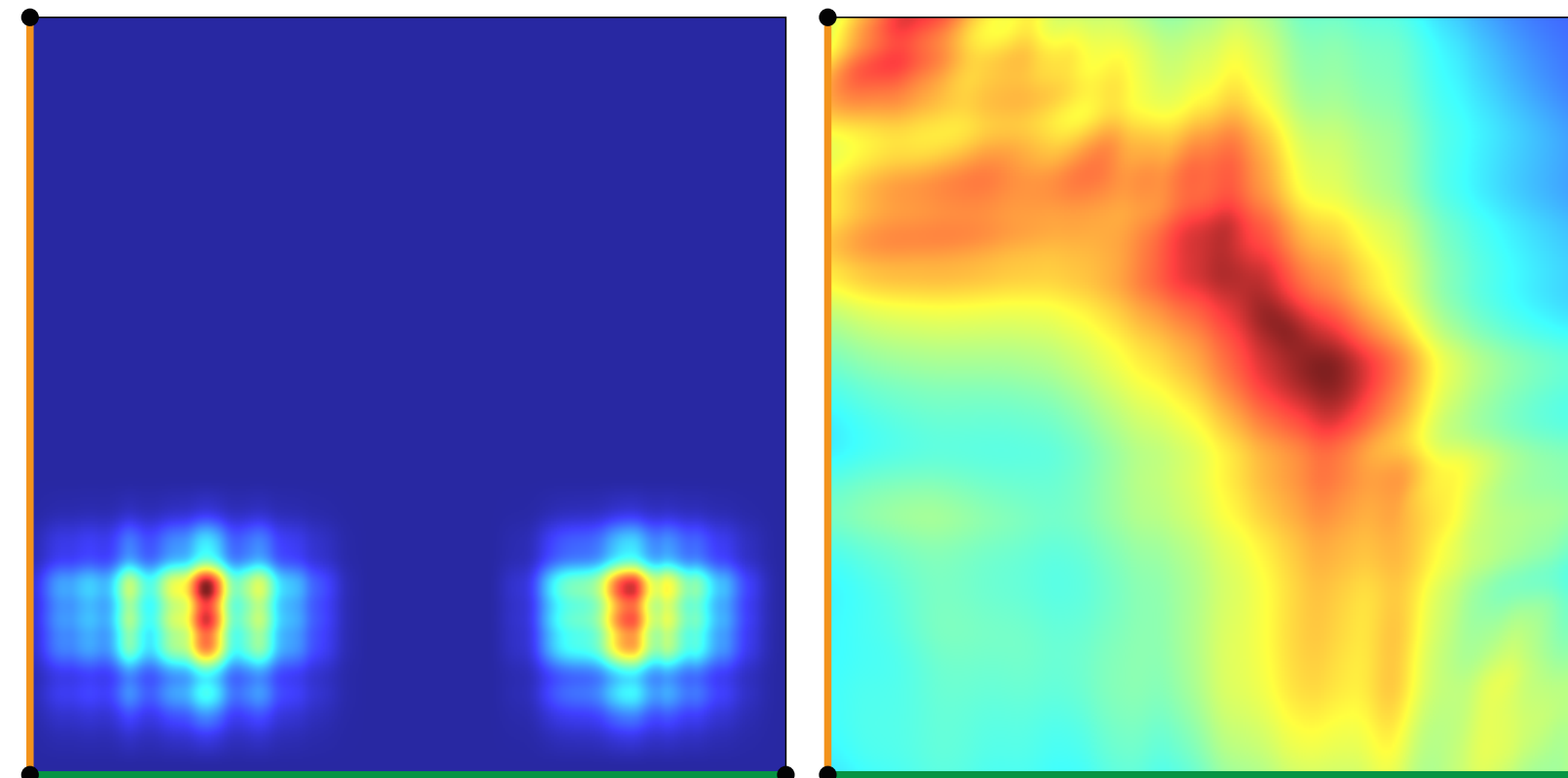
$\frac{\text{anisotropy}}{\text{distance}^2}$

phase functions × inverse squared distance



heterogeneity

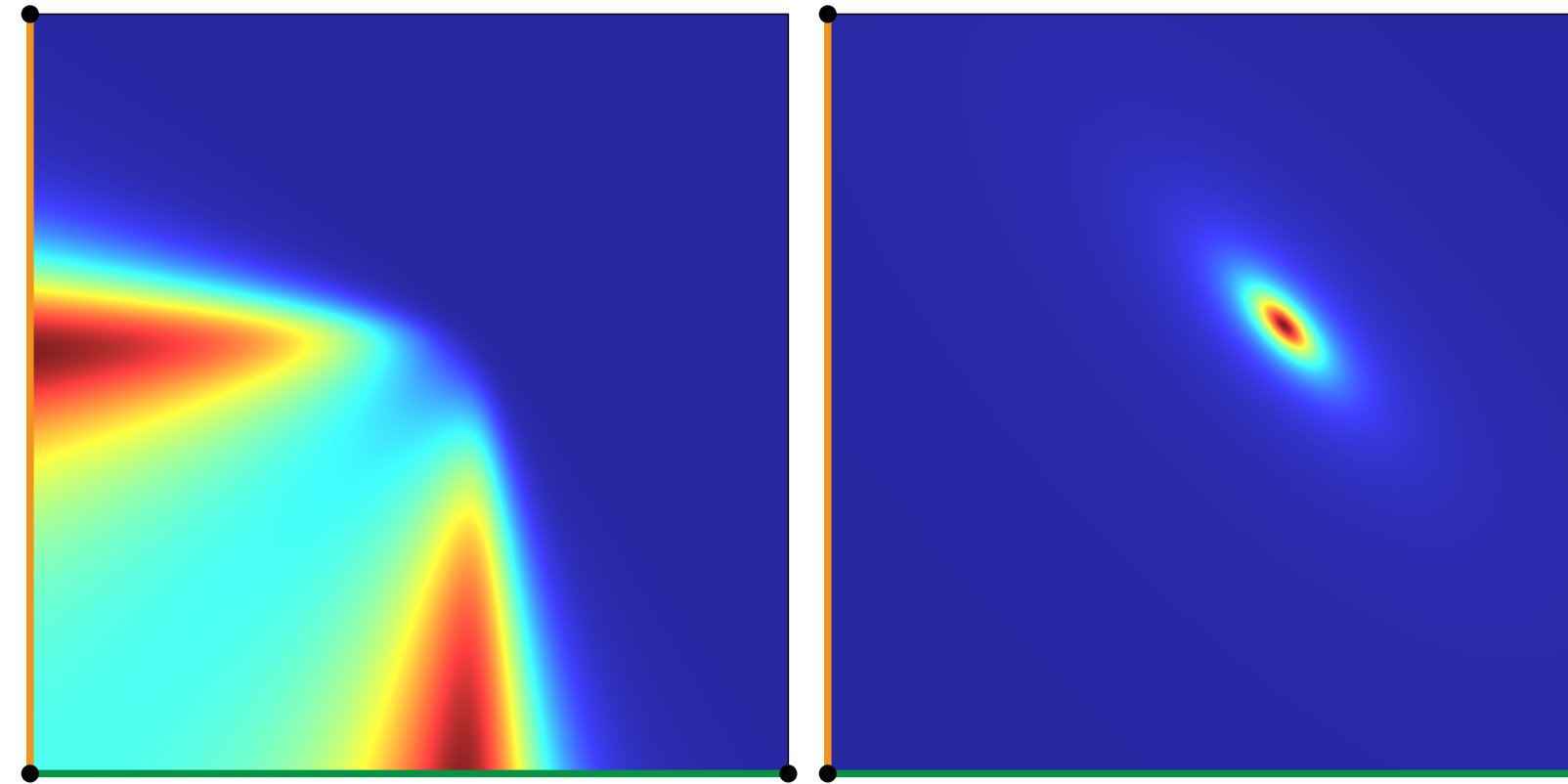
scattering × transmittance



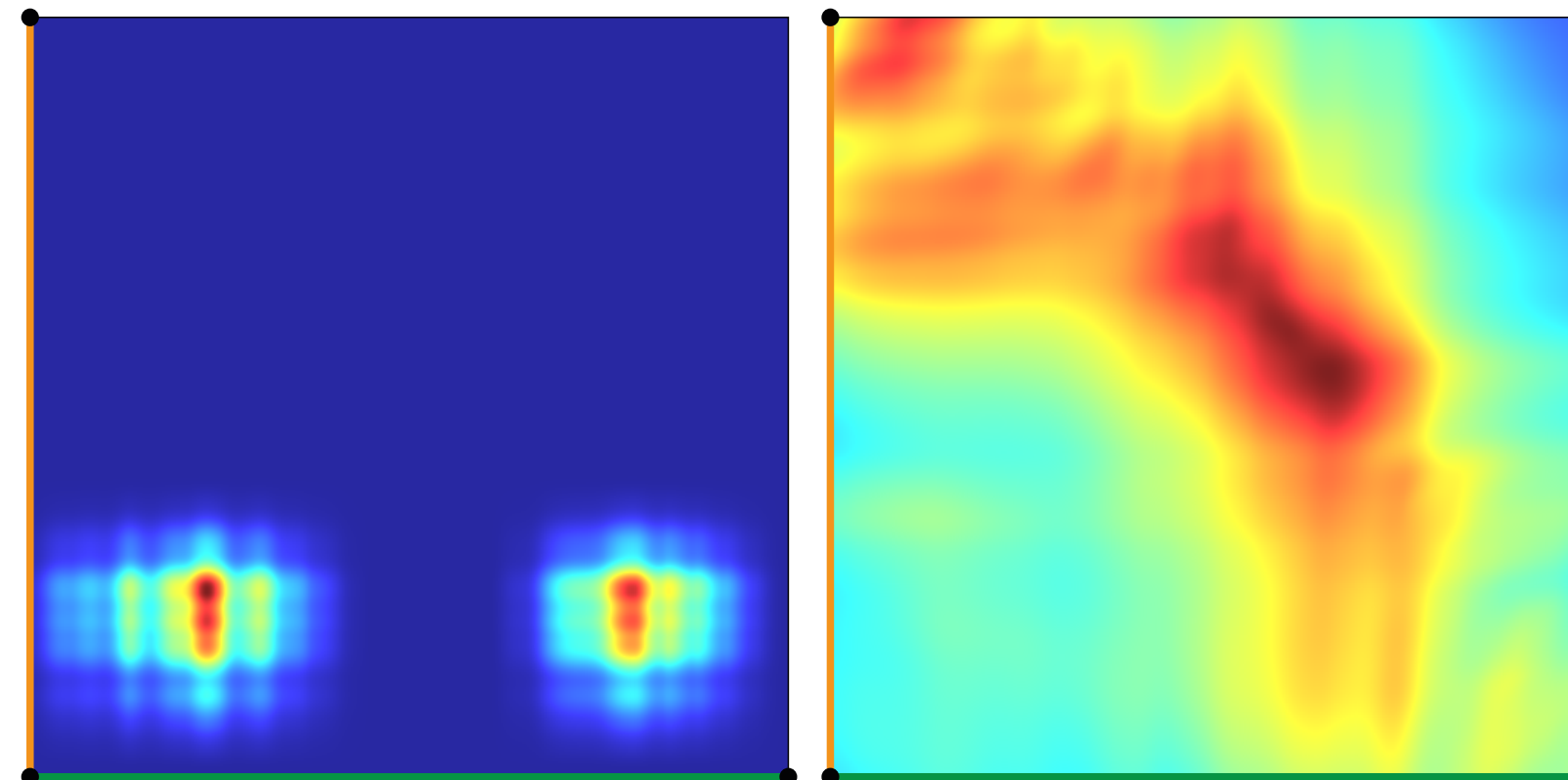
Importance sampling

$\frac{\text{anisotropy}}{\text{distance}^2}$

phase functions × inverse squared distance



scattering × transmittance



**Combine using
MIS**

heterogeneity

Heterogeneity

Heterogeneity

$$\text{pdf}(u, v) = \sigma_s(u) T(u) \sigma_s(v) T(v) T(u, v)$$

Heterogeneity

$$\text{pdf}(u, v) = \sigma_s(u) T(u) \sigma_s(v) T(v) T(u, v)$$

Heterogeneity

$$\text{pdf}(u, v) = \underbrace{\sigma_s(u) T(u)}_{\substack{\text{along camera} \\ \text{ray}}} \underbrace{\sigma_s(v) T(v)}_{\text{along VRL}} T(u, v)$$

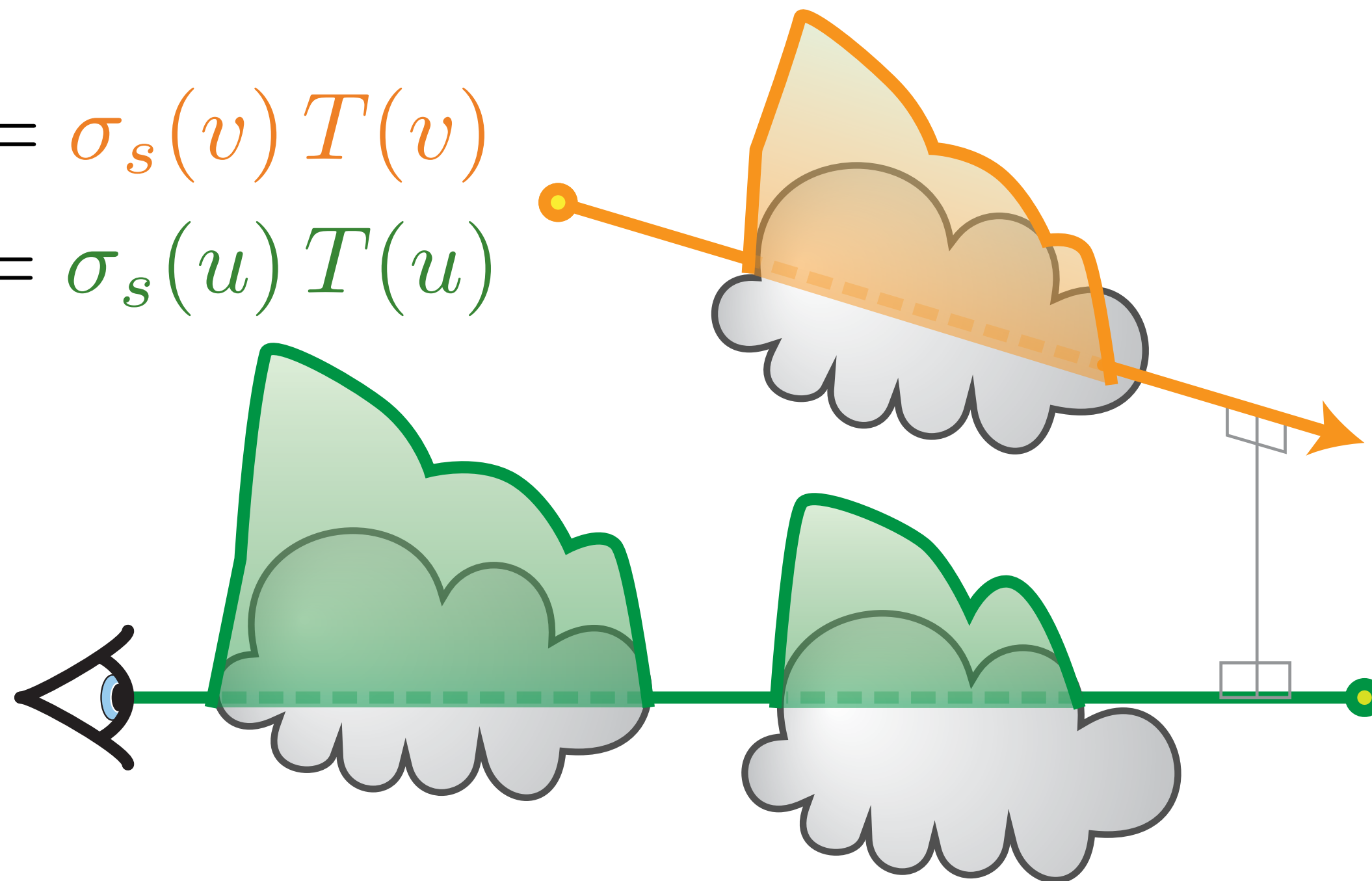
Separable!

Heterogeneity

$$\text{pdf}(u, v) = \underbrace{\sigma_s(u) T(u)}_{\substack{\text{along camera} \\ \text{ray}}} \underbrace{\sigma_s(v) T(v)}_{\substack{\text{along VRL} \\ \text{ray}}} T(u, v)$$

Separable!

$$\begin{aligned} \text{pdf}(v) &= \sigma_s(v) T(v) \\ \text{pdf}(u) &= \sigma_s(u) T(u) \end{aligned}$$

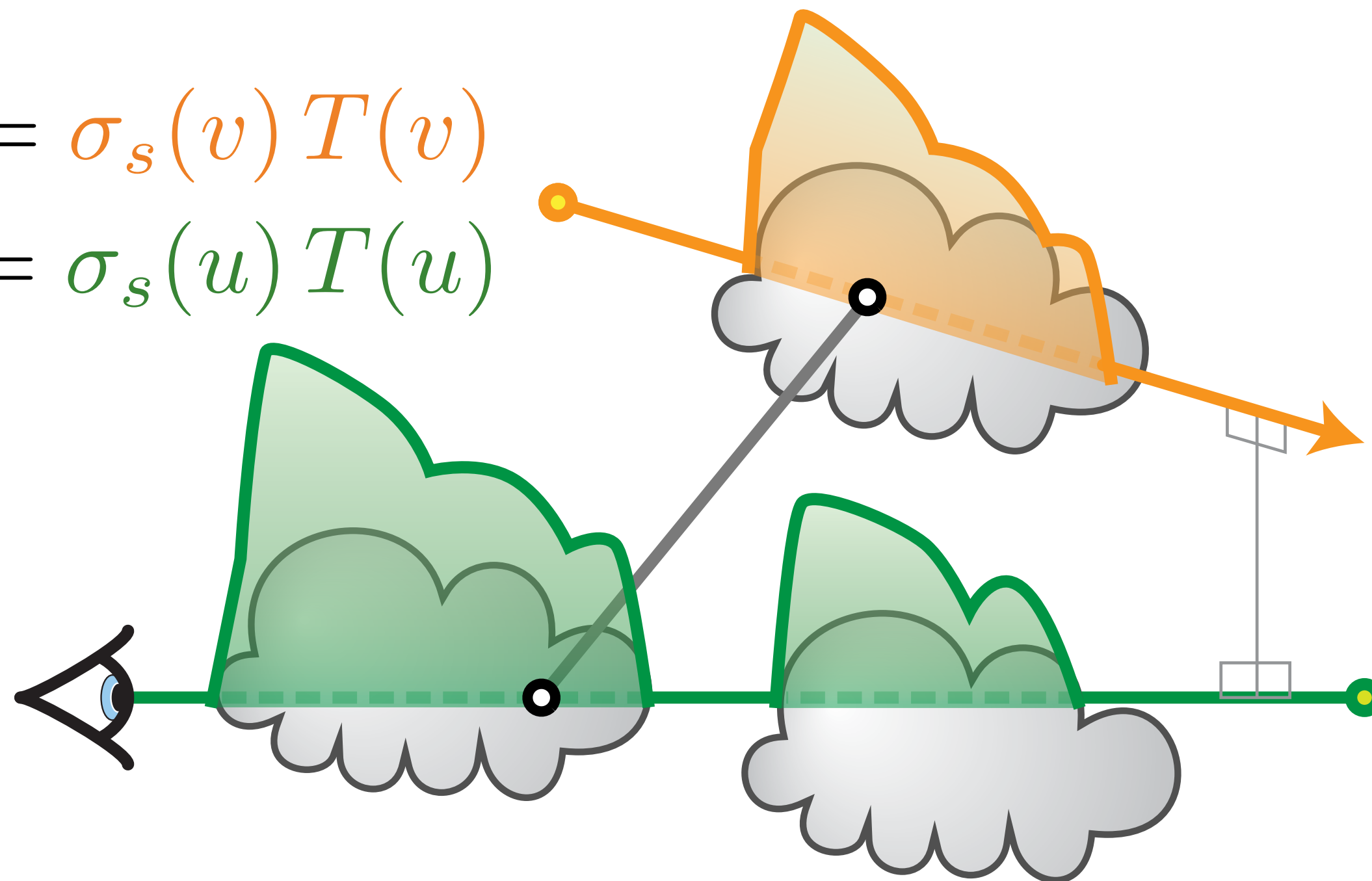


Heterogeneity

$$\text{pdf}(u, v) = \underbrace{\sigma_s(u) T(u)}_{\substack{\text{along camera} \\ \text{ray}}} \underbrace{\sigma_s(v) T(v)}_{\substack{\text{along VRL}}} T(u, v)$$

Separable!

$$\begin{aligned} \text{pdf}(v) &= \sigma_s(v) T(v) \\ \text{pdf}(u) &= \sigma_s(u) T(u) \end{aligned}$$



