
Realistic Image Synthesis

- Perception-based Rendering
&
Advanced Displays-

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Outline

- **Perceptually based adaptive sampling algorithm**
- **Eye tracking driven rendering**
- **Binocular 3D displays**
- **Autostereoscopic (Glass-free 3D) Displays**
 - Parallax Barriers
 - Integral Imaging
 - Multi-layer displays
 - Holographic displays
- **Head-Mounted Displays with accommodation cues**

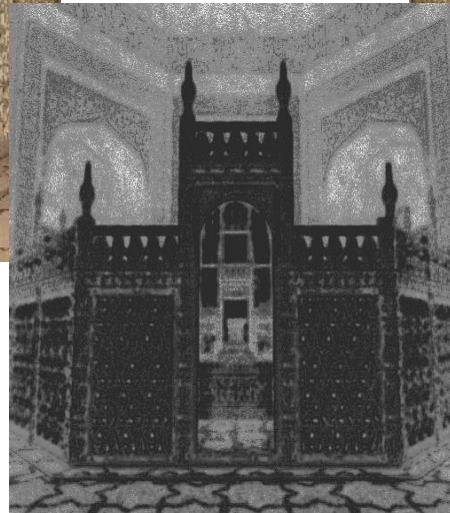
Perceptually Based Rendering

6% effort



physically
accurate

effort
distribution
(darker
regions -
less effort)



perceptually
accurate

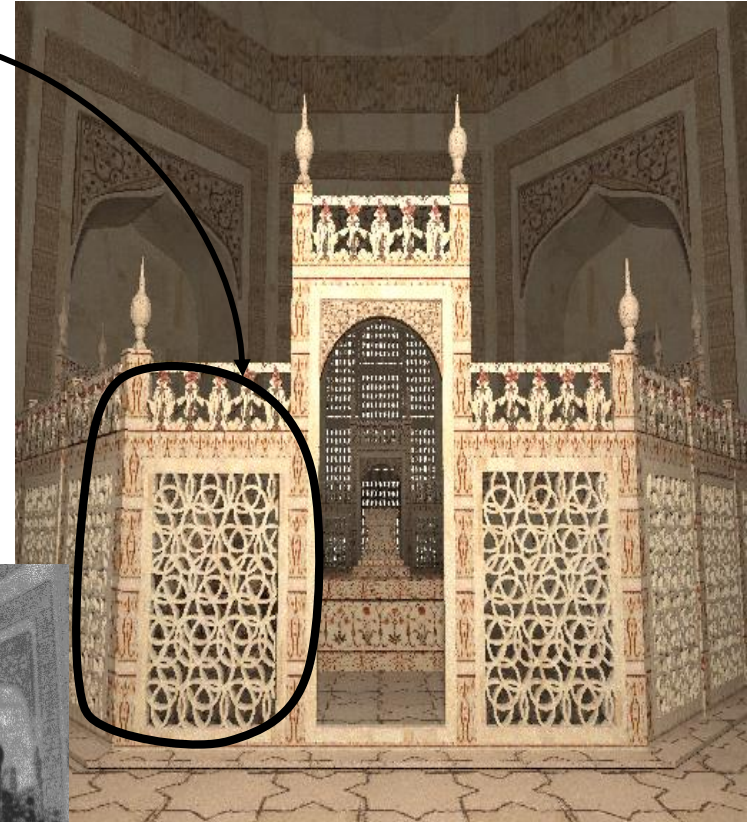
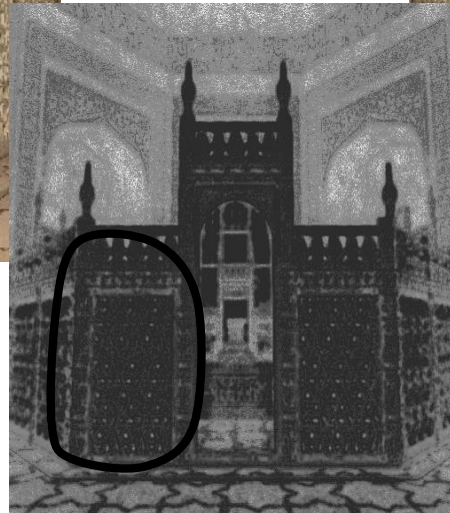
Perceptually Based Rendering

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perceptually
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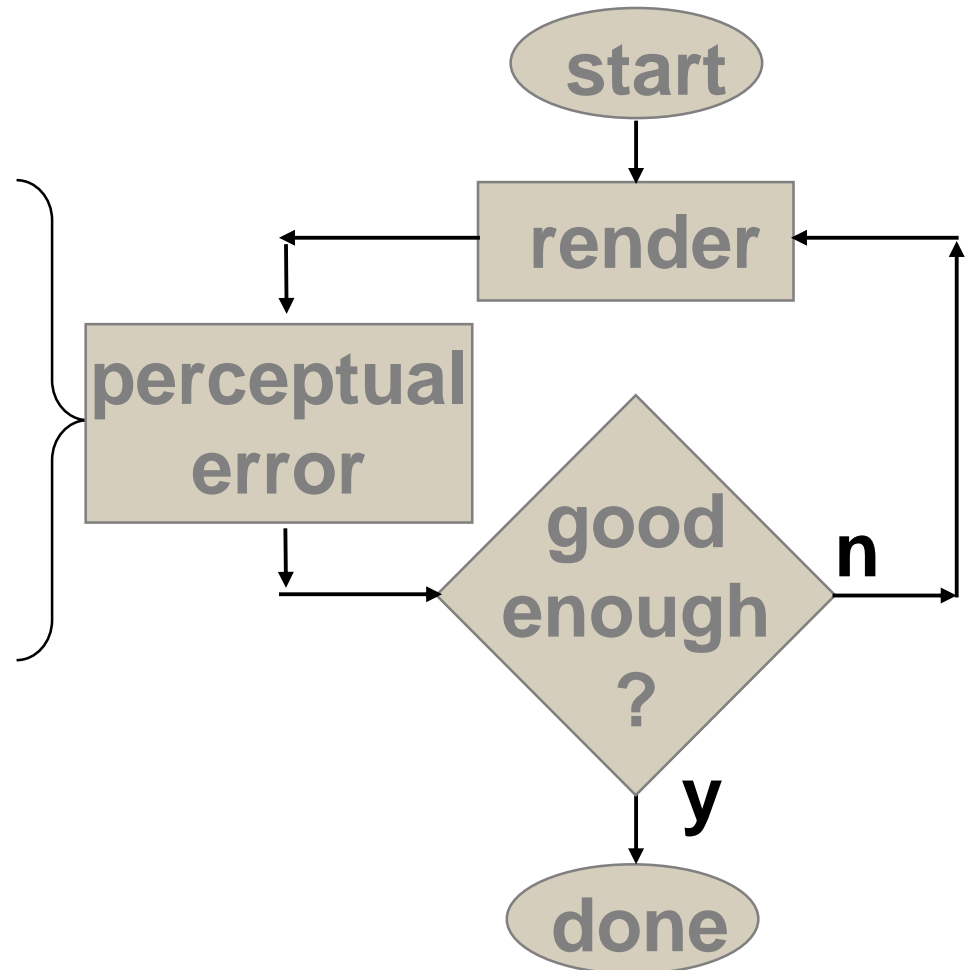
Perceptually Based Rendering

Traditional approach:

Pair of images to compare at each time step

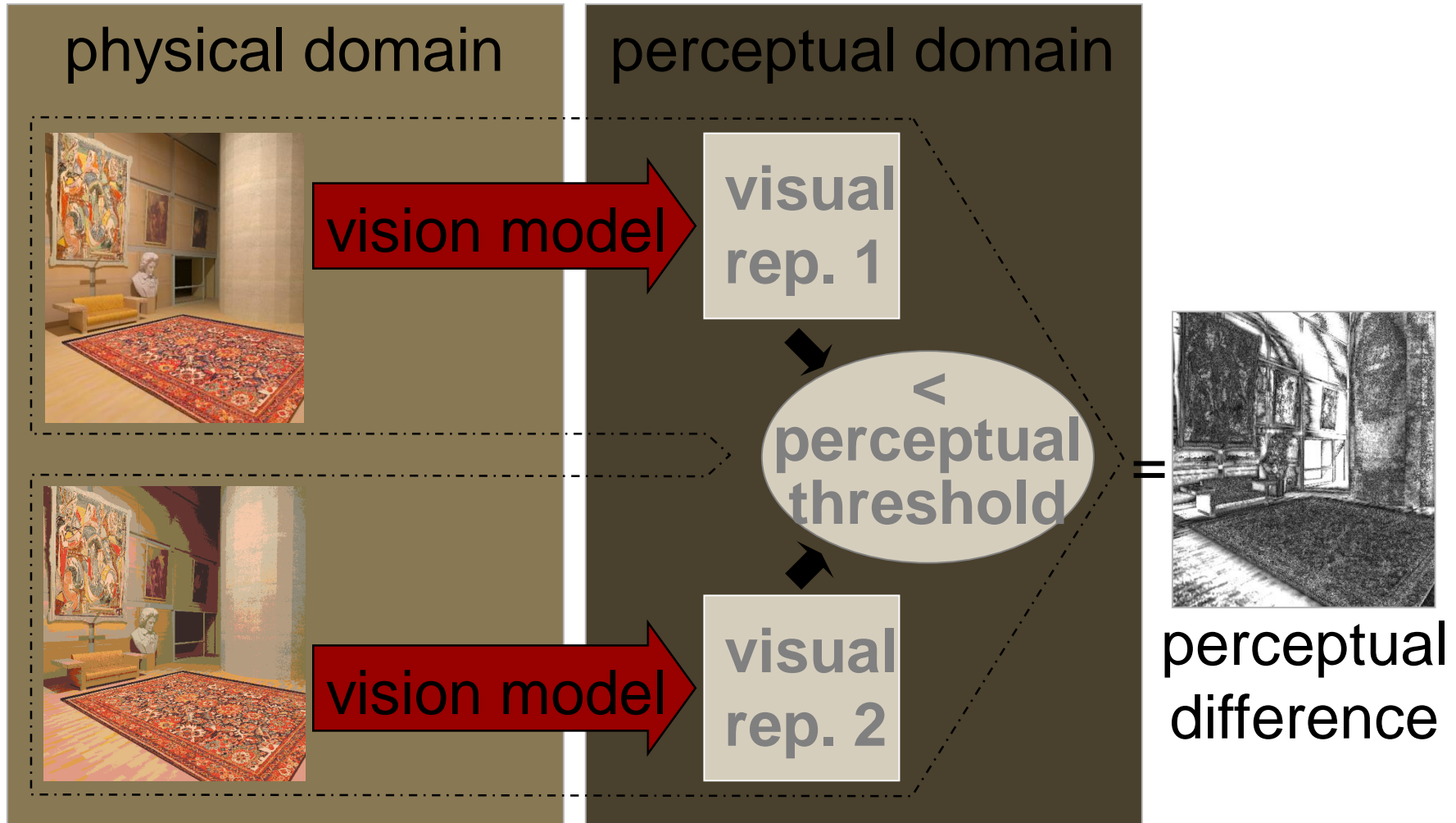
(a) intermediate images at consecutive time steps.

(b) upper and lower bound images at each time step.

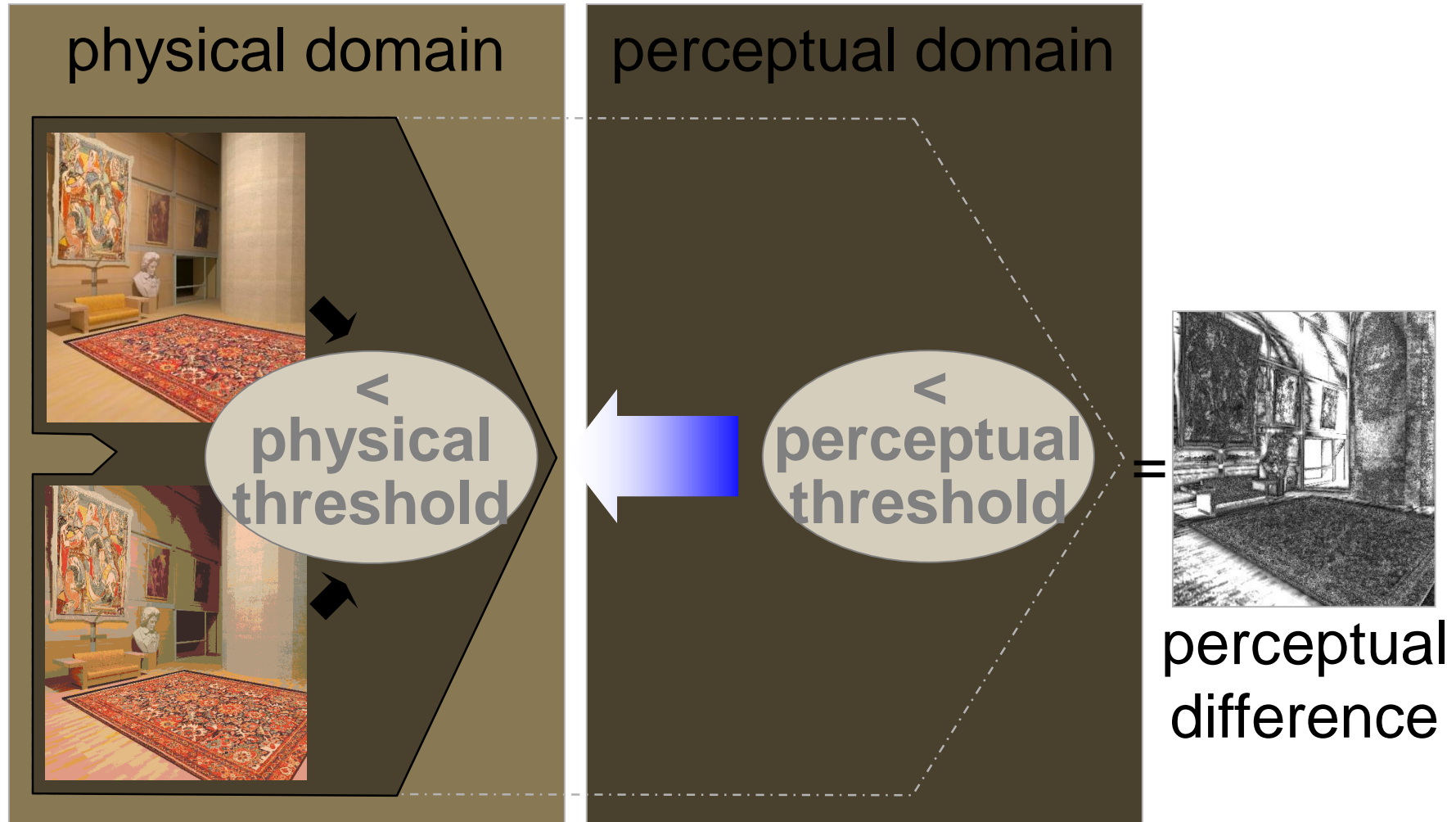


Perceptual Error Metric

Vision model - expensive



Perceptually Based Physical Error Metric



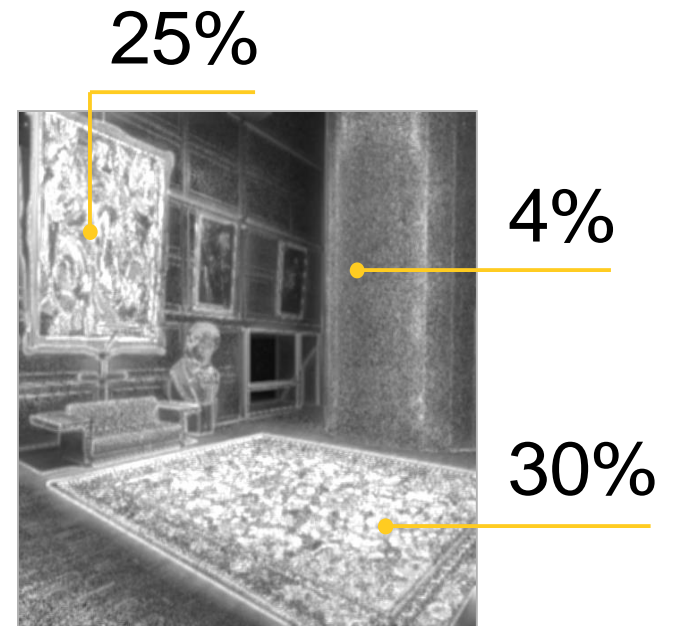
Physical Threshold Map

Predicted bounds of permissible luminance error



input image

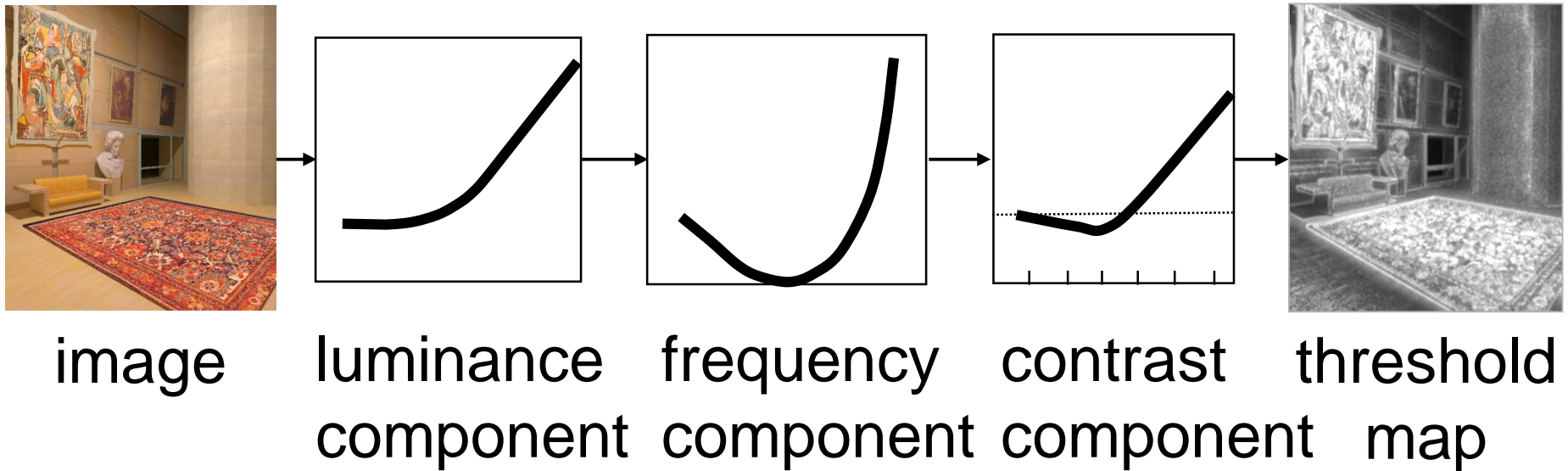
threshold
model



physical threshold
(brighter regions
- higher thresholds)

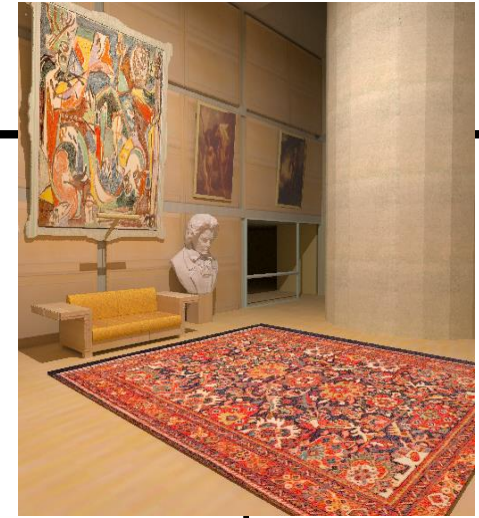
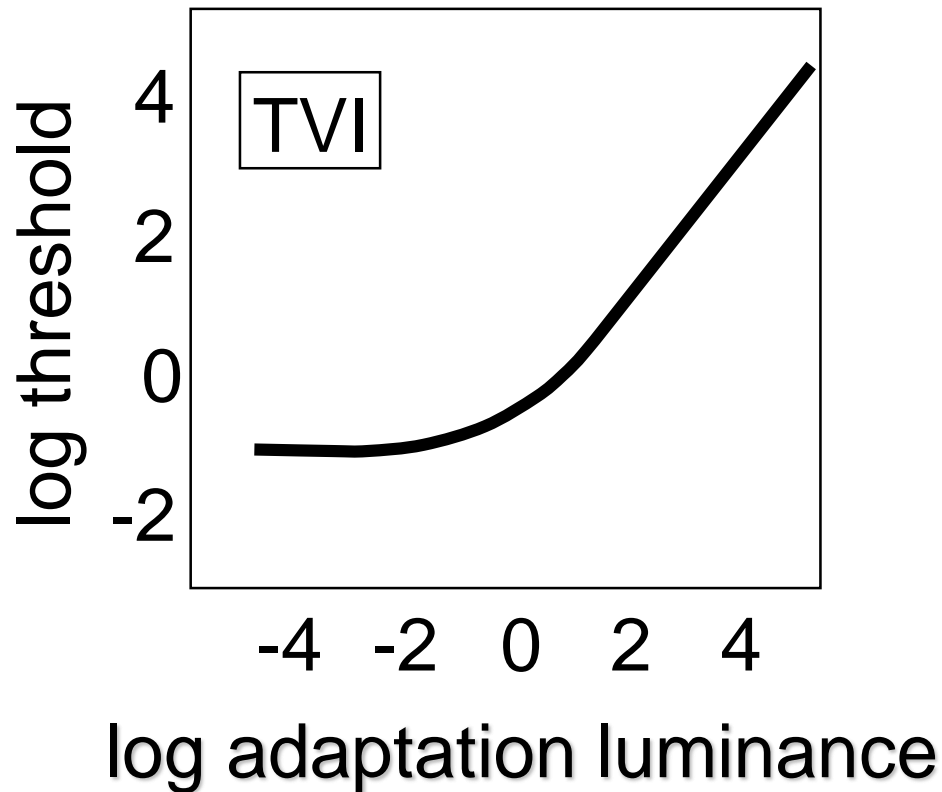
Threshold Model

Components



Threshold Model

1. Luminance component

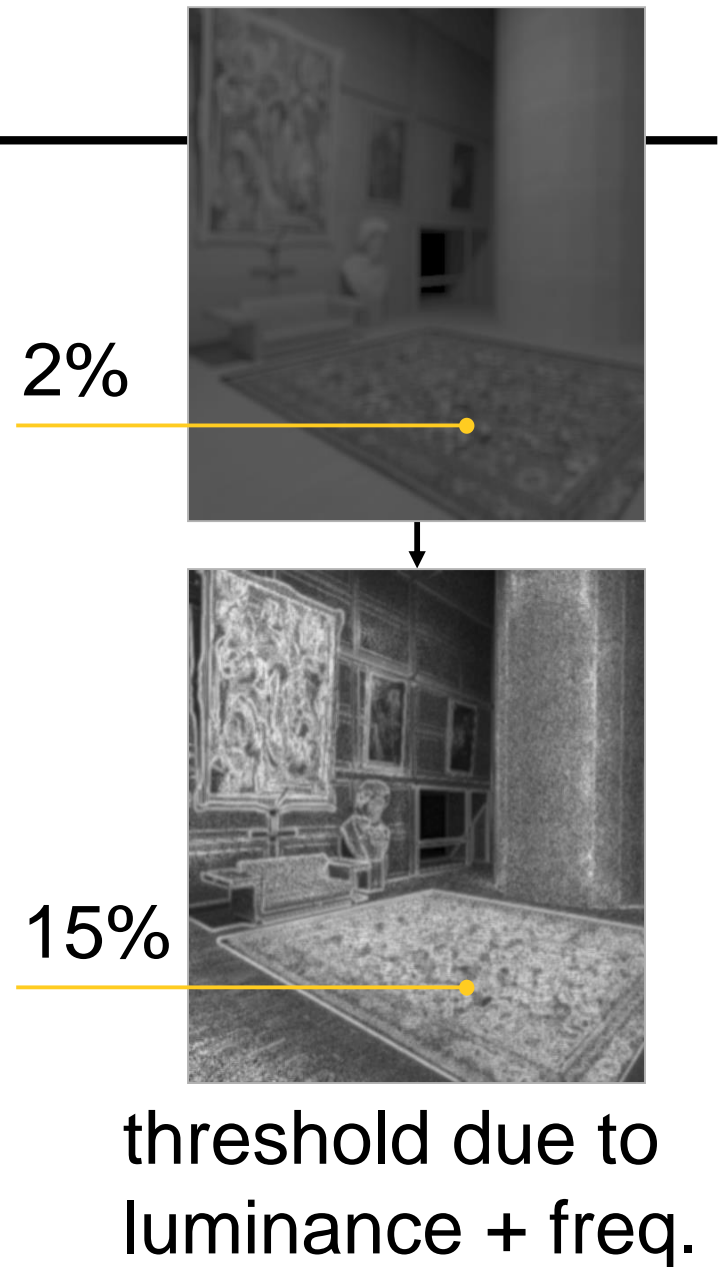
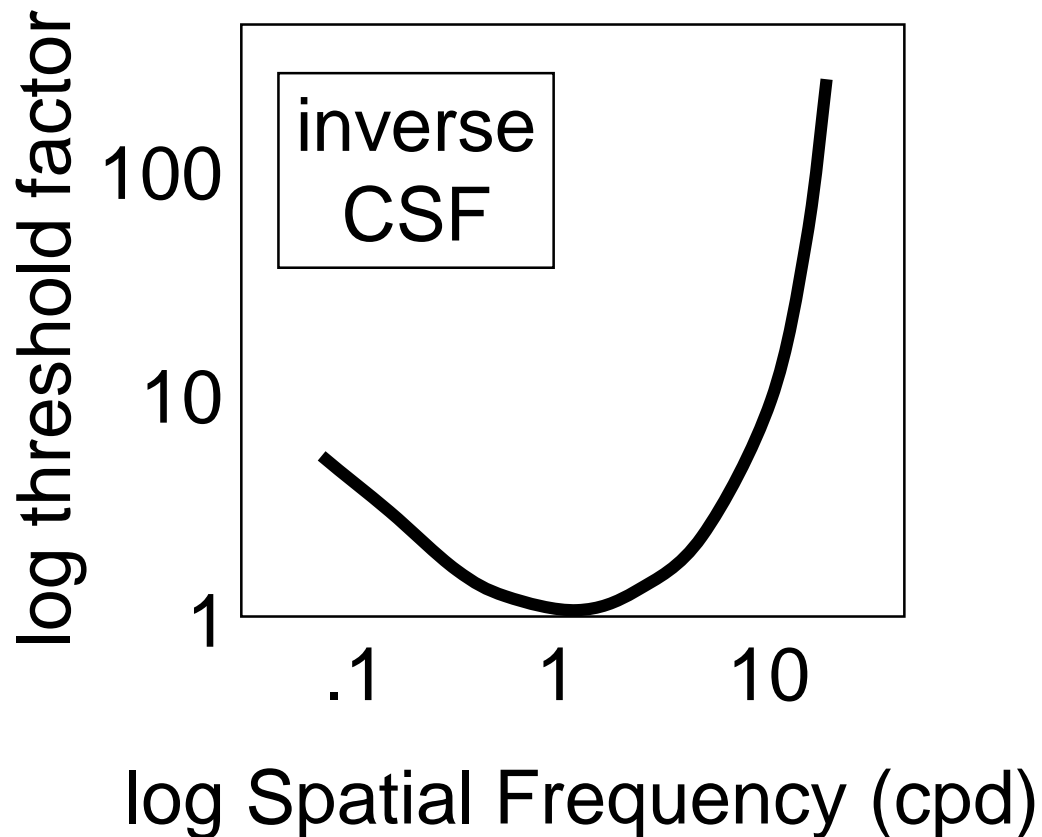