Analysis and Results



Fruit Juice
homogeneous
anisotropic (HG $g = 0.55$)
512x512



Multiple Scattering

Virtual Ray Lights



4K VRLs

Virtual Point Lights



4K VPLs

6 seconds

Multiple Scattering

Virtual Ray Lights



4K VRLs

Virtual Point Lights



4K VPLs

6 seconds

Multiple Scattering

Virtual Ray Lights



Virtual Point Lights





Smoky Room

heterogeneous

1280x720

Media-to-Media

Virtual Ray Lights



6K VRLs

Virtual Point Lights



8K VPLs

5 seconds

Media-to-Media

Virtual Ray Lights



6K VRLs

Virtual Point Lights



8K VPLs

5 seconds

Media-to-Media

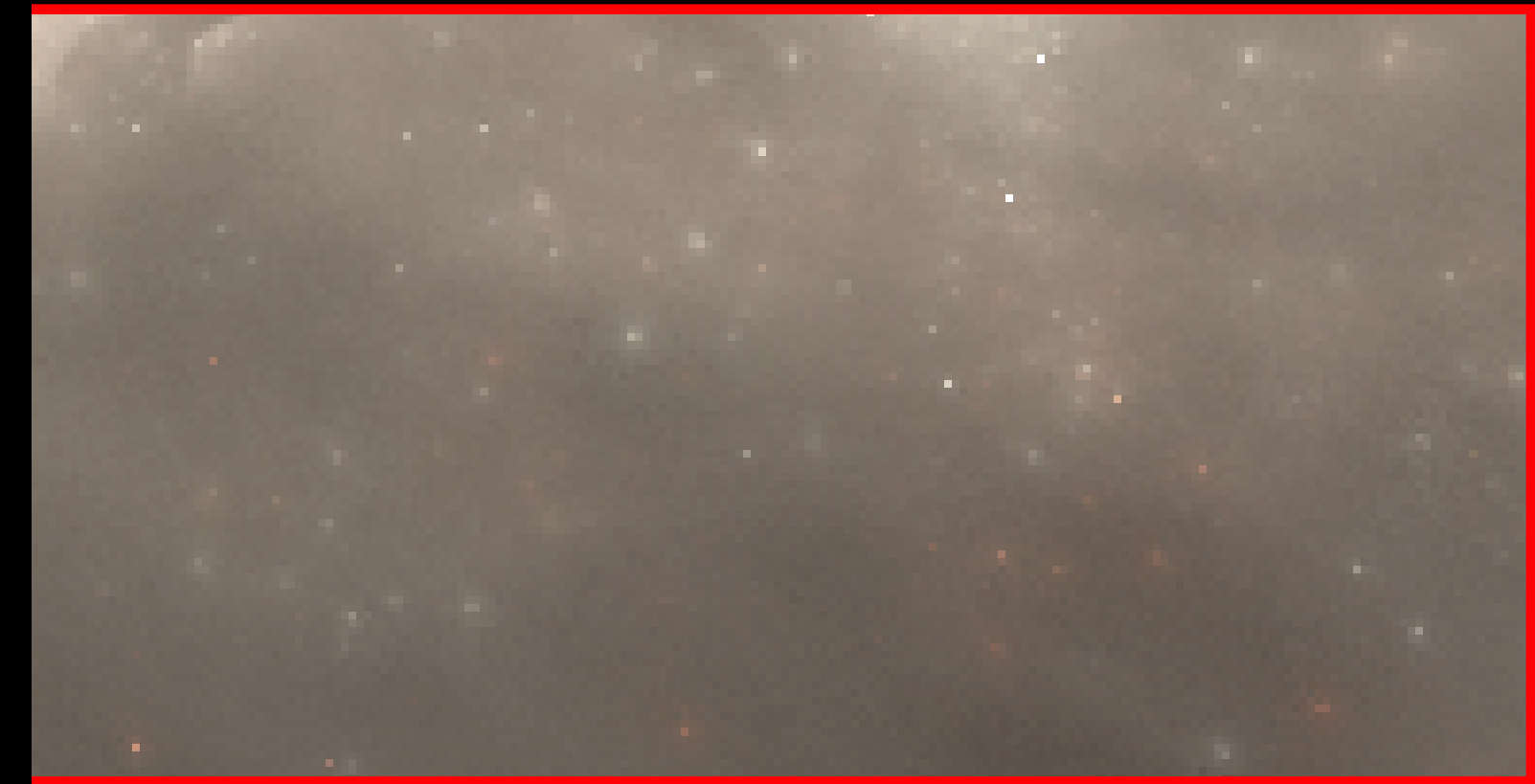
Virtual Ray Lights

101 seconds



Virtual Point Lights

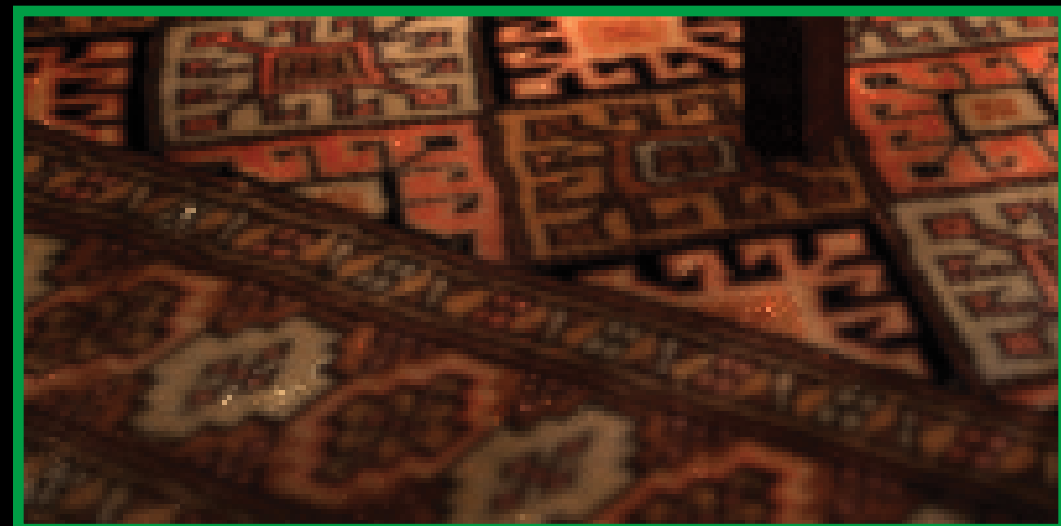
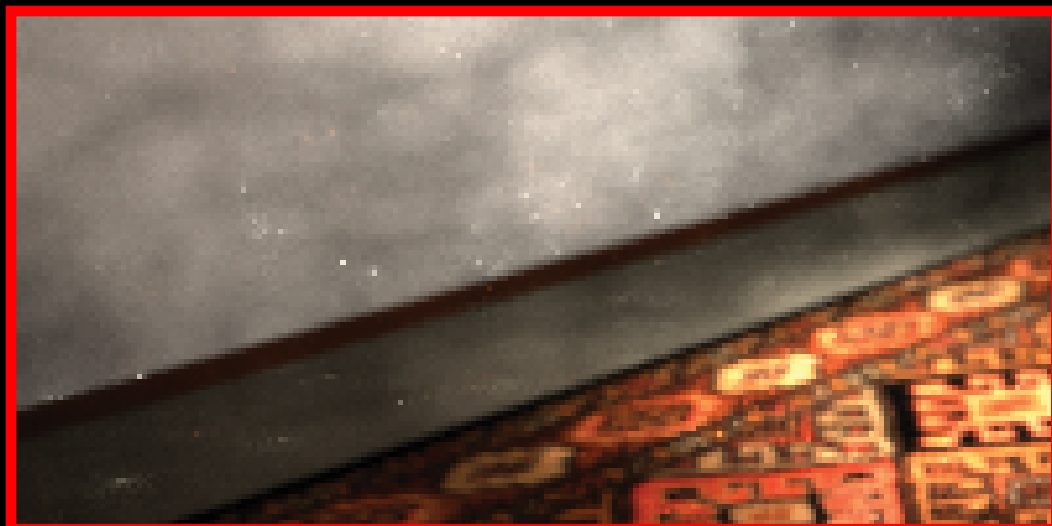
102 seconds



Media-to-Surface

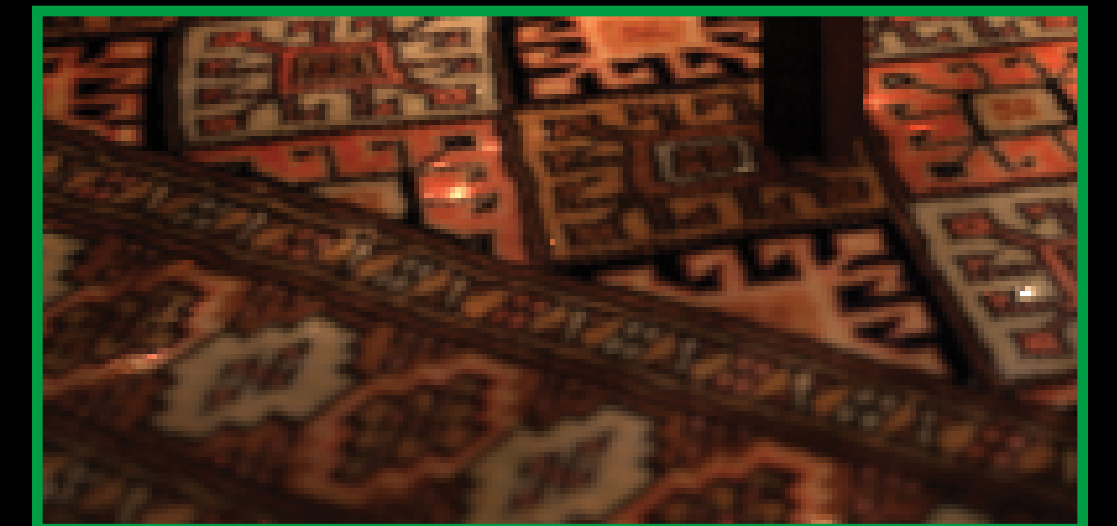
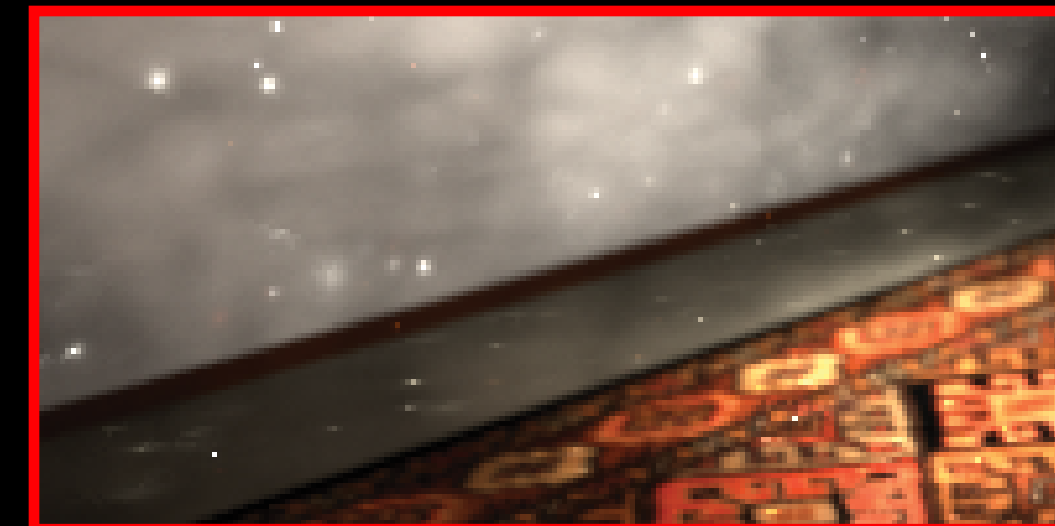
Virtual Ray Lights