2%

threshold due to
luminance

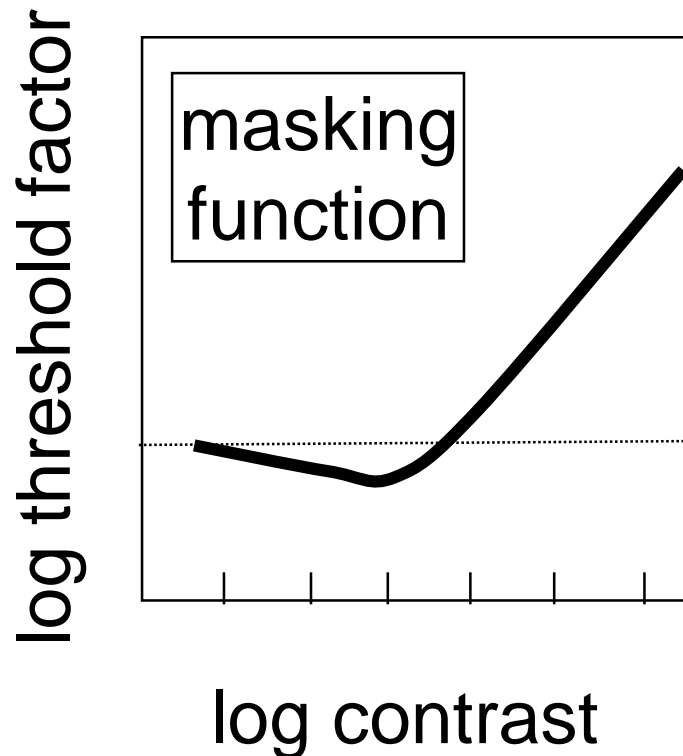
Threshold Model

2. Frequency component

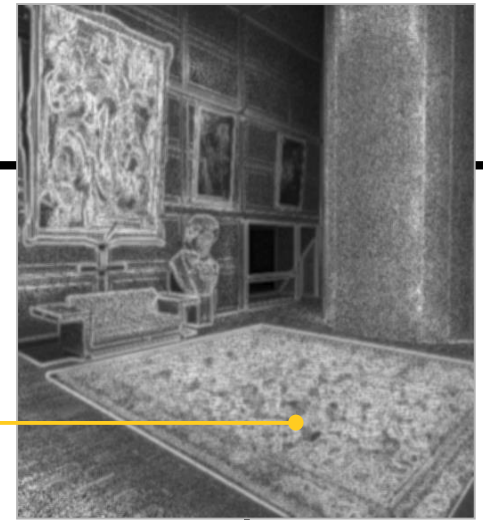


Threshold Model

3. Contrast component (visual masking)



15%



30%

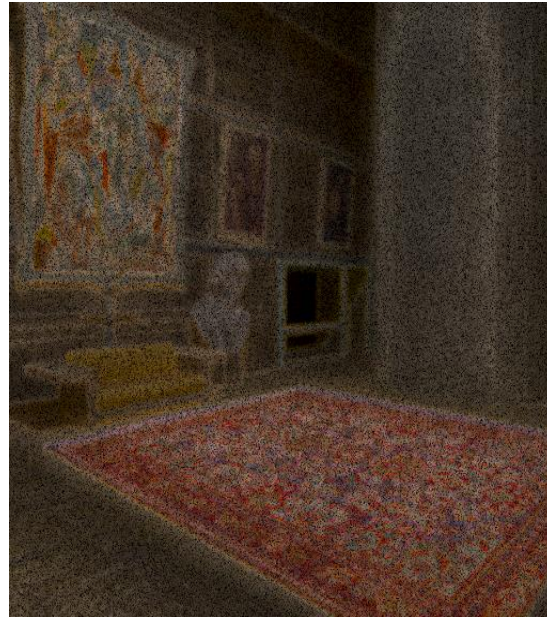


threshold due to
luminance + freq.
+ contrast

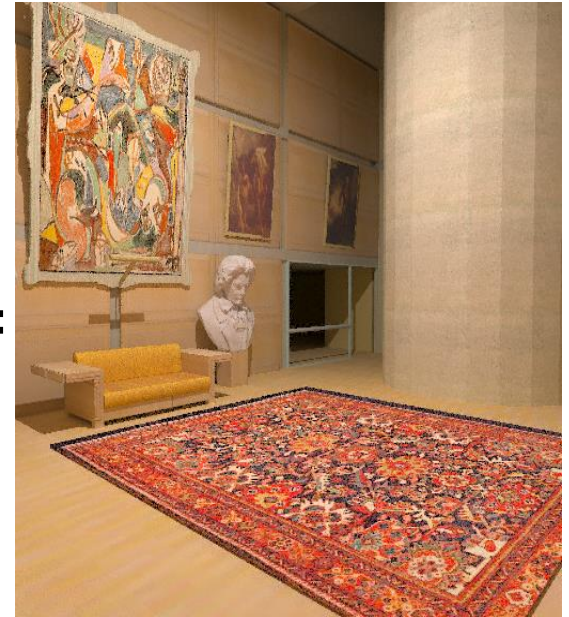
Validation



+



=

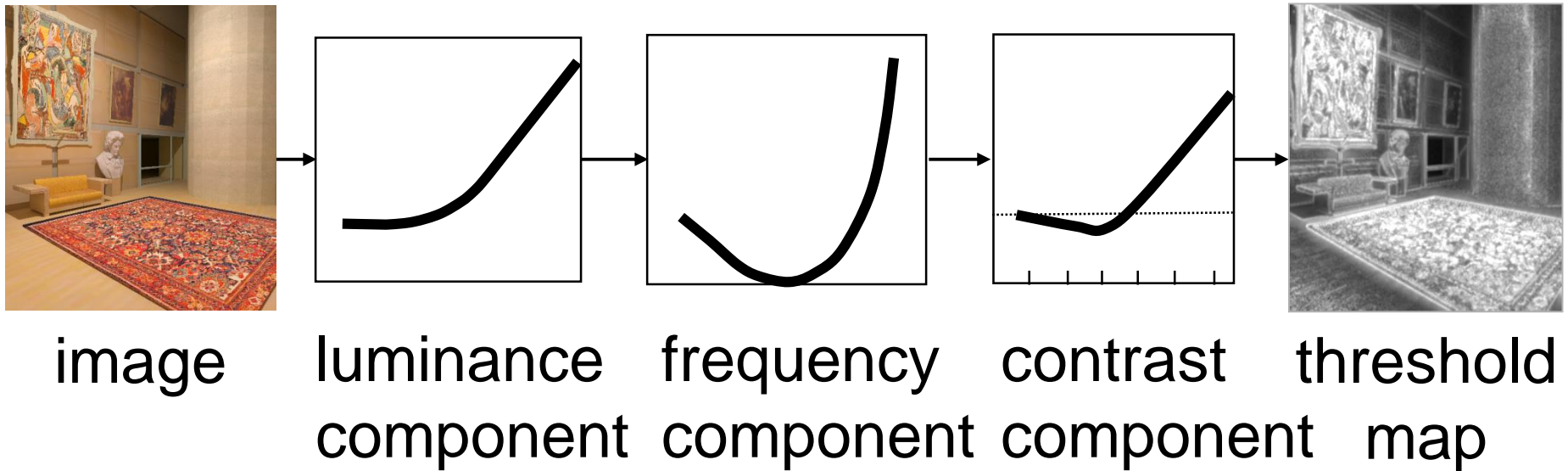


image

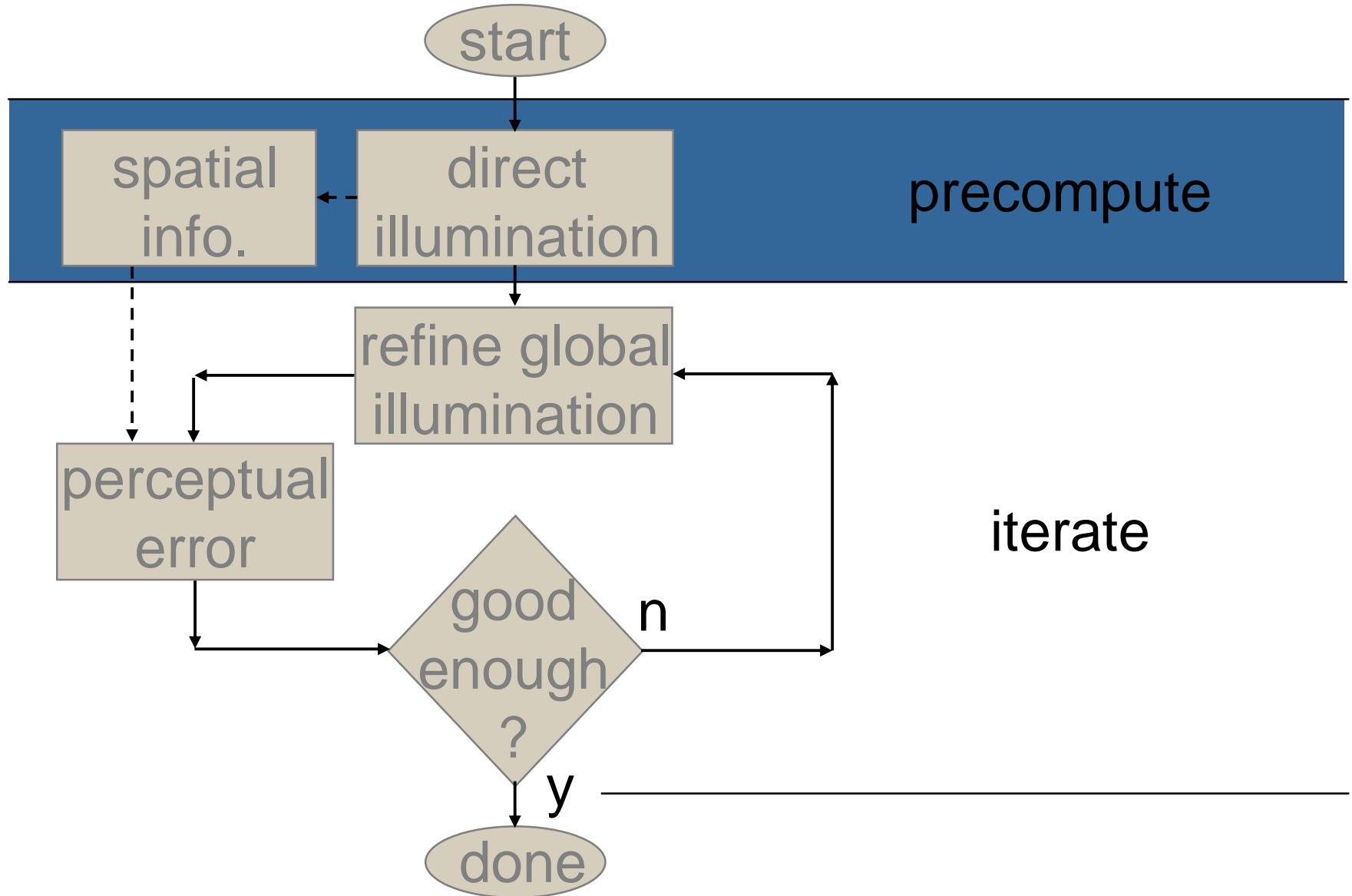
noise

image + noise

Threshold Model



Adaptive Rendering Algorithm



Results

5% effort



reference
solution

effort
distribution
(darker
regions -
less effort)



adaptive
solution

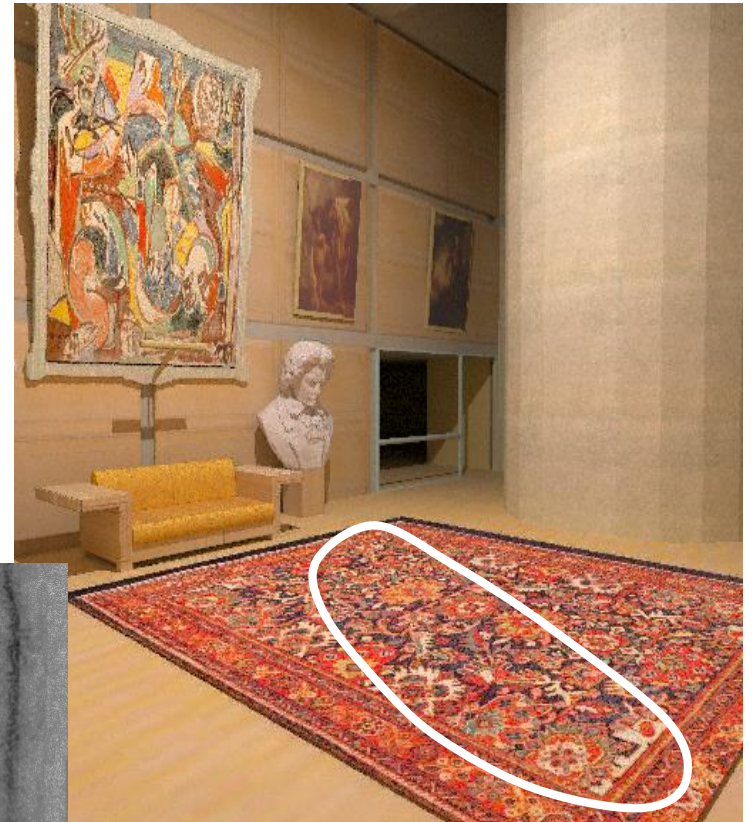
Results: Masking by Textures

5% effort



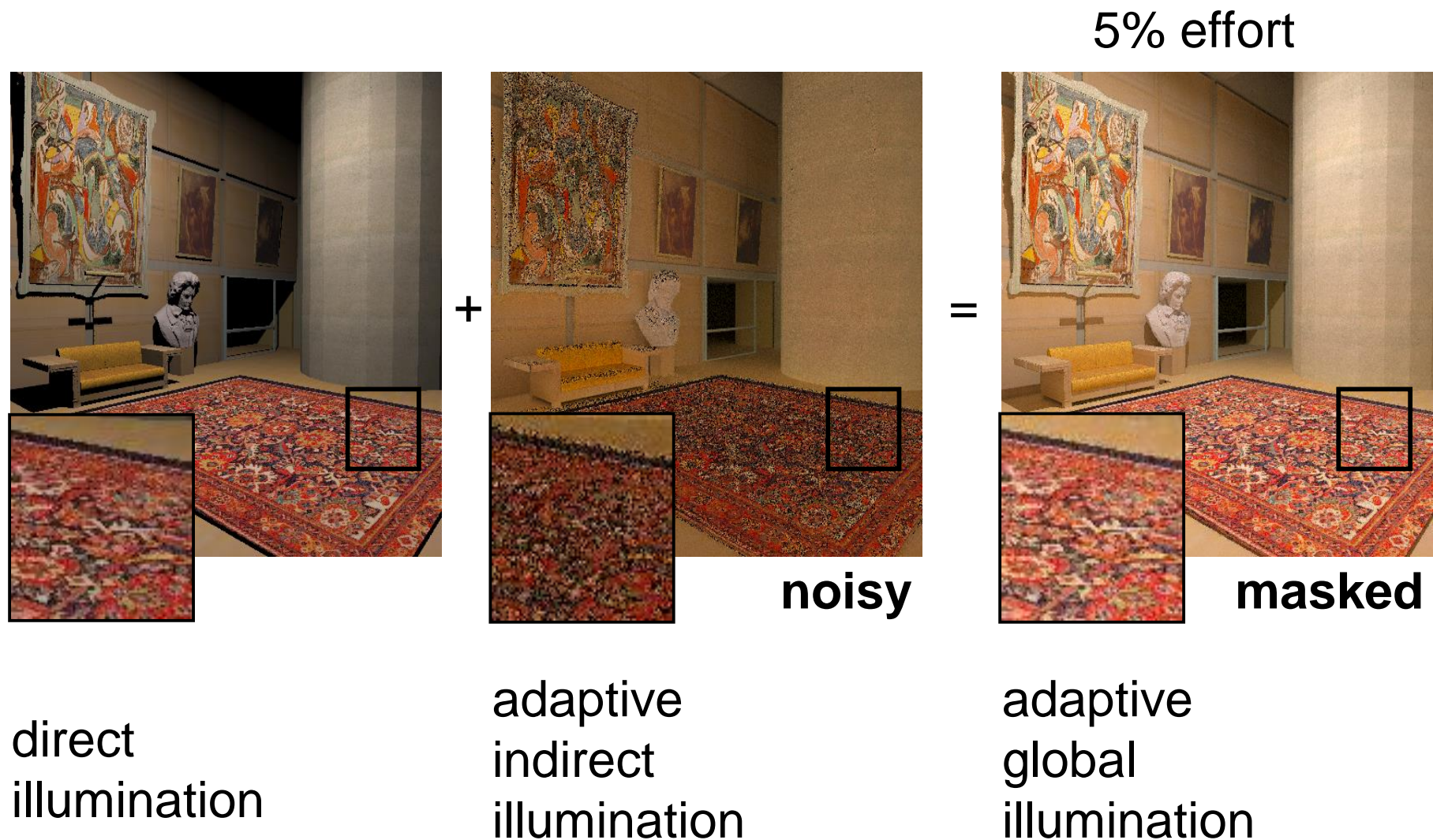
reference
solution

effort
distribution
(darker
regions -
less effort)



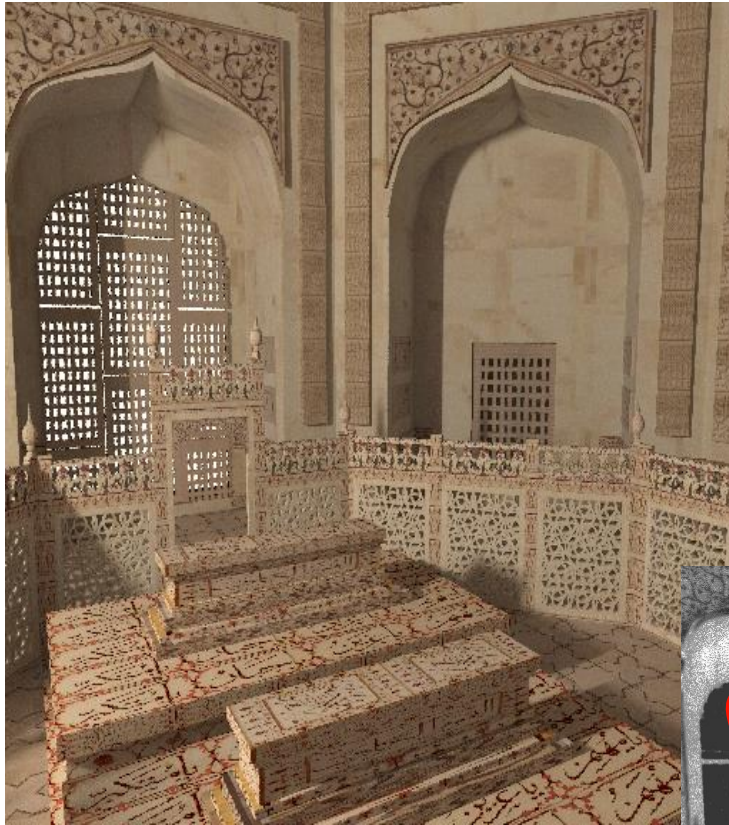
adaptive
solution

Results



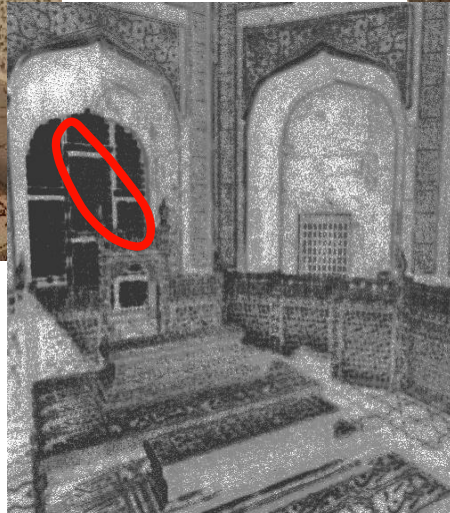
Results: Masking by Geometry

5% effort



reference
solution

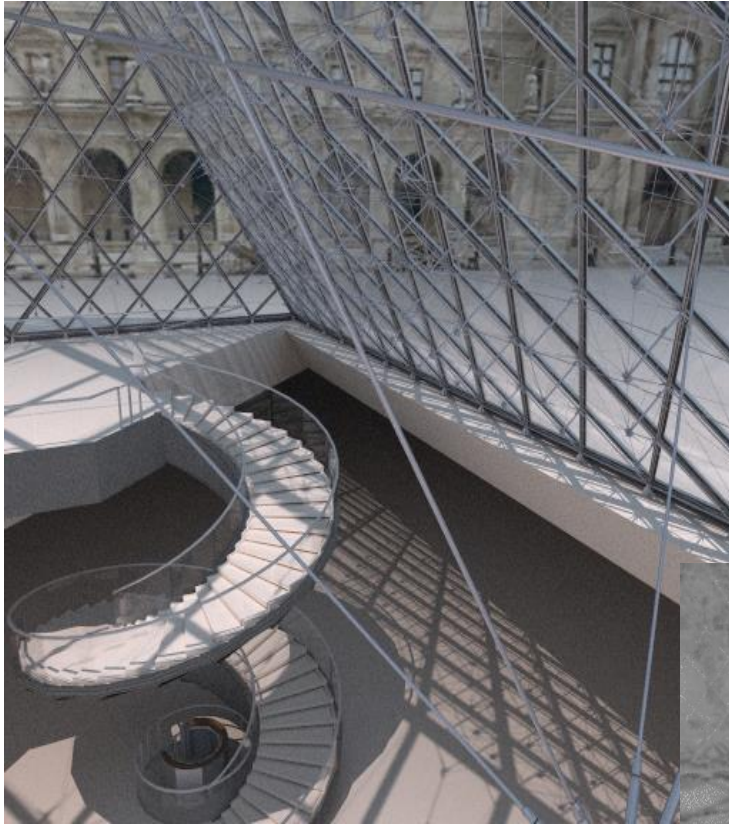
effort
distribution
(darker
regions -
less effort)



adaptive
solution

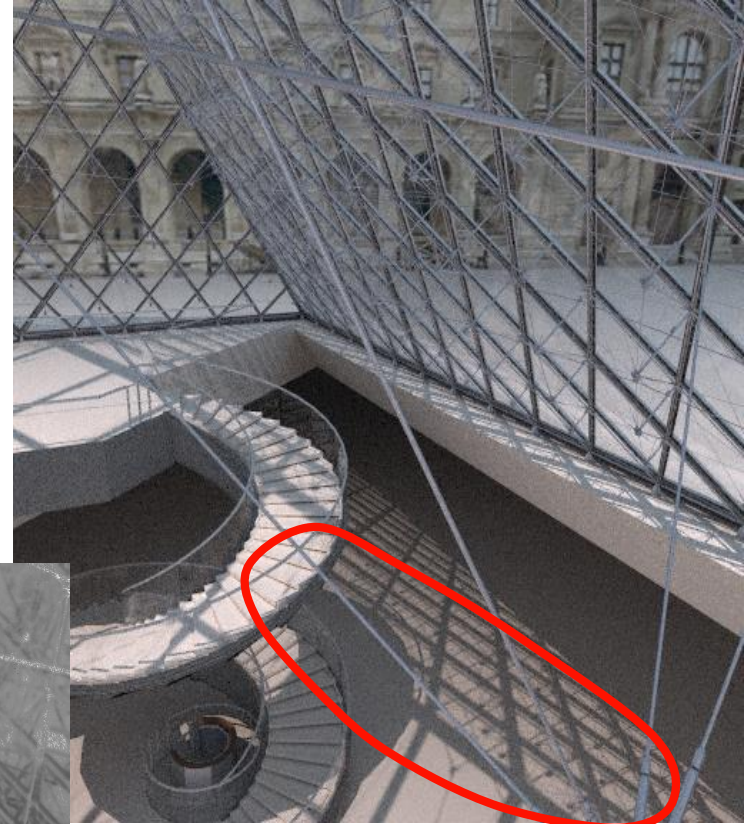
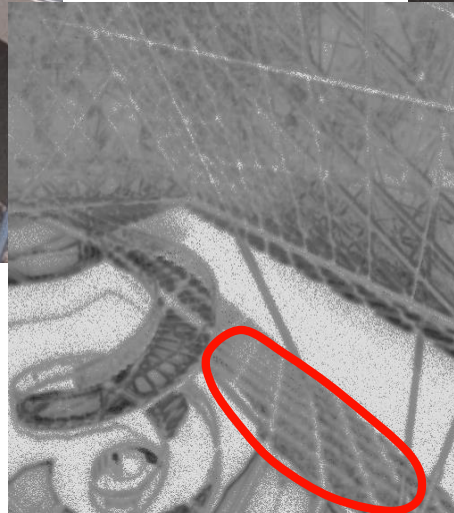
Results: Masking by Shadows

6% effort



reference
solution

effort
distribution
(darker
regions -
less effort)



adaptive
solution

Eye Tracking - Motivation

1. Improving computational efficiency

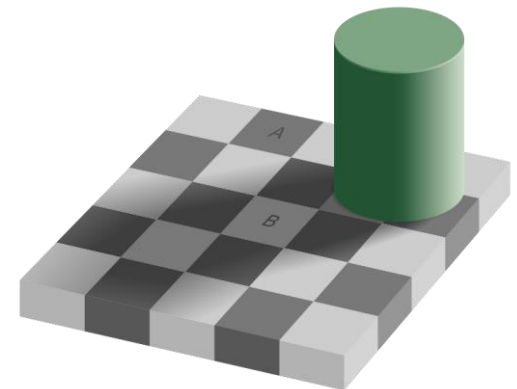
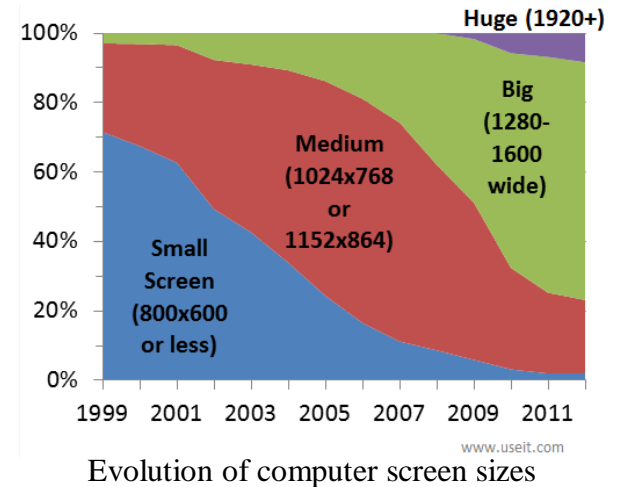
- There is a trend towards higher resolution displays
→ Higher computational requirement for 3D rendering
- Only a fraction of pixels is consciously attended and perceived in the full-resolution

2. Improving realism

- Eye is always focused on the screen plane; nevertheless, it is possible to simulate Depth-of-Field (DoF) effect by artificially blurring out-of-focus regions according to the gaze location

3. Improve perceived quality

- Human Visual System (HVS) has local adaptation property
- Perception of luminance, contrast and color are not absolute and highly dependent on both spatial and temporal neighborhood of the gaze location

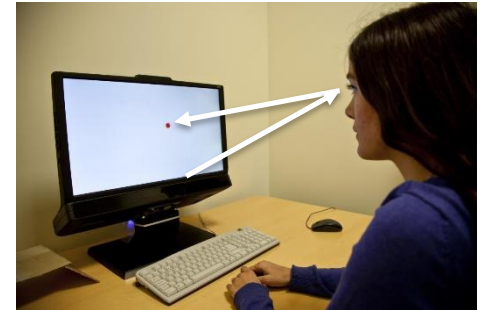
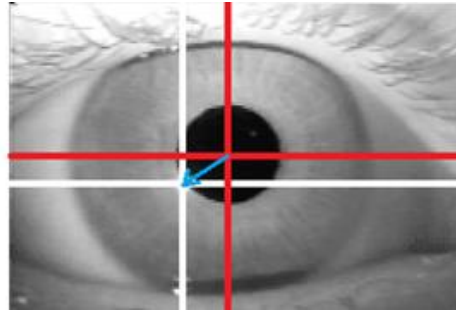
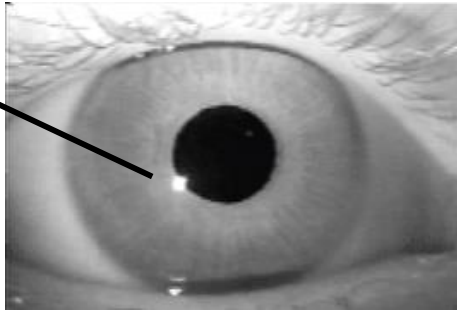


Checker shadow illusion

Eye Tracking

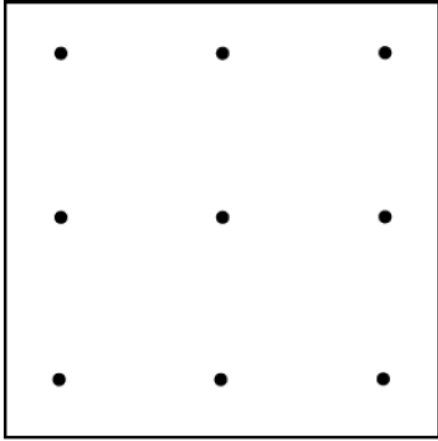
- **Basic Technology:**

Corneal
Reflection
(also known
as “glint” or
“1st Purkinje
Reflection”)

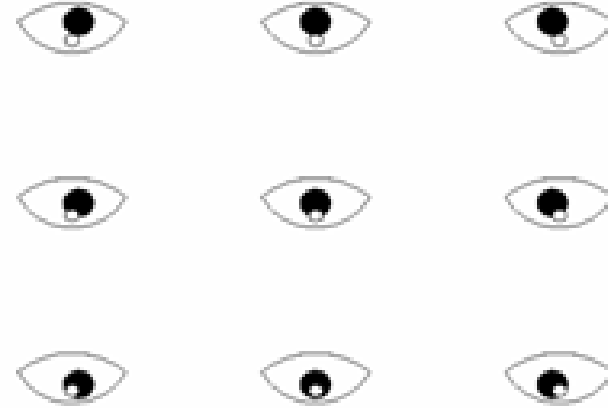


- **Eye trackers mostly operate using infrared imaging technology**
- **Once the pupil is detected the vector between the center of the pupil and the corneal reflection of the infrared light source is translated into the gaze location on screen coordinates**
- **Requires calibration at the beginning**

Eye Tracking



Sample 9-point calibration grid



Relative positions of the pupil and the corneal reflection

- **Individual calibration is necessary for each observer**
- **Relative location of the corneal reflection and the pupil is different among the population due to**
 - Difference in eye ball radius and shape
 - Eye-glasses

Images adapted from <http://wiki.cogain.org>

Eye Tracking



Chin-rest (EyeLink 1000/2000)



Glasses (SMI Eye Tracking Glasses)



Head-mounted displays (Oculus Rift)

- **Some of the other types of setups are used only for specific applications since they may be highly intrusive (e.g. chin-rest eye trackers) and not comfortable for the end-users in practice**
- **Head-mounted displays (HMD) offer 3D stereo and augmented reality capabilities in addition to eye tracking**

Types of Eye Motion

Type	Duration (ms)	Amplitude (1° = 60')	Velocity
Fixation	200-300	-	-
<i>Microsaccade</i>	10-30	10-40'	15-50°/s
<i>Tremor</i>	-	<1'	20'/sec
<i>Drift</i>	200-1000	1-60'	6-25'/s
Saccade	30-80	4-20°	30-500°/s
Glissade	10-40	0.5-2°	20-140°/s
Smooth Pursuit	variable	variable	10-30°/s

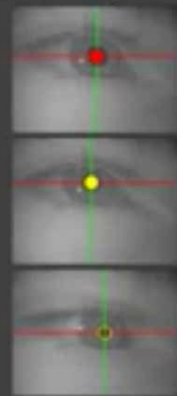
- While the mechanisms are not exactly known, it is thought that the brain performs visual suppression and compensation during **saccades** and smooth pursuits against motion blur on the retina.

Reference: Holmqvist, K., Nyström, M., Andersson, R., Dewhurst, R., Jarodzka, H., & Van de Weijer, J. (2011). Eye tracking: A comprehensive guide to methods and measures. OUP Oxford.

Eye Tracking in Action

Bayesian Identification of Fixations, Saccades, and Smooth Pursuits

An example of I-BDT classification



Fixation = Solid Red Circle

Saccade = Solid Yellow Circle

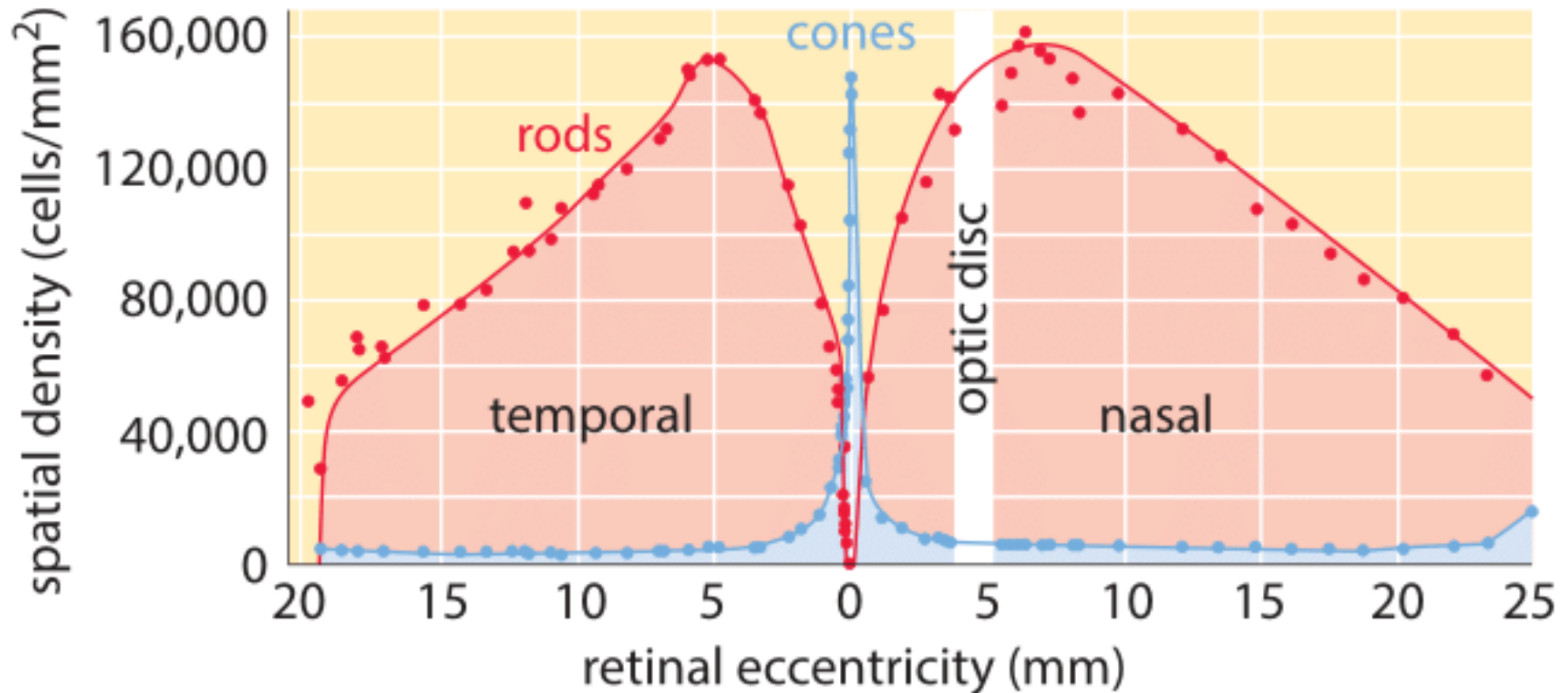
Smooth Pursuit = Hollow Yellow Circle

Original framerate: 30 Hz
Playback framerate: 10 Hz

Adapted from T. Santini, W. Fuhl, T. Kübler, and E. Kasneci. Bayesian Identification of Fixations, Saccades, and Smooth Pursuits ACM Symposium on Eye Tracking Research & Applications, ETRA 2016.

Visual Acuity

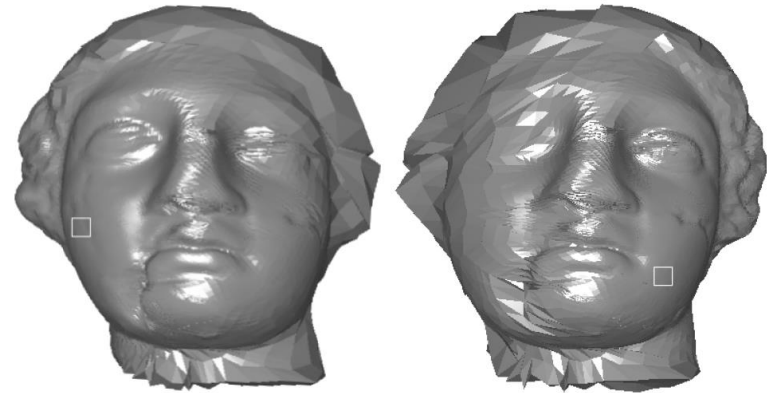
- **Distribution of photoreceptor cells in the retina**



Adapted from R. W. Rodieck, *The First Steps of Seeing*, Sinauer Associates, 1998.

Level-of-Detail Rendering

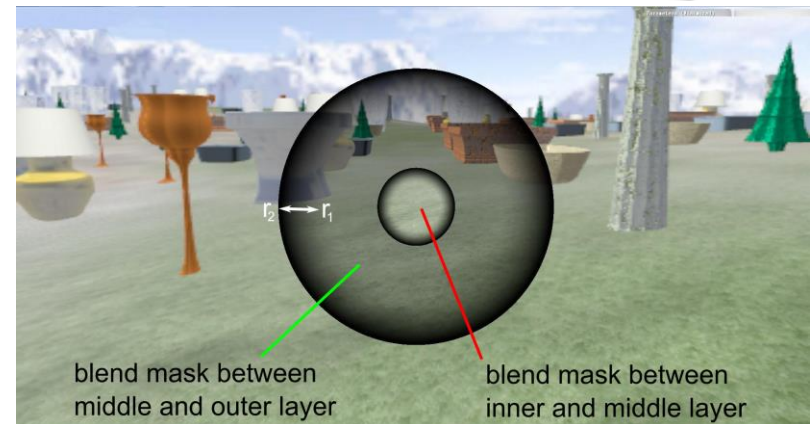
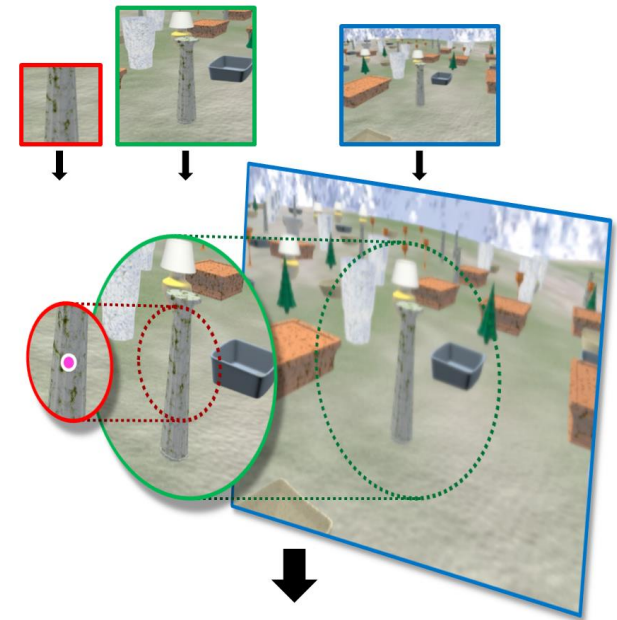
- **The model resolution may be degraded according to the visual angle and the acuity of HVS at the given angle**
 - Mesh structure of the model is partitioned into tiles using Voronoi diagram
 - Tiles are mapped to planar polygons
 - Remeshing into multiresolution form



Adapted from Murphy, Hunter, and Andrew T. Duchowski. "Gaze-contingent level of detail rendering." EuroGraphics 2001 (2001).

Foveated 3D Graphics

- Screen-based (in contrast to model-based methods)
- Human eye has full acuity in around 5° foveal region
- The efficiency of image generation can be improved by maintaining high image resolution only around the gaze location
- Using 60Hz monitor and Tobii X50 eye tracker with 50Hz sampling frequency and 35ms latency caused artifacts for the observer
- Results using 120Hz monitor and Tobii TX300 with 300Hz sampling frequency and 10ms latency were tolerable



Foveated 3D Graphics

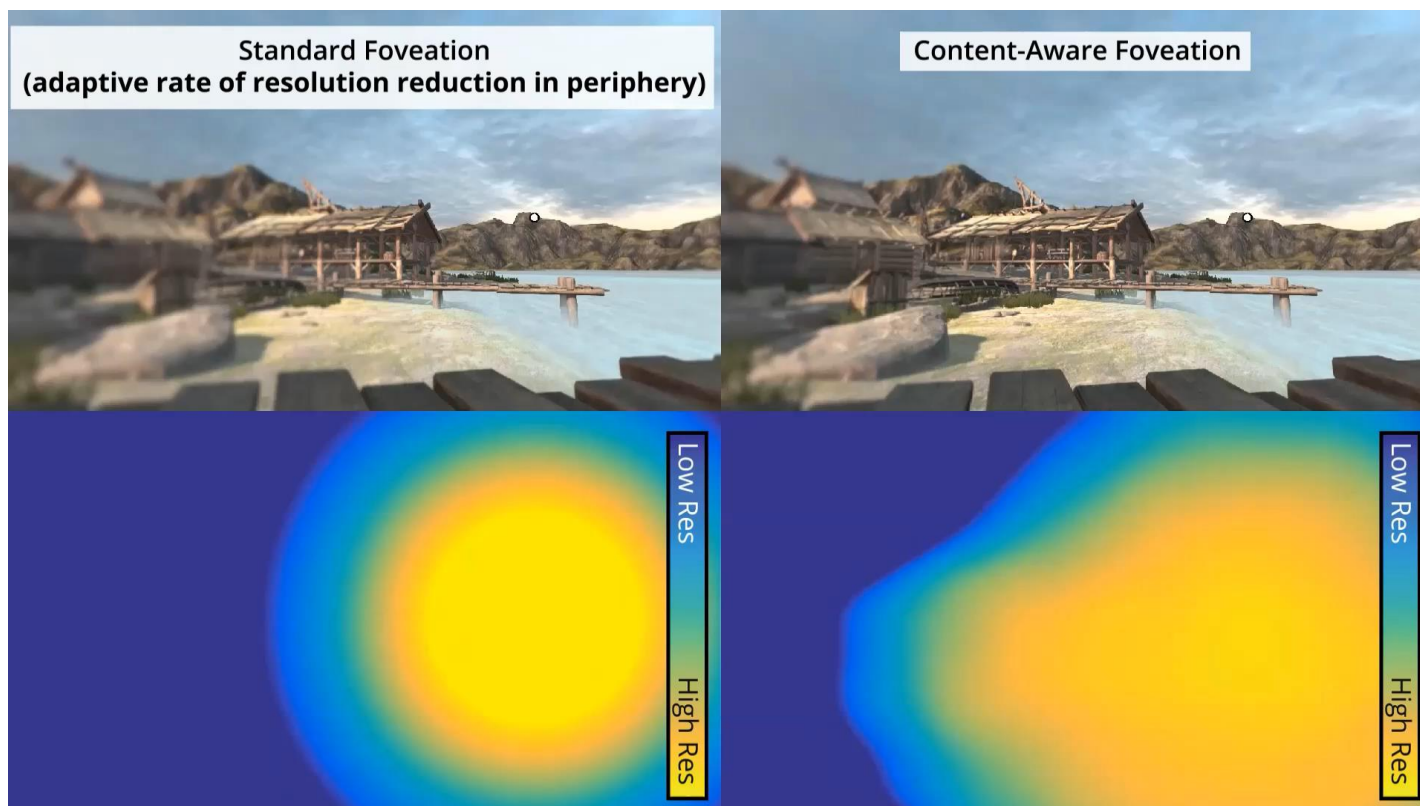


Video adapted from <http://research.microsoft.com>

Luminance-Contrast-Aware Foveated Rendering



Luminance-Contrast-Aware Foveated Rendering



Effect of Depth-of-Field

- Improves the rendering realism and enhances the depth perception



(a) Image focused on objects at shallow depth (flower)



(b) Image focused on objects at large depth (Main Quad)



(c) Image with everything in focus



Images adapted from Gupta, Kushagr, and Suleman Kazi, "Gaze Contingent Depth of Field Display", 2016. Video adapted from Mantiuk, Radoslaw, Bartosz Bazyluk, and Rafal K. Mantiuk. "Gaze-driven Object Tracking for Real Time Rendering." Computer Graphics Forum. Vol. 32. No. 2pt2. Blackwell Publishing Ltd, 2013.

Depth-of-Field Rendering

- **Circle of Confusion :**

$$CoC = a \cdot \left| \frac{f}{d_0 - f} \right| \cdot \left| 1 - \frac{d_0}{d_p} \right|$$

a - diameter of the lens aperture

f - focal length of the lens

d_0 - distance between the focal plane and lens

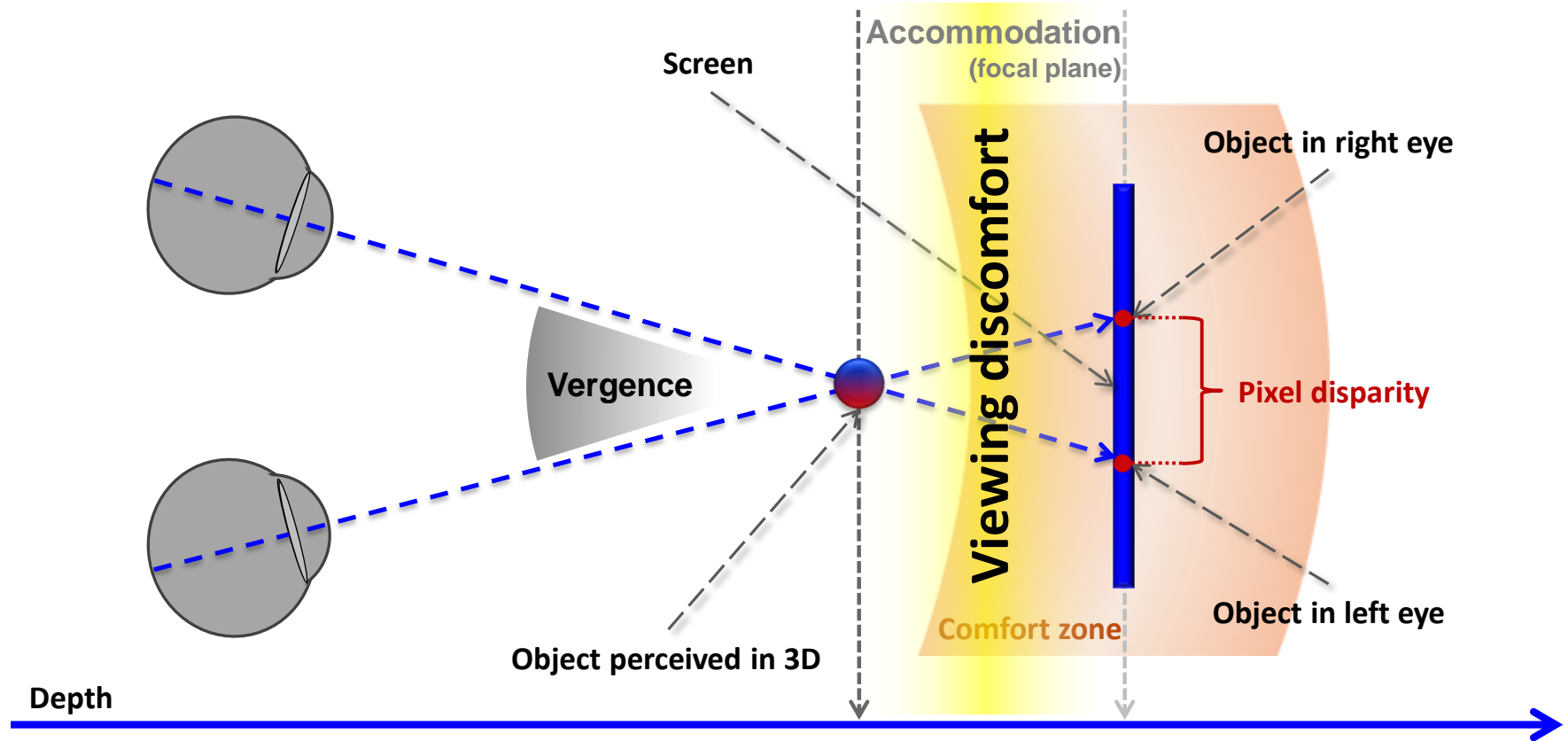
d_p - distance from an object to the lens

- d_p is obtained from reverse mapping of the z-buffer
- **Addresses the artifacts due to the depth discontinuity near object boundaries by spreading the blur outside the object boundary**



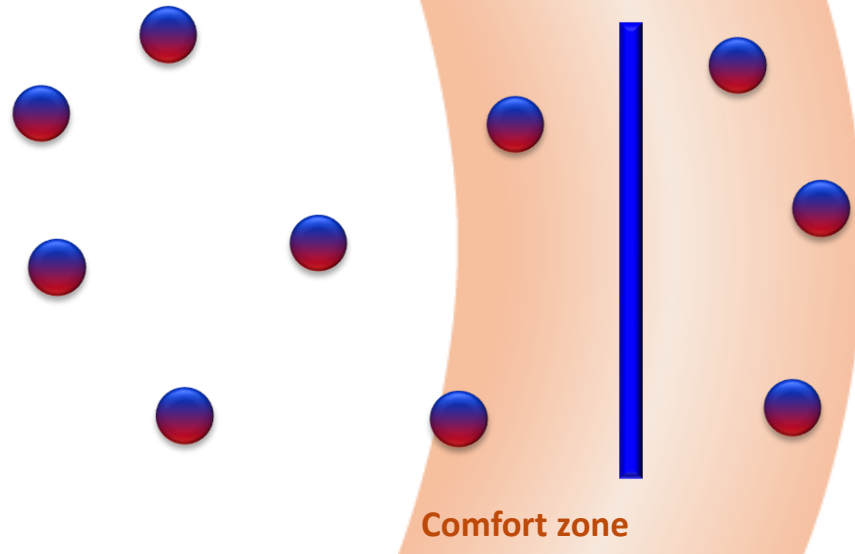
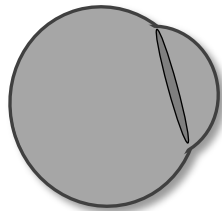
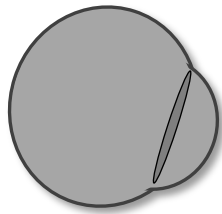
Vergence-accommodation Conflict

Stereo 3D: Binocular Disparity



Vergence-accommodation Conflict

Depth Manipulation



~~Scene manipulation~~
Viewing discomfort → **Viewing comfort**

Vergence-accommodation Conflict

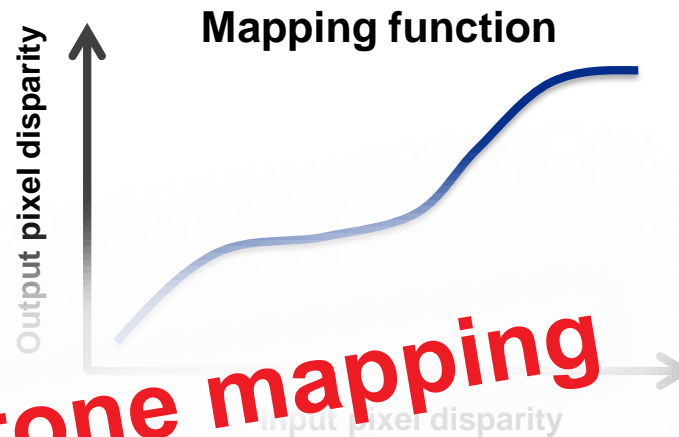
Depth Manipulation



Pixel disparity map



Modified pixel disparity



Similar to tone mapping

Function:

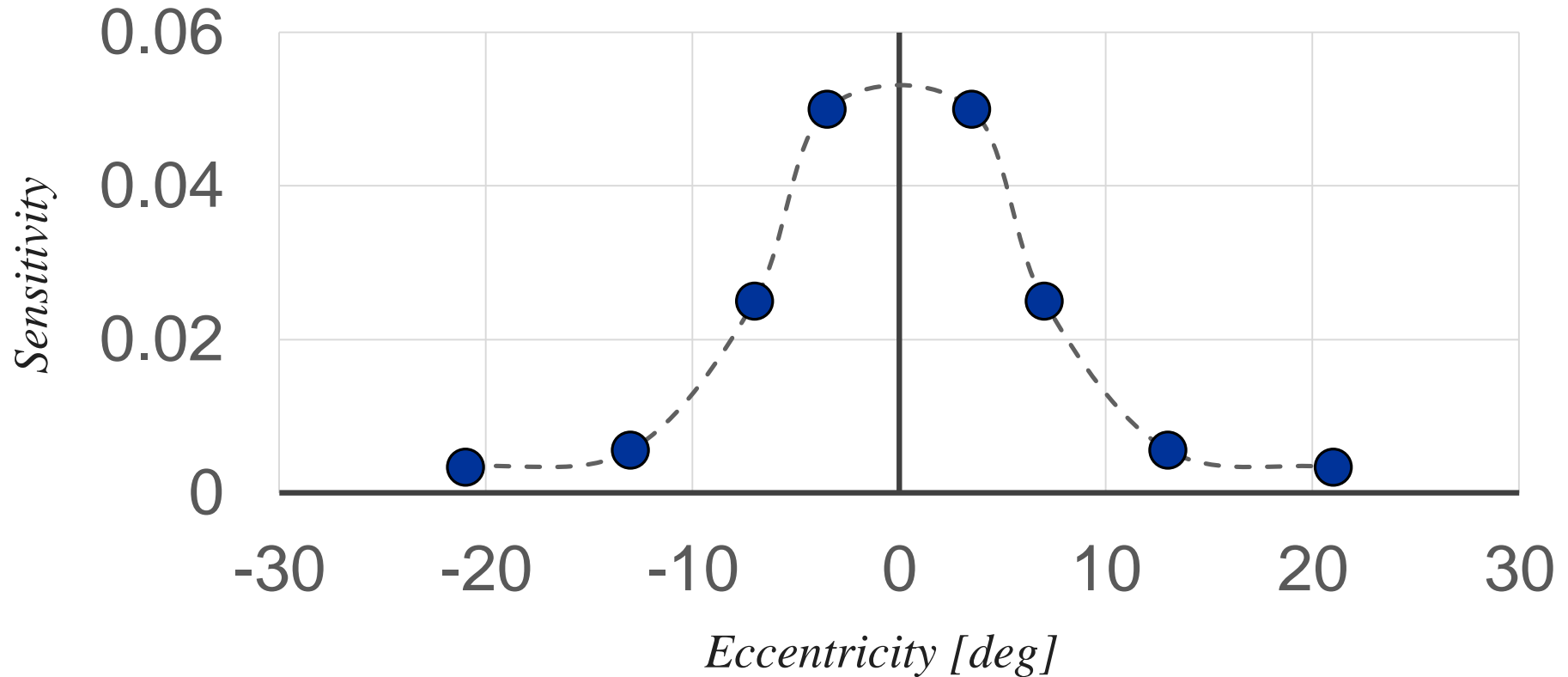
- Linear
- Logarithmic
- Content dependent

Other possibilities:

- Gradient domain
- Local operators

“Nonlinear Disparity Mapping for Stereoscopic 3D” [Lang et al. 2010]

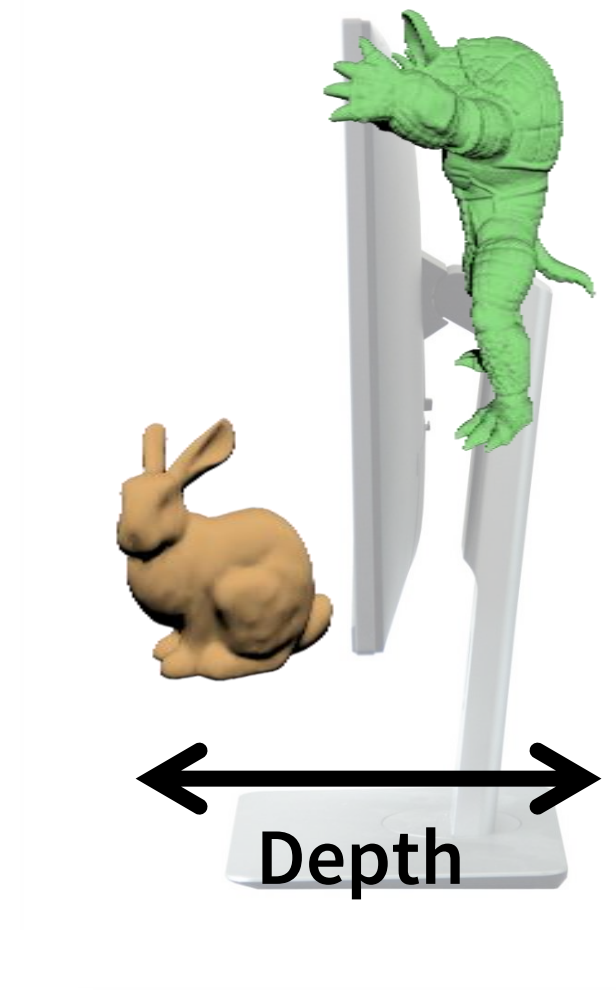
Disparity Perception (Stereo 3D)



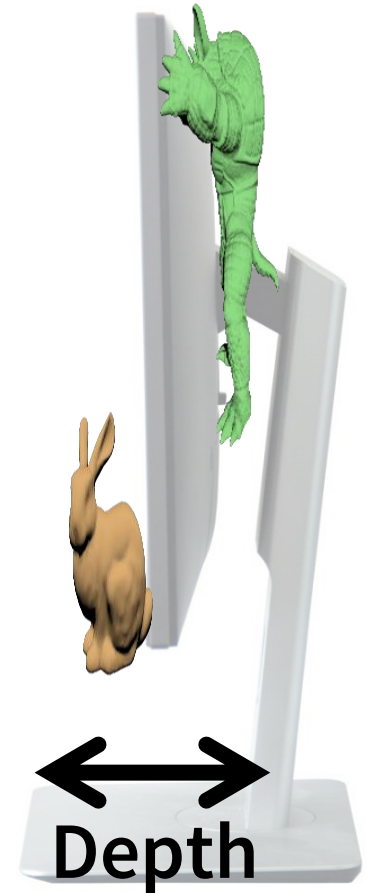
Replotted from Figure 3 of Simon J.D Prince, Brian J Rogers

Sensitivity to disparity corrugations in peripheral vision, Vision Research, Volume 38, Issue 17, September 1998

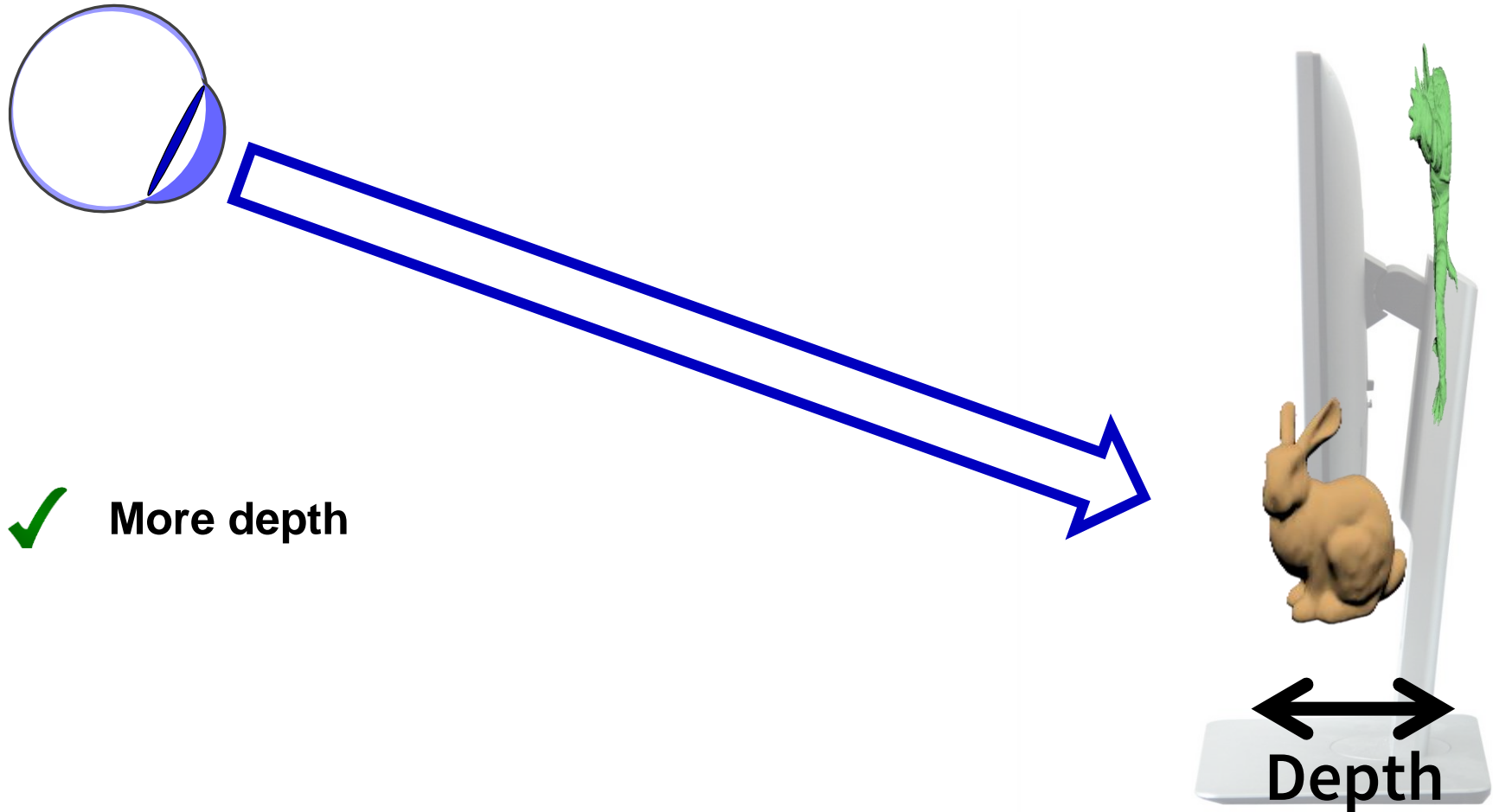
Vergence-accommodation Conflict



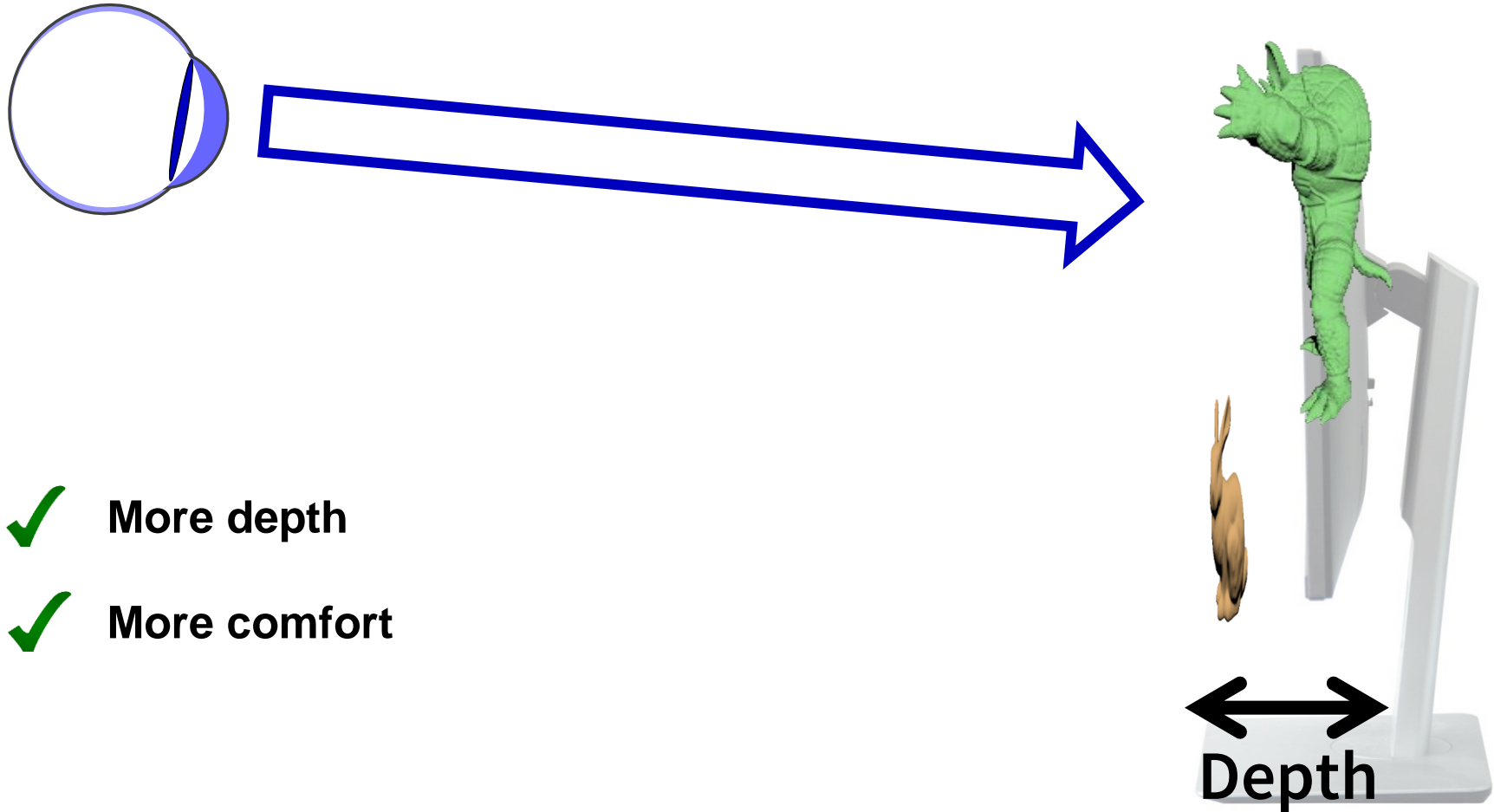
Vergence-accommodation Conflict



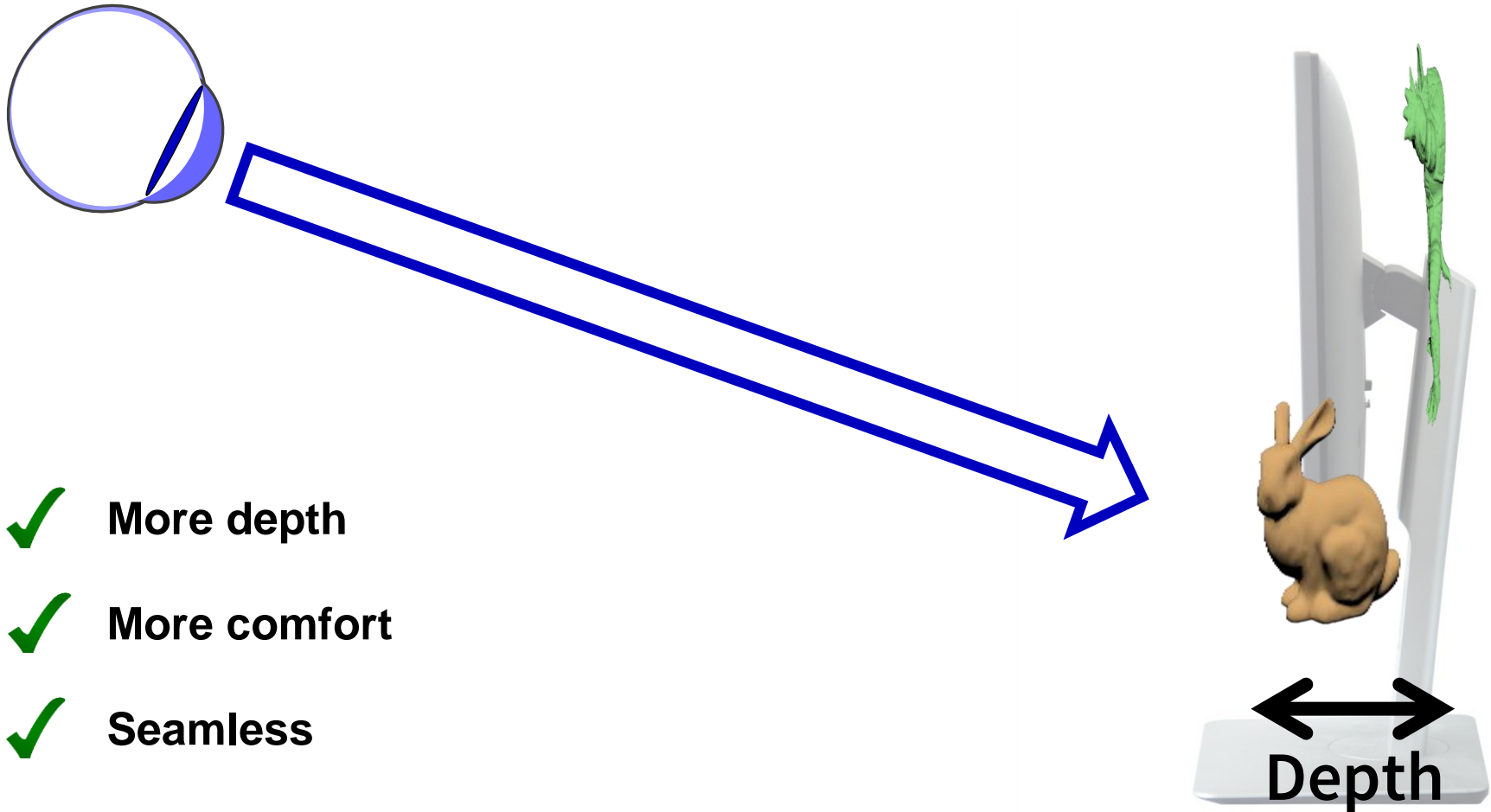
Vergence-accommodation Conflict



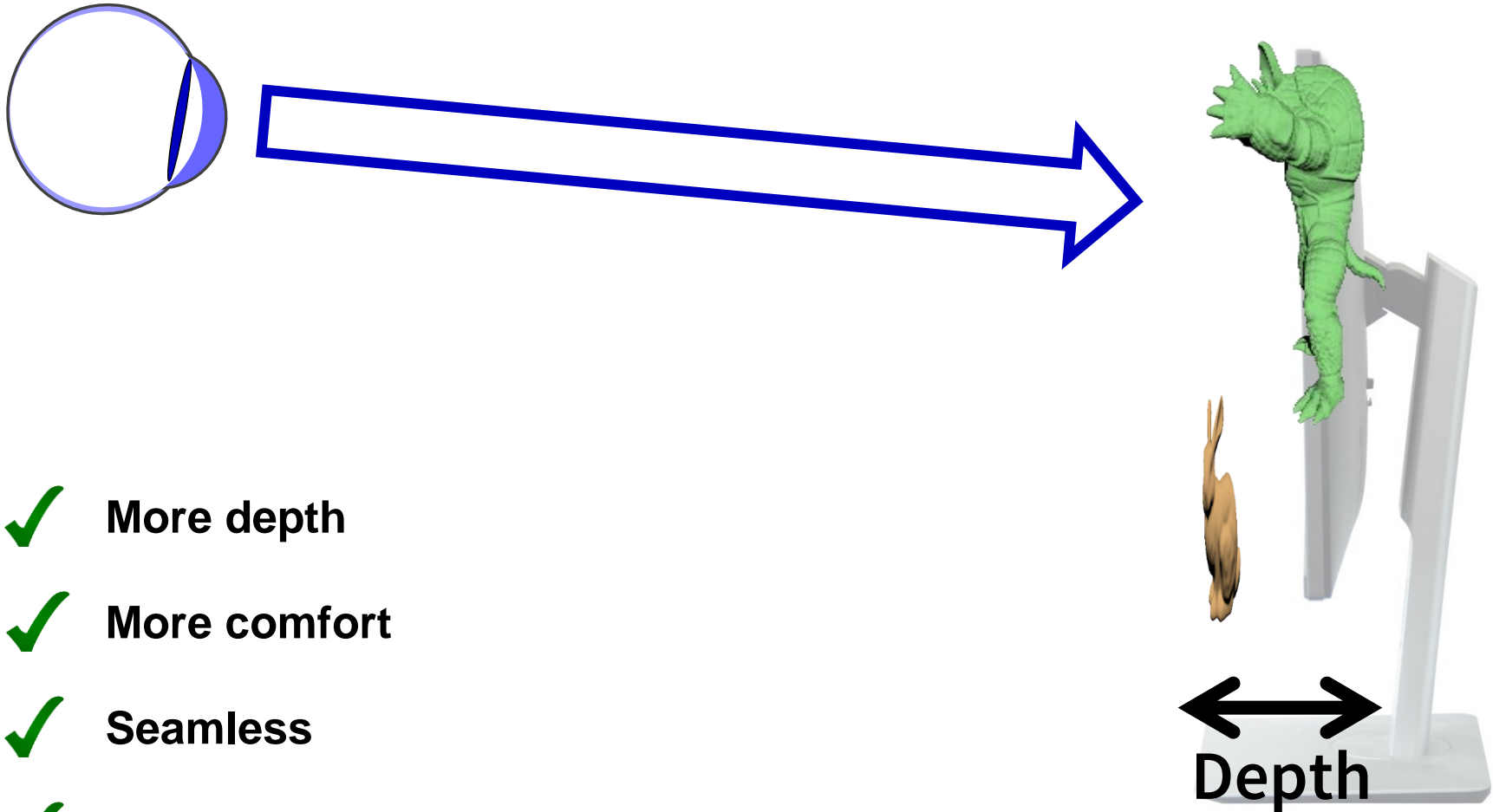
Vergence-accommodation Conflict



Vergence-accommodation Conflict



Vergence-accommodation Conflict



- ✓ More depth
- ✓ More comfort
- ✓ Seamless
- ✓ Low cost

Gaze-contingent Stereo

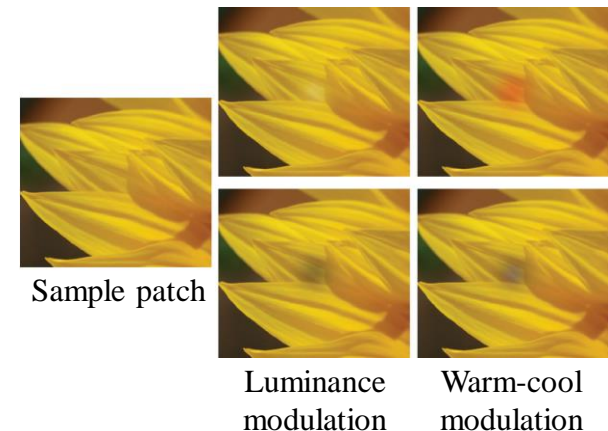
- The region of attention may be predicted to manipulate disparity for comfortable viewing
- The online predictor uses Decision Forests (DF) to predict the object category that the viewer looks at
- A total of 13 game variables are used for prediction (e.g. Health, Hunger, Thirst, Ammo, Distance to the closest robot, ...) which are selected among 300 as the most “informative” ones (ignoring variables with little or no variability)
- The predicted objects in the current scene are placed as close to the plane of zero-disparity as possible



Images adapted from Koulteris, George Alex, et al. "Gaze Prediction using Machine Learning for Dynamic Stereo Manipulation in Games." IEEE Virtual Reality. 2016.

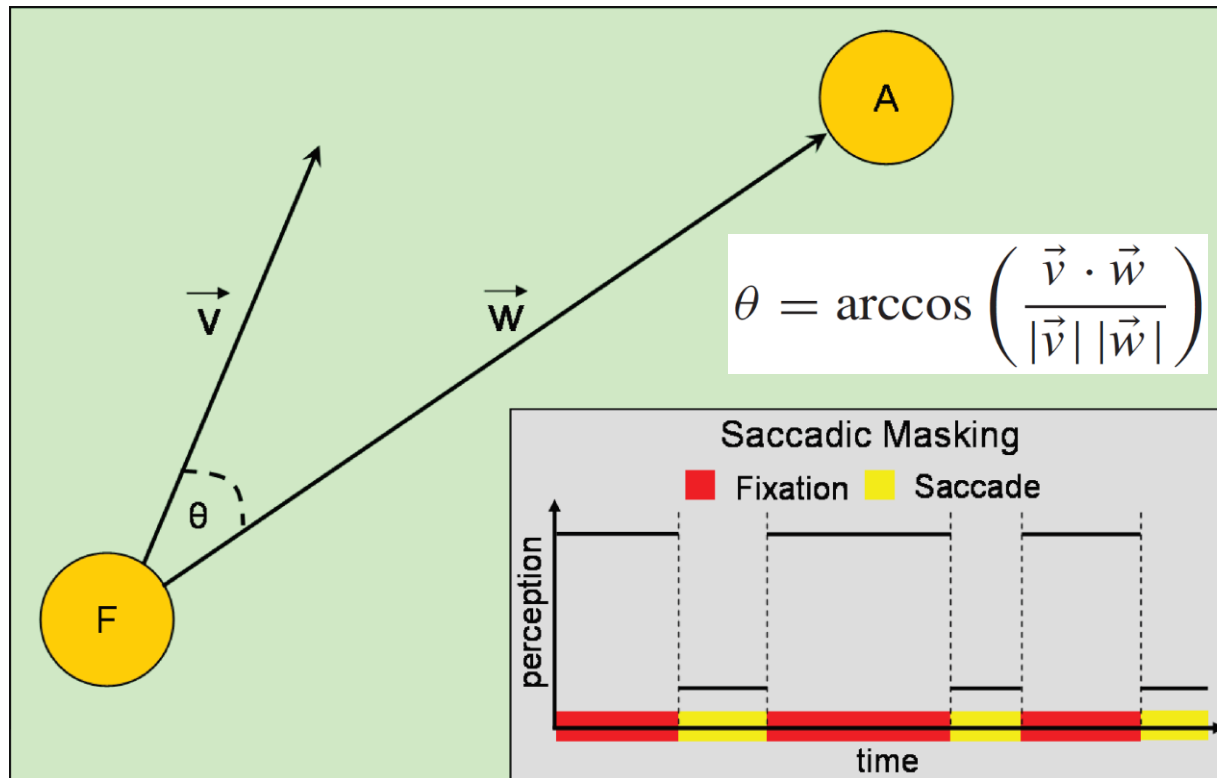
Subtle Gaze Direction

- When viewing an image low-acuity peripheral vision detects areas of interest, then HVS directs gaze to those locations
- HVS is very sensitive to changes in luminance (Spillmann et al. 1990) and opponent color channels (Hurvich and Jameson 1957)
- Introduces subtle image modulation to control the gaze direction of the observer
- Luminance and warm-cool modulations are studied and both are found successful



Images adapted from Bailey, R., McNamara, A., Sudarsanam, N., & Grimm, C. (2009). Subtle gaze direction. ACM Transactions on Graphics (TOG), 28(4), 100.