600 seconds



Virtual Point Lights

600 seconds

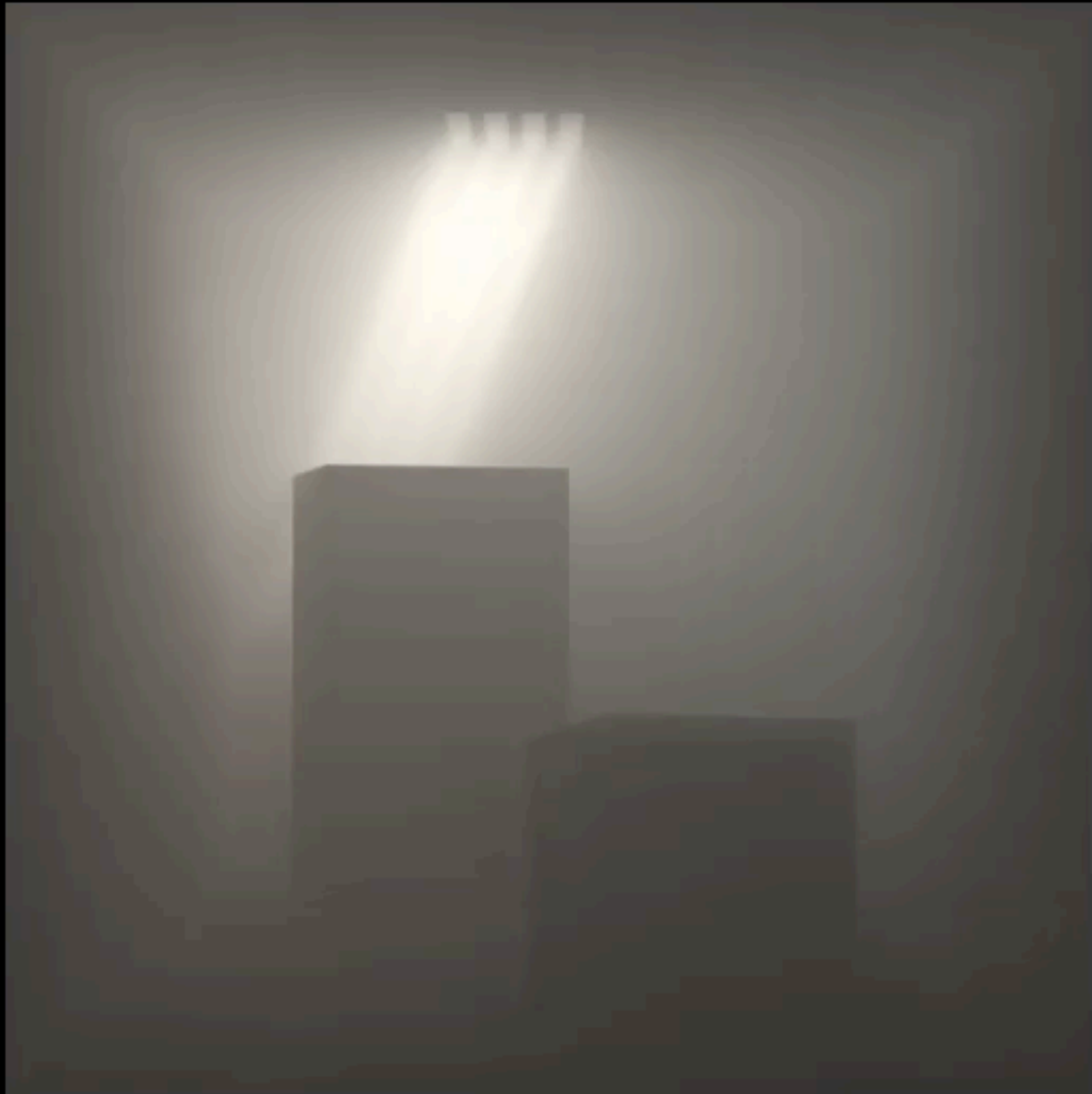


Temporal coherence

VPLs vs. VRLs

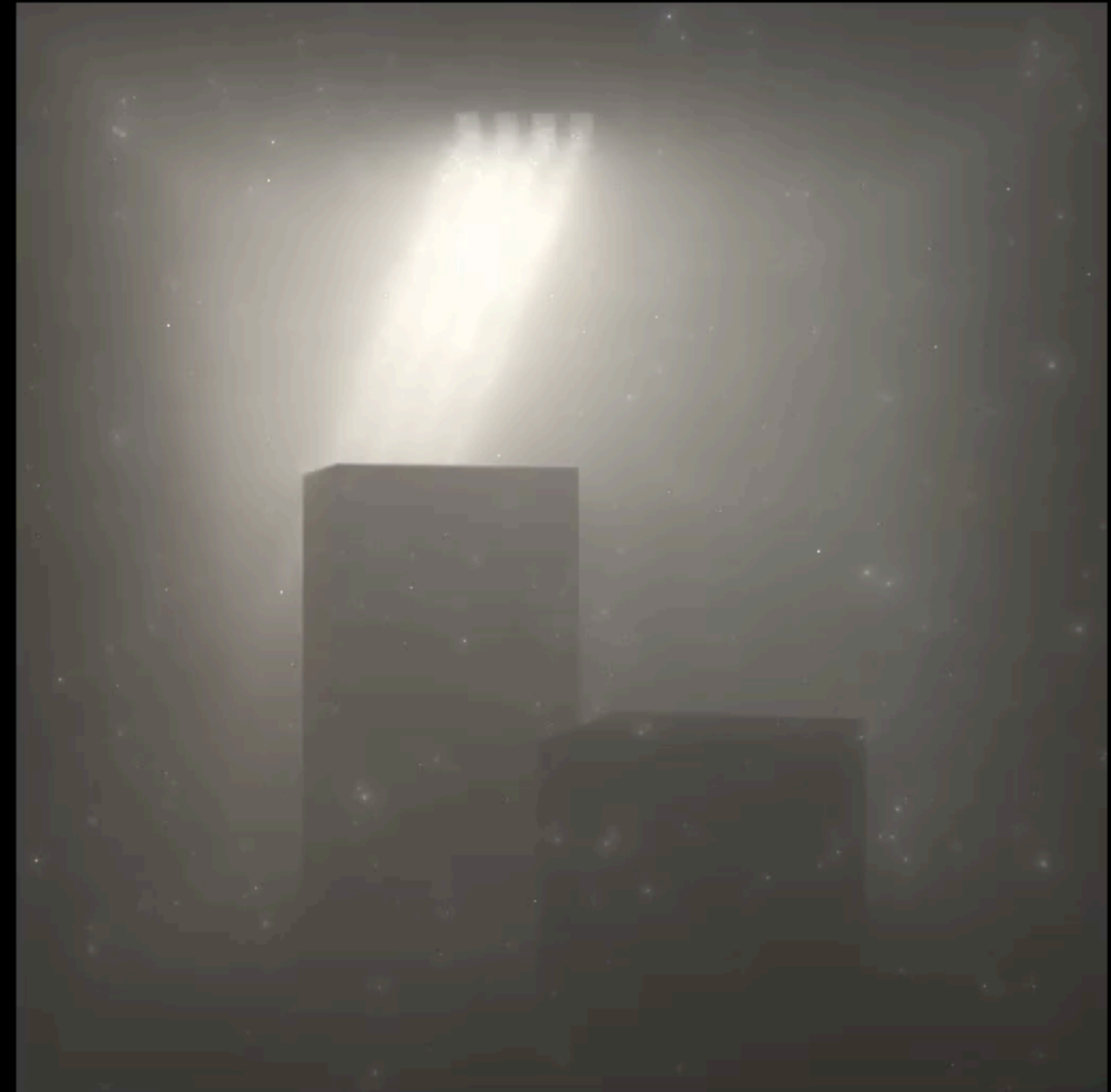
Media-to-Media

Virtual Ray Lights



1 minute/frame

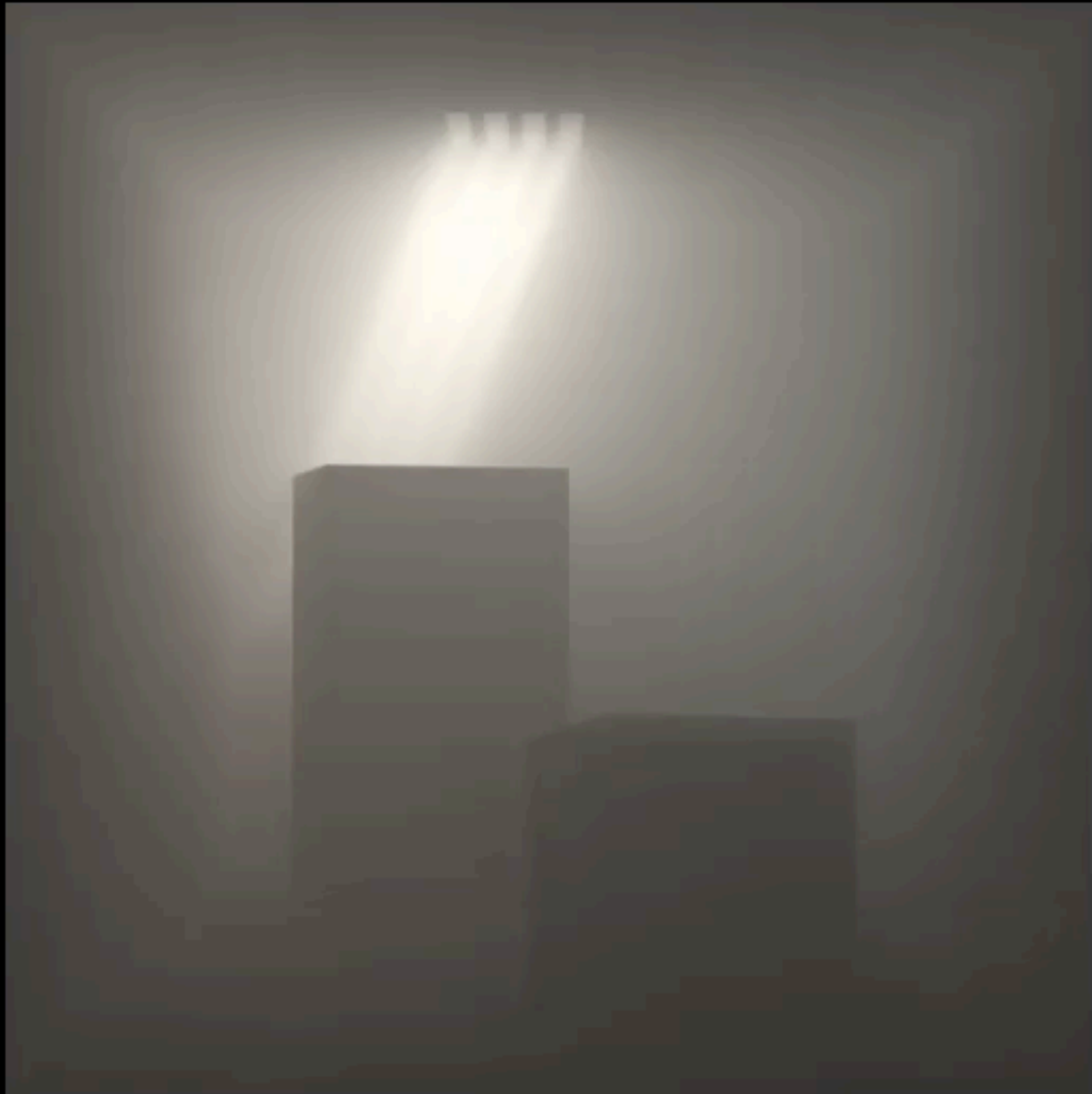
Virtual Point Lights



1 minute/frame

Media-to-Media

Virtual Ray Lights



1 minute/frame

Virtual Point Lights



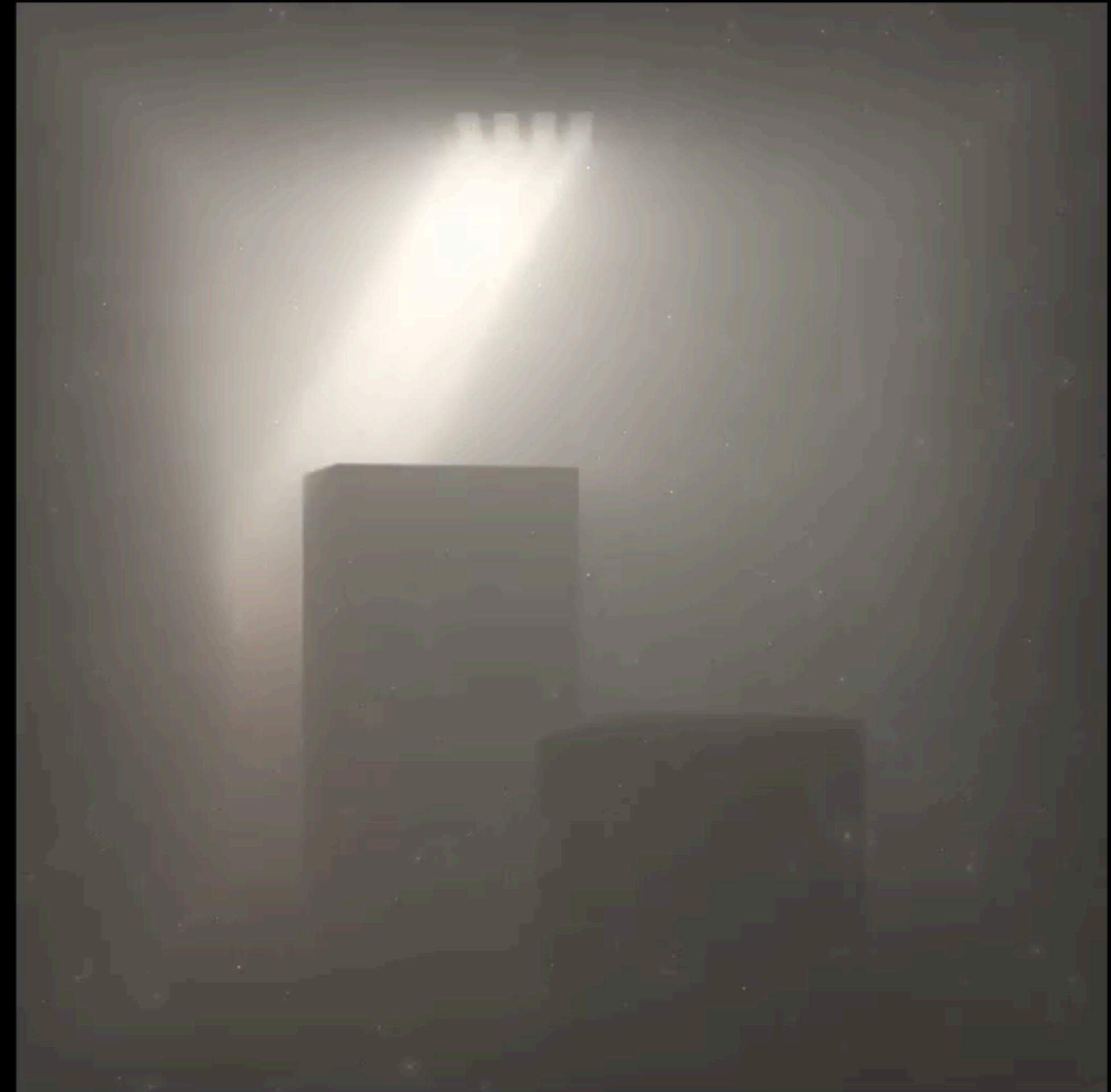
1 minute/frame

Media-to-Media

Virtual Ray Lights



Virtual Point Lights



1 minute/frame

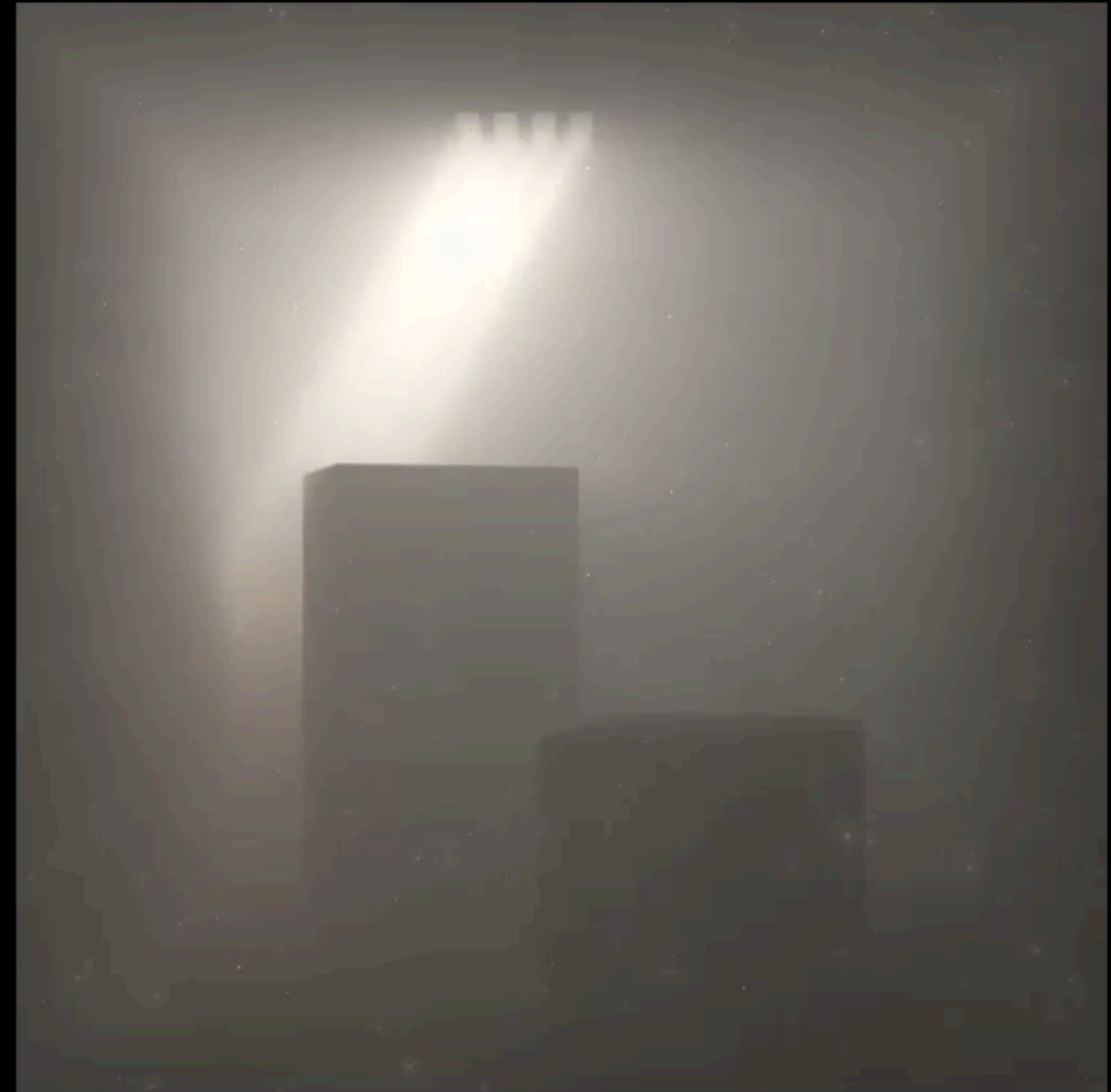
Media-to-Media

Virtual Ray Lights



1 minute/frame

Virtual Point Lights



3 minutes/frame

Spreading the Energy

Turn segments of paths into light sources

Advantages:

- energy is spread along lines, singularity is reduced (not removed)
- unbiased, temporally stable

Disadvantages:

- requires 2D integration (along both rays)

LightCuts

Only for Virtual Point Lights

Walter et al. [2005]

Scalability

Why Many Lights?

Simulate complex illumination using point lights

- Area lights
- Environment map lighting
- Sun and Sky lights
- Indirect Illumination

Unified Illumination: Enable trade-offs among components

Many-Lights Problem

Brute Force: Consider all lights

Too Slow

Many-Lights Problem

Brute Force: Consider all lights

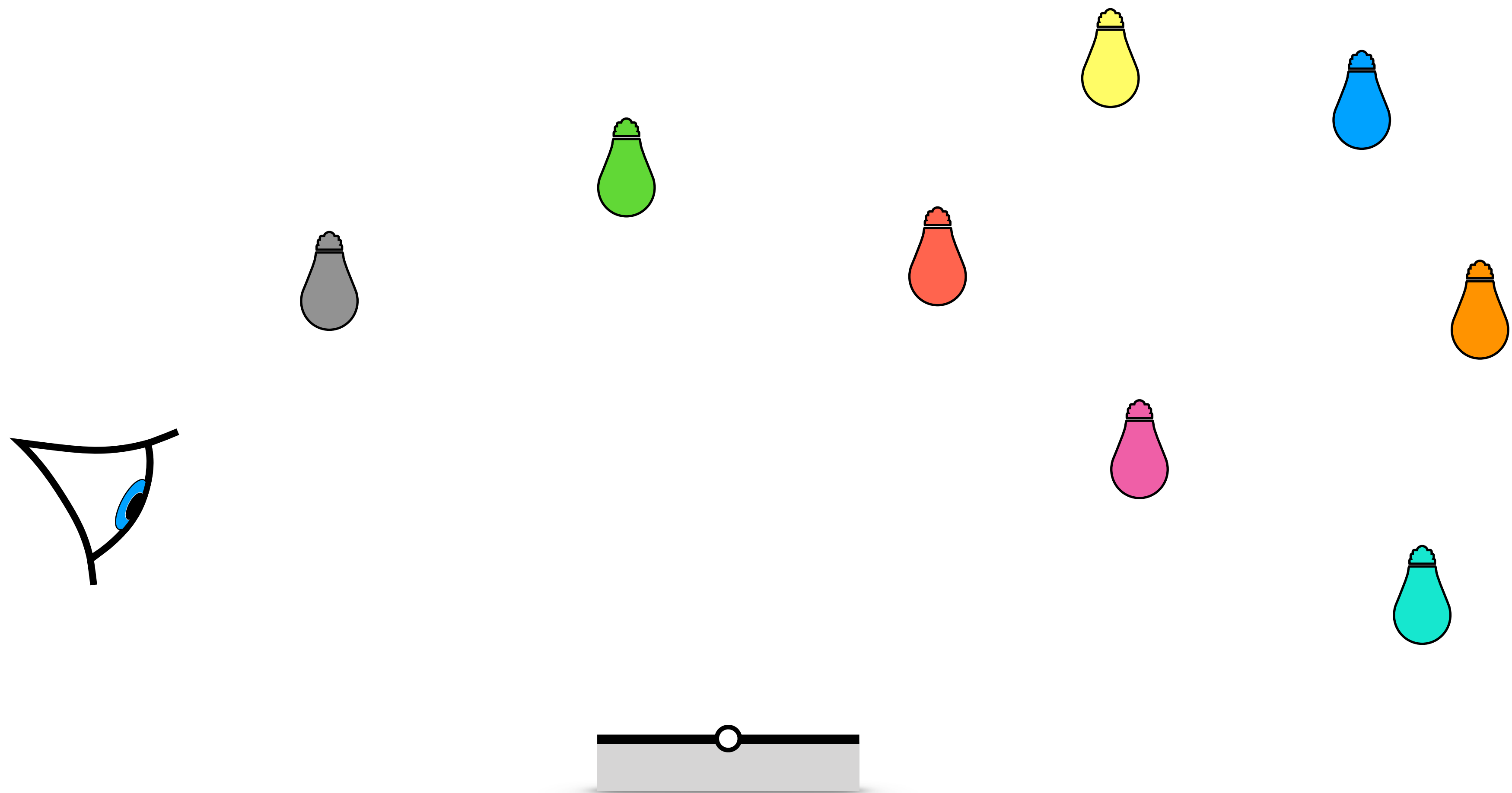
Too Slow

Importance Sampling: Shirley et al. [1996]

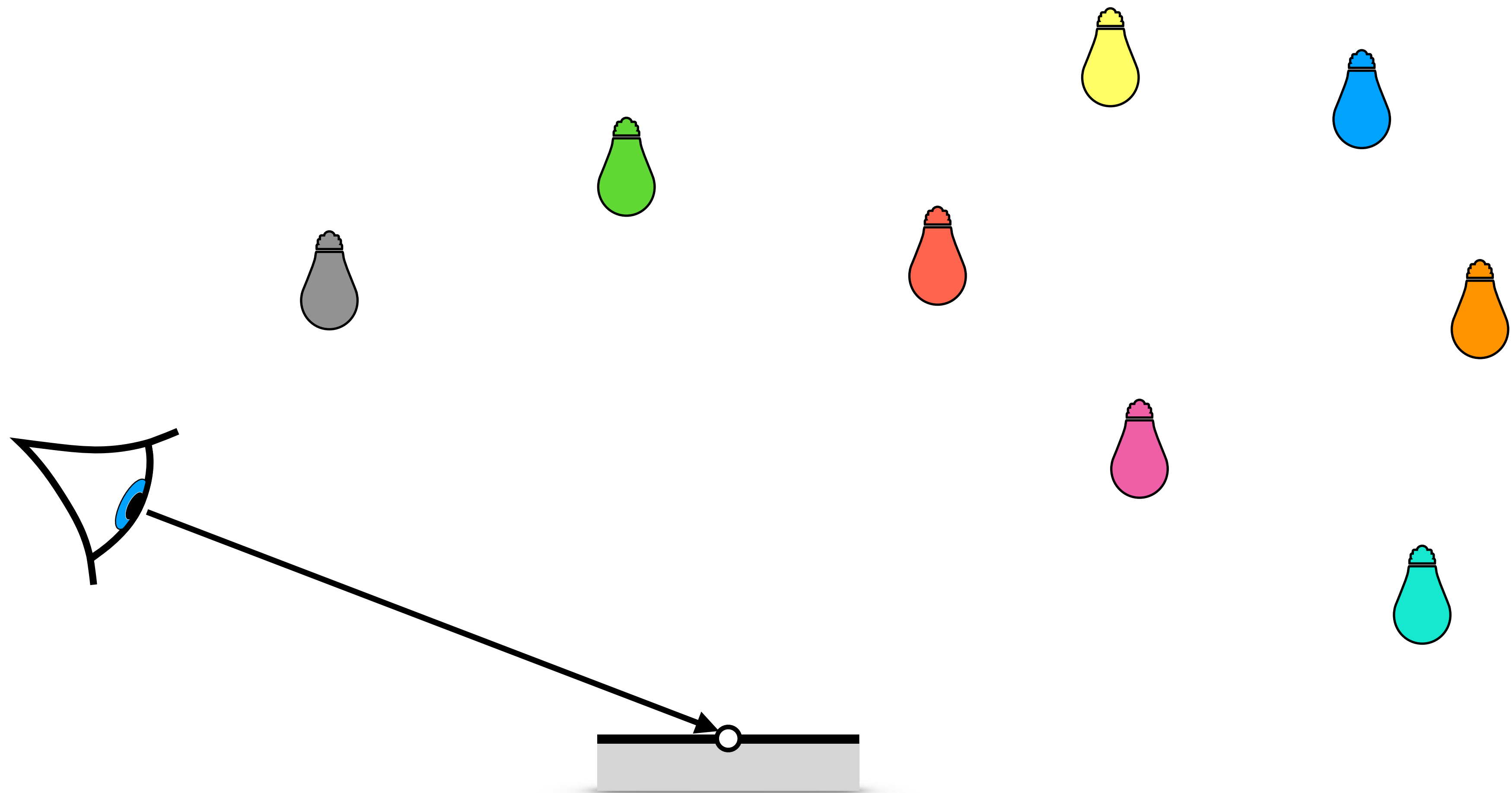
- By considering only a fraction of lights.
- The method suggests using light intensities as importance weights
- Does not give different set of weights, on different parts of the scenes.

Too Noisy

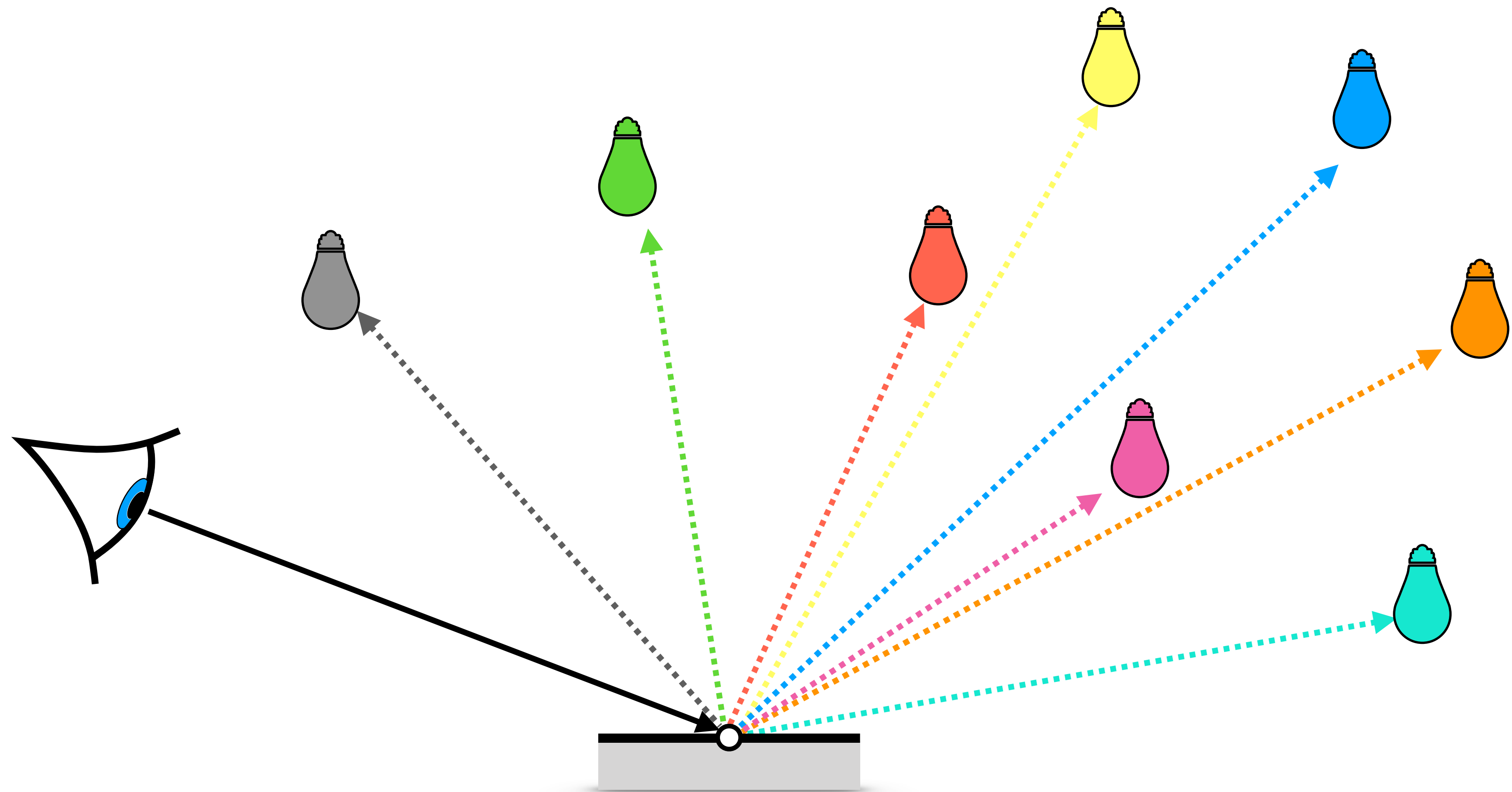
LightCuts Problem



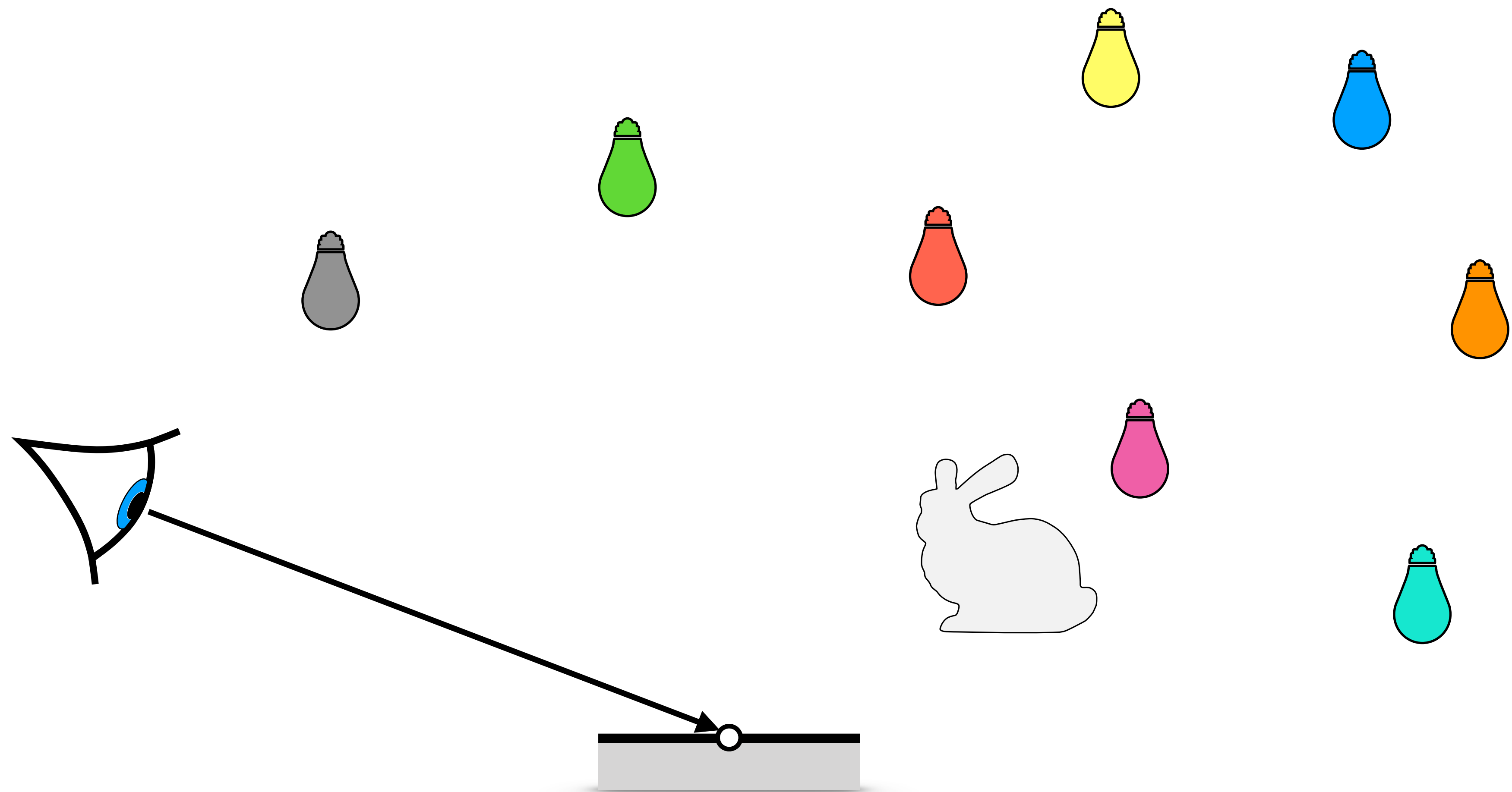
LightCuts Problem



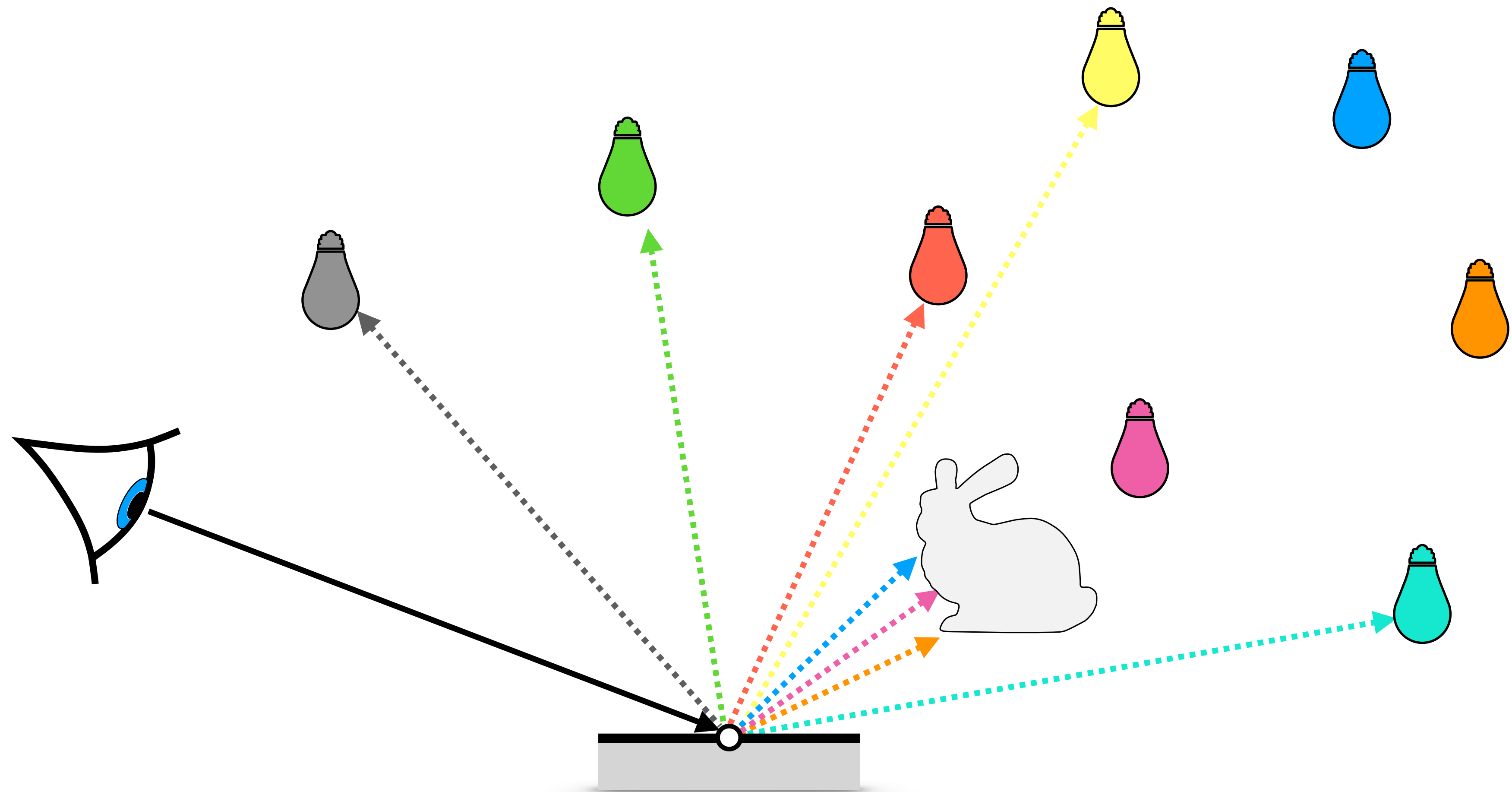
LightCuts Problem



LightCuts Problem



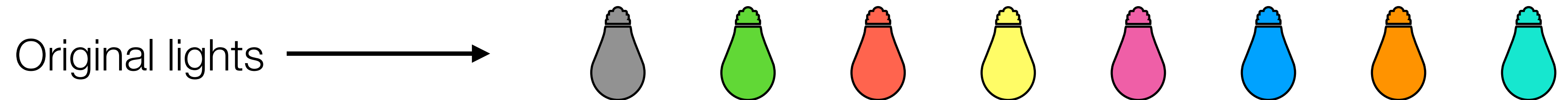
LightCuts Problem



LightCuts: Key Concept

Light Clusters

Light Tree



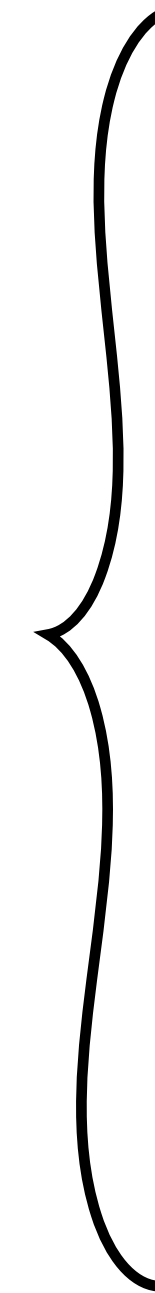
LightCuts: Key Concept

Light Clusters

Light Tree

Light Clusters

Original lights



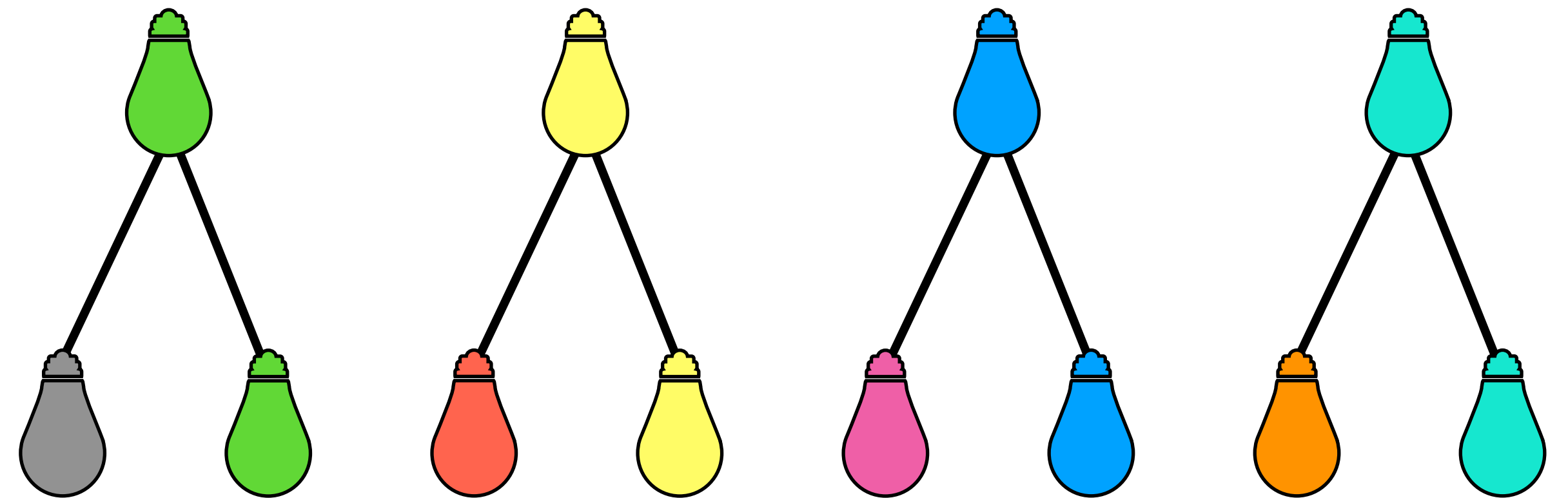
LightCuts: Key Concept

Light Clusters

Light Tree

Light Clusters

Original lights →



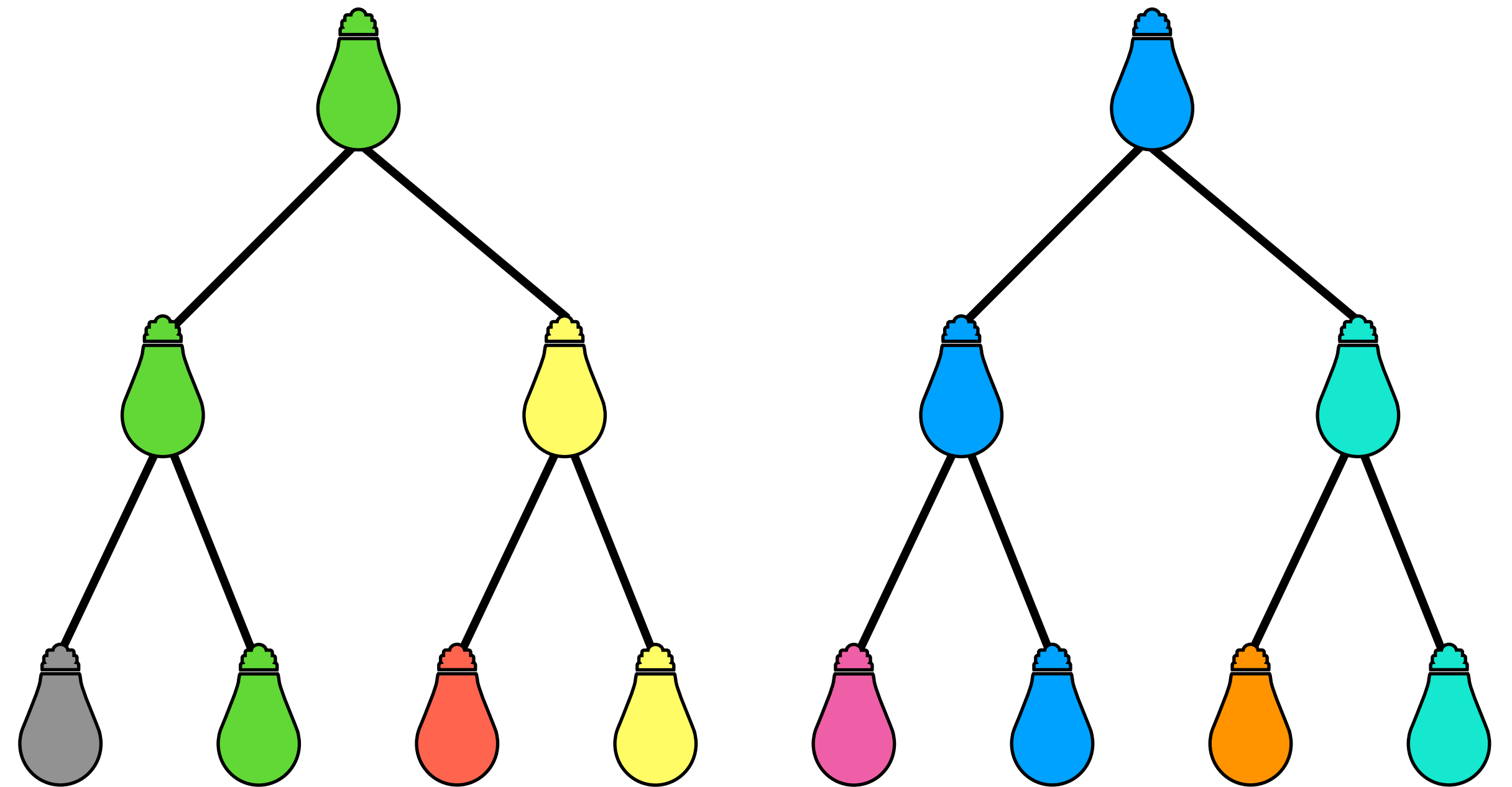
LightCuts: Key Concept

Light Clusters

Light Tree

Light Clusters

Original lights →



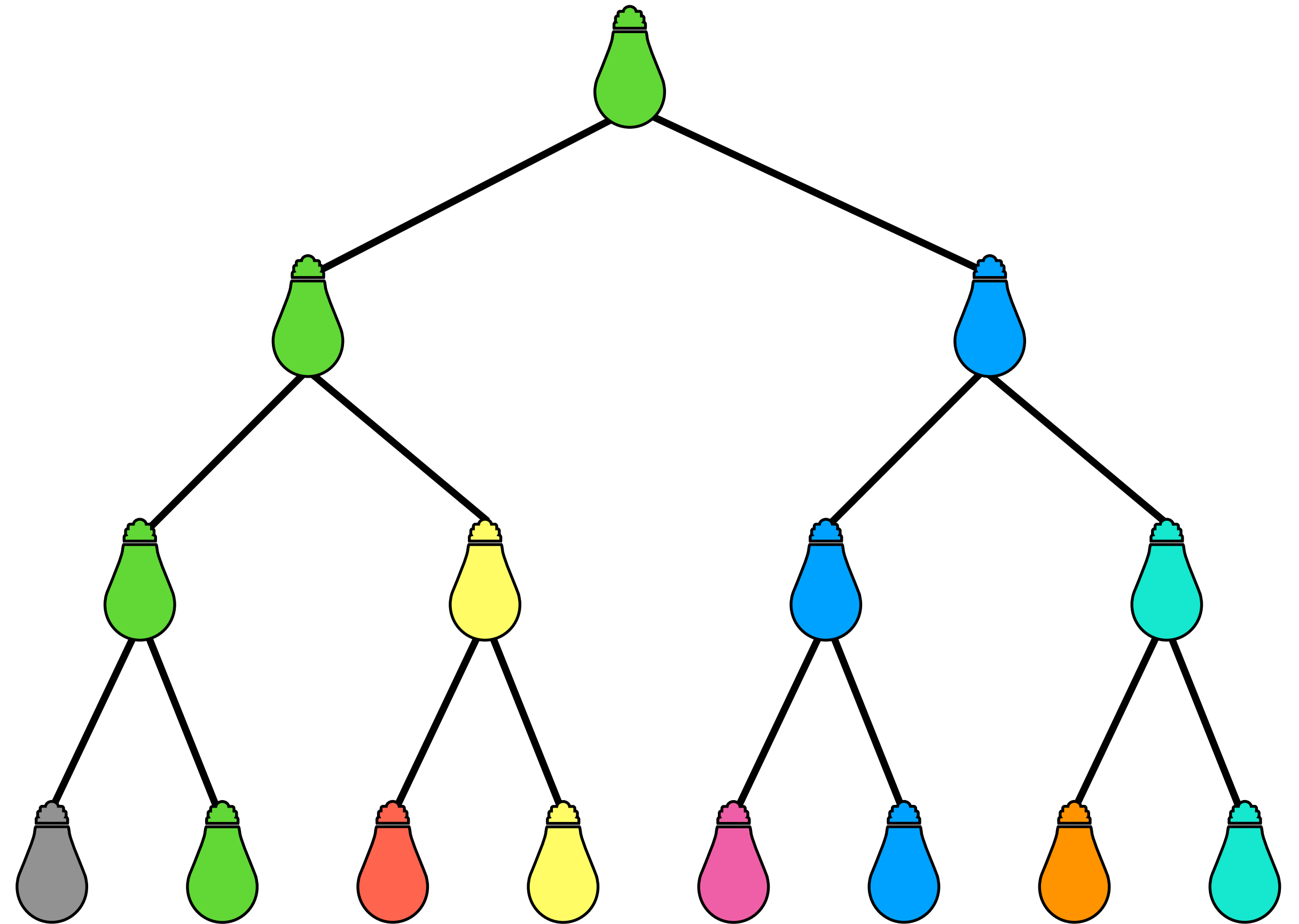
LightCuts: Key Concept

Light Clusters

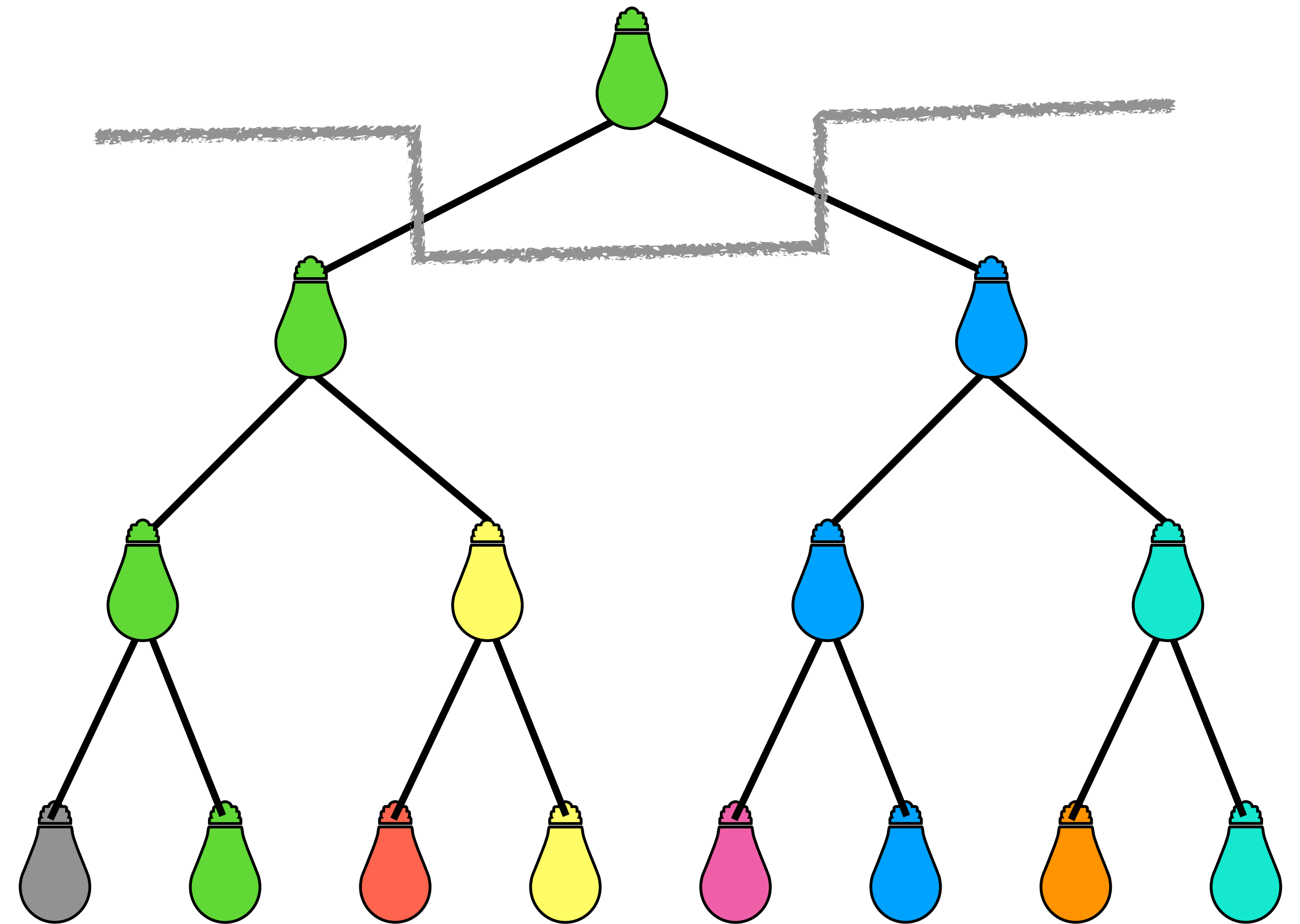
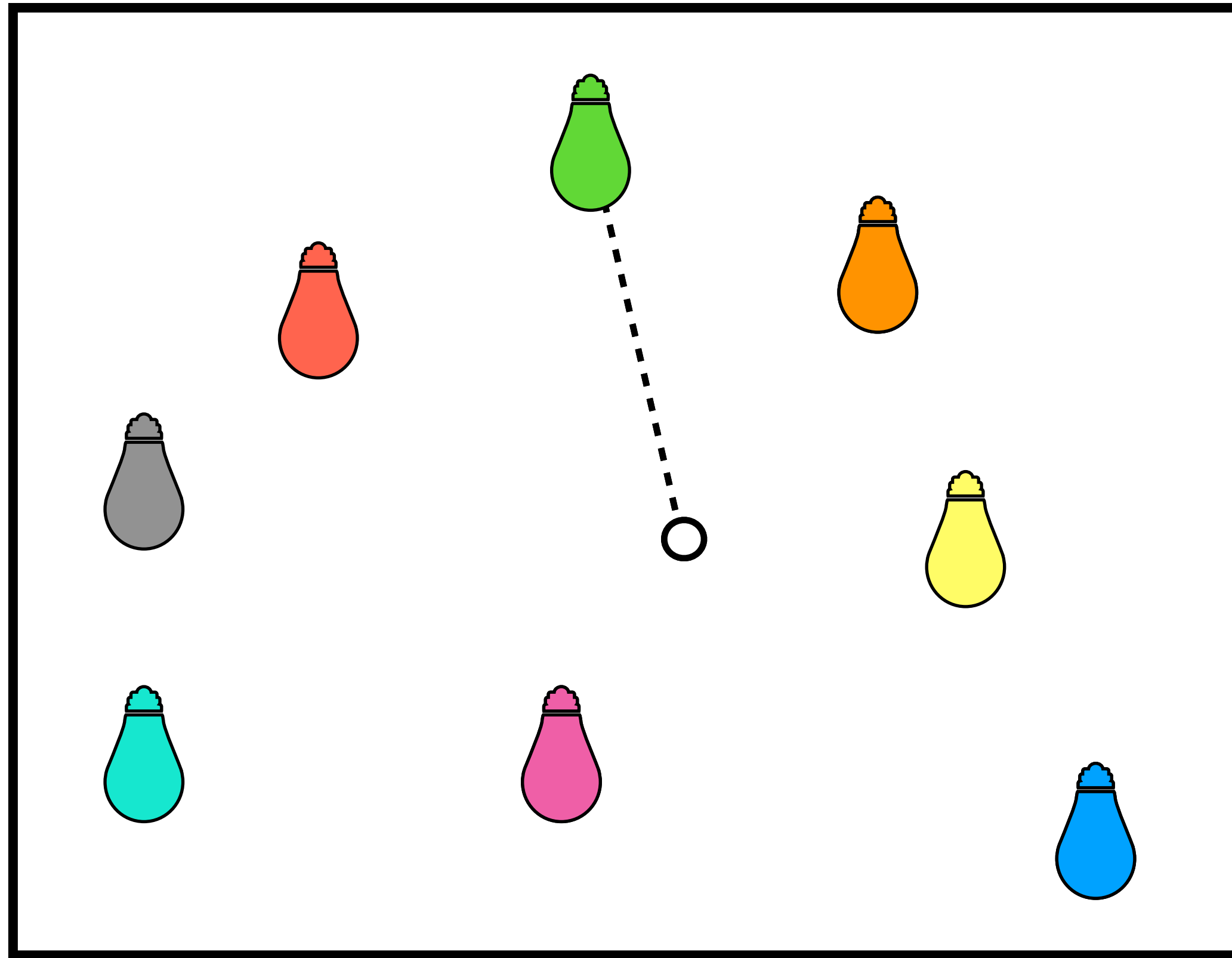
Light Tree