Subtle Gaze Direction



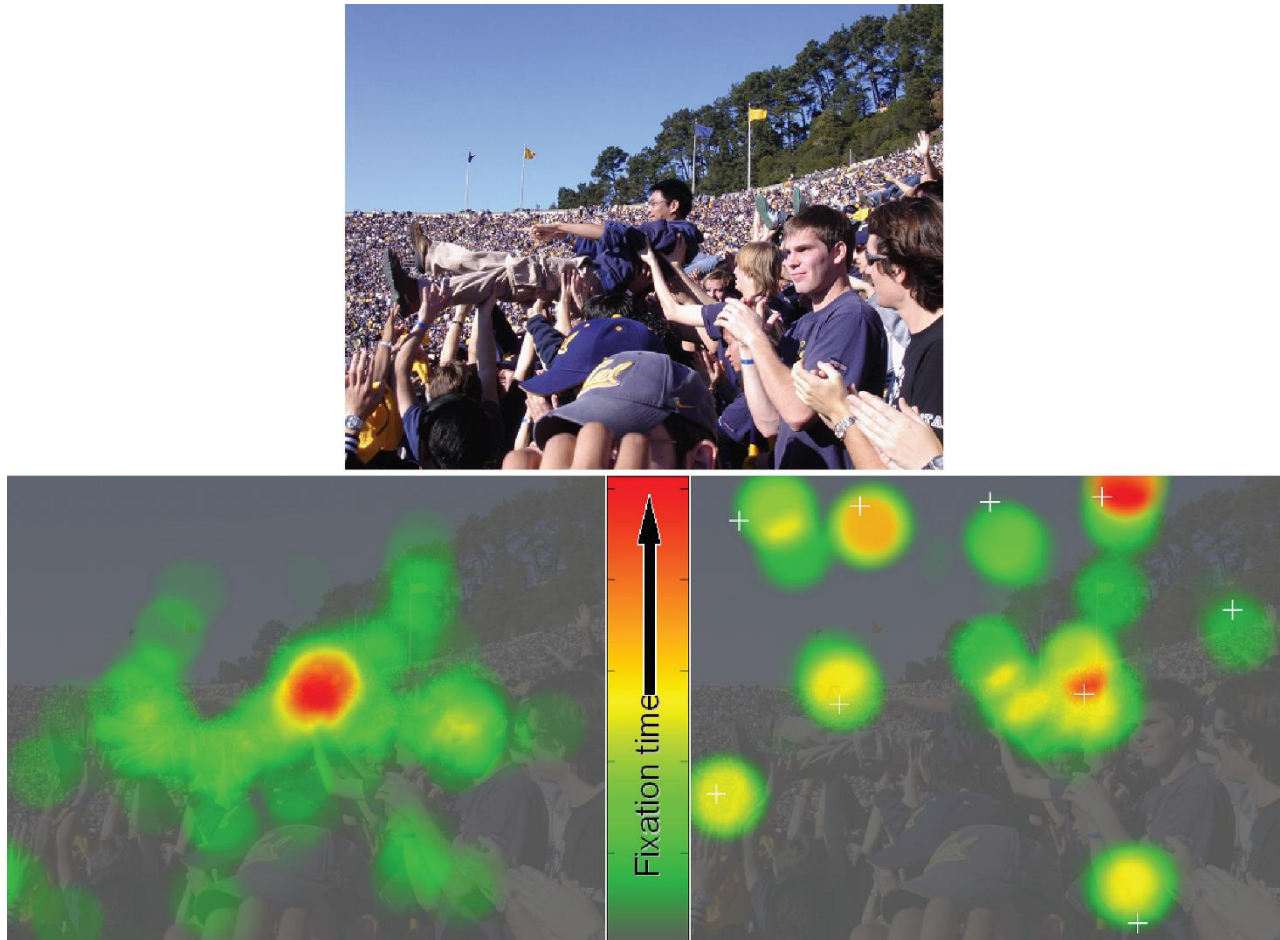
F: Fixation point, **A:** Predetermined Area of Interest

Goal: To direct the user attention to from **F** to **A**

Modulation is applied to A and θ is monitored real-time.

When $\theta \leq 10^\circ$, the modulation is terminated immediately.

Subtle Gaze Direction



Top: Input image, **Left:** No modulation, **Right:** Modulation at white crosses

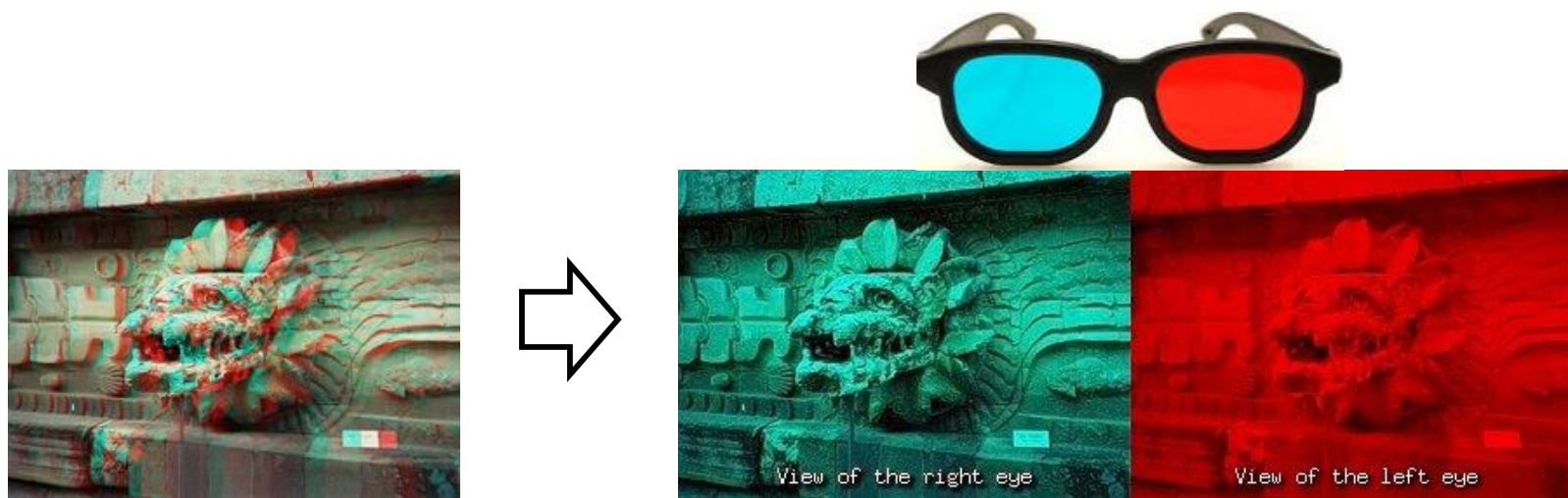
Images adapted from Bailey, R., McNamara, A., Sudarsanam, N., & Grimm, C. (2009). Subtle gaze direction. ACM Transactions on Graphics (TOG), 28(4), 100.

Binocular 3D Displays

- **Capable of providing sense of 3D by simulating binocular disparity**
 - Color Anaglyphs
 - Polarization
 - Shutter Glasses
 - Head-Mounted Displays
- **They mostly do not provide accommodation depth cue**

Color Anaglyphs

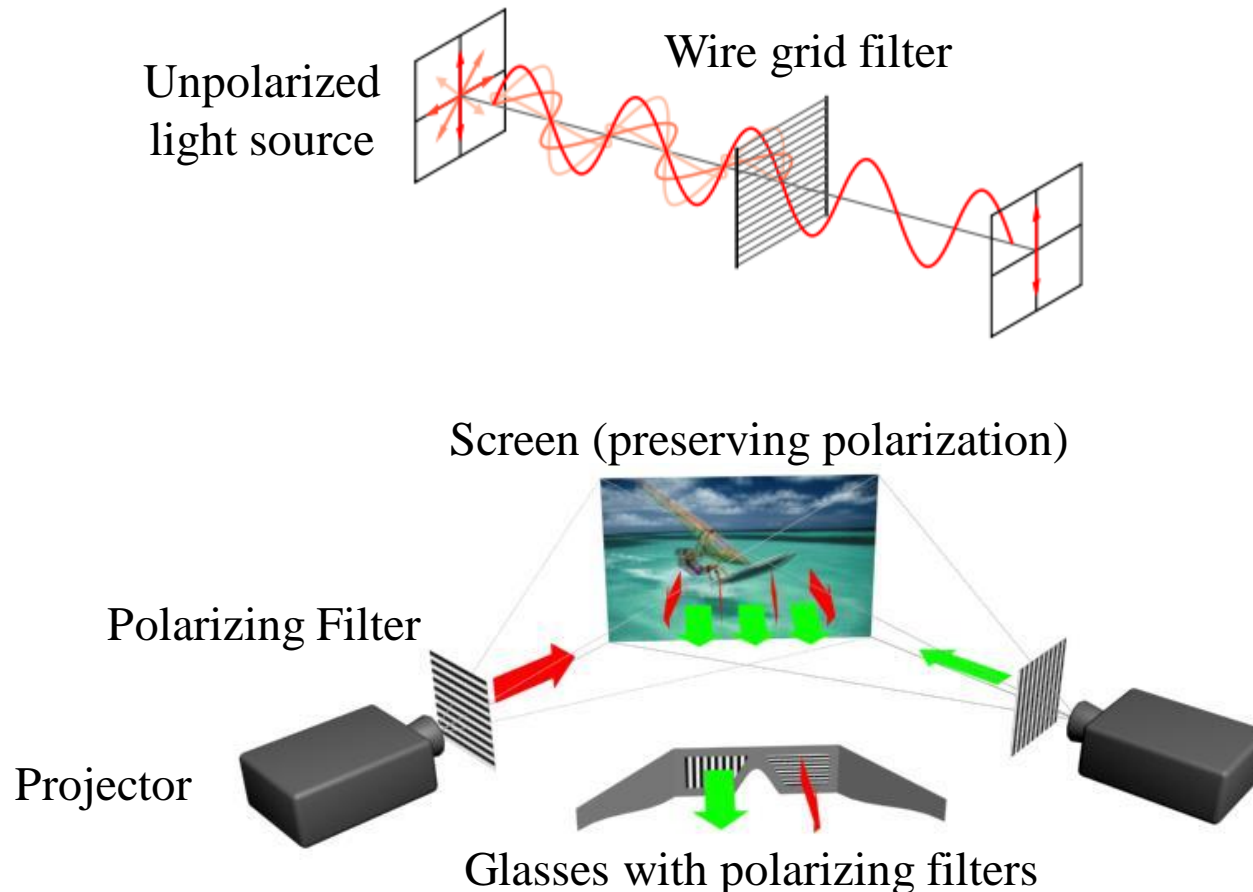
- **Left and right images are filtered using different colors (usually complementary):**
 - Red – Green, Red – Cyan, Green – Magenta
 - Amber – Blue (ColorCode 3D, patented [Sorensen et al. 2004])
- **Limited color perception (since each eye sees only a subset of whole colorspace)**



Images adapted from http://axon.physik.uni-bremen.de/research/stereo/color_anaglyph/

Polarization

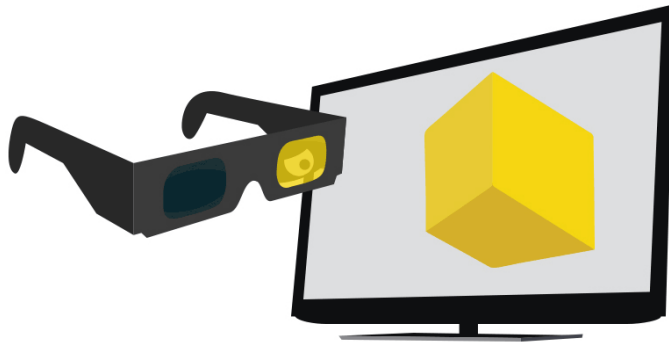
- Usually a wire grid filter converts the unpolarized light beam to a polarized one



Images adapted from https://cpinettes.u-cergy.fr/S6-Electromag_files/fig1.pdf

Shutter Glasses

- Exploits the “memory effect” of the Human Visual System [Coltheart 1980]
- Glasses have shutters which operate in synchronization with the display system
- Left and right eye images are shown in alternation
- Color neutral; however, temporal resolution is reduced



IR receiver for
synchronization

Images adapted from https://en.wikipedia.org/wiki/Active_shutter_3D_system

Head-Mounted Displays

- **Separate displays for the left and right eye**
- **May provide current orientation of the head (and update the stimuli accordingly to provide a VR)**



Images adapted from <http://www.oculus.com>

Autostereoscopic Displays

- Stereo displays which are viewable without special glasses or head-wear equipment
- Simulate an approximate lightfield with a finite number of views
 - Parallax Barriers
 - Integral Imaging
 - Multi-layer Displays

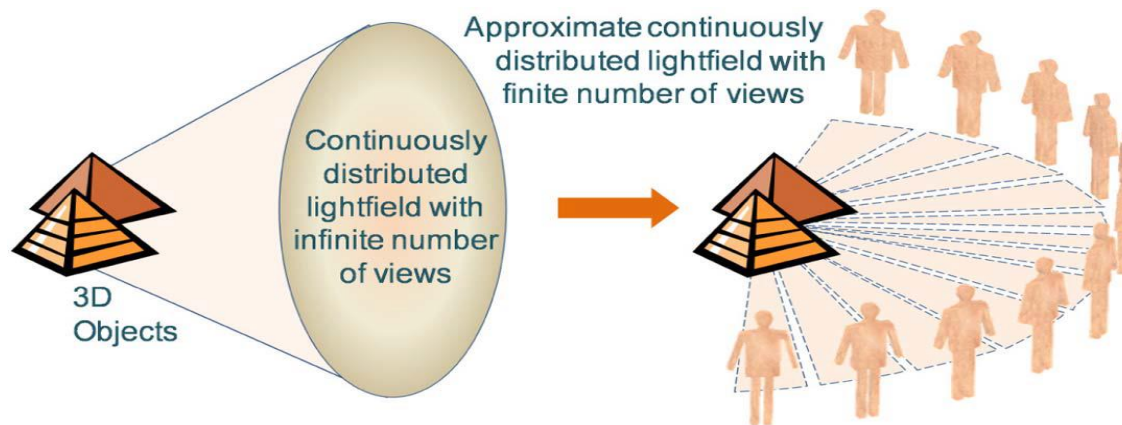
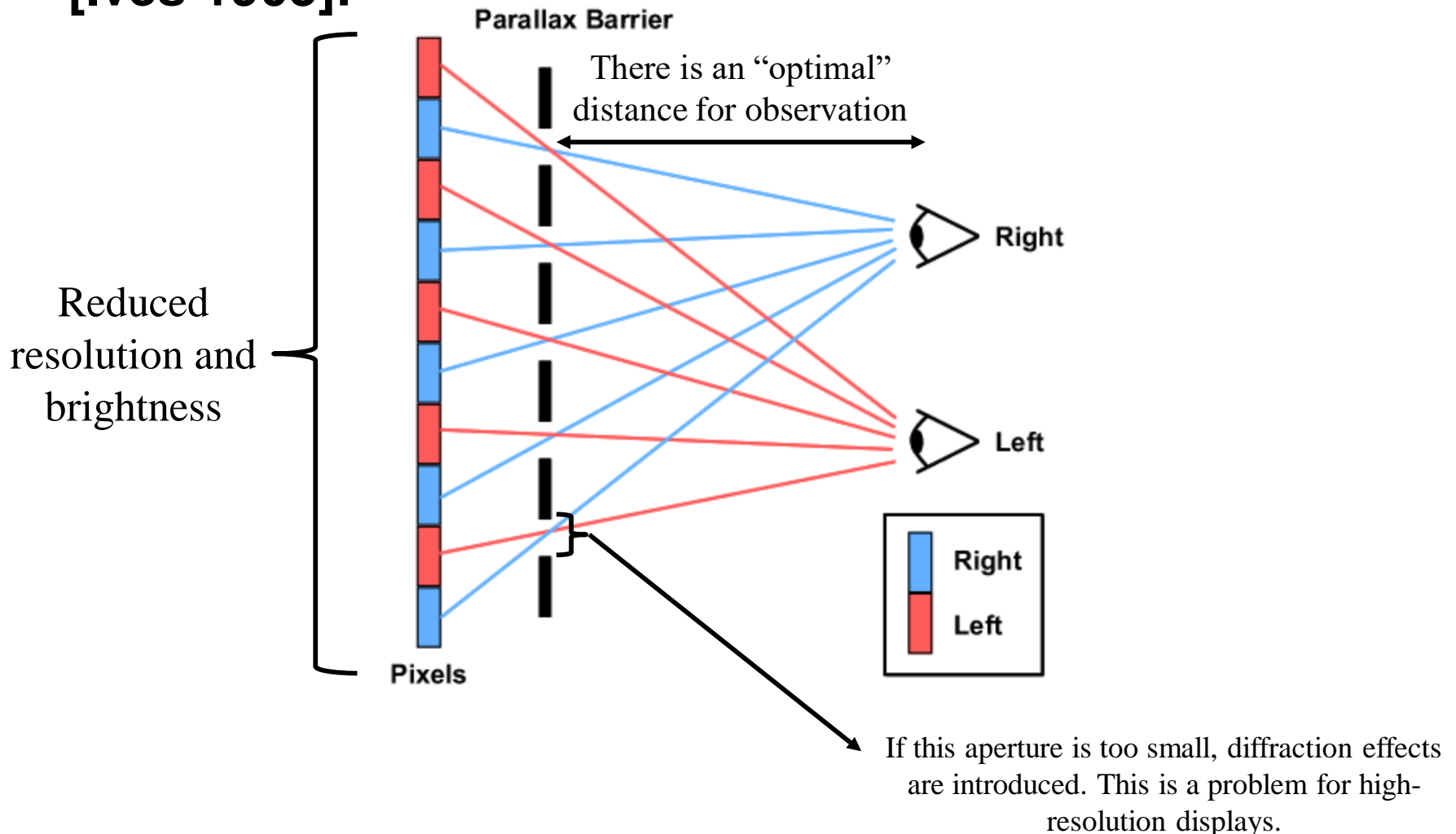


Image adapted from Geng, Jason. "Three-dimensional display technologies." *Advances in optics and photonics* 5.4 (2013): 456-535.

Parallax Barriers

- Occlusion-based working principle and key features [Ives 1903]:



Parallax Barriers

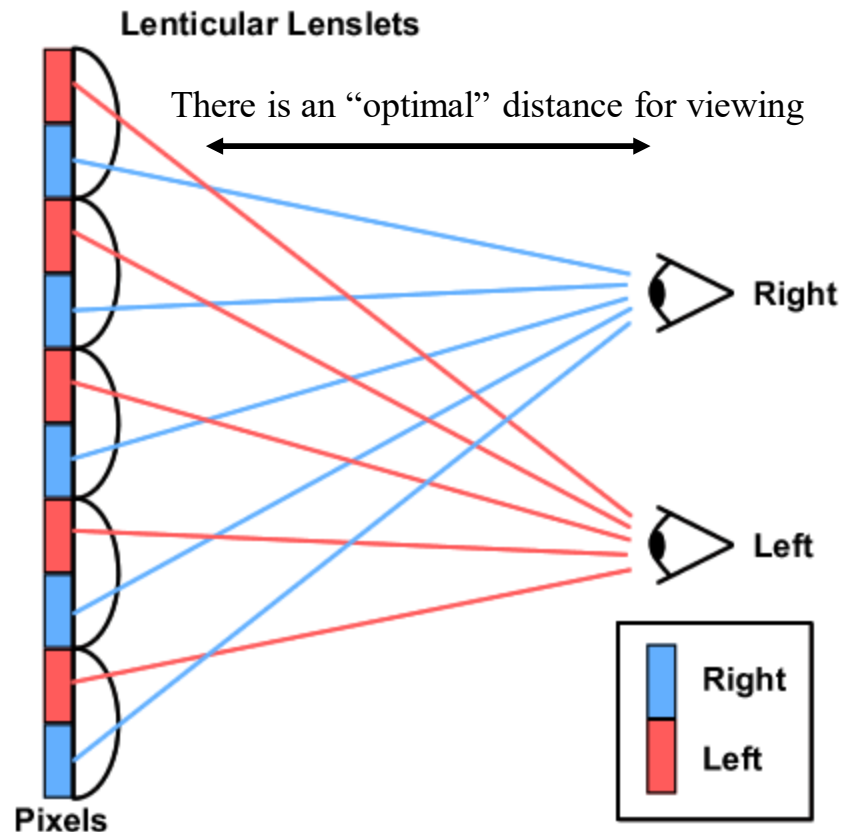


Video adapted from: <http://www.youtube.com/watch?v=sxF9PGRiabw> “Glasses-Free 3D Gaming for \$5 (Parallax Barrier)”

Integral Imaging

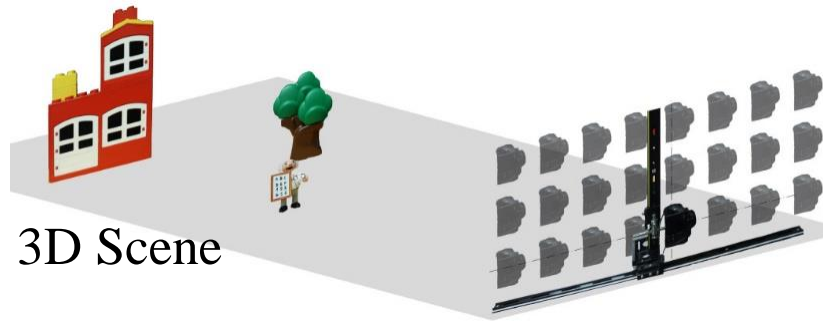
- Refraction-based working principle [Lippmann 1908]:

Reduction in resolution and brightness is still a problem.



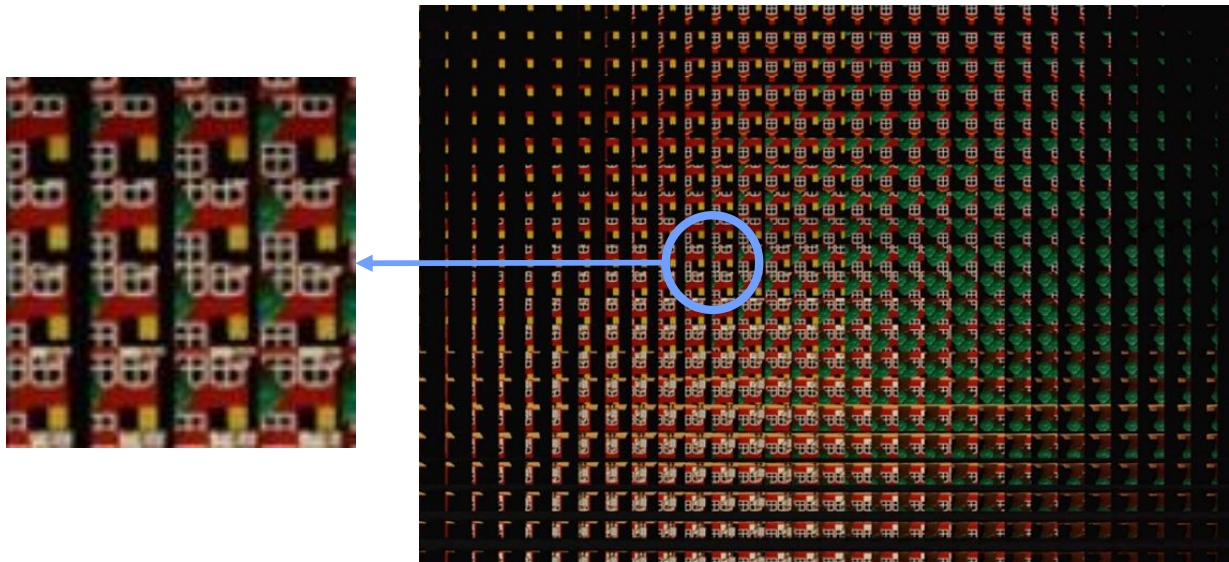
It is possible to reproduce parallax, perspective shift and accommodation depth cues.

Integral Imaging



3D Scene

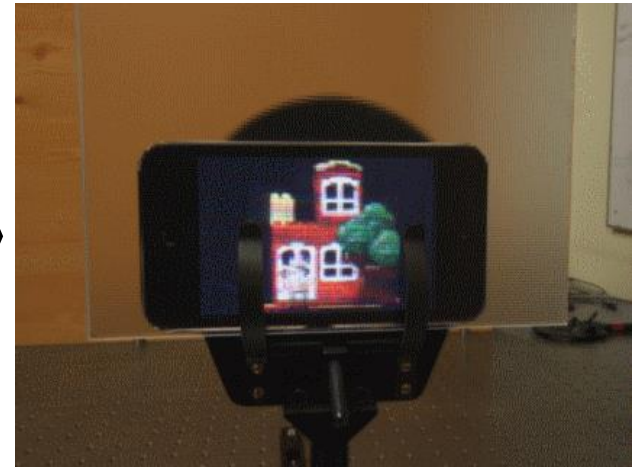
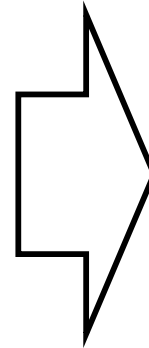
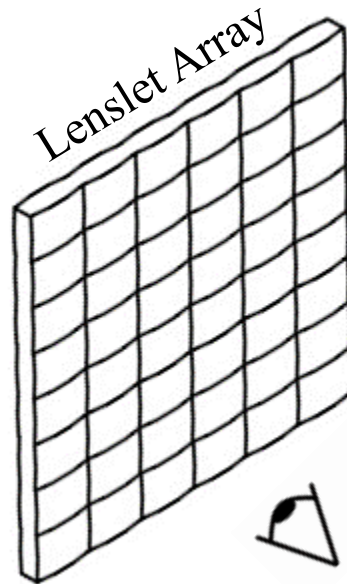
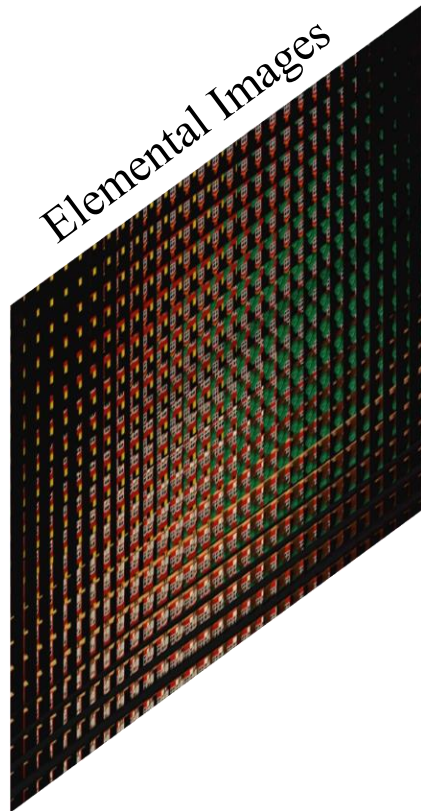
Array of lenses (multiple cameras each with a single lens [Wilburn 2005] or a single camera with multiple lenses in front of the sensor [Ng 2005])



Elemental Images

Images adapted from Martinez-Corral, Manuel, et al. "3D integral imaging monitors with fully programmable display parameters."

Integral Imaging



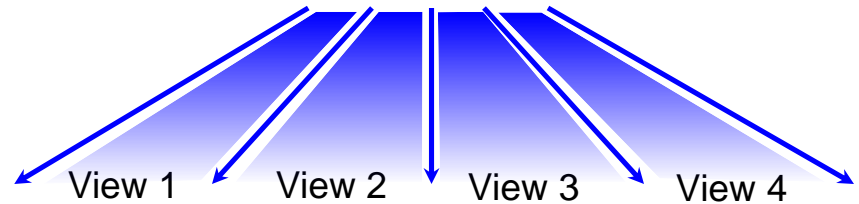
Integral Image as seen by the observer

Images adapted from Martinez-Corral, Manuel, et al. "3D integral imaging monitors with fully programmable display parameters."

Multi-view Autostereoscopic Display

- **Smooth transitions**

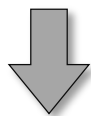
Multi-view autostereoscopic display



„Antialiasing for automultiscopic 3D displays” [Zwicker et al. 2006]

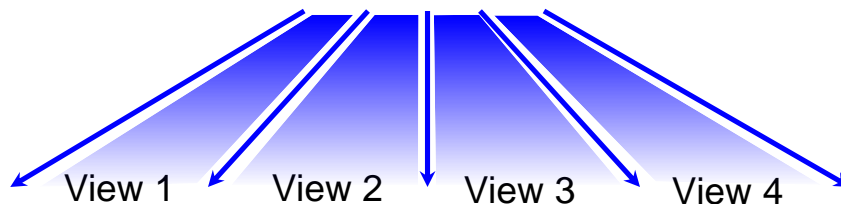
Multi-view Autostereoscopic Display

- **Smooth transitions**
- **Blur increases with depth**



Weaker depth percept

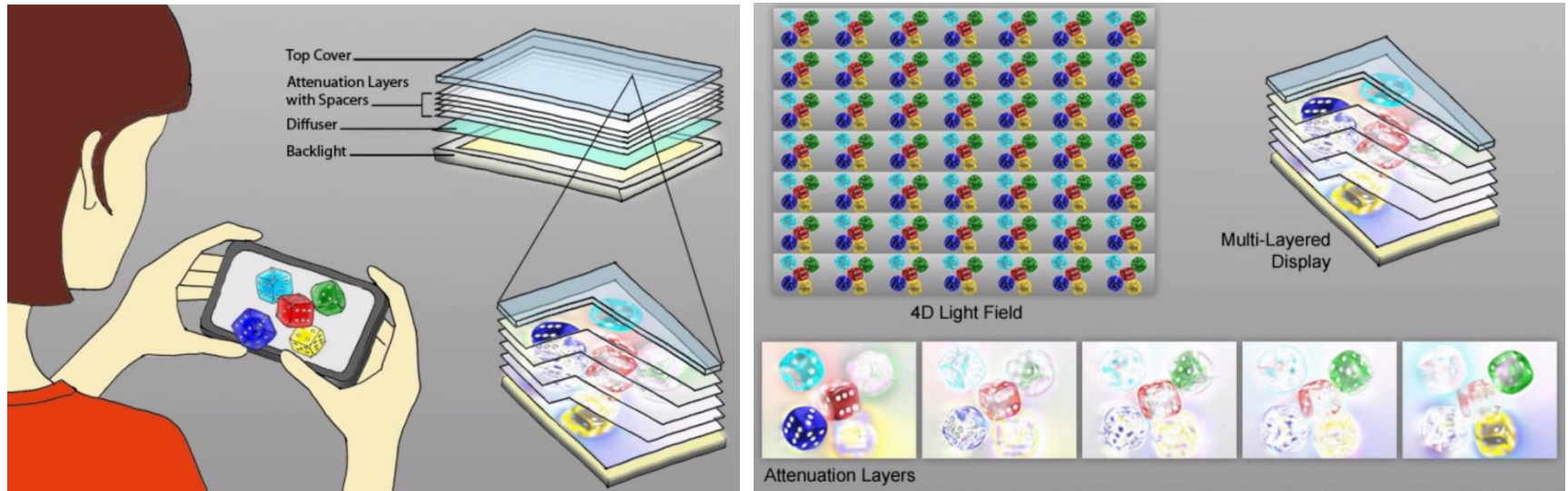
Multi-view autostereoscopic display



„Antialiasing for automultiscopic 3D displays” [Zwicker et al. 2006]

Multi-layer Displays

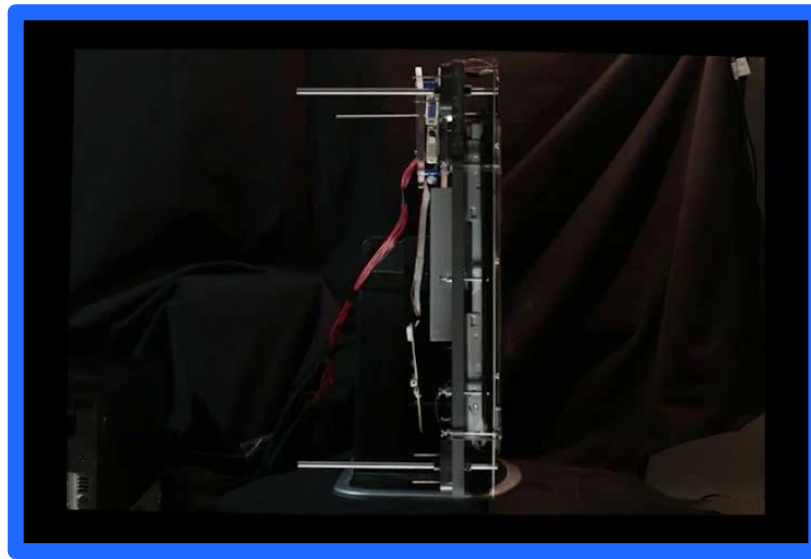
- Improved resolution over parallax barriers and lenslet arrays
- Provides a solution to accommodation-vergence conflict



Images adapted from Wetzstein, Gordon, et al. "Layered 3D: tomographic image synthesis for attenuation-based light field and high dynamic range displays." ACM Transactions on Graphics (ToG). Vol. 30. No. 4. ACM, 2011.

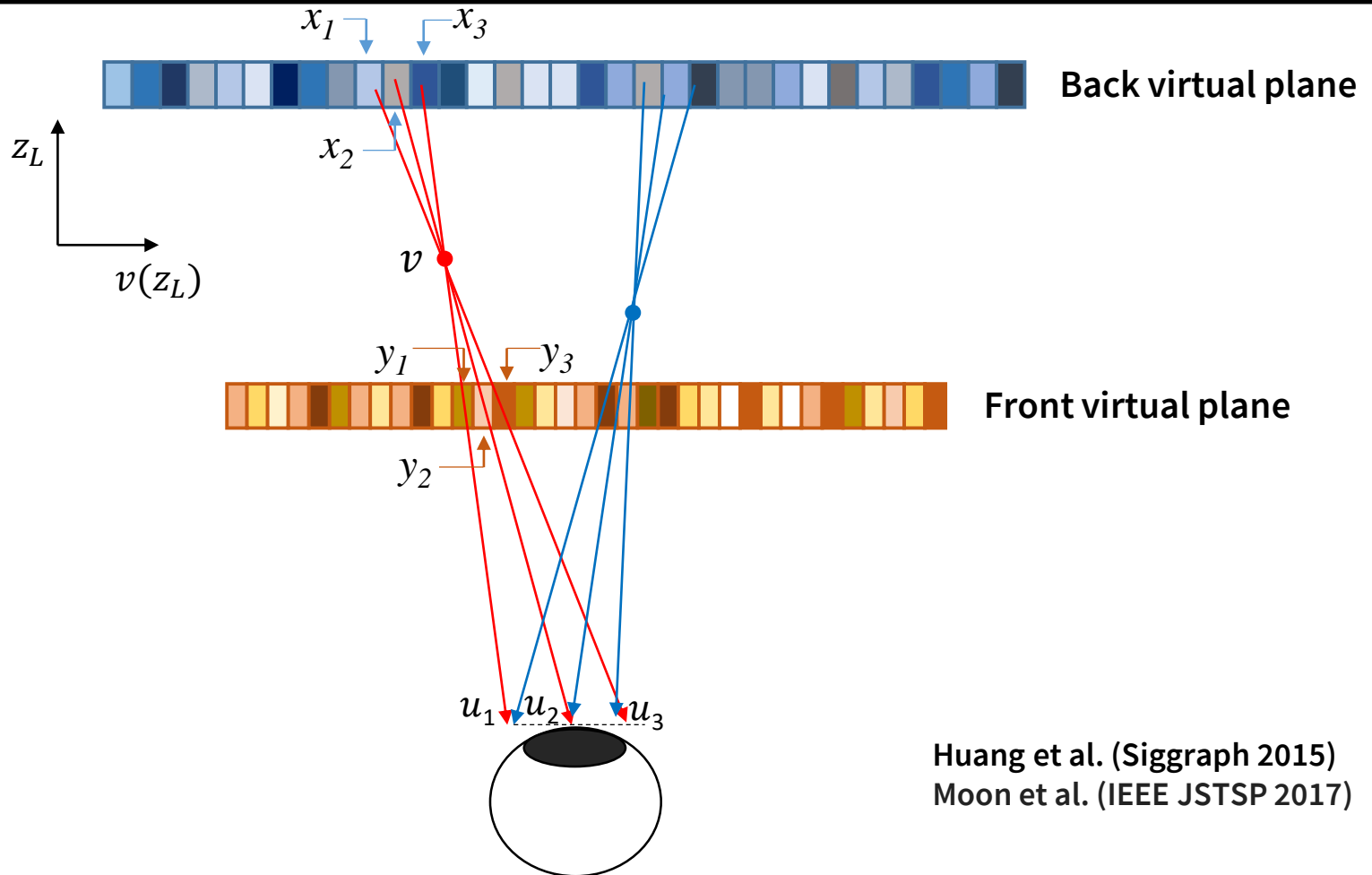
Tensor Displays

- **Lightfield emitted by a multi-layer display is represented by a tensor where rays span a 2D plane in 3D tensor space**
- **Target lightfield is decomposed into Rank-1 tensors using Nonnegative Tensor Factorization**
- **Rank-1 tensors are shown in quick succession with a high refresh rate, which are perceptually averaged over time by the Human Visual System**



Video adapted from Wetzstein, Gordon, et al. "Tensor displays: compressive light field synthesis using multilayer displays with directional backlighting." (2012).

Rendering images in Tensor Displays



Target Light-fields: $L(v, u_1) = L(v, u_2) = L(v, u_3) = R$

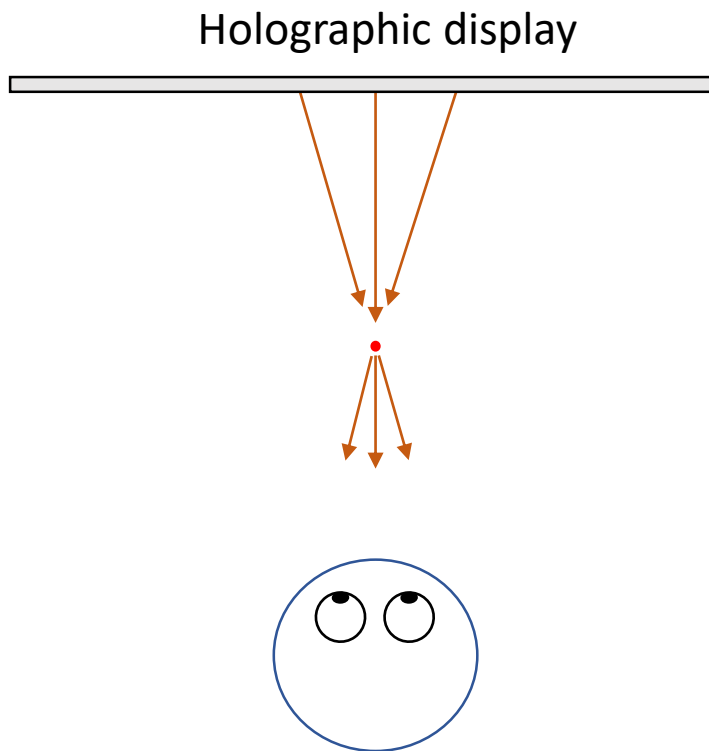
Optimization equation : $L(v, u_1) = x_3 \times y_1$
 $L(v, u_2) = x_2 \times y_2$
 $L(v, u_3) = x_1 \times y_3$

Lightfield Displays



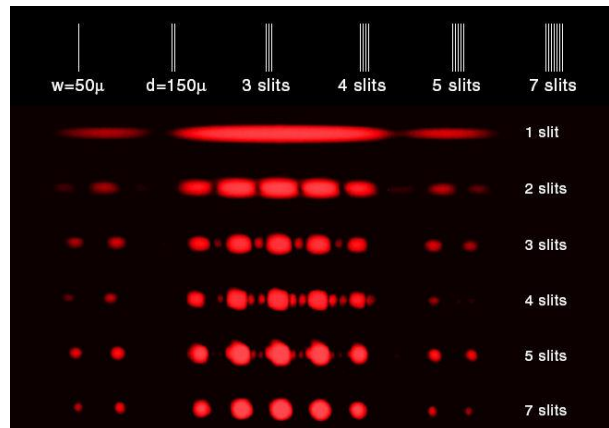
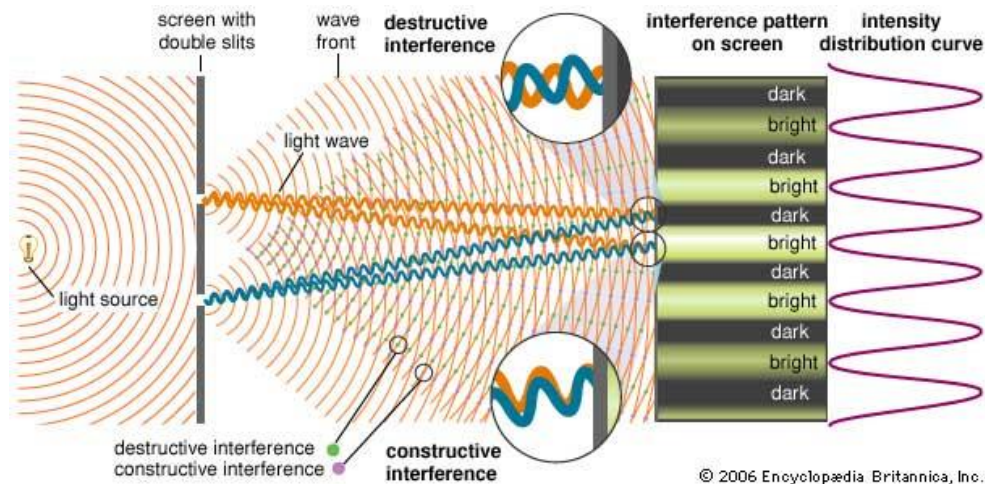
Holographic display

Holographic display : generating 3D images **in the air** without any scatterer



What is the meaning of “focusing the light”?

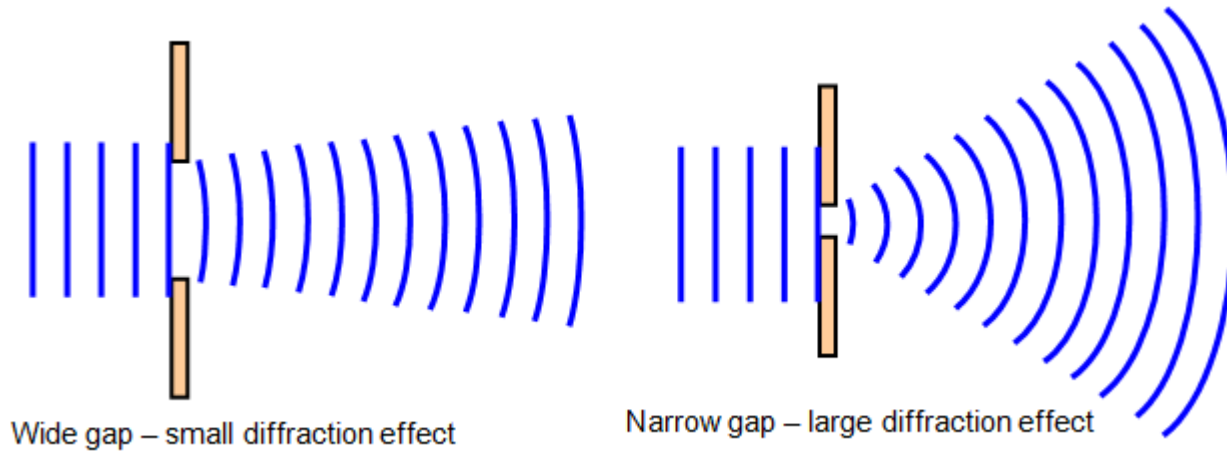
Focusing == interference



<http://labman.phys.utk.edu/phys136>

Focusing = constructive interference of multiple pixels
(but it requires coherent light sources such as laser)

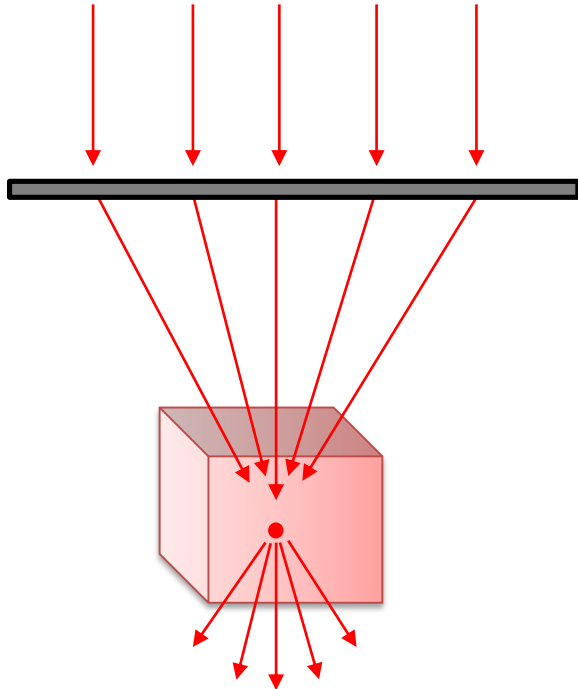
Smaller pixel size == Large diffraction angle



	Pixel size	Viewing angle
LCD monitor	$200\ \mu m$	0.1°
LCoS Spatial light modulator	$16\ \mu m$	2°
Ideal pixel size	$1\ \mu m$	30°

Ultimate 3D display: Holographic display

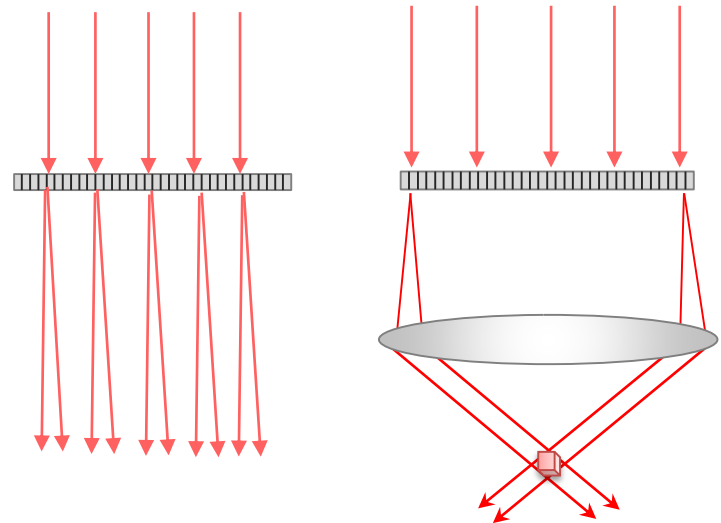
Ideal holographic monitor



Pixel size : $1\ \mu\text{m}$
Screen size : 30 cm x 30 cm
Resolution : 300000 x 300000

Viewing angle : 30°
Image size : 30 cm x 30 cm

Current holographic monitor



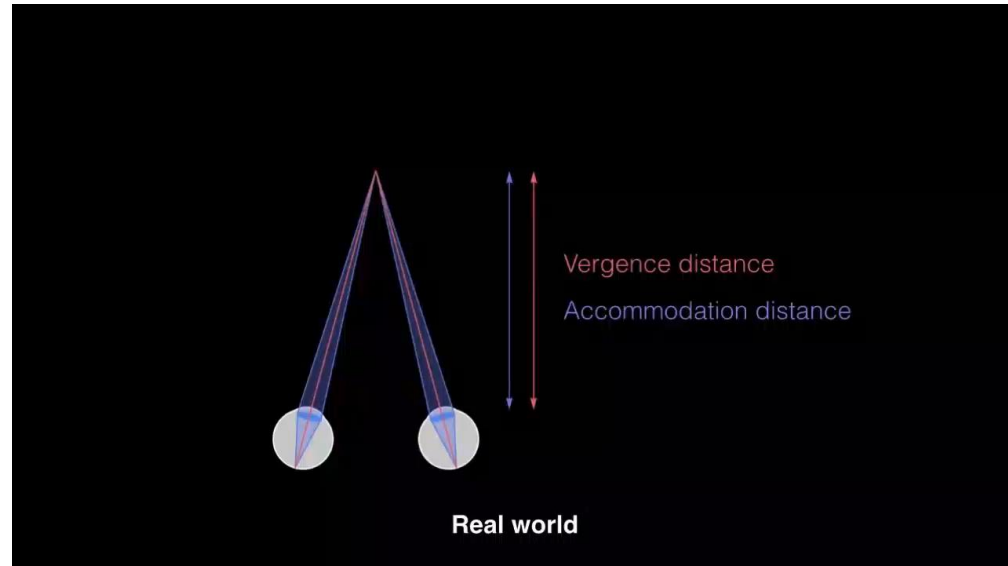
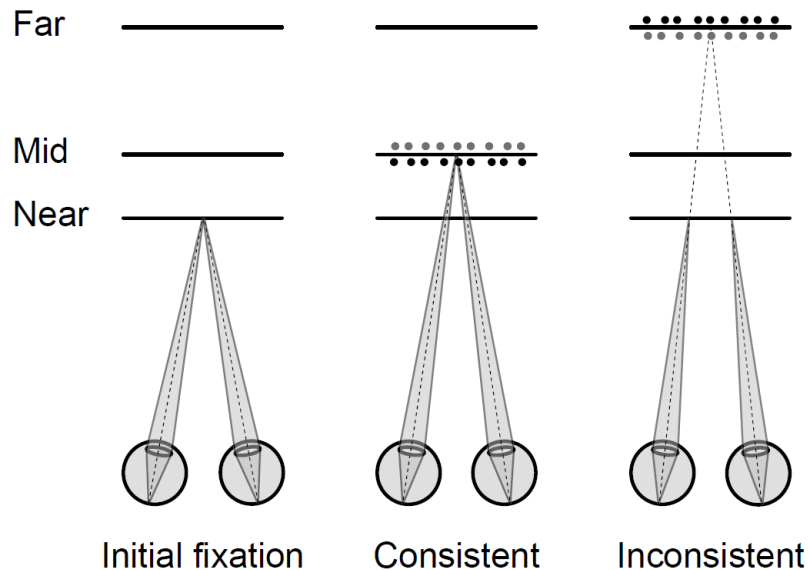
Pixel size : $16\ \mu\text{m}$
Screen size : 1 cm x 1 cm
Resolution : 1024 x 768

Viewing angle : 2°
Image size : 1 cm x 1 cm

Displays Comparison

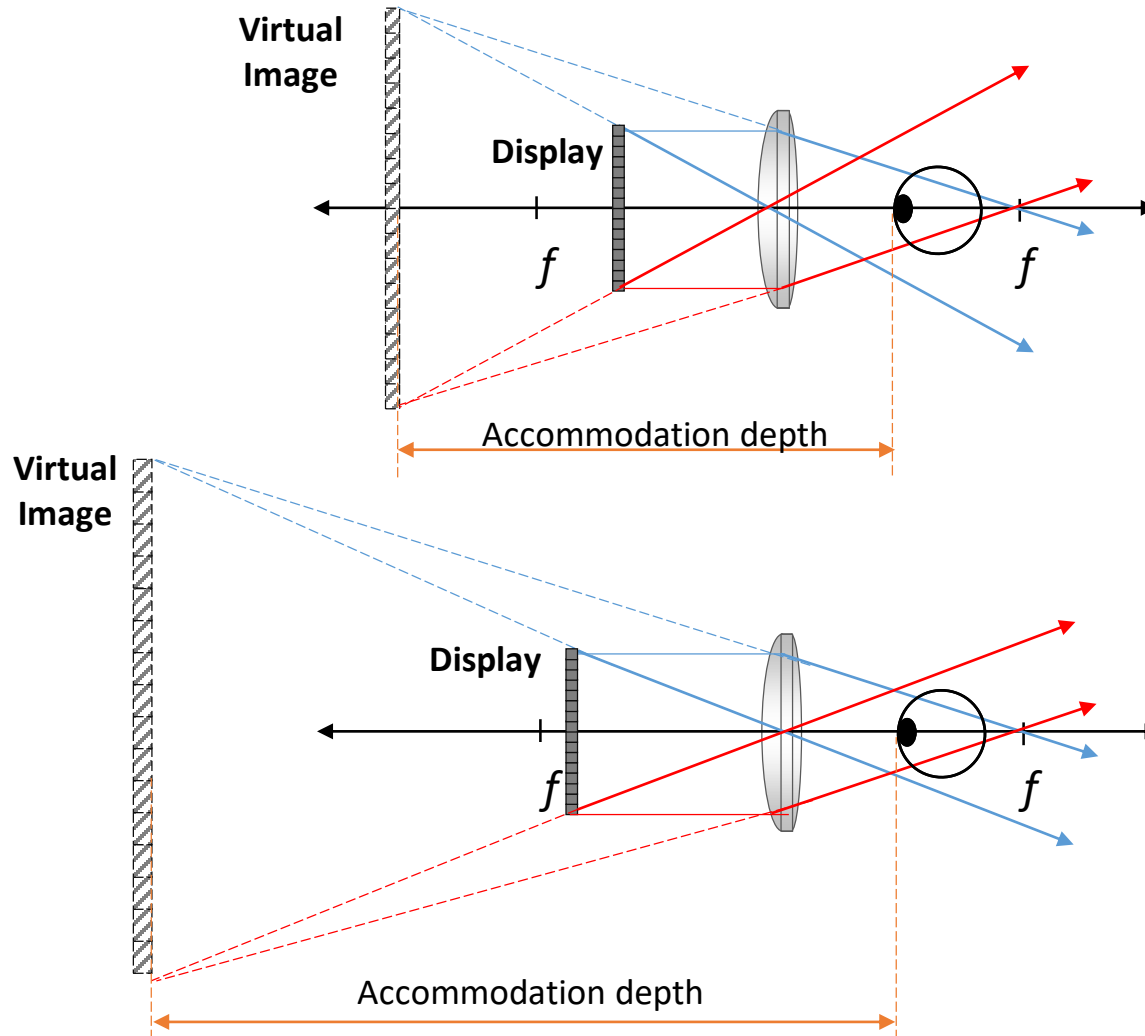
	Pictorial Cues	Disparity	Motion Parallax	Glasses-free	Accommodation
2D Display	✓	✗	✗	✓	✗
Stereoscopic Display	✓	✓	✗	✗	✗
Head-mounted Display	✓	✓	✓	✗	✗
Autostereoscopic Display	✓	✓	✓	✓	✗
Light field Display	✓	✓	✓	✓	✓
Holographic Display	✓	✓	✓	✓	✓

Accommodation-Vergence Conflict

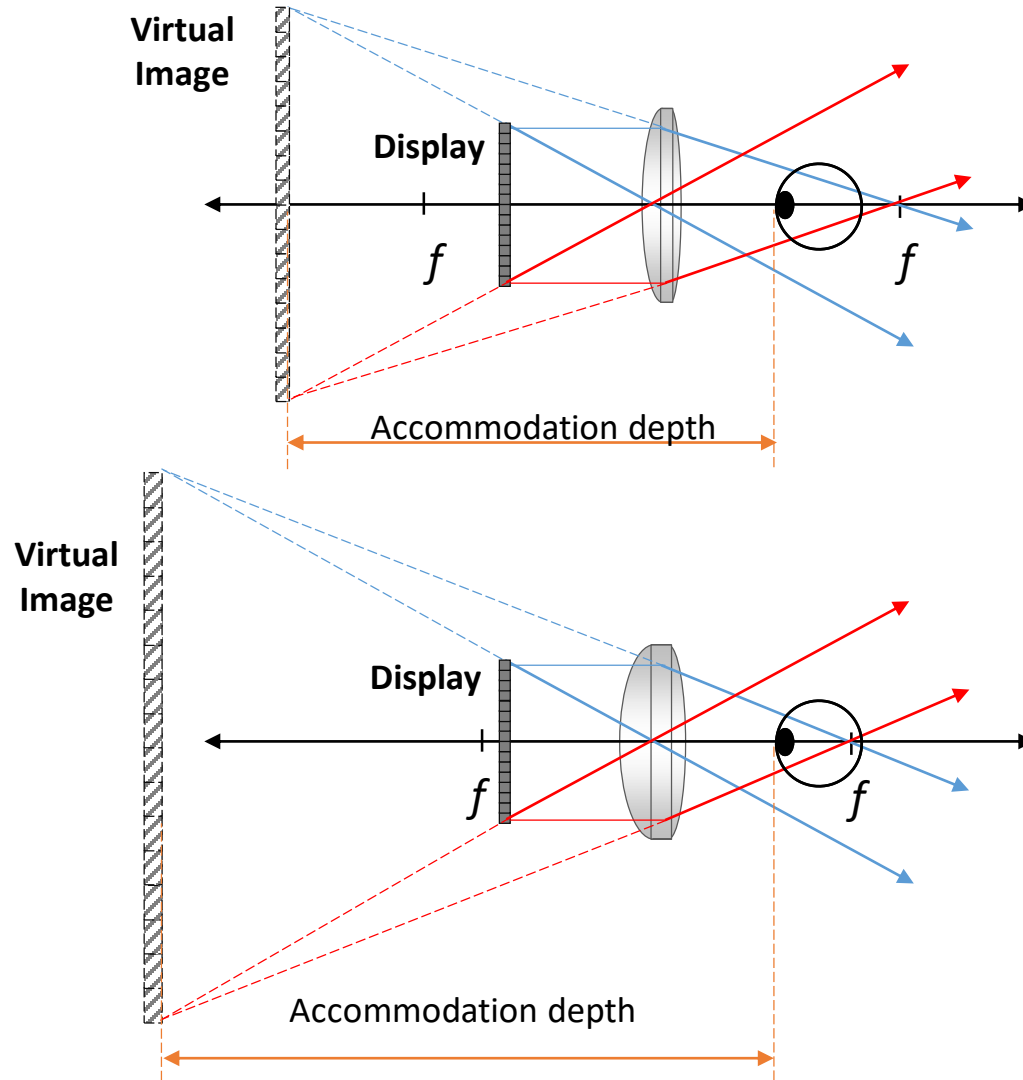


Visuals adapted from Akeley, Kurt, et al. "A stereo display prototype with multiple focal distances." ACM transactions on graphics (TOG). Vol. 23. No. 3. ACM, 2004. and Narain, Rahul, et al. "Optimal presentation of imagery with focus cues on multi-plane displays." ACM Transactions on Graphics (TOG) 34.4 (2015): 59.