Light Clusters

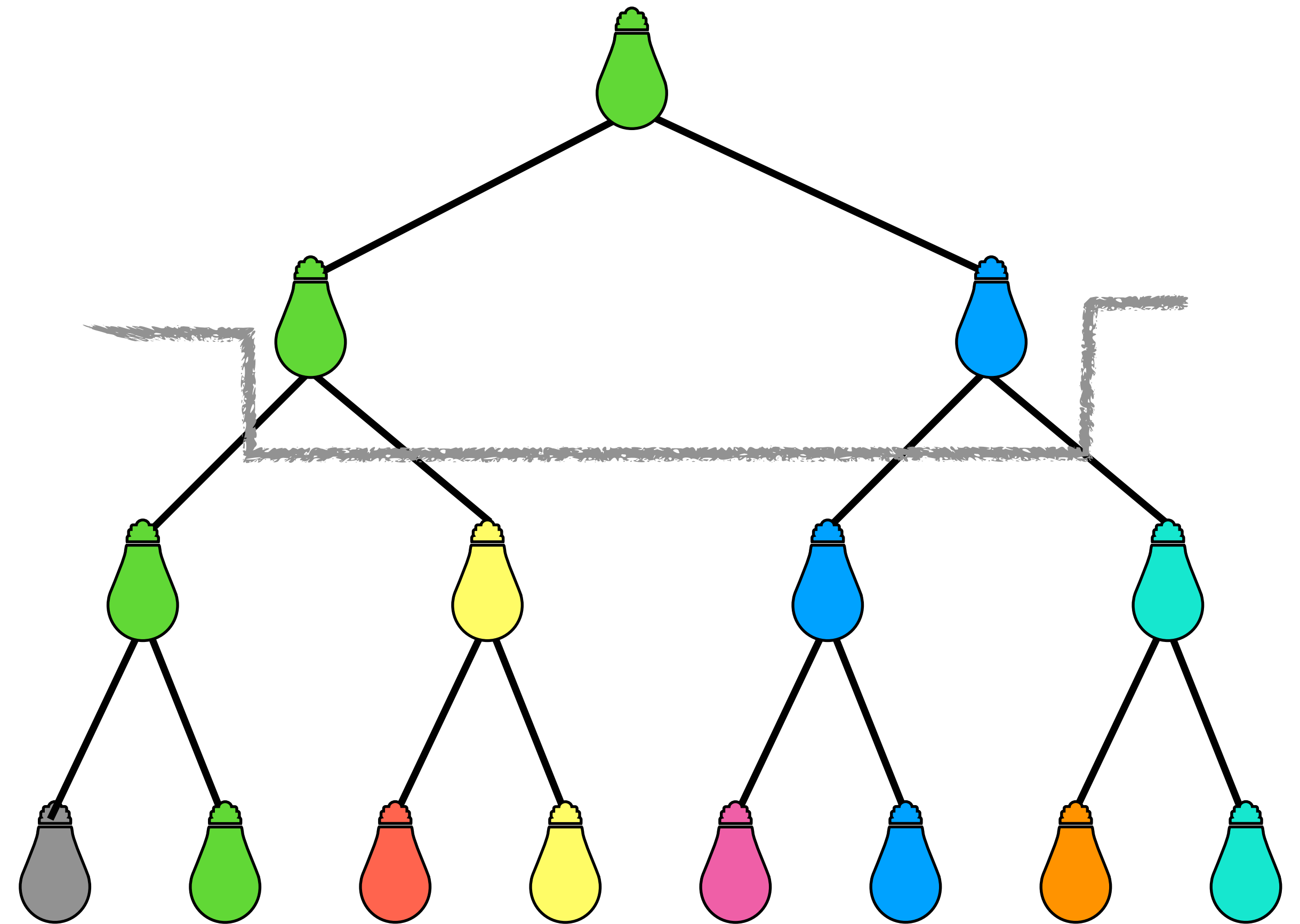
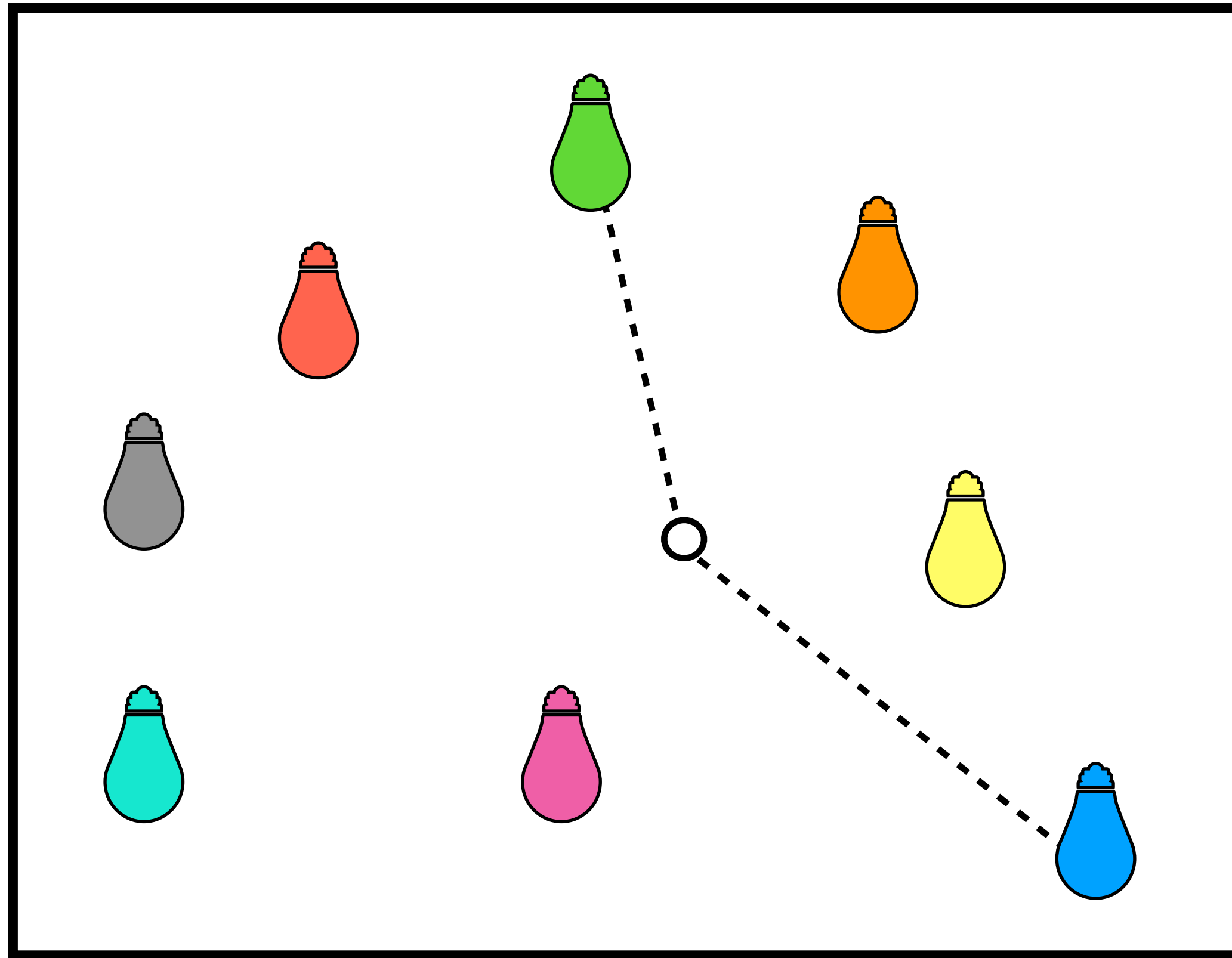
Original lights →



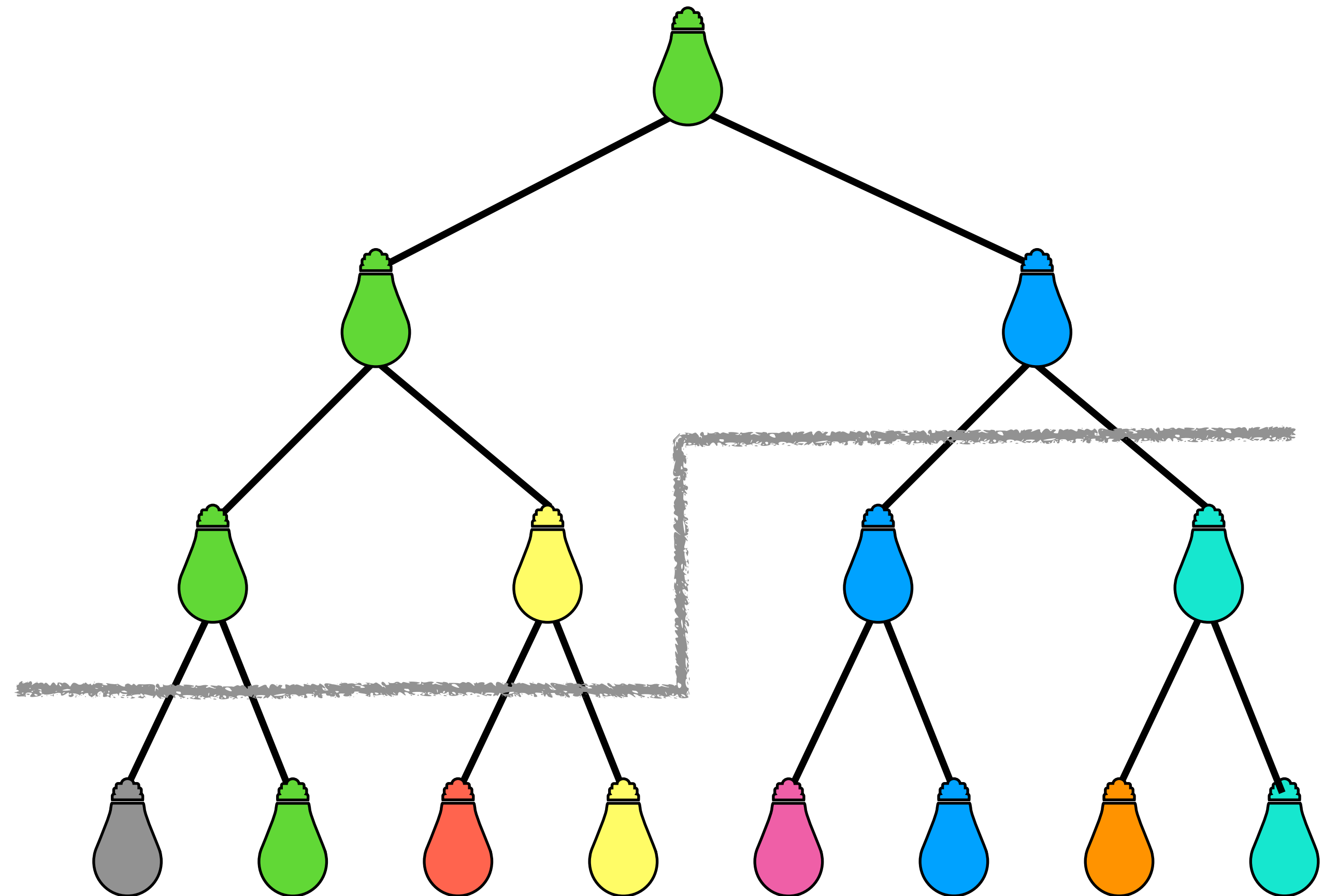
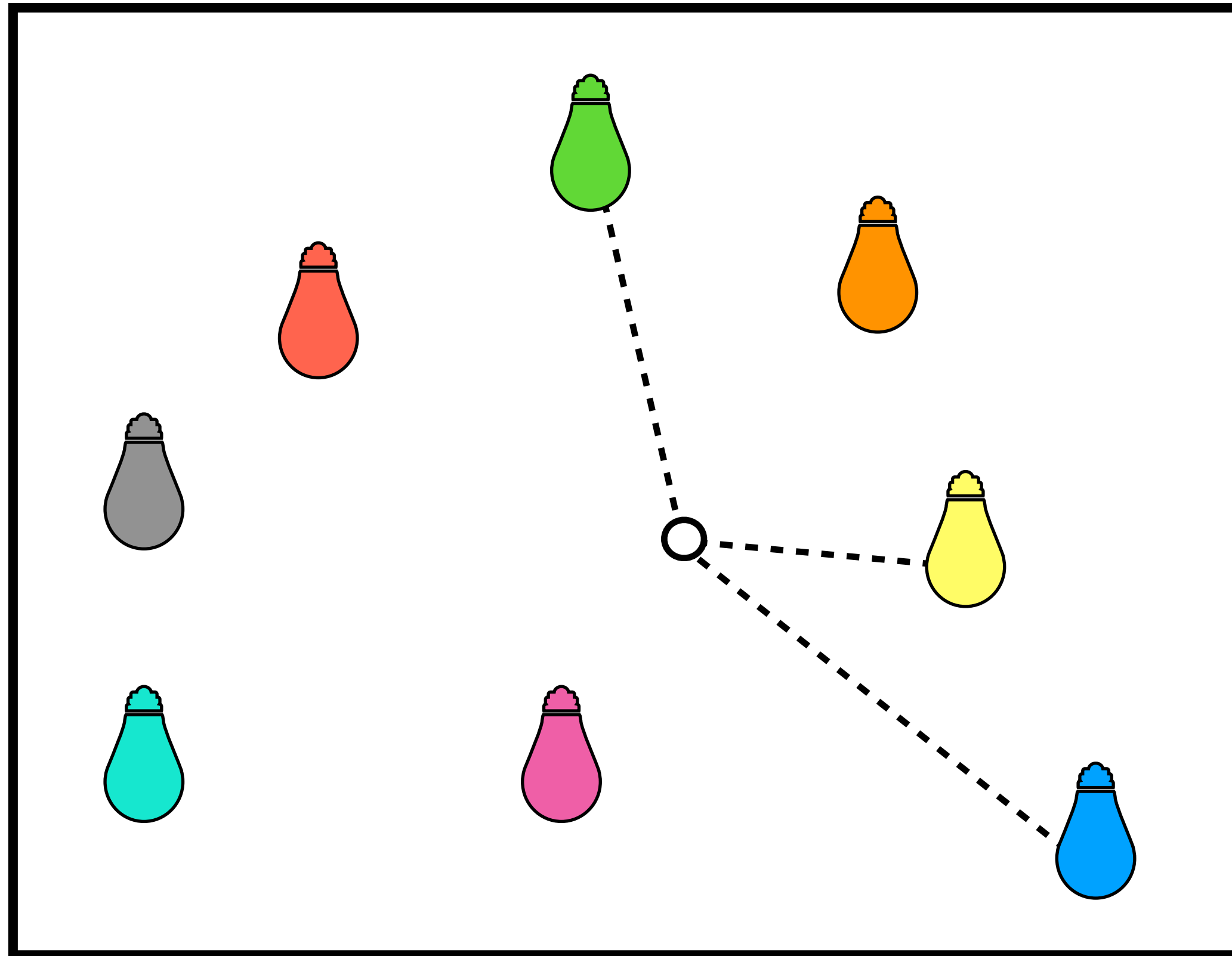
LightCuts: Key Concept



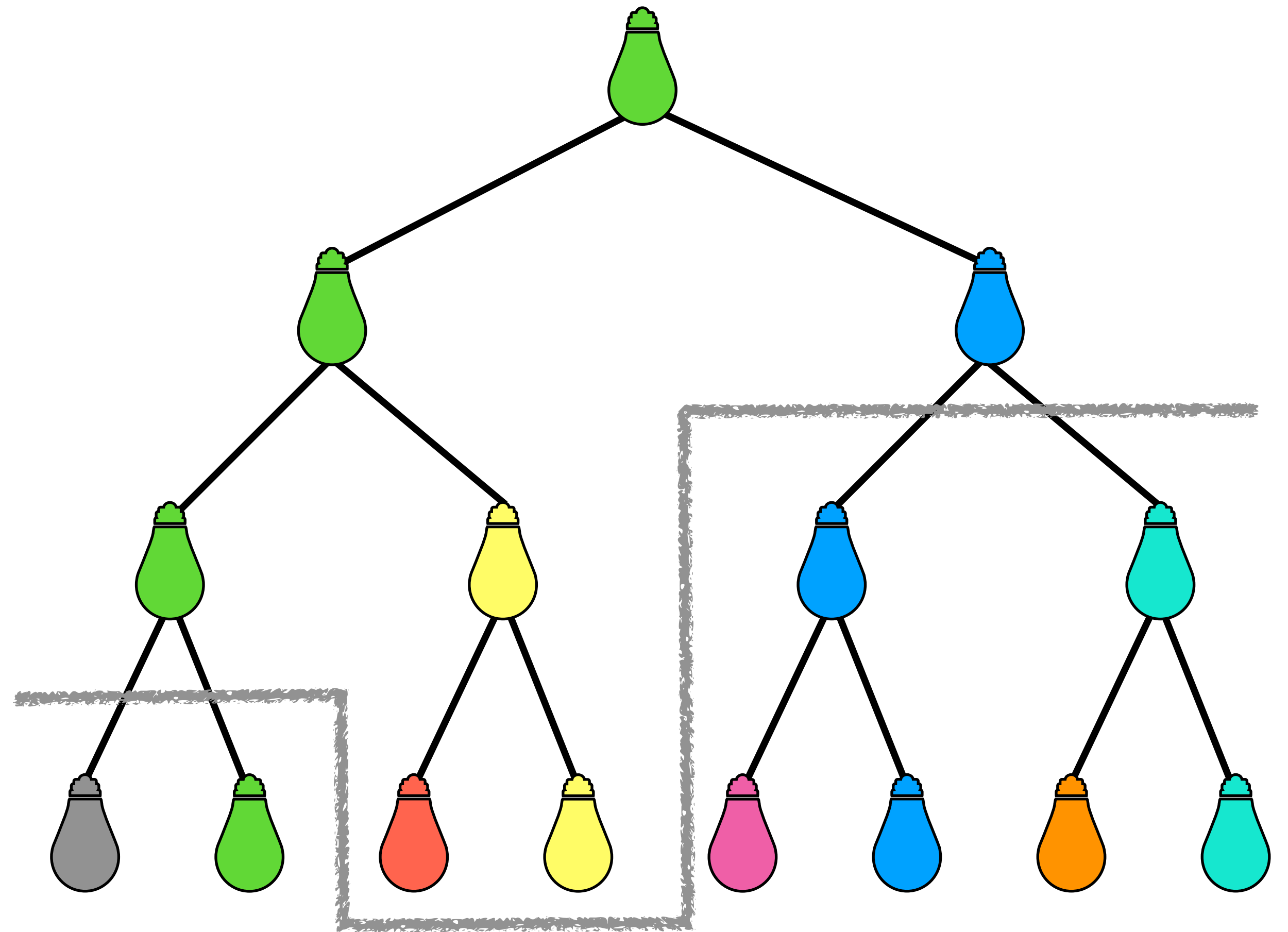
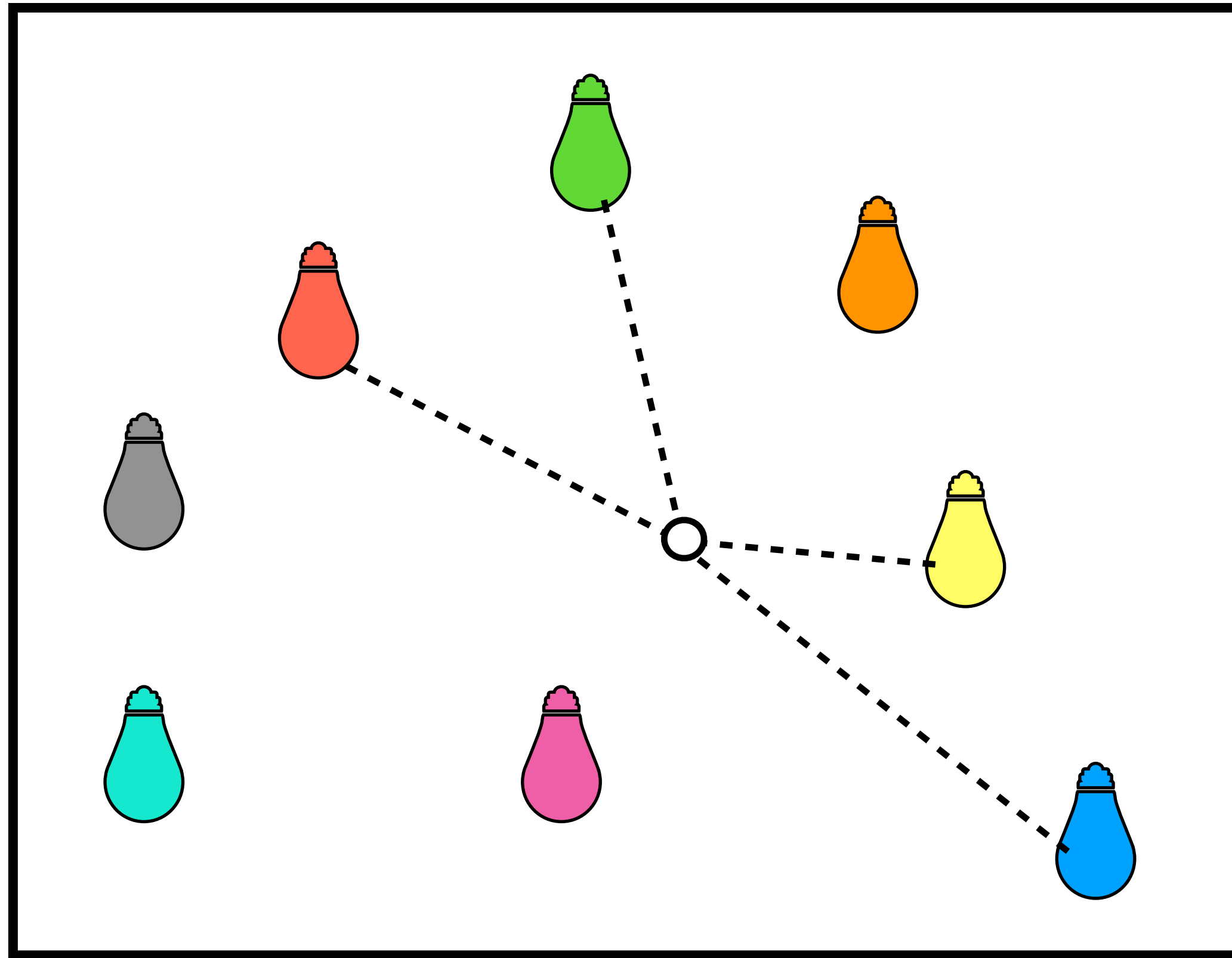
LightCuts: Key Concept



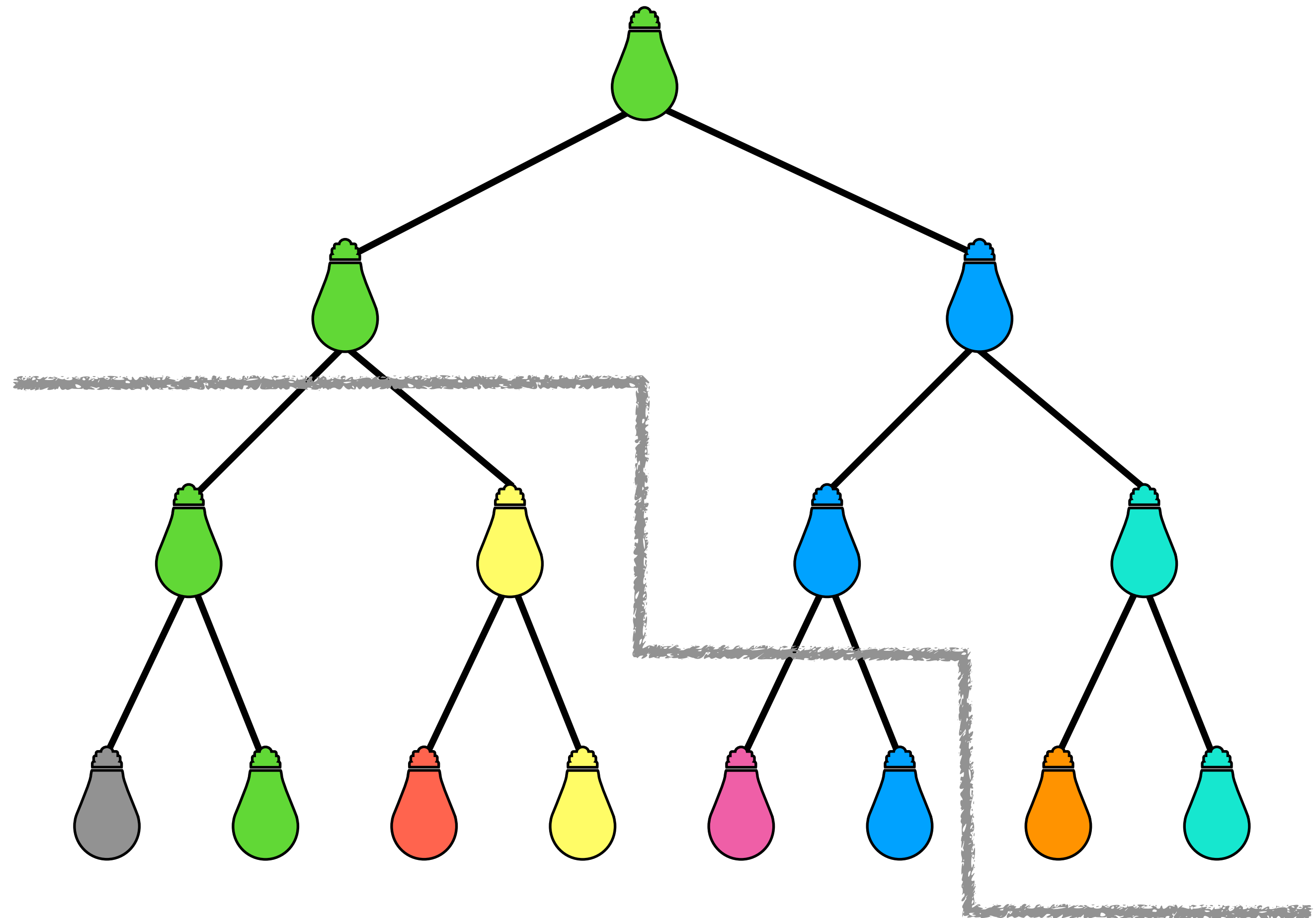
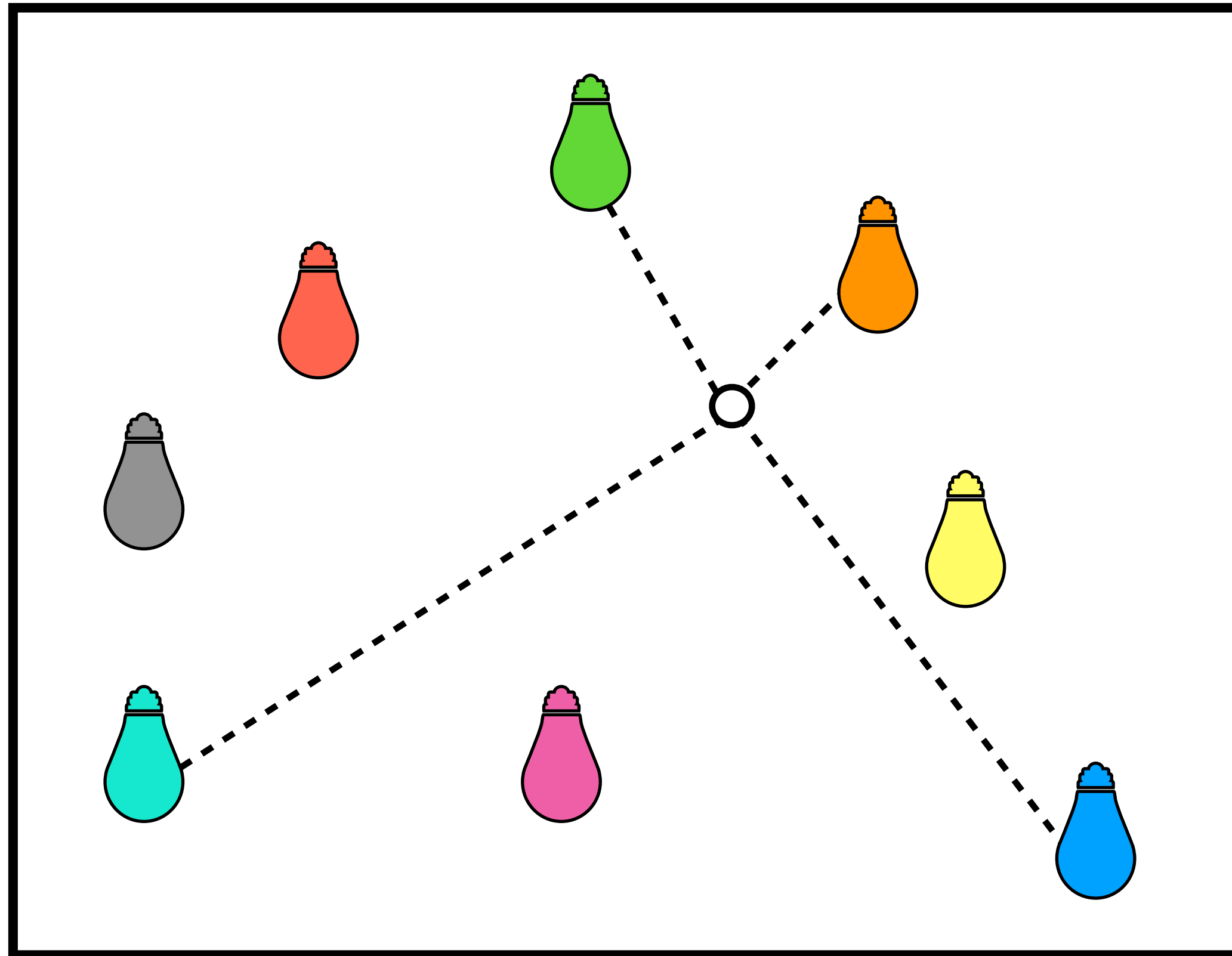
LightCuts: Key Concept



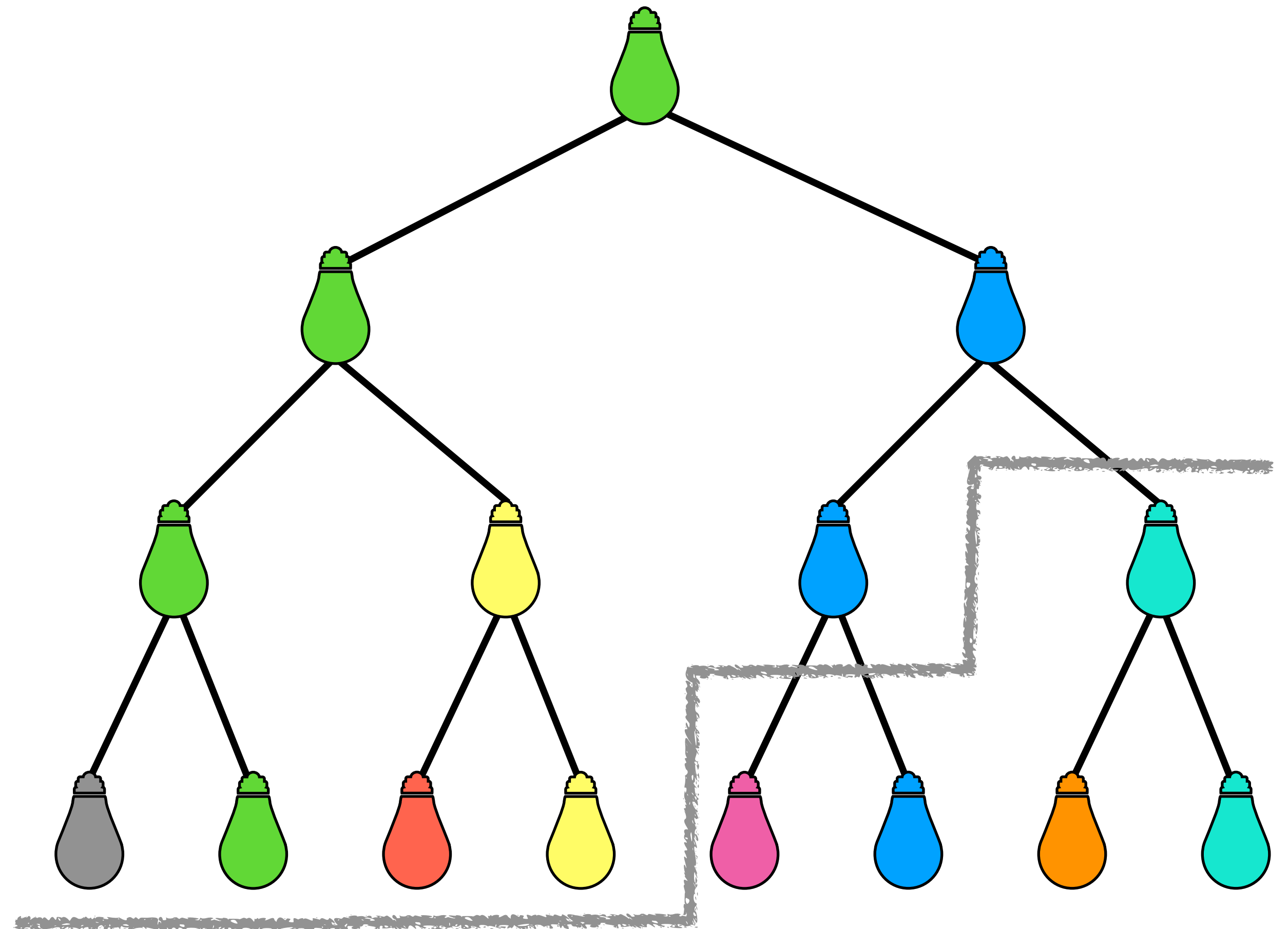
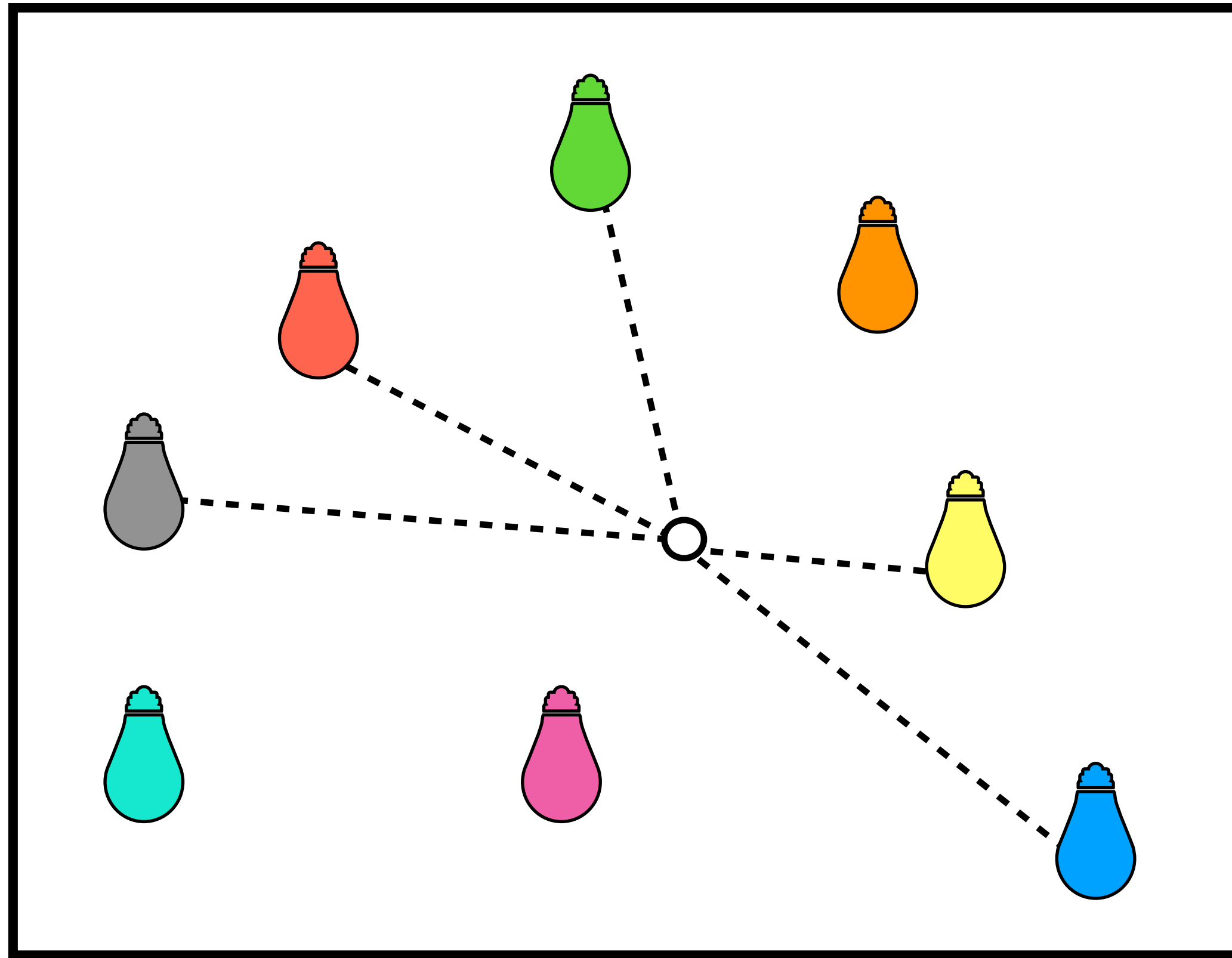
LightCuts: Key Concept



LightCuts: Key Concept



LightCuts: Key Concept



LightCuts: Algorithm Overview

Pre-process:

- Convert illumination to virtual point light sources
- Build light tree

For each ray:

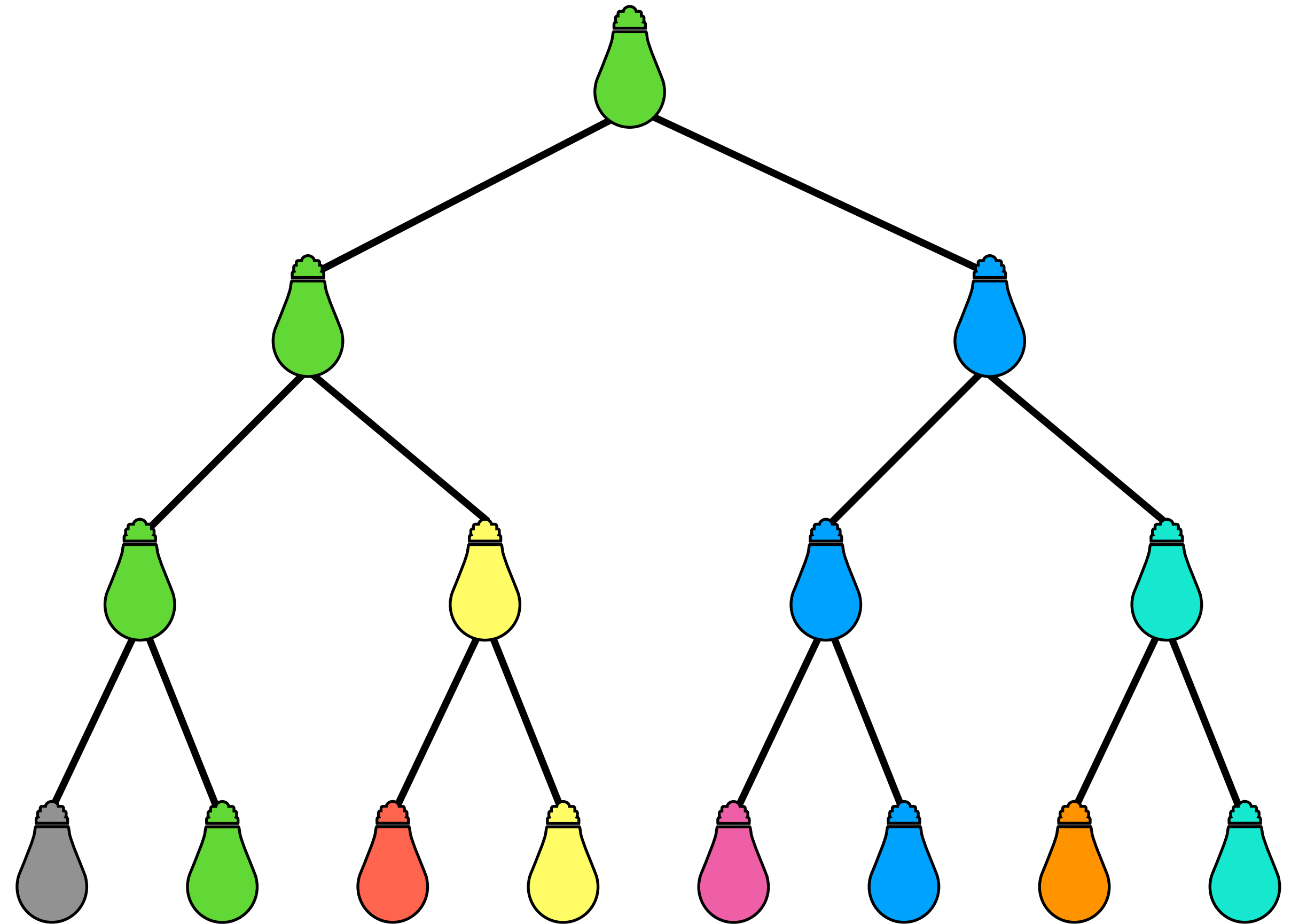
- Choose a cut to approximate the illumination

LightCuts: Issues

Light near the top of the tree more likely to be sampled

Sampling correlations

Different light trees favor different lights







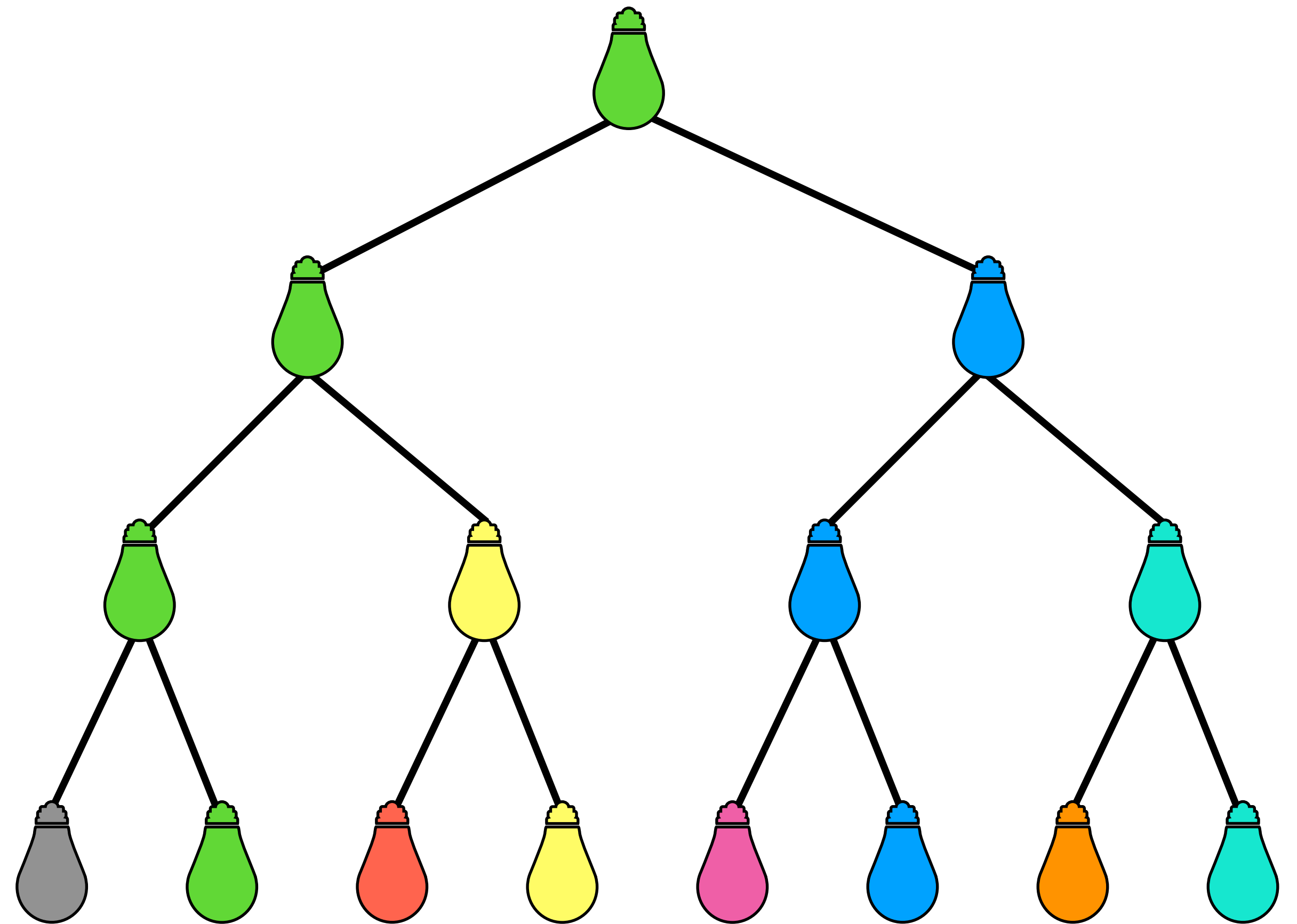
Stochastic LightCuts

Only for Virtual Point Lights

Cem Yuksel [2019]

Stochastic LightCut

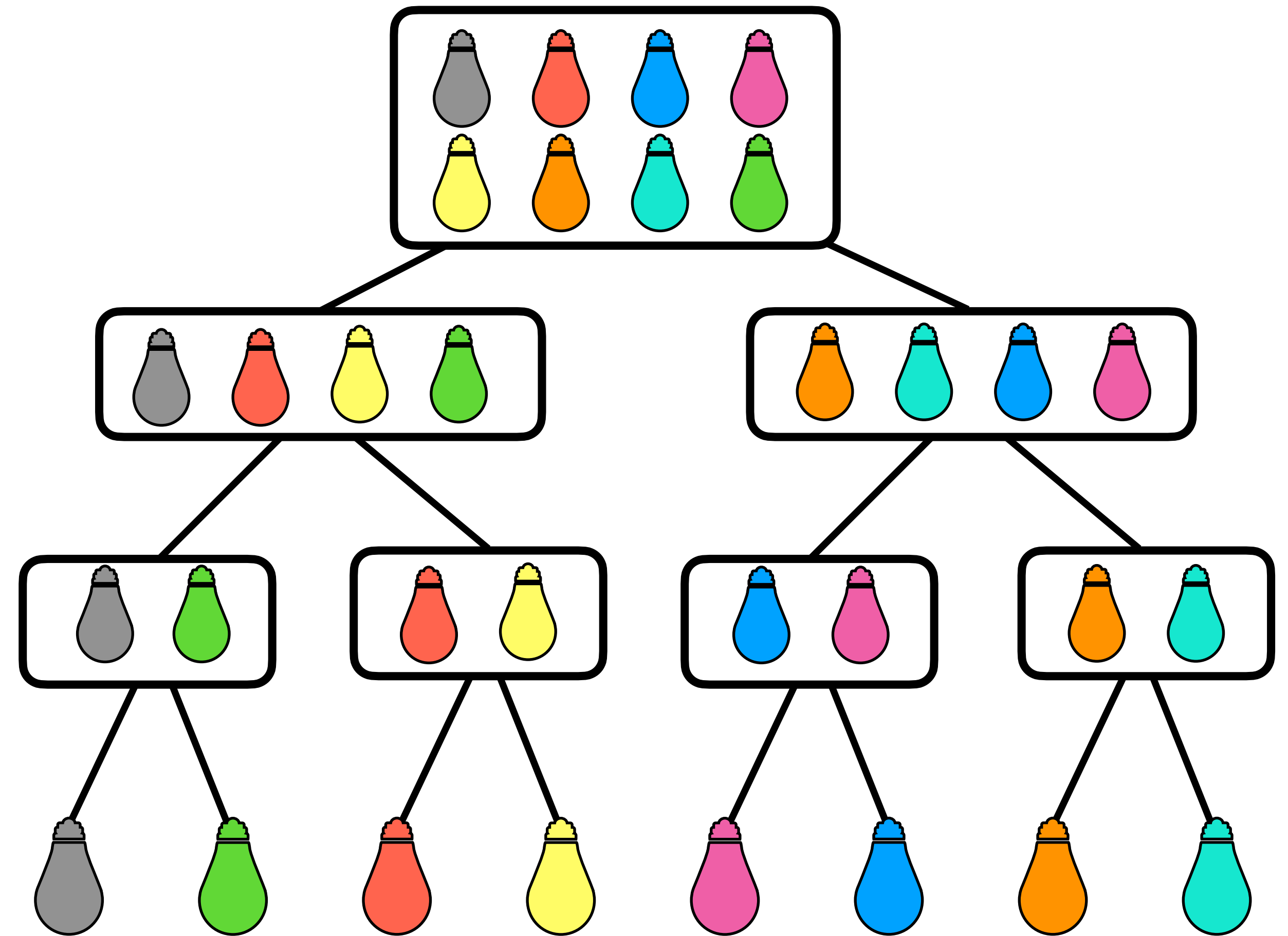
No representative lights



Stochastic LightCut

No representative lights

Randomly select lights



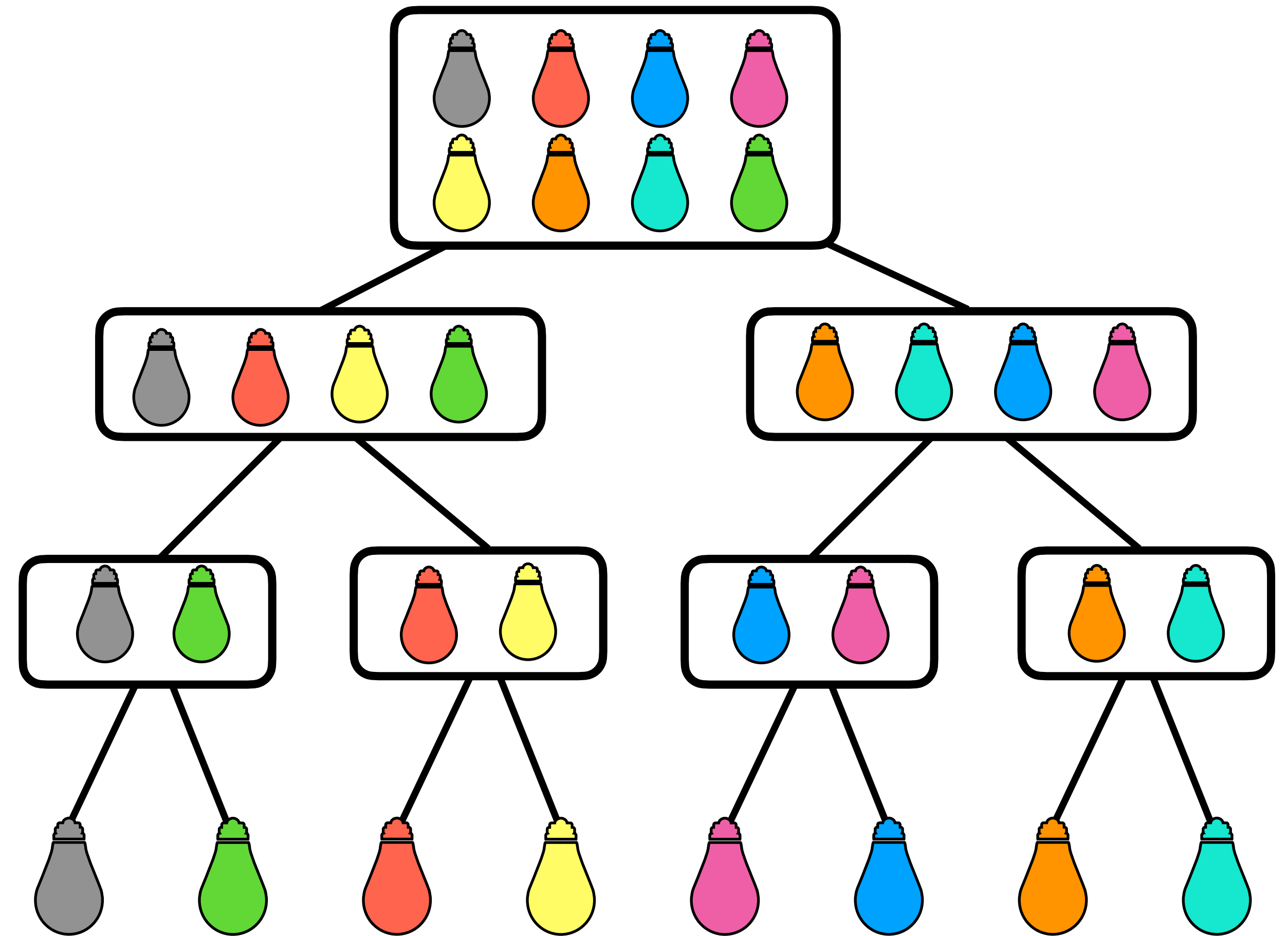
Light Tree

Stochastic LightCut

No sampling correlation
(i.e. no flickering)