How to change accommodation? : (1) the display position

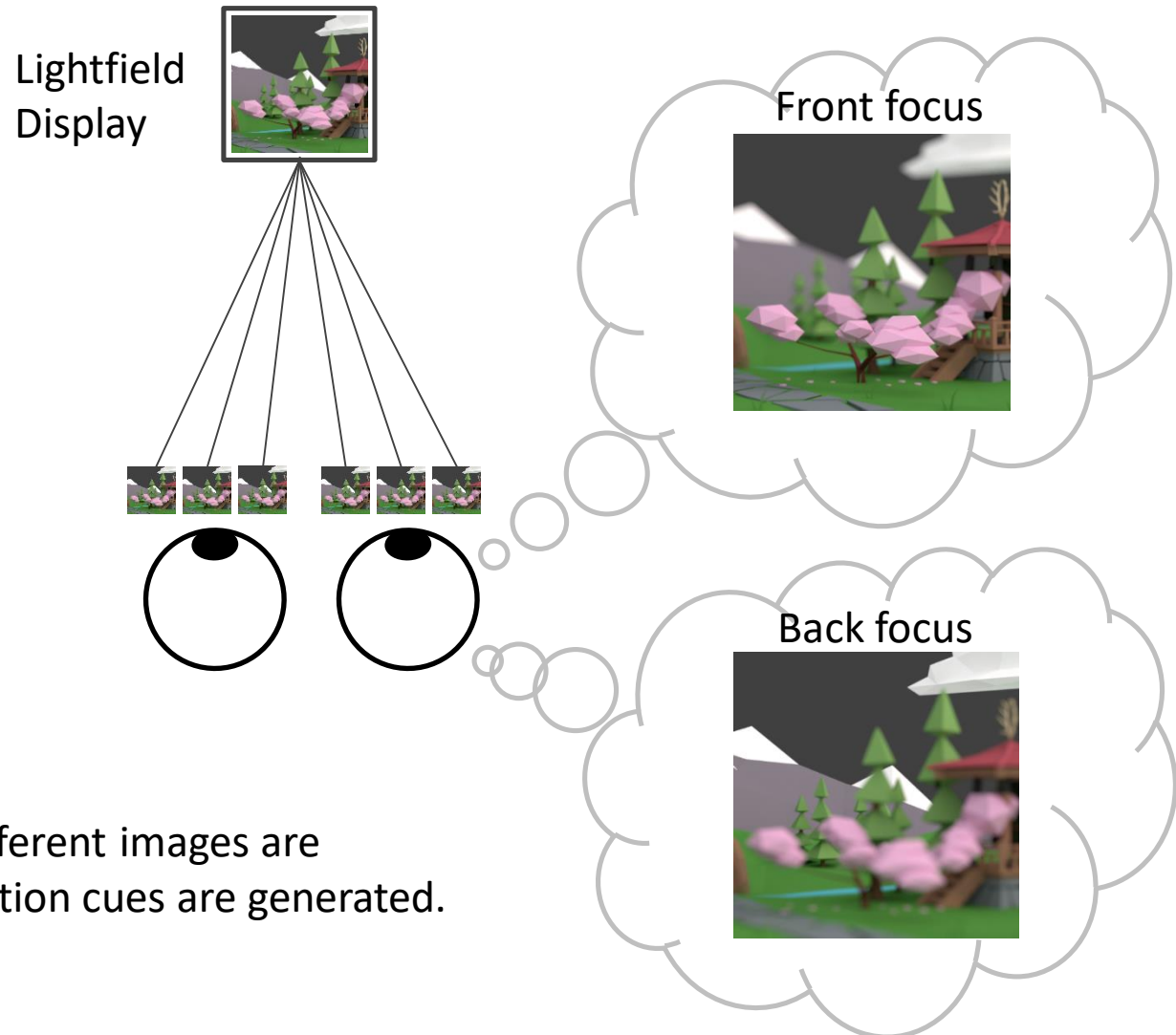


How to change accommodation? : (2) the lens focal length



Requirement for supporting accommodation

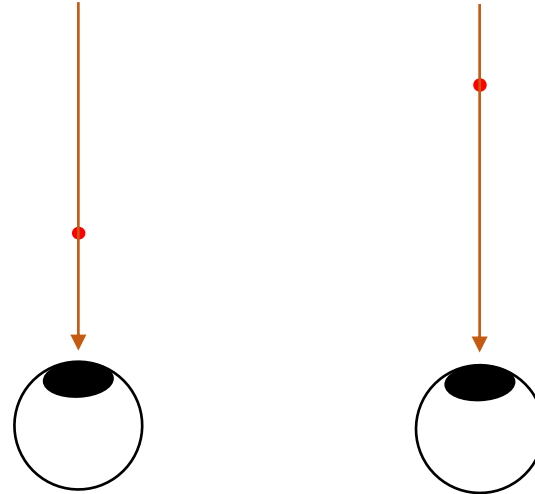
High angular resolution or dense light fields: Accommodation



Towards each eye, multiple different images are projected: proper accommodation cues are generated.

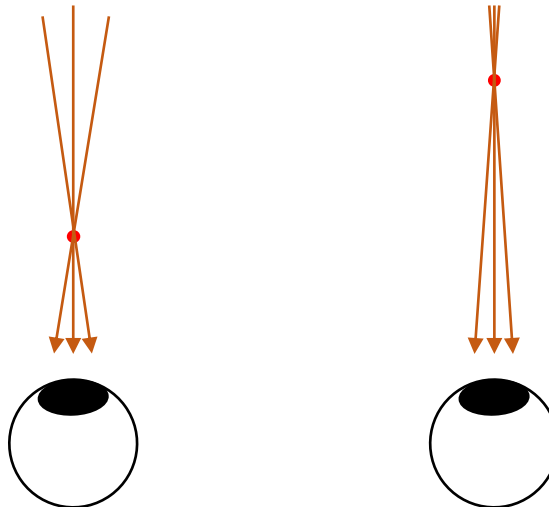
Requirement for supporting accommodation

Single ray is not enough
(depth ambiguity)

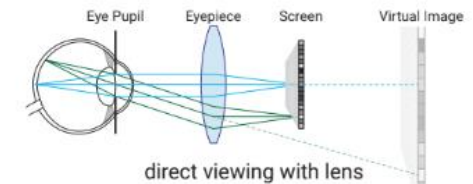
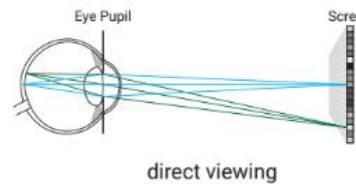


Mathematically, minimum two rays
should be projected inside the pupil
In practice,

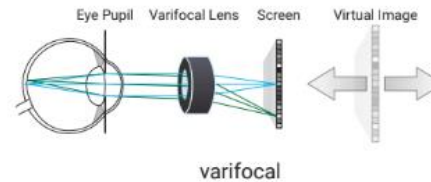
3 rays for 1-D
3 x 3 rays for 2-D



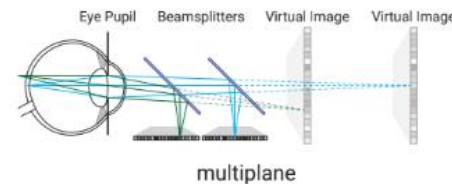
HMD with accommodation cues



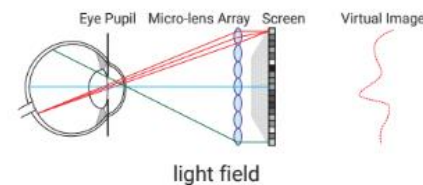
- **Varifocal display**
- **Multi-focal displays**
- **Light field displays**
- **Holographic displays**



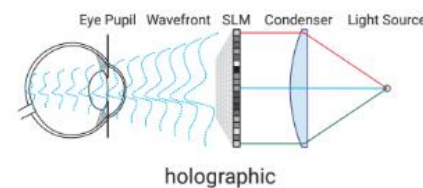
Akşit et al. (2017)



Akeley et al. (2004)



Lanman and Luebke (2013)



Maimone et al. (2017)

Varifocal display: Deformable Beamsplitter

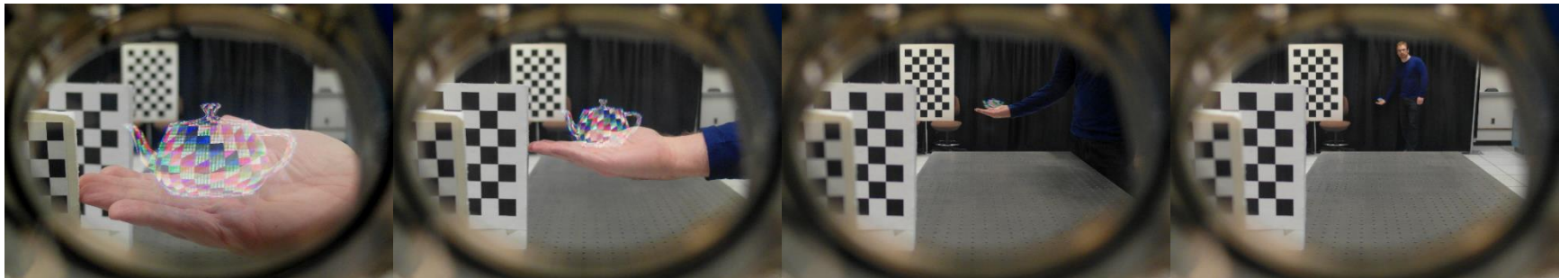


See-through

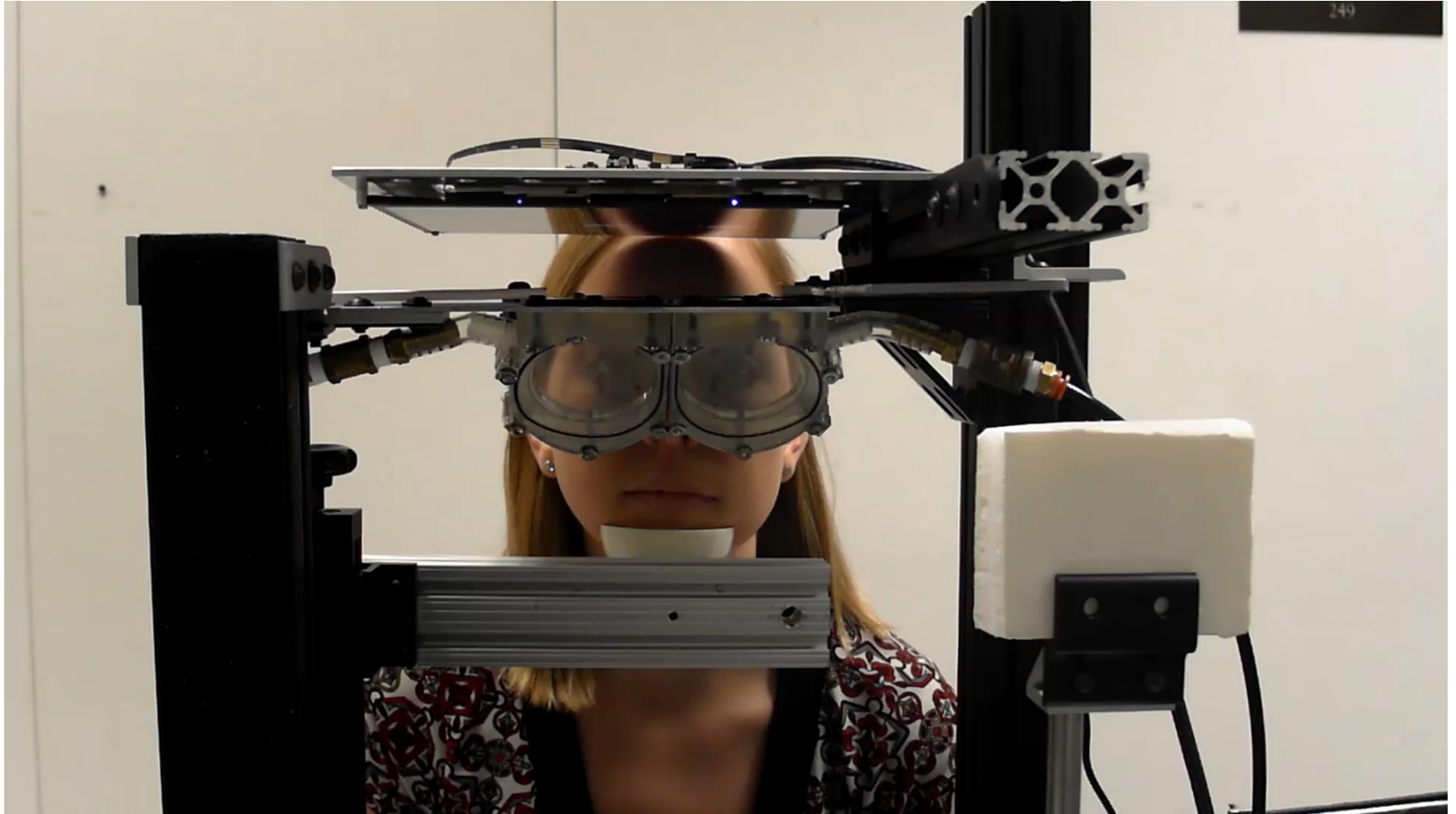
Dynamic focal depth: objects at any depth

Wide field of view

Optics are simple



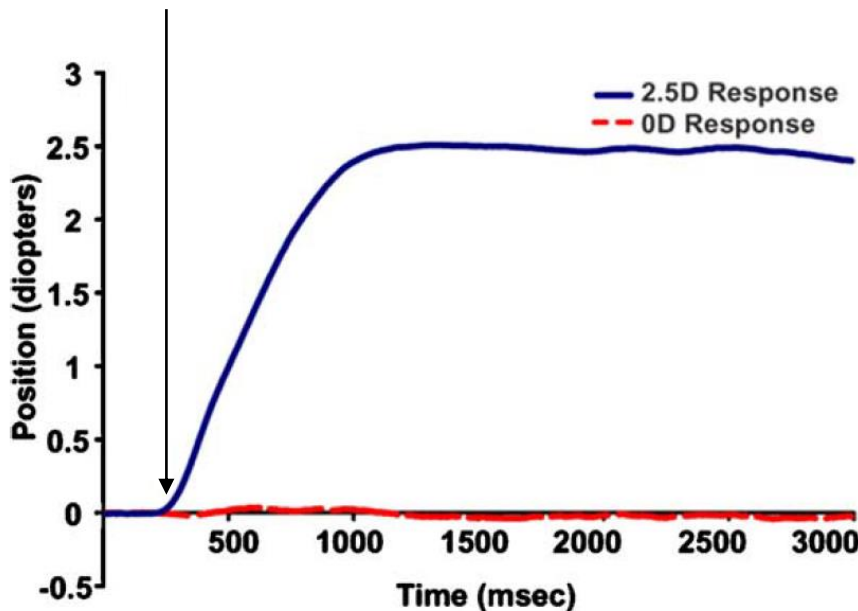
Varifocal display: Deformable Beamsplitter





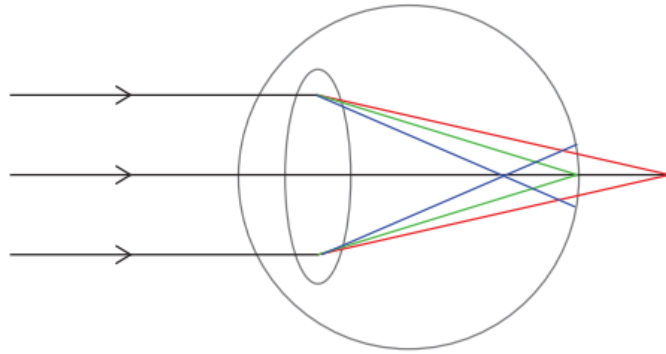
Accommodation Response

- Step change of fixated object depth
 - Smooth and steady accommodation increase
 - up to 1 second to achieve the full accommodation state
 - ~300 ms latency



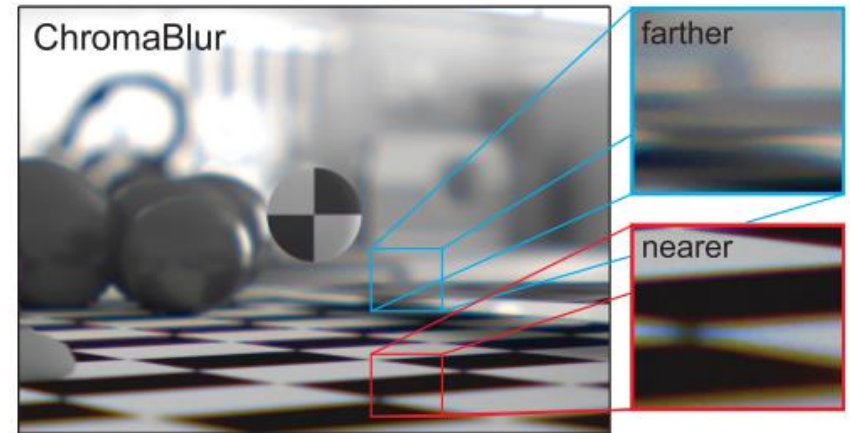
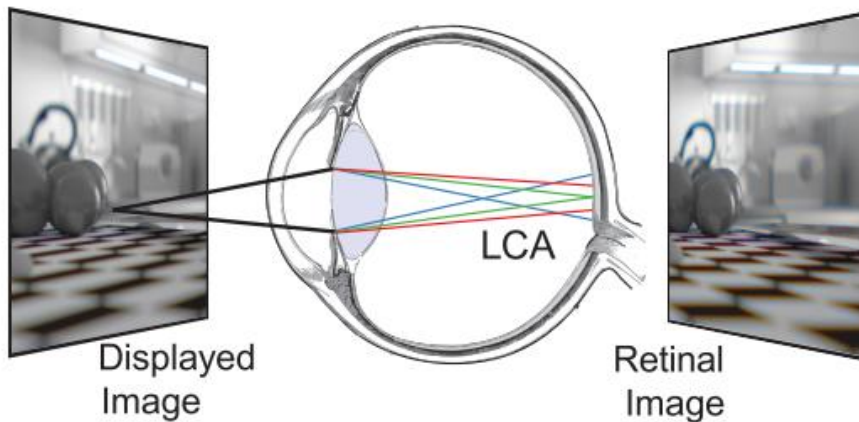
Bharadwaj and Schor, Vision Research 2004

Rendering Chromatic Eye Aberration



$$D(\lambda) = 1.731 - \frac{633.46}{\lambda - 214.10}$$

Short wavelengths (blue) are refracted more than long (red). Medium wavelengths are generally in best focus for broadband lights.

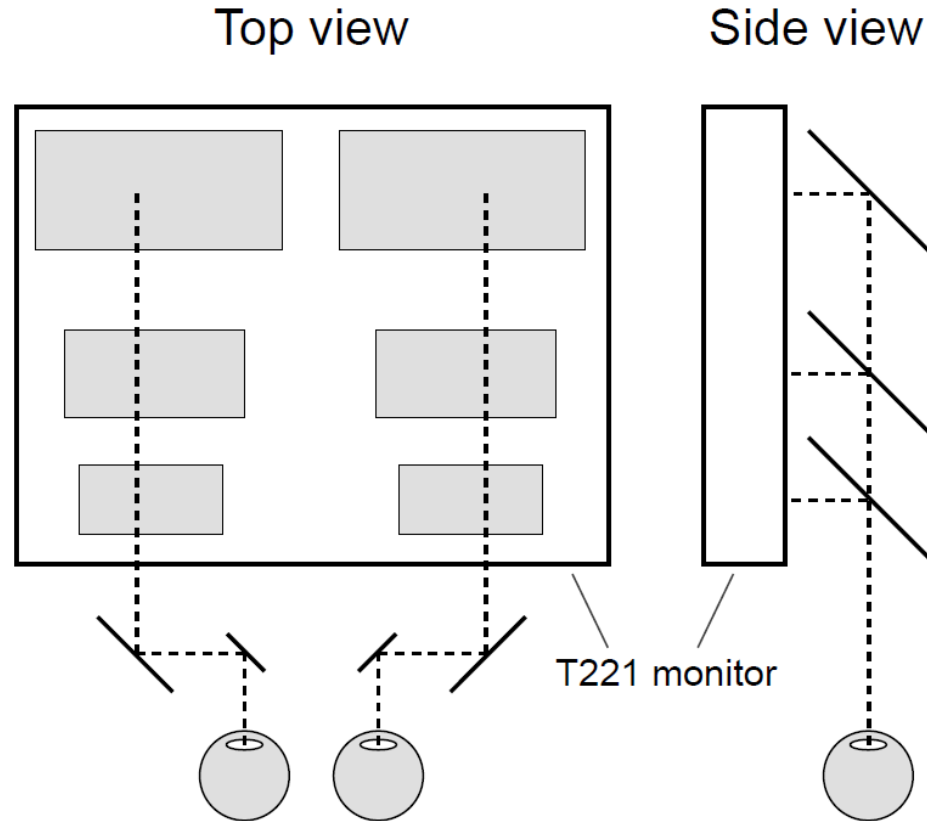


Rendering chromatic blur can provide accommodation effect (but not fully) and improve the realism

CHOLEWIAK ET AL, 2017. ChromaBlur: Rendering Chromatic Eye Aberration Improves Accommodation and Realism in HMDs. *Siggraph*

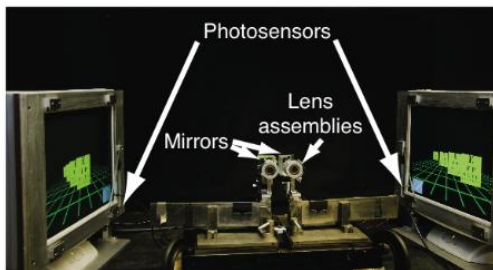
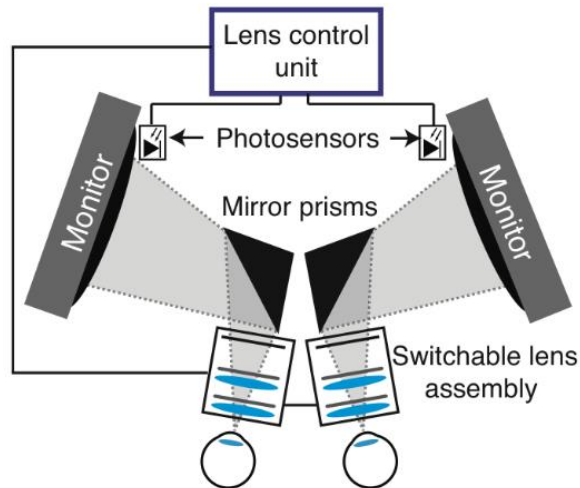
Multi-focal Plane Displays

- A display prototype with multiple focal distances using beam-splitters

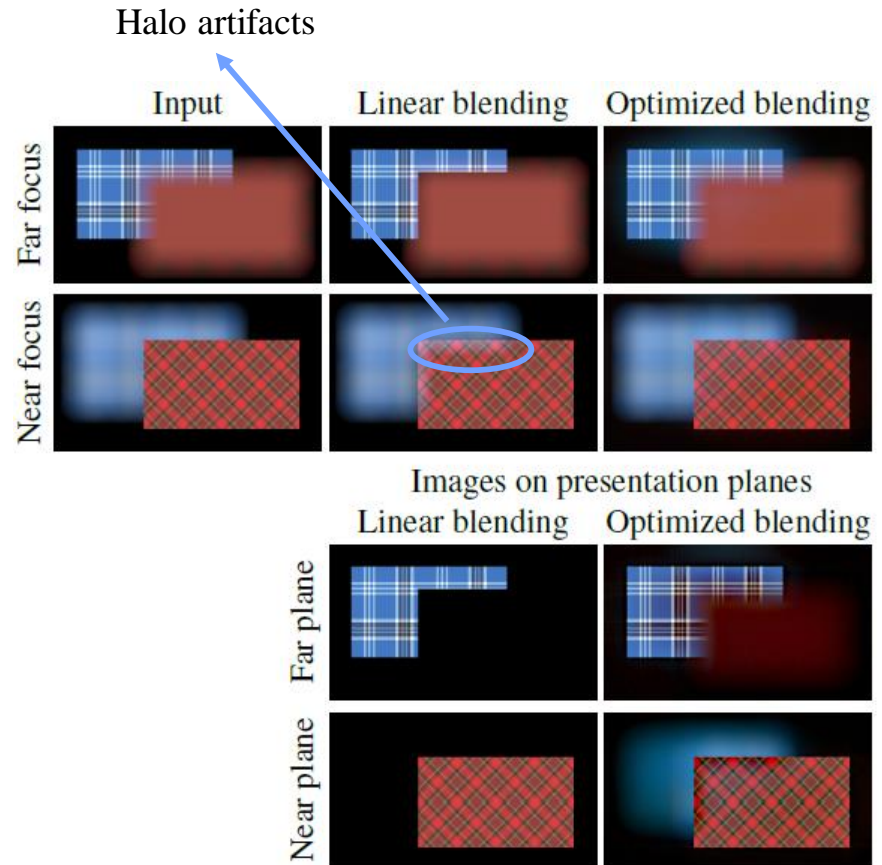


Images adapted from Akeley, Kurt, et al. "A stereo display prototype with multiple focal distances." ACM transactions on graphics (TOG). Vol. 23. No. 3. ACM, 2004.