Any type of light
(no representative light)

Light sample count can be limited



Light Tree

Direct Illumination



1400 light sources

Cem Yuksel [2019]

Direct Illumination



1400 light sources

Cem Yuksel [2019]

Lighting Grid Hierarchy

Only for Virtual Point Lights



Yuksel and Yuksel [2017]



Explosion Rendering

Challenges:

- Animated volumetric light source
- High variation in fire
- Shadows from a heavy smoke layer

Industry Practices

Smoke illumination by the fire of the explosion :

- No illumination
- 2D filtering in compositing
- 3D filtering / diffusion techniques

Environment illumination by the fire of the explosion :

- No illumination
- Few hand-placed lights to approximate illumination
- Some inferior representation of the fire volume as light source

Lighting Grid Hierarchy

- Convert **volume** to many **point lights**
- Build **Lighting Grid Hierarchy**
- Pre-compute volumetric **shadows**
- Add **multiple scattering**, if desired
- Finally, **render** using hierarchy

Lighting Grid Hierarchy

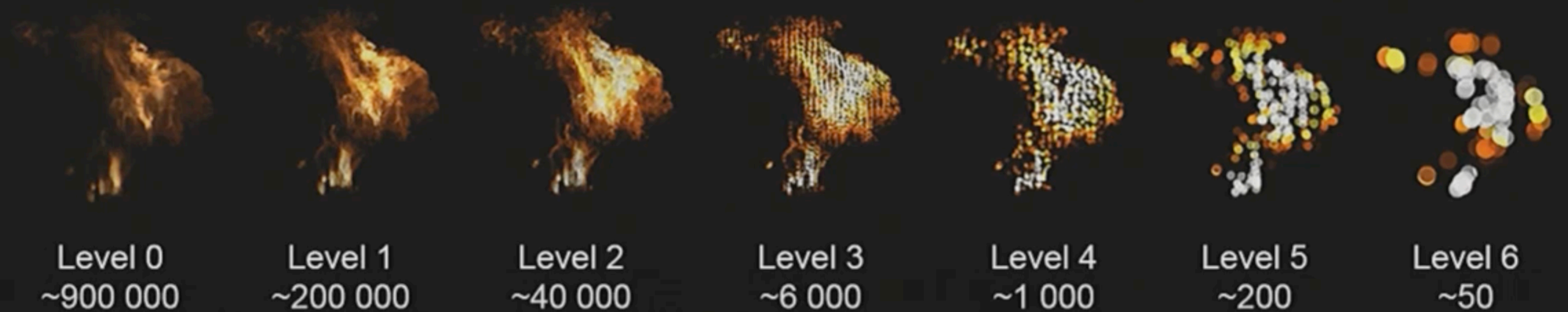
A multi-resolution representation of lighting

Temporary coherency:

- No clustering
- No binary decisions
- No sharp thresholds

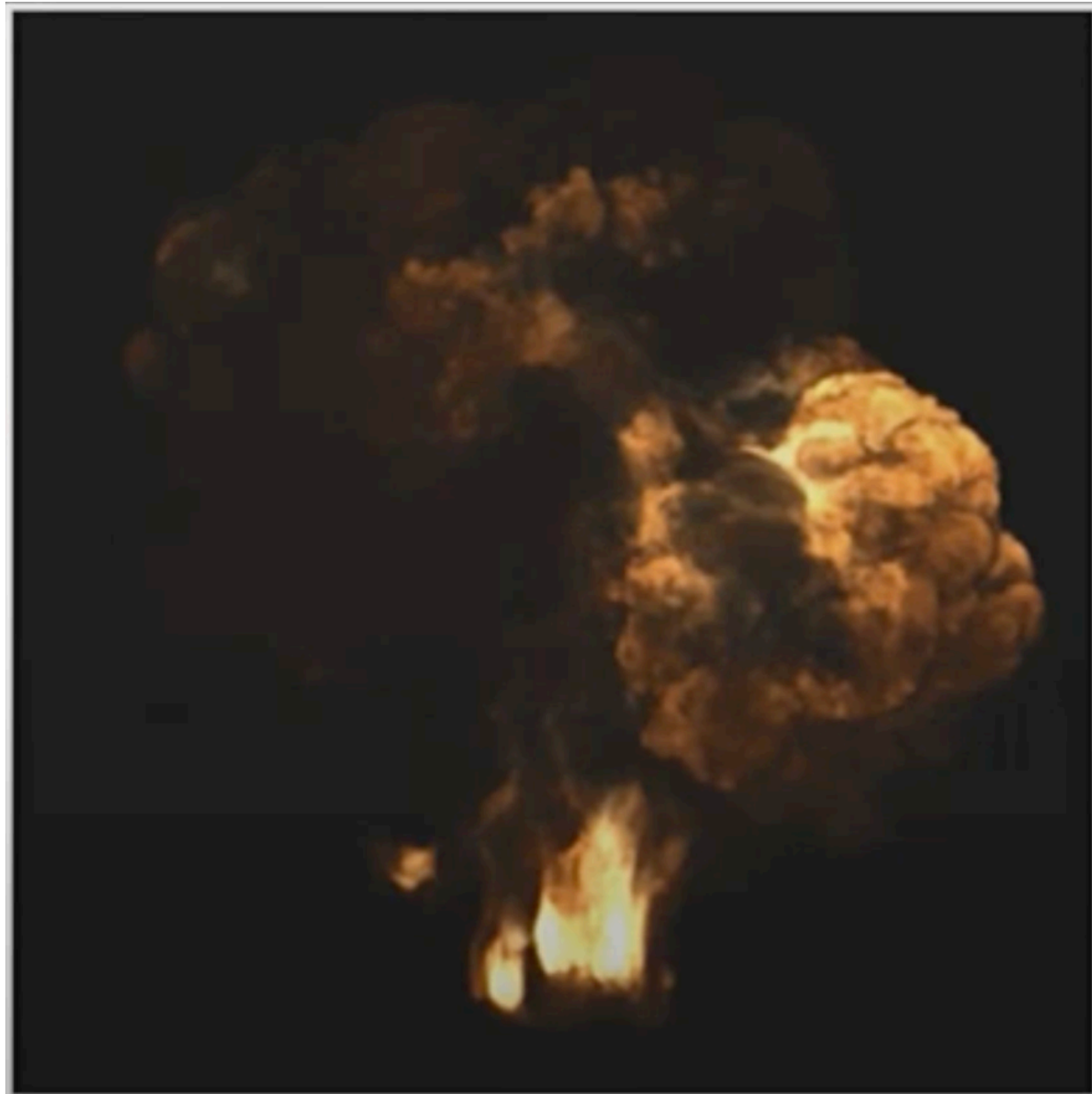
Lighting Grid Hierarchy

Multi-resolution representation:

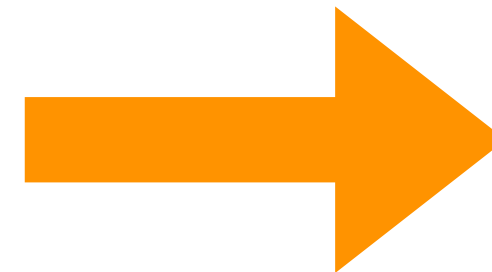


Lighting Grid Hierarchy

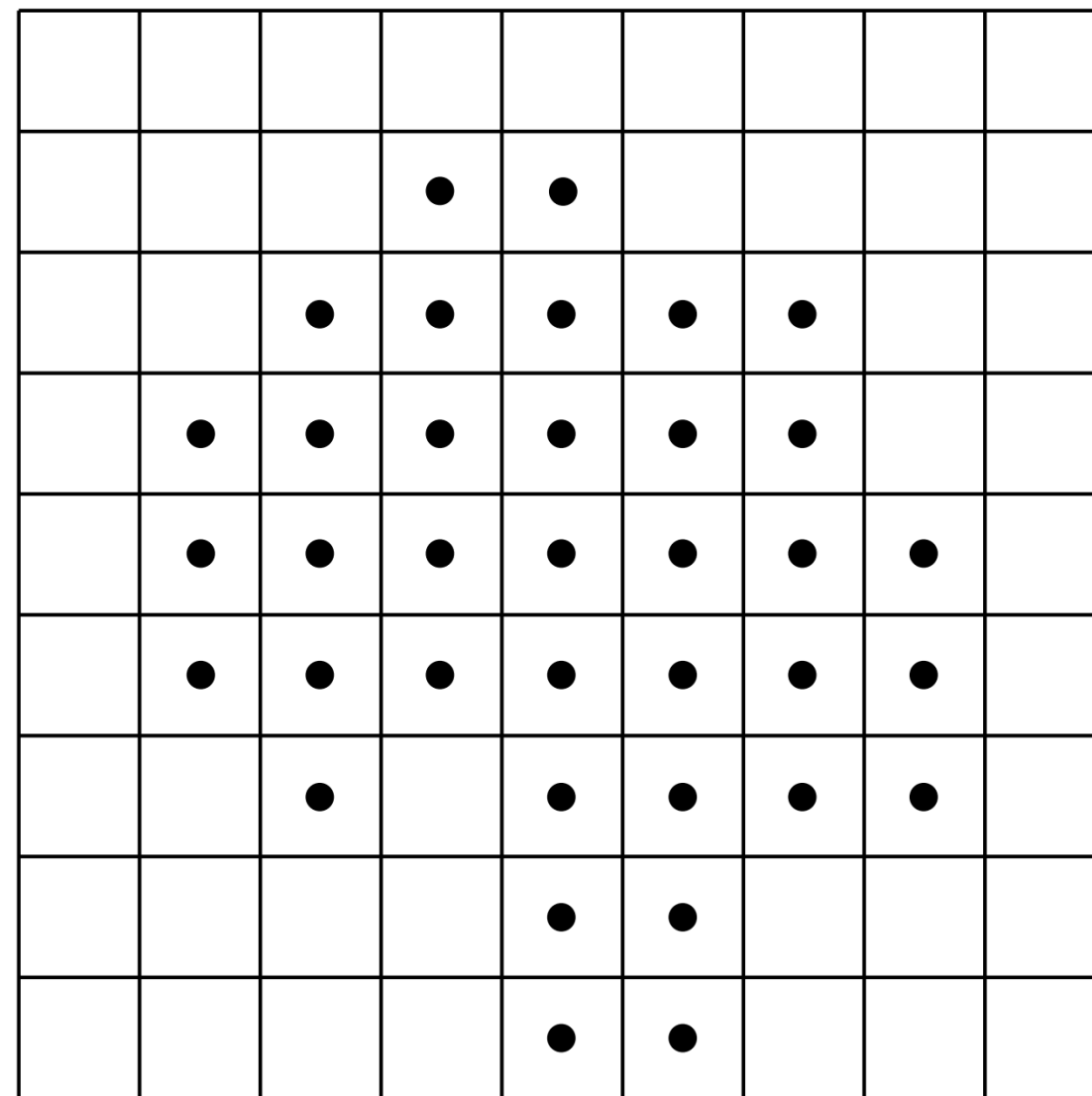
Volume Data



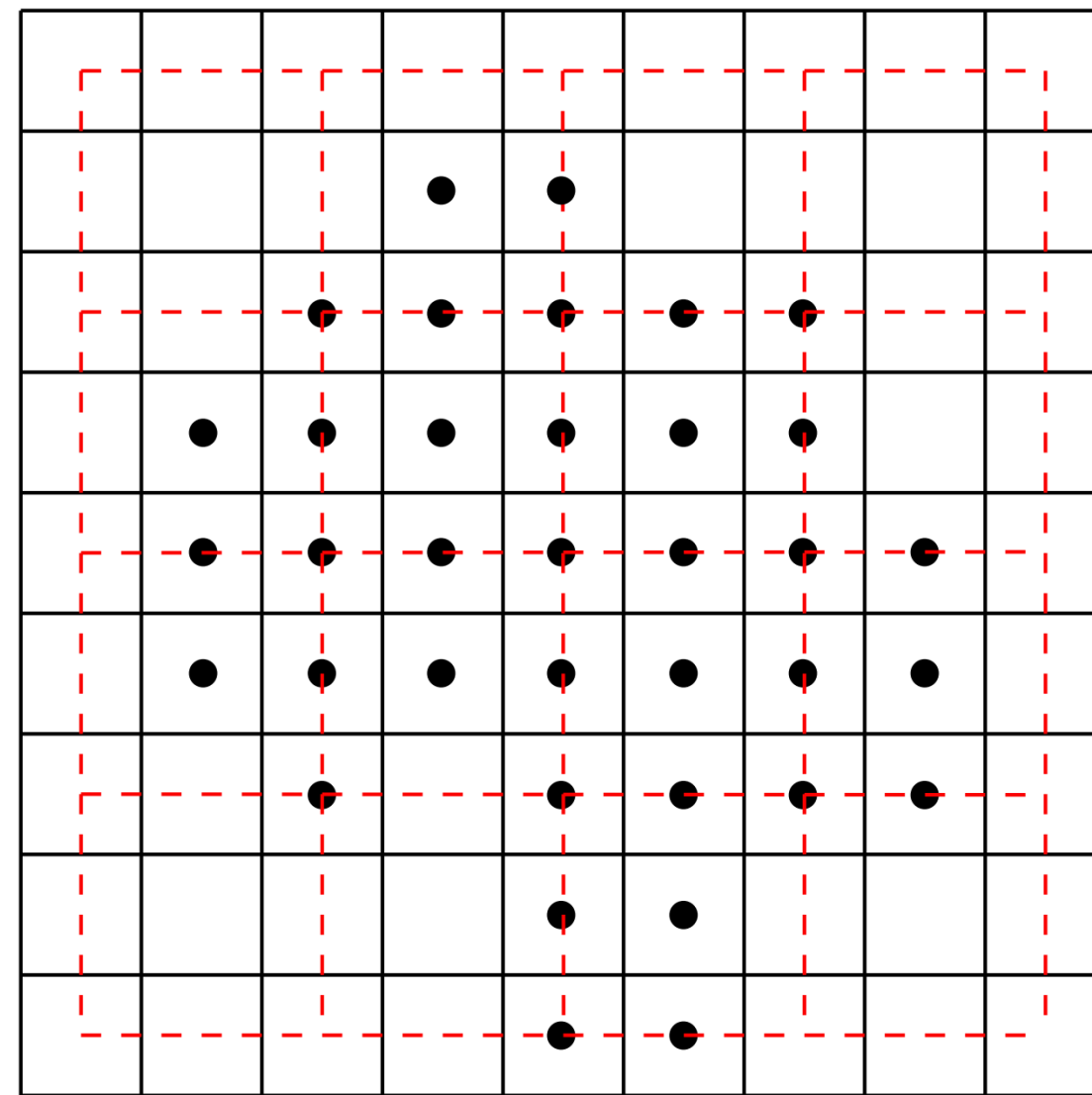
Point Lights



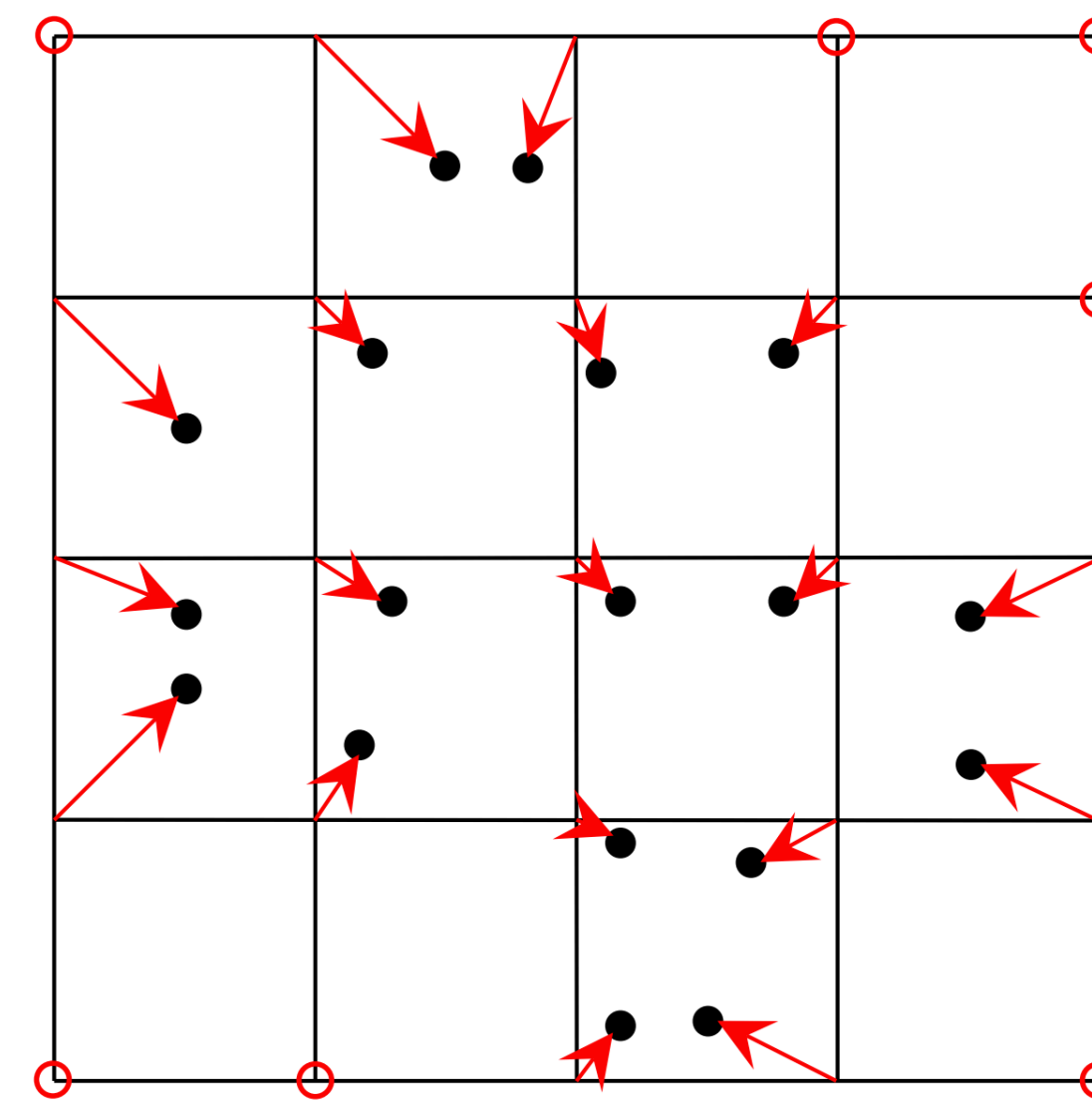
Generation



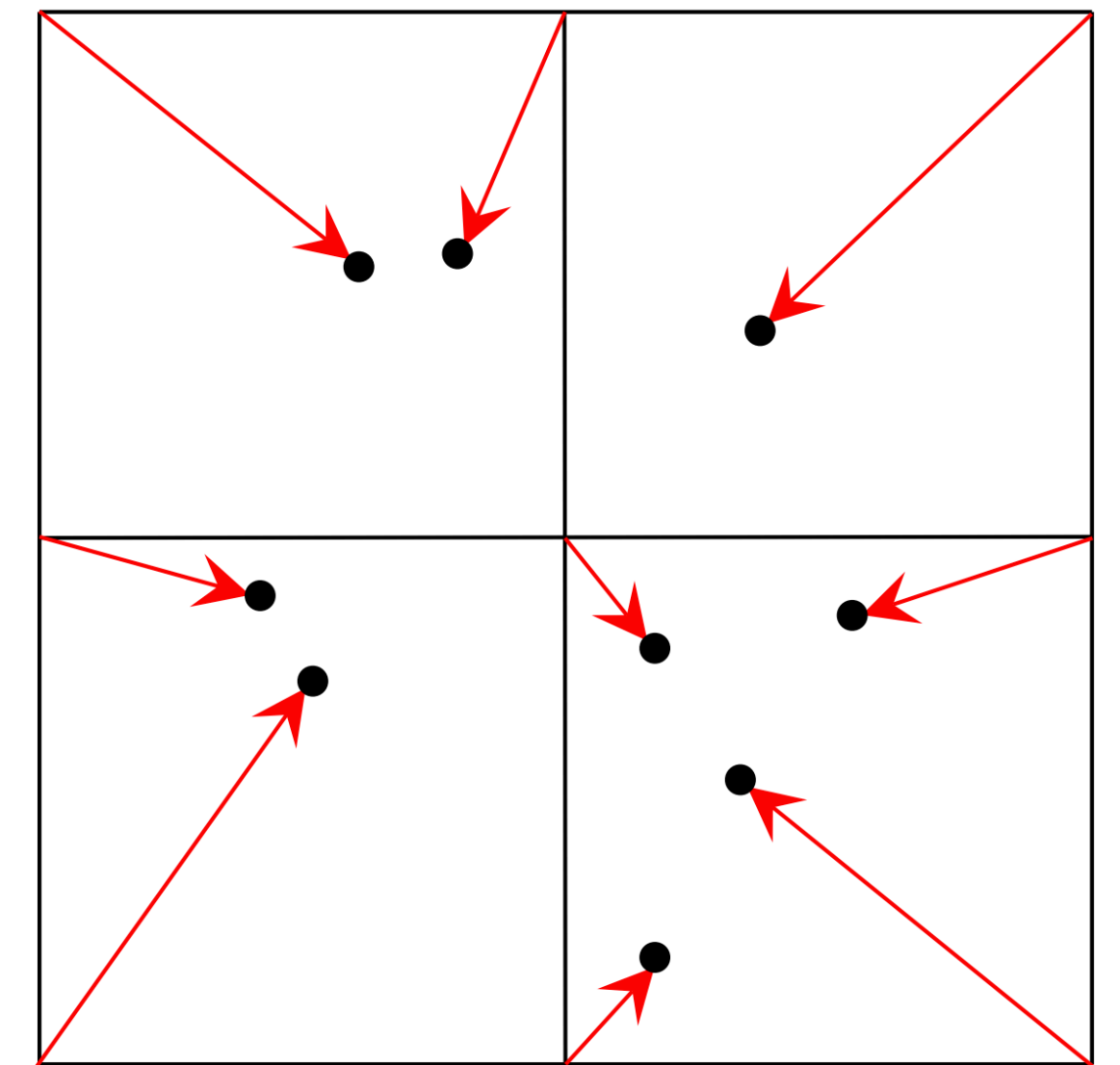
Simulation Grid 0-th level



Level-1 grid over simulation grid



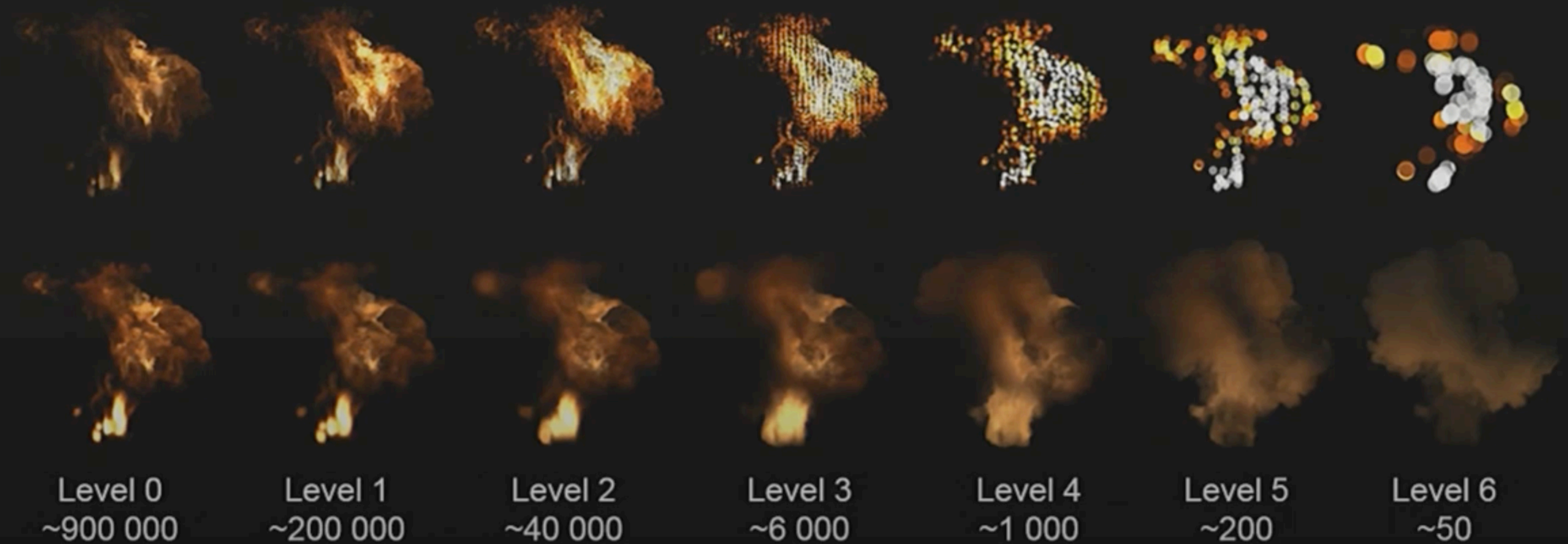
Level-1 grid



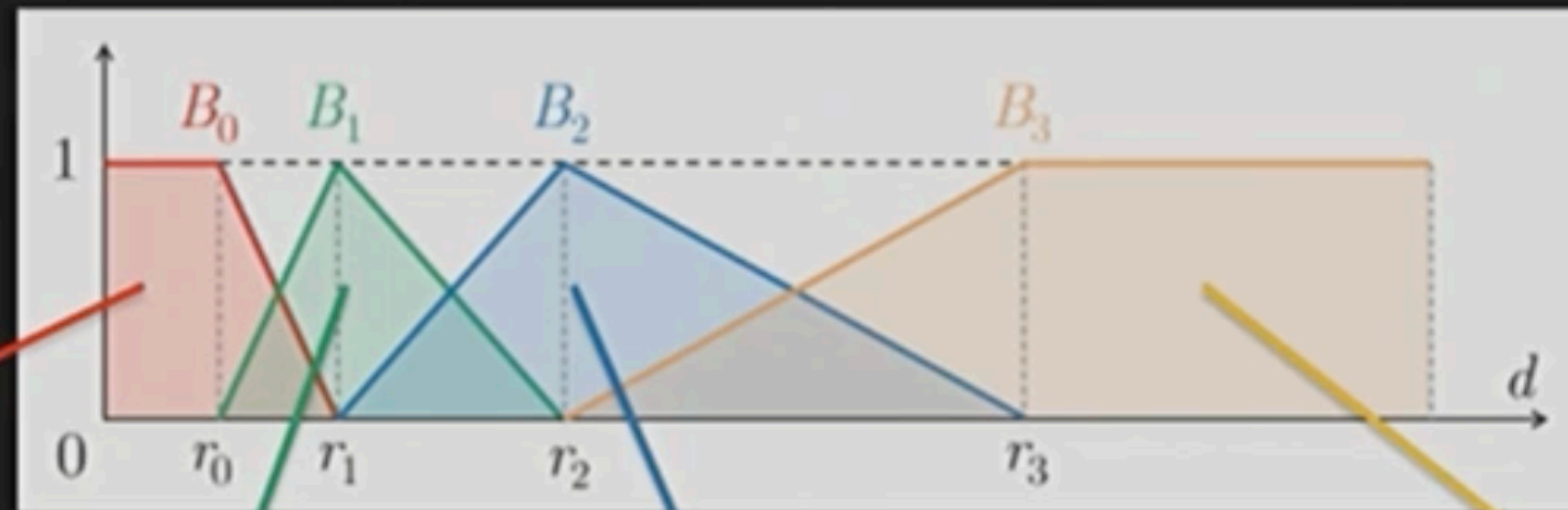
Level-2 grid

Lighting Grid Hierarchy

Multi-resolution representation of illumination:



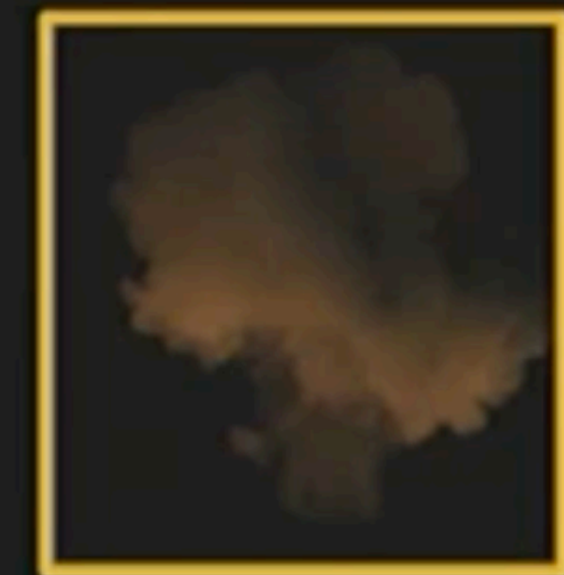
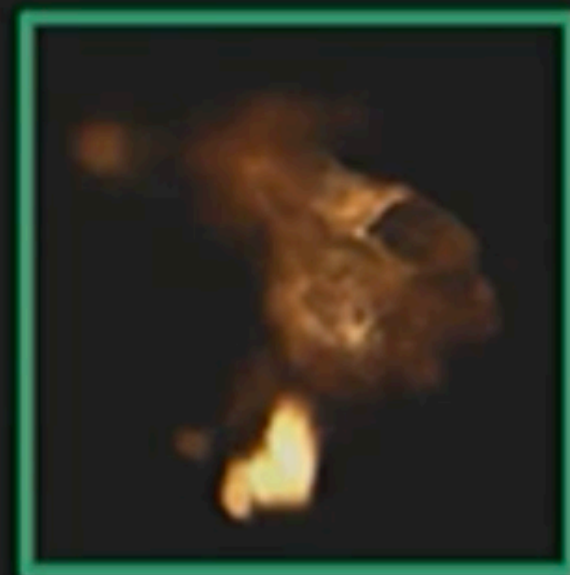
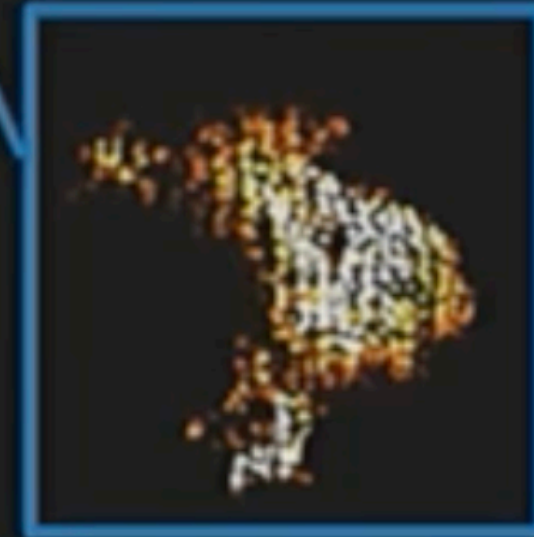
Blending Function



$$r_1 = 2 \times r_0$$

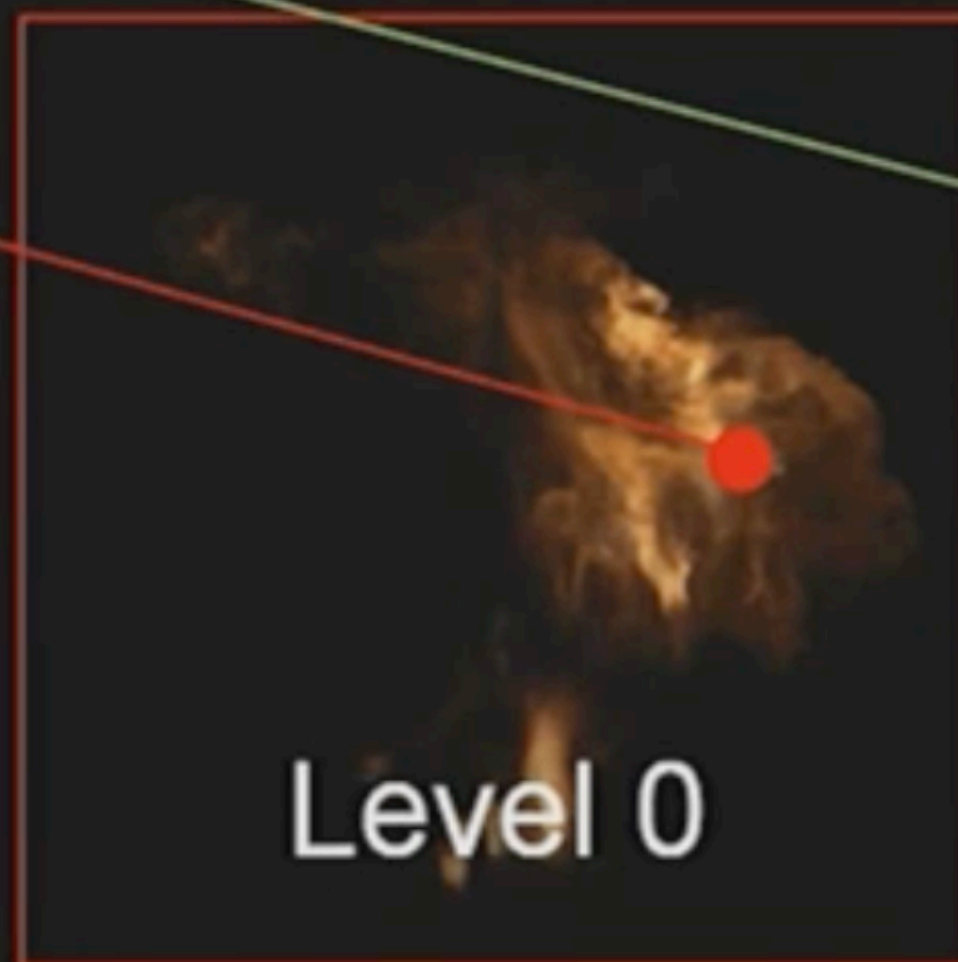
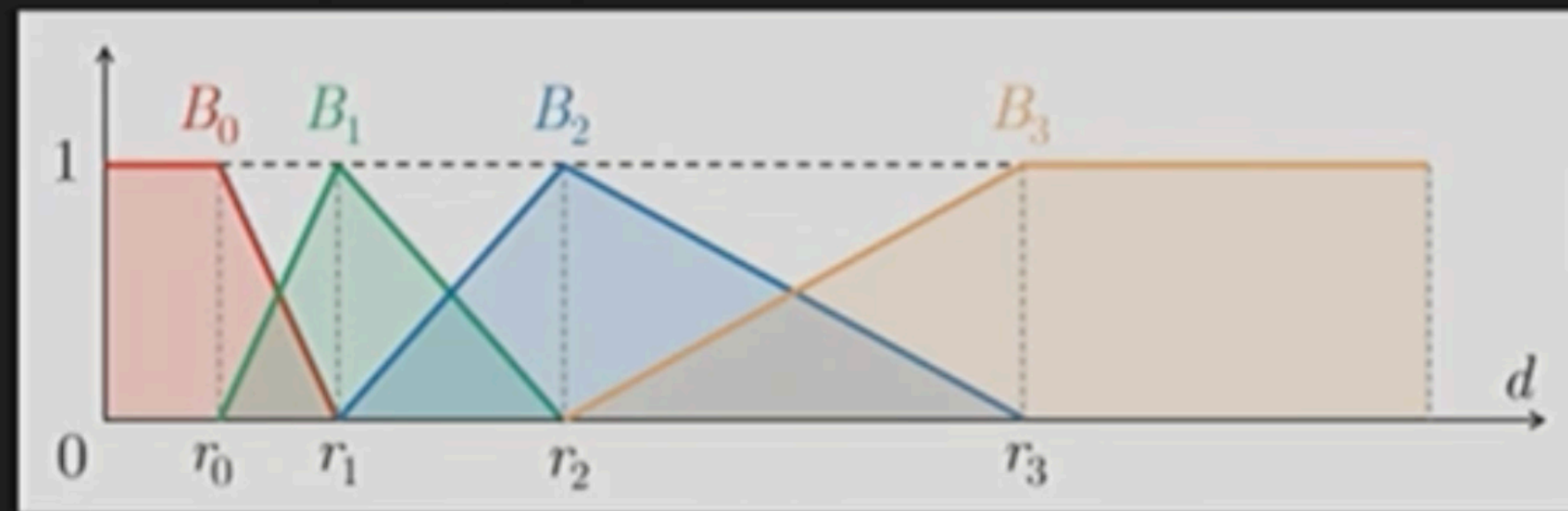
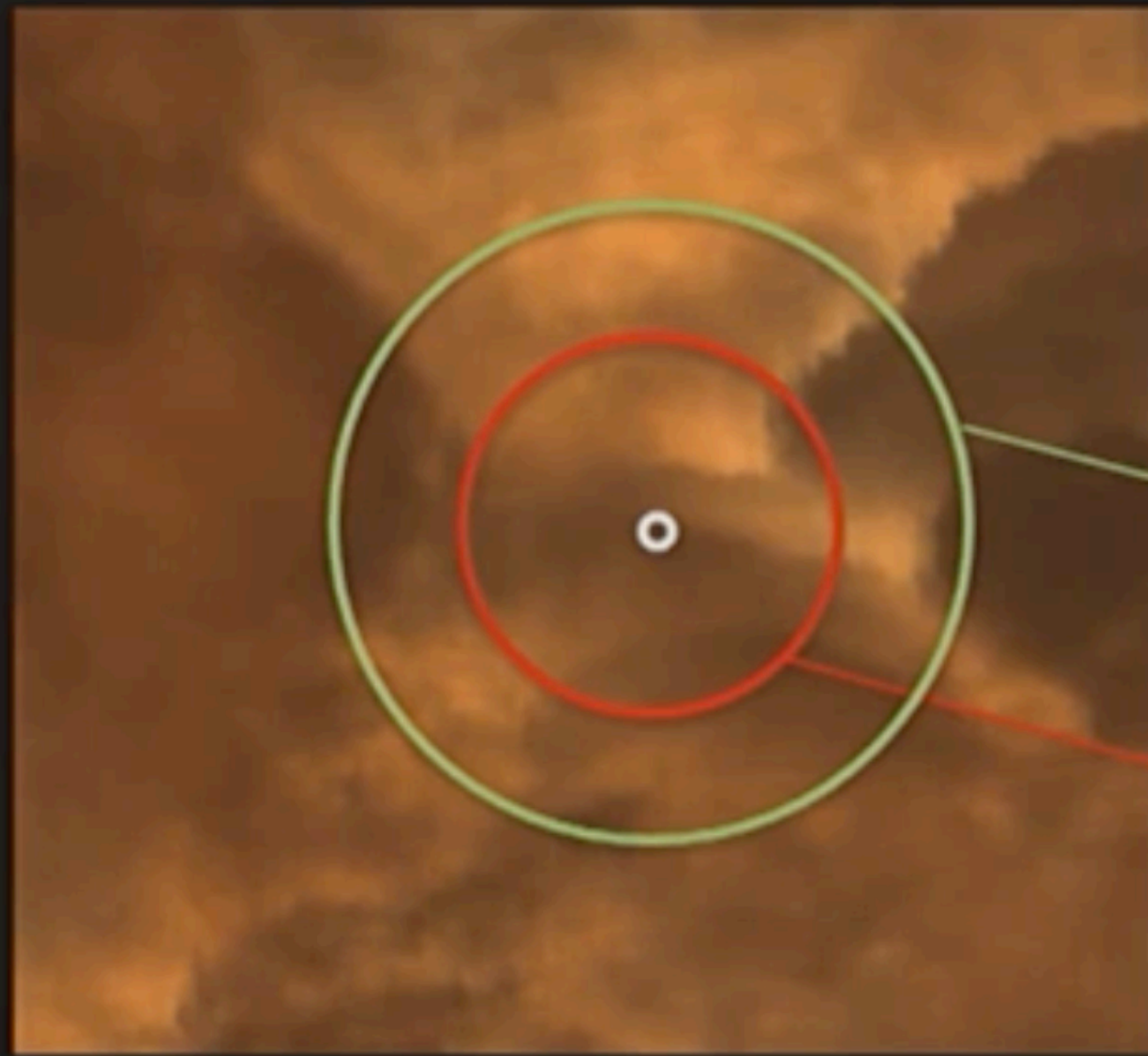
$$r_2 = 2 \times r_1$$

$$r_3 = 2 \times r_2$$

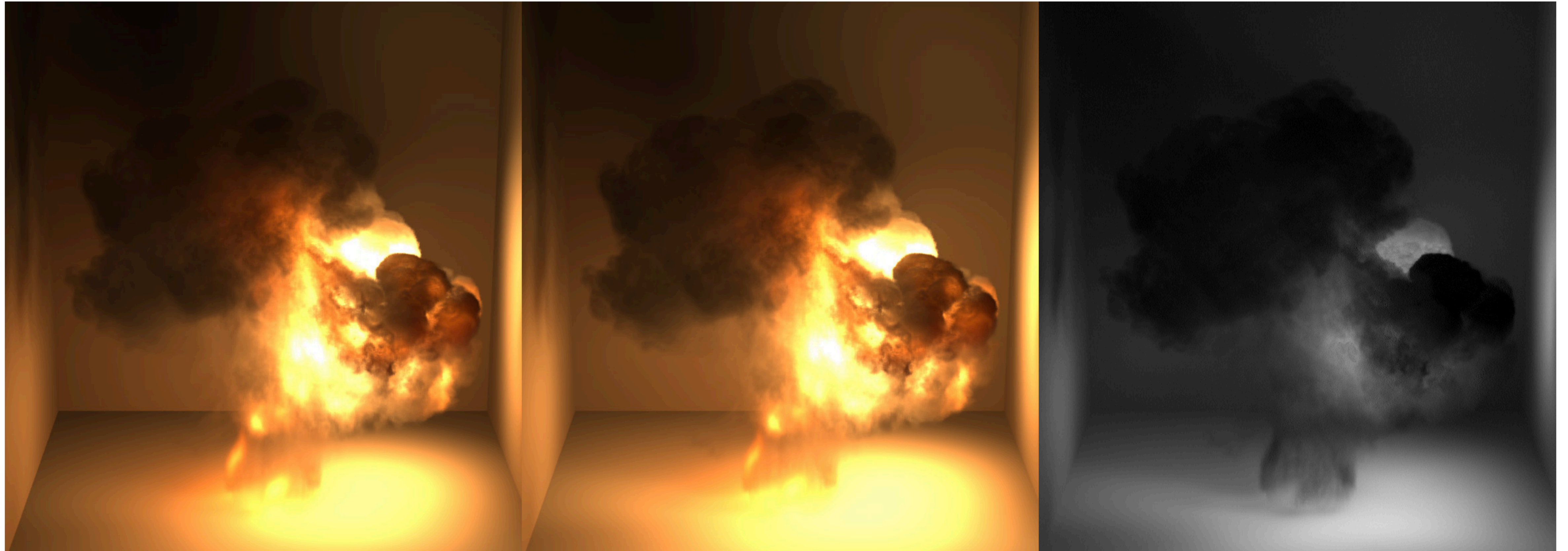


Shading

Shading a point:



Multiple Scattering



Single Scattering

Multiple Scattering

Luminance Diff. $\times 2$



Path Tracing



Lighting Grid Hierarchy



Path Tracing



Lighting Grid Hierarchy



Figure 1



Figure 1

Acknowledgements

We thank all the people who make their work available online which helped shape these slides.

Special thanks to Walter et al., Hasan et al., Carsten Dachsbacher et al., Jan Novak et al. for making their EG STAR Many-Light methods slides online, Can Yuksel and Cem Yuksel for making their slides and videos available online.

Scalable Realistic Rendering with Many-Light Methods [Dachsbacher et al. 2013]

Virtual Ray Lights for Rendering Scenes with Participating Media [Jan Novak et al. 2012]

LightCuts [Walter et al. 2005]

Stochastic LightCuts [Cem Yuksel 2019]