Multi-focal Plane Displays



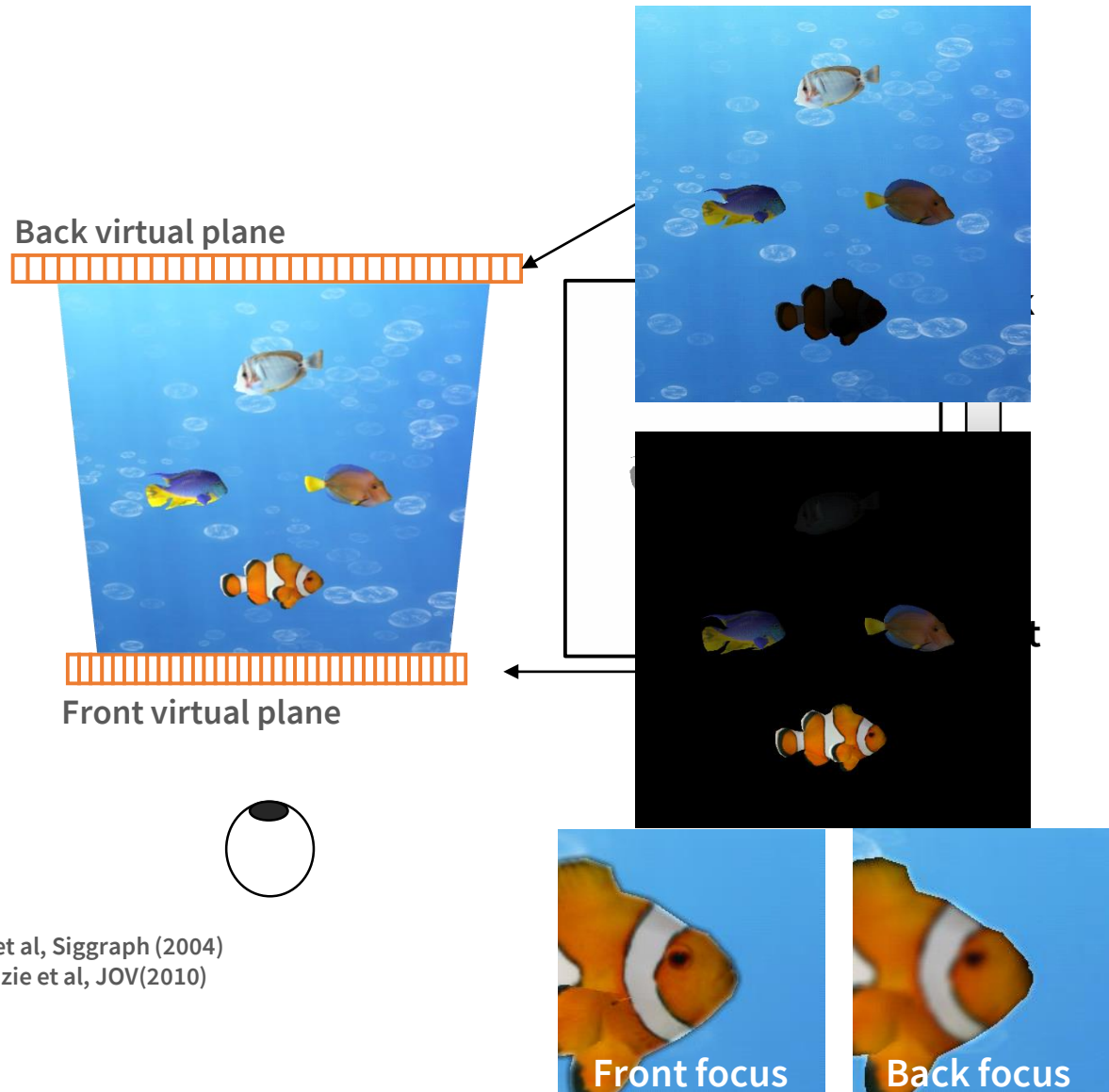
Prototype introduced by Love et al [2009]



Narain et al. [2015] optimize the focus cues for improved realism.

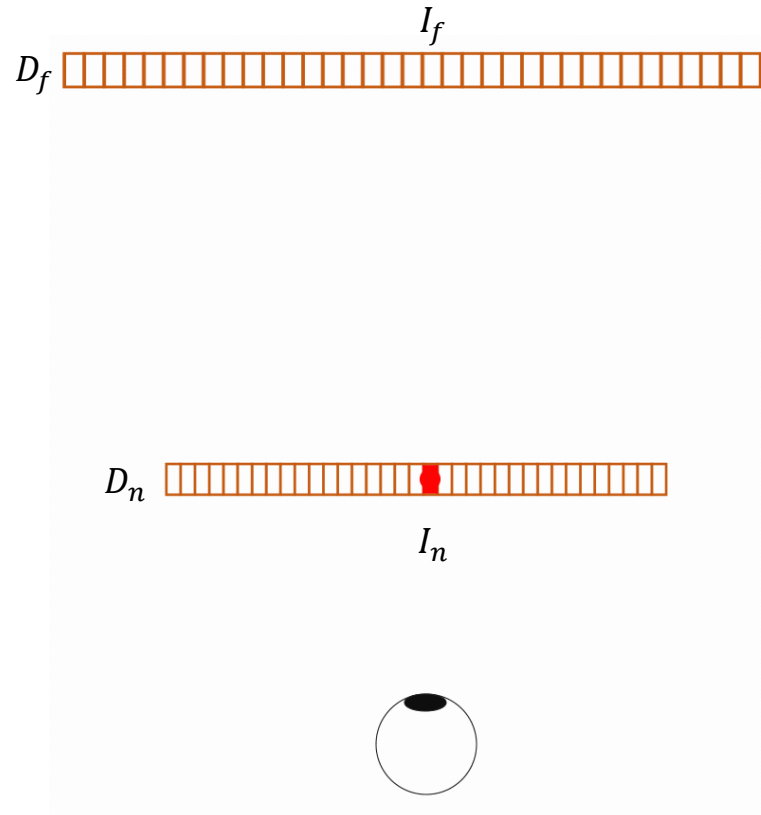
Images adapted from Narain, Rahul, et al. "Optimal presentation of imagery with focus cues on multi-plane displays." ACM Transactions on Graphics (TOG) 34.4 (2015): 59.

Rendering for multi plane displays: (1) linear Blending Rule



Akeley et al, Siggraph (2004)
MacKenzie et al, JOV(2010)

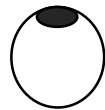
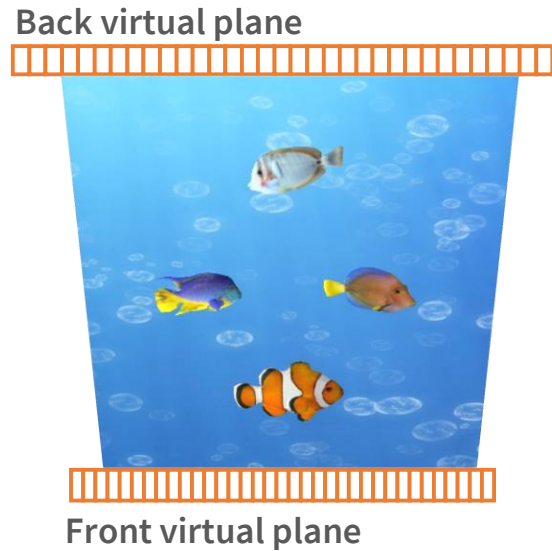
Rendering for multi plane displays: (1) linear Blending Rule



$$I_n = \left[1 - \frac{(D_n - D_s)}{(D_n - D_f)} \right] I_s \quad I_f = \left[\frac{(D_n - D_s)}{(D_n - D_f)} \right] I_s.$$

Akeley et al, Siggraph (2004)
MacKenzie et al, JOV(2010)

Rendering for multi plane displays: (2) Retinal Optimization



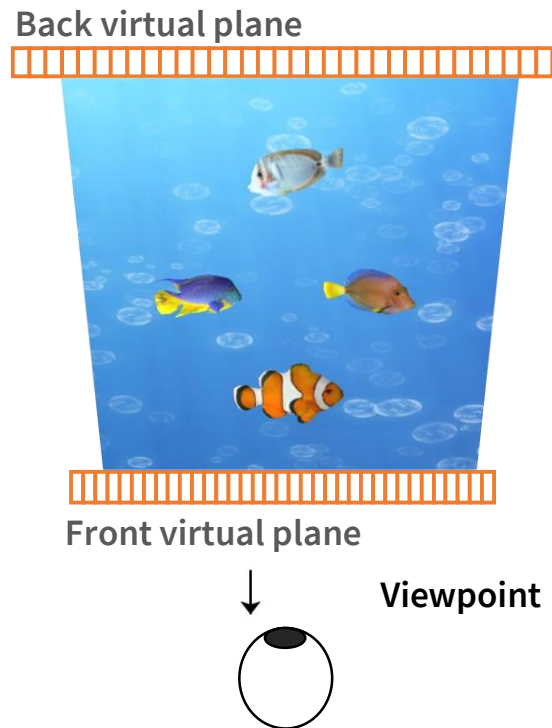
Narain et al (Siggraph 2015)
Mercier et al (Siggraph Asia 2017)

Optimization objective



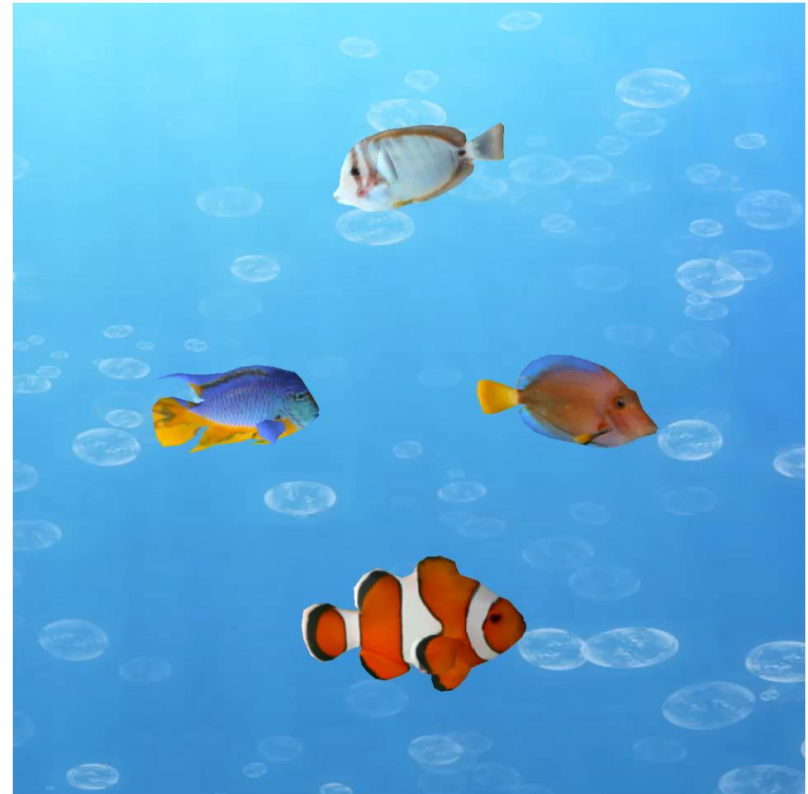
A focal stack

Rendering for multi plane displays: (3) Light field synthesis



Huang et al. (Siggraph2015)
Moon et al. (IEEE JSTSP 2017)

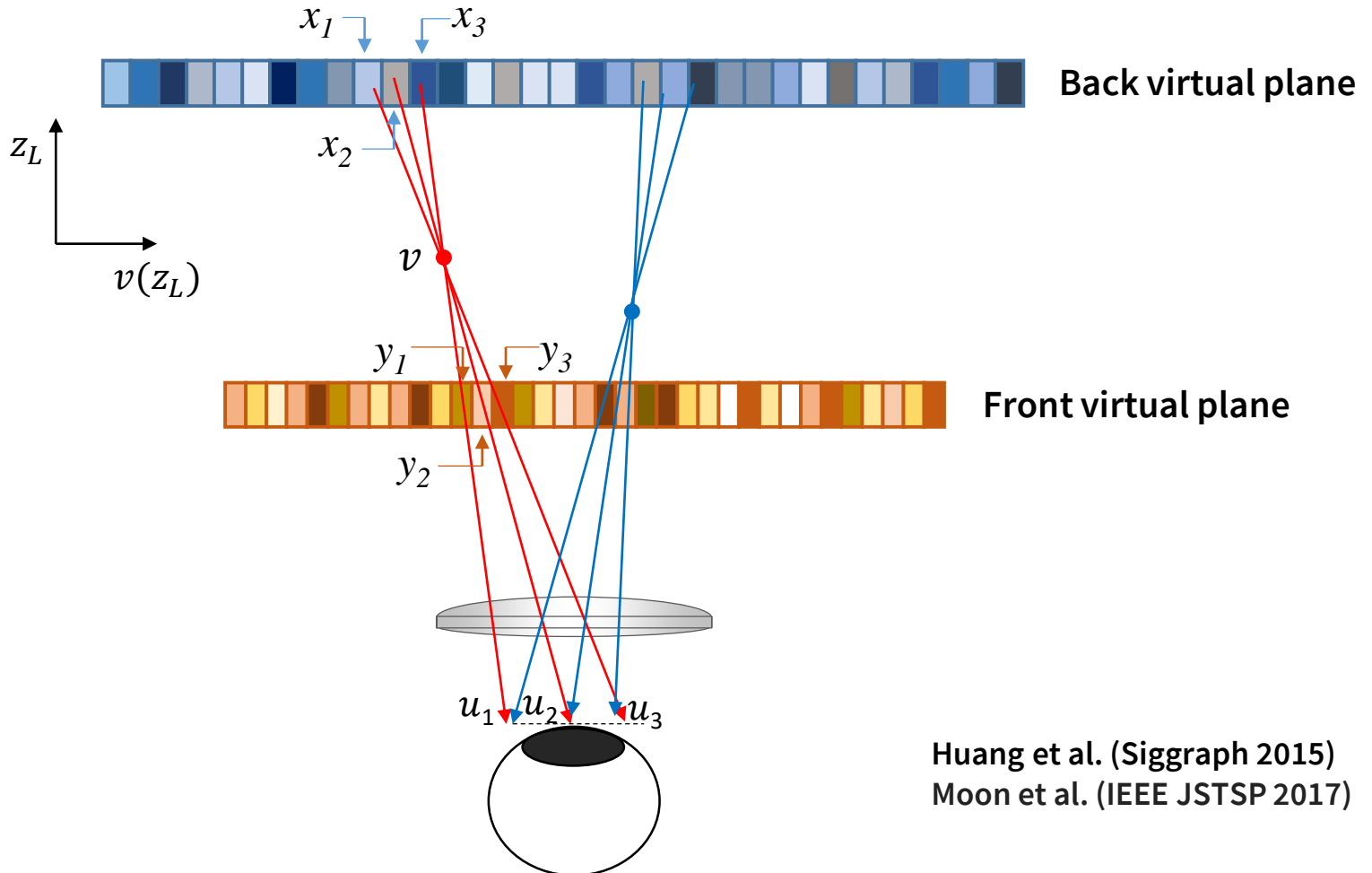
Optimization objective



Light field

Rendering for multi plane displays

(3) Light field synthesis



Target Light-fields: $L(v, u_1) = L(v, u_2) = L(v, u_3) = R$

Optimization equation : $L(v, u_1) = x_3 + y_1$

$$L(v, u_2) = x_2 + y_2$$

$$L(v, u_3) = x_1 + y_3$$

Comparison

	Initial input	Optimization Algorithm	Occlusion & Non-Lambertian surfaces
Linear Blending ^[1]	Single image + depth map	Fast	Incorrect
Retinal Optimization ^[2,3]	Focal stack	Slow	Correct
Light-field synthesis ^[4]	Light field	Slow	Correct
Ours	Sparse light field	Fast	Correct

[1] Akeley et al, Siggraph (2014)

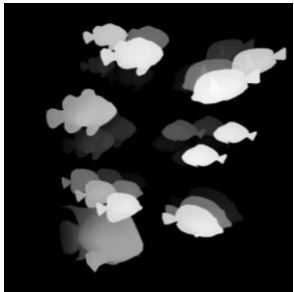
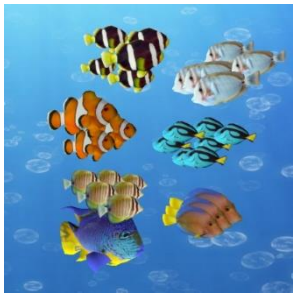
[2] Narain et al (Siggraph 2015)

[3] Mercier et al, Siggraph Asia (2017)

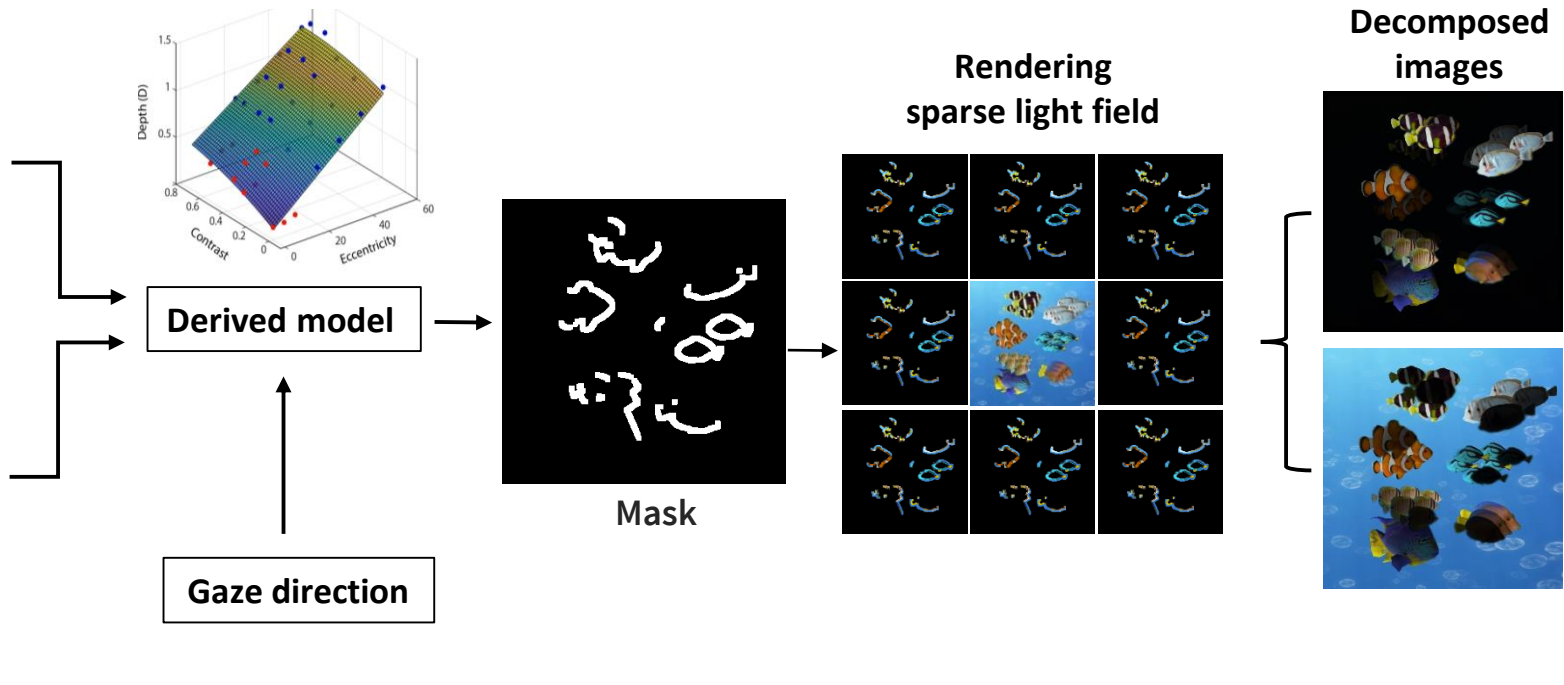
[4] Moon et al, IEEE JSTSP (2017)

Hybrid optimization

Single view

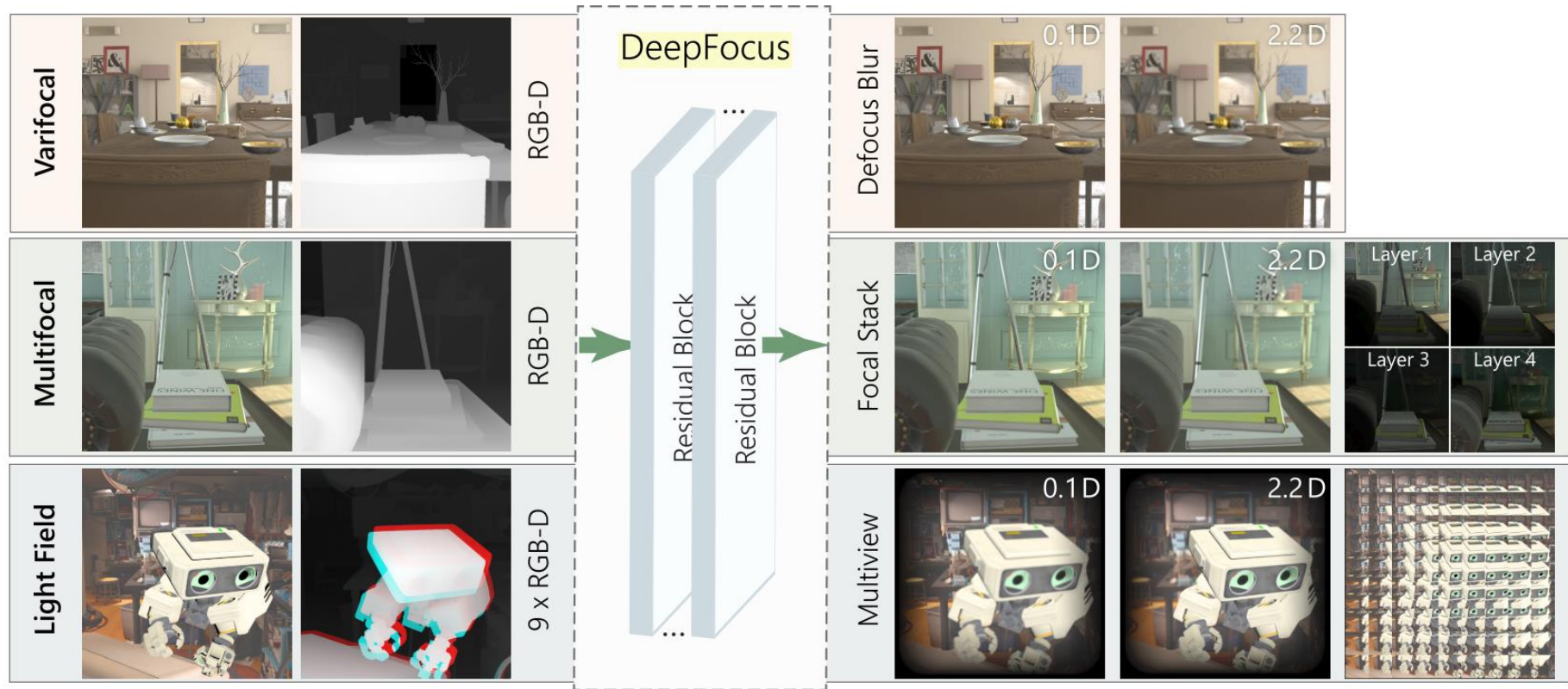


Depth map



Yu et al, "A Perception-driven Hybrid Decomposition for Multi-layer Accommodative Displays" IEEE Transactions on Visualization and Computer Graphics (2019)

Deep learning solution for various displays



XIAO ET AL, 2018. DeepFocus : Learned Image Synthesis for Accommodation-Supporting Displays. *Siggraph Asia*

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- Wetzstein, Gordon, et al. "Tensor displays: compressive light field synthesis using multilayer displays with directional backlighting." (2012).
- Narain, Rahul, et al. "Optimal presentation of imagery with focus cues on multi-plane displays." *ACM Transactions on Graphics (TOG)* 34.4 (2015): 59.
- Maimone, Andrew, et al. "Holographic near-eye displays for virtual and augmented reality". *ACM Transactions on Graphics* 36, 4 (2017),
- Xiao et al, "DeepFocus : Learned Image Synthesis for Accommodation-Supporting Displays". *ACM Transactions on Graphics (TOG)* (2018)
- Lanman, D. and Luebke, "Near-eye light field displays". *ACM Transactions on Graphics* 32, 6, 1–10. (2013)
- Cholewiak et al, "ChromaBlur: Rendering Chromatic Eye Aberration Improves Accommodation and Realism in HMDs". *ACM Transactions on Graphics*, (2017)
- Yu et al, "A Perception-driven Hybrid Decomposition for Multi-layer Accommodative Displays" *IEEE Transactions on Visualization and Computer Graphics* (2019